

# Pre-Read Notes

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# 1 Chapter 1: Function Characts. and Props.

## 1.1 Functions

- A relationship is a function if all values on the domain have less than or equal to 1 value on the range
- circular motion is represented by sinusoidal functions
- functions can be represented in many ways

## 1.2 Absolute value

- $f(x) = |x|$  describes values  $\geq 0$

## 1.3 Properties

- Each function has a unique mixture of elements, usually most visually apparent on a graph
- This can be used to distinguish them

## 1.4 Sketching Graphs

- Do transformations in steps
- Do translations last when listing transformations
- general formula:  $y = af(k(x - d)) + c$

## 1.5 Inverse

- Inverse is done by swapping x and y variables
- graphically a reflection about x and y axis (along  $y = x$ )
- denoted by  $f^{-1}(x)$
- not all inverses are functions

## 1.6 Piecewise

- A function with multiple rules
- Related to specific intervals in the domain
- filled circle for inclusive, empty circle for exclusive
- Does not have to be continuous

## 1.7 Operations within

- If functions have overlapping domains they can be combined
- By combining the dependant variable in some way
- Properties carry onwards

# 2 Chapter 3: Polynomial Functions

## 2.1 Polynomial Functions

- A polynomial arranged in this formula
- $a_n x^n + a_{n-1} x^{n-1} + \dots + a_2 x^2 + a_1 x + a_0$
- where  $n$  are whole numbers and  $a$  are real numbers
- most simplified form
- the “degree” is the highest exponent in the polynomial
- degree is proportional to the number of “lines/curves” in the graph

## 2.2 Properties

- P. function’s degree can indicate a lot:
- shape, turning points, zeroes, and end behavior
- odd degree  $\rightarrow$  opposite end dir., even degree  $\rightarrow$  same end dir.
- if even
- if leading coefficient is pos  $\rightarrow$  goes positive to negative
- if leading coefficient is neg  $\rightarrow$  goes negative to positive

- if odd
- neg  $\rightarrow$  face negative, pos  $\rightarrow$  face positive
- turning points proportional to  $n - 1$
- y axis symmetrical  $\rightarrow$  even function, rotational symmetry  $\rightarrow$  odd function

## 2.3 Factored Form

- Polynomial function family  $\rightarrow$  P. functions of similar properties
- zeroes of a P. function are same as roots of related P equation (when factored?)
- Factored form gives roots, factored form at 0 gives zeroes
- Use zeroes and a point to get equation from  $f(x) = a(x - b)(x - c) \dots$  where a is solved using the extra point and b, c,  $\dots$  are zeroes
- if root is exponent 1  $\rightarrow$  passes through as if linear
- if root is exponent 2  $\rightarrow$  glances off like quad vertex
- if root is exponent 3  $\rightarrow$  passes flat before going through, like parent root function

## 2.4 Transformations

- Like any other function

## 2.5 Dividing

- Polynomials can be divided in similar manner to numbers
- Like with long division
- remainders are added to the end of the equation, rest becomes factors

## 2.6 Factoring

- Remainder theorem:  $\frac{f(x)}{x-a} = f(a)$
- Factor theorem:  $x - a$  is a factor if  $f(a) = 0$
- To factor:
  1. use factor theorem to determine factor
  2. divide by factor

## 2.7 Factoring Sum or Difference

- Expressions with two perfect cubes
- $A^3 + B^3 = (A + B)(A^2 - AB + B^2)$
- $A^3 - B^3 = (A - B)(A^2 + AB + B^2)$

## 3 Chapter 4: Polynomial Equ. and Ineq.

### 3.1 Solving

- Solutions of  $f(x) = 0$  are zeroes
- sometimes you need to ignore the values outside of the defined intervals

### 3.2 Solving Linear Inequalities

- Solve linear inequalities by rearranging, like solving linear equations
- If you multiply or divide by a negative number, flip over the inequality sign

### 3.3 Solving Polynomial Inequalities

- To solve:
  1. Solve for main points, like roots
  2. Plot on some sort of line system
  3. This will give you your solution ranges

### 3.4 Rates of Change in Polynomials

- Rate of change is  $\frac{\text{change in range}}{\text{change in domain}}$
- On interval  $x_1 \leq x \leq x_2$  is  $\frac{f(x_2) - f(x_1)}{x_2 - x_1}$
- When  $x$  is very small,  $roc = \frac{f(x+h) - f(x)}{h}$
- On any “indexes” the roc is near 0

## 4 Chapter 5: Rational funcs., eqs., ineqs.

### 4.1 Graph of Reciprocals

- Reciprocals of linear and quadratic functions follow a similar general graphed form
- Take characteristics from original to graph Reciprocals
- Y coordinates mostly the same to the original
- original's zeroes determine vertical asymptotes
- Reciprocals always start with a asymptote on  $y = 0$  unless translated

### 4.2 Quotients of Polynomials

- Rational function is  $f(x) = \frac{g(x)}{h(x)}$  where  $f(x)$  and  $g(x)$  are Polynomials
- Has breaks or gaps where denominator is zero, must be restricted
- vertical asymptotes and gaps determine restrictions on the domain
- end behavior determined by vertical or oblique asymptotes
- oblique asymptote: slanted asymptote
- Horizontal asymptote  $\rightarrow g(x)$  degree is less than or equal to  $h(x)$
- Otherwise, if greater, slanted asymptote

### 4.3 graph in form $\frac{ax+b}{cx+d}$

- Most have vertical and horizontal asymptotes
- Determine vertical asymptote by finding what creates 0 on the denominator
- Determine horizontal asymptote by comparing the ratio between numerator and denominator leading coefficient
- in form  $\frac{b}{cx+d}$  vertical asymptote at  $x = -\frac{d}{c}$  and horizontal asymptote at  $y = 0$
- If numerator and denominator have a common linear factor, line has hole where the zero of the common factor occurs



## 4.4 Solving Rational Equations

- Solve algebraically
- zeroes in rational function are zeroes of the numerator
- Make sure to check for extraneous answers

## 4.5 Solving Rational Inequalities

- Find all values that satisfy inequality
- Use roots and an inequality table

## 4.6 Rates of Change

- Use previous methods to calculate rates of change
- Cannot calculate where there is a hole
- roc at vertical gaps or asymptotes are undefined
- roc  $\rightarrow$  horizontal asymptotes approach zero

# 5 Chapter 6

## 5.1

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## 5.2

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## 5.3

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## 5.4

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5.5

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5.6

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5.7

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6 Chapter 7

7 Chapter 8

8 Chapter 9

9 Chapter 2