## MHF4U : Advanced Functions

## Assignment #4

## Reference Declaration

Complete the Reference Declaration section below in order for your assignment to be graded.

If you used any references beyond the course text and lectures (such as other texts, discussions with peers or online resources), indicate this information in the space below. If you did not use any aids, state this in the space provided.

Be sure to cite appropriate theorems throughout your work. You may use shorthand for well-known theorems like the FT (Factor Theorem), RRT (Rational Root Theorem), etc.

Note: Your submitted work must be your original work.

Family Name: First Name:

Declared References:

1. **Determine** all real numbers x that satisfy the equation  $\log_3(x-7) + \log_3(x-9) = 1$ .

- 2. After Judgement Day, crows rose to become the dominant species and took over the planet Earth. Initially, there were 40000 crows and with no competition for food sources, this population of crows tripled in population every 1.5 years. A "mega-murder" is a murder of crows with a population of one million.
  - (a) Model the relationship between the population of crows and time since Judgement Day.
  - (b) **Determine** after how many years is Earth ruled by a mega-murder.

3. **Prove** that if a, b, c are the first three terms of a geometric sequence then  $\log(a), \log(b), \log(c)$  are the first three terms of an arithmetic sequence.

4. Given  $a, b, c \in \mathbb{R}^+$  with  $a \neq 1, b \neq 1, c \neq 1$  **prove** 

$$\frac{1}{1 + \log_a(bc)} + \frac{1}{1 + \log_b(ac)} + \frac{1}{1 + \log_c(ab)} = 1$$

.

5. **Determine** the set of real numbers a for which the equation

$$\log_8(x - a + 1) + \log_8(x - a - 1) = 1$$

has exactly one real solution for x.