MHF4U : Advanced Functions

Assignment #2

Reference Declaration

Complete the Reference Declaration section below in order for your assigment to be graded.

If you used any references beyond the course text and lectures (such as other texts, discussions with peers or online resources), indicate this information in the space below. If you did not use any aids, state this in the space provided.

Be sure to cite appropriate theorems throughout your work. You may use shorthand for well-known theorems like the FT (Factor Theorem), RRT (Rational Root Theorem), etc.

Note: Your submitted work must be **your original work**.

Family Name:
First Name:

Declared References:

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1. Given the volume of a rectangular box is $V(x) = x^3 + 6x^2 + 11x + 6$, if the length of the box is $x + 3$ cm, and its width is $x + 2$ cm then **determine** the height of the box. Also, **determine** the domain and range of the function V.

2. Consider the quartic polynomial function $f(x) = x^4 - 5x^3 + x^2 + 21x - 18$. Given that there is a local minimum on $f(x)$ at $(-1, -32)$, use a logical argument to **prove** that this must the absolute minimum of $f(x)$ without graphing the function.

   Recall that $x = c$, where $c \in \mathbb{R}$, corresponds to a *local minimum* of a function $f(x)$ on an interval $I = (a, b)$ which contains c provided that for every value of x on the interval I we have that $f(c) \leq f(x)$.

3. Recall that a prime number is defined as an integer $n > 1$ such that its only positive divisors are 1 and n. Let $\mathbb{P}$ represent the set of prime numbers. Suppose that you know that when you divide $g(x) = x^3 + 2x^2 + cx + d$ by $x - 2$ you obtain a remainder of 14, **determine** the specific values of c and d given that $c \in \mathbb{Z}$ and $d \in \mathbb{P}$.

4. **Solve** $\dfrac{7}{x+2} + \dfrac{5}{x-2} = \dfrac{10x-2}{x^2-4}$.

5. **Solve** $\left|\dfrac{x-4}{x+5}\right| \leq 4$.