University of Edinburgh, School of Mathematics Incomplete Data Analysis, 2020/2021 Assignment 3

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All code included in this assignment is available in a GitHub repository at https://github.com/mworlidge/incomplete-data-analysis/blob/main.R. First I need to load all the necessary packages.

```
require("mice")
require(JointAI)
require(devtools)
require(reshape2)
require(RColorBrewer)
require(ggplot2)
source_url("https://gist.githubusercontent.com/NErler/Od00375da460dd33839b98faeee2fdab/raw/c6f537ecf80ee
```

Question 1

Considering the nhanes dataset, we can use the functions dim and str to explore the data and to see what we're working with.

```
dim(nhanes)

## [1] 25 4

str(nhanes)

## 'data.frame': 25 obs. of 4 variables:
## $ age: num 1 2 1 3 1 3 1 1 2 2 ...
## $ bmi: num NA 22.7 NA NA 20.4 NA 22.5 30.1 22 NA ...
## $ hyp: num NA 1 1 NA 1 NA 1 1 1 NA ...
## $ chl: num NA 187 187 NA 113 184 118 187 238 NA ...
```

This shows that we have 25 cases of 4 variables, age, bmi, hyp and chl.

 $\mathbf{a})$

The following code chunk shows that there are 13 complete cases and 12 incomplete cases. Therefore 48% of cases are incomplete.

```
# number of complete cases
cc <- nrow(cc(nhanes))
# total number of cases
n <- nrow(nhanes)
# percentage of missing cases
(n - cc)/n * 100</pre>
```

[1] 48

b)

Now we can impute the data using the package mice using the default seed = 1. In step 2 of the imputation (the with() function), we can predict bmi from age, hyp and chl by the normal linear regression model.

```
imps <- mice(nhanes, printFlag = FALSE, seed = 1)
fits <- with(imps, lm(bmi ~ age + hyp + chl))</pre>
```

Now we can proceed to step 3 and pool the analyses.

```
ests <- pool(fits)
ests$pooled[, c(1, 3, 10)]</pre>
```

```
## term estimate lambda

## 1 (Intercept) 19.61789252 0.08938989

## 2 age -3.55287155 0.68640637

## 3 hyp 2.19701748 0.35043452

## 4 chl 0.05378081 0.30408063
```

The proportions of variance due to the missing data from each parameter is denoted by the column λ which is given by $\frac{B+\frac{B}{M}}{V^{+}}$. Therefore we have $\lambda_{\rm age}=0.6864,\ \lambda_{\rm hyp}=0.3504,\ \lambda_{\rm chl}=0.3040$. The parameter that appears to be most affected by the nonresponse is **age** since it has the highest value for the proportions of variance due to the missing data.

c)

We can now repeat this analysis with seeds 2, 3, 4, 5, and 6.

```
#using the default M=6 but changing the seed
ests2 <- pool(with(mice(nhanes, printFlag = FALSE, seed = 2), lm(bmi ~ age + hyp + chl)))
ests3 <- pool(with(mice(nhanes, printFlag = FALSE, seed = 3), lm(bmi ~ age + hyp + chl)))
ests4 <- pool(with(mice(nhanes, printFlag = FALSE, seed = 4), lm(bmi ~ age + hyp + chl)))
ests5 <- pool(with(mice(nhanes, printFlag = FALSE, seed = 5), lm(bmi ~ age + hyp + chl)))
ests6 <- pool(with(mice(nhanes, printFlag = FALSE, seed = 6), lm(bmi ~ age + hyp + chl)))</pre>
ests2$pooled[, c(1, 3, 10)]
```

```
## term estimate lambda

## 1 (Intercept) 19.9464142 0.4144454

## 2 age -4.0615093 0.4033924

## 3 hyp 1.5304762 0.1430995

## 4 chl 0.0628349 0.2959966
```

```
ests3$pooled[, c(1, 3, 10)]
##
                    estimate
                                lambda
            term
## 1 (Intercept) 20.55844343 0.2772900
             age -3.85753338 0.5895051
## 3
             hyp 1.35281238 0.4101152
## 4
             chl 0.05872834 0.5621346
ests4$pooled[, c(1, 3, 10)]
##
                                lambda
            term
                    estimate
## 1 (Intercept) 19.39540373 0.1315114
## 2
             age -3.50603350 0.2189333
## 3
             hyp 2.75053046 0.1961083
## 4
             chl 0.04920611 0.3305334
ests5$pooled[, c(1, 3, 10)]
##
                    estimate
                                lambda
            term
## 1 (Intercept) 19.17135935 0.4855733
## 2
             age -3.49672250 0.4511896
## 3
             hyp 1.50954775 0.5942866
## 4
             chl 0.06081272 0.2346065
ests6$pooled[, c(1, 3, 10)]
##
                                lambda
            term
                    estimate
## 1 (Intercept) 20.52083805 0.4168136
             age -2.92141353 0.6549523
## 2
## 3
             hyp 1.22474596 0.2960364
## 4
                  0.04949218 0.5196295
             chl
```

From these results we can see that λ changes significantly as the seed changes. The conclusions made for seed= 1 are not the same as the conclusions made for the other seeds. When seed = 4, the parameter that is most affected by the nonresponse is chl, and when seed = 5, the parameter that is most affected by the nonresponse is hyp. For seed = 3 and seed = 3, the parameter age is still the parameter most affected by the nonresponse. When seed = 2 the Intercept is the parameter most affected by the nonresponse.

d)

The conclusions from the previous question suggest that we should increase the number of datasets M. Therefore we repeat the analysis with M = 100.

```
lm(bmi ~ age + hyp + chl)))
ests4m100 <- pool(with(mice(nhanes, M=100, printFlag = FALSE, seed = 4),</pre>
                       lm(bmi ~ age + hyp + chl)))
ests5m100 <- pool(with(mice(nhanes, M=100, printFlag = FALSE, seed = 5),
                       lm(bmi ~ age + hyp + chl)))
ests6m100 <- pool(with(mice(nhanes, M=100, printFlag = FALSE, seed = 6),
                       lm(bmi ~ age + hyp + chl)))
ests1m100$pooled[, c(1, 3, 10)]
            term
                    estimate
## 1 (Intercept) 19.61789252 0.08938989
            age -3.55287155 0.68640637
## 3
            hyp 2.19701748 0.35043452
## 4
            chl 0.05378081 0.30408063
ests2m100$pooled[, c(1, 3, 10)]
            term
                   estimate
                               lambda
## 1 (Intercept) 19.9464142 0.4144454
            age -4.0615093 0.4033924
## 3
            hyp 1.5304762 0.1430995
## 4
            chl 0.0628349 0.2959966
ests3m100$pooled[, c(1, 3, 10)]
                                lambda
            term
                    estimate
## 1 (Intercept) 20.55844343 0.2772900
            age -3.85753338 0.5895051
## 3
            hyp 1.35281238 0.4101152
## 4
            chl 0.05872834 0.5621346
ests4m100$pooled[, c(1, 3, 10)]
            term
                    estimate
                                lambda
## 1 (Intercept) 19.39540373 0.1315114
            age -3.50603350 0.2189333
            hyp 2.75053046 0.1961083
## 3
            chl 0.04920611 0.3305334
## 4
ests5m100$pooled[, c(1, 3, 10)]
##
                    estimate
                                lambda
            term
## 1 (Intercept) 19.17135935 0.4855733
           age -3.49672250 0.4511896
## 3
            hyp 1.50954775 0.5942866
## 4
            chl 0.06081272 0.2346065
```

```
ests6m100$pooled[, c(1, 3, 10)]
```

```
## term estimate lambda
## 1 (Intercept) 20.52083805 0.4168136
## 2 age -2.92141353 0.6549523
## 3 hyp 1.22474596 0.2960364
## 4 chl 0.04949218 0.5196295
```

The (pooled) estimates should get more stable as M increases so we can be more confident in any one specific run. Therefore, I would prefer these analyses over M=5

Question 2

The file dataex2 consists of 100 datasets that were generated in the following way

$$y_i|x_i \stackrel{\text{iid}}{\sim} \mathcal{N}(\beta_0 + \beta_1 x_i, 1) \quad x_i \stackrel{\text{iid}}{\sim} \text{Unif}(-1, 1) \quad \beta_0 = 1, \quad \beta_1 = 3$$

for i = 1, ..., 100. Additionally some of the responses have been set to missing from the datasets under the MAR mechanism.

```
# load the data
load("dataex2.Rdata")
# store the number of datasets as n
n <- dim(dataex2)[1]</pre>
```

Stochastic Regression Imputation

[1] 0.88

Bootstrap version

[1] 0.95

Using stochastic regression imputation we get an empirical coverage probability of 88%. However when using the Bootstrap method we get an empirical coverage probability of 95%. The bootstrap method implements (normal linear) stochastic regression but takes parameter uncertainty into account. However the stochastic regression method implements (normal linear) stochastic regression for each copy m of the dataset we have made m=1,...,20. Therefore parameter uncertainty is not taken into account since the same estimates are used for imputing all 20 copies of the dataset. Therefore, the confidence intervals may be too narrow and affect the coverage of the intervals.

Question 3

Given a dataset $\{y_i, x_{1i}, ..., x_{pi}\}$. We can consider a linear (in the coefficients) regression model

$$y_i = \beta_0 + \beta_1 x_{1i} + \dots + \beta_p x_{pi} + \epsilon_i, \qquad \epsilon_i \sim N(0, \sigma^2).$$

For strategy (i), we first compute the predicted values from each fitted model in step 2,

$$\hat{y}_i^{(m)} = \hat{\beta}_0^{(m)} + \hat{\beta}_1^{(m)} x_{1i} + \dots + \hat{\beta}_p^{(m)} x_{pi},$$

where $\hat{\beta}_{j}^{(m)}$ is the estimate of β_{j} , j=(0,...,p), for the m^{th} dataset. Then pool them according to Rubin's rule for point estimates,

$$\bar{y}_{i} = \frac{1}{M} \sum_{i=1}^{M} \hat{y}_{i}^{(m)}
= \frac{1}{M} \hat{\beta}_{0}^{(m)} + \hat{\beta}_{1}^{(m)} x_{1i} + \dots + \hat{\beta}_{p}^{(m)} x_{pi}
= \frac{1}{M} \sum_{i=1}^{M} \hat{\beta}_{0}^{(m)} + \frac{1}{M} \sum_{i=1}^{M} \hat{\beta}_{1}^{(m)} x_{1i} + \dots + \frac{1}{M} \sum_{i=1}^{M} \hat{\beta}_{p}^{(m)} x_{pi}
= \bar{\beta}_{0} + \bar{\beta}_{1} x_{1i} + \dots + \bar{\beta}_{p} x_{pi}$$

Using strategy (ii), first we need to pool the regression coefficients from each fitted model in step 2 using Rubin's rule for point estimates,

$$\bar{\beta}_0 = \frac{1}{M} \sum_{m=1}^{M} \hat{\beta}_0^{(m)}$$

 $\bar{\beta}_p = \frac{1}{M} \sum_{m=1}^{M} \hat{\beta}_p^{(m)}.$

Then we can compute the predicted values,

$$\bar{y}_i = \bar{\beta}_0 + \bar{\beta}_1 x_{1i} + \dots + \bar{\beta}_p x_{pi}$$

These two equations show that computing the predicted values from each fitted model in step 2 and then pooling them according to Rubin's rule for point estimates is the mathematically equivalent to pooling the regression coefficients from each fitted model in step 2 using Rubin's rule for point estimates and then computing the predicted values afterwards.

Question 4

The model used to generate the data, which corresponds to our model of interest in step 2, was the following one:

$$y_{i} = \beta_{0} + \beta_{1}x_{1i} + \beta_{2}x_{2i} + \beta_{3}x_{1i}x_{2i} + \epsilon_{i},$$

$$x_{1i} \stackrel{\text{iid}}{\sim} N(0, 1), \qquad x_{2i} \stackrel{\text{iid}}{\sim} N(1.5, 1), \qquad \epsilon_{i} \stackrel{\text{iid}}{\sim} N(0, 1),$$

for $i=1,...,1000, \beta_0=1.5, \beta_1=1, \beta_2=2, \beta_3=1$. Missingness has been imposed on y and x_1 .

```
load("dataex4.Rdata")
```

a) Impute, then transform

By only imputing the y and x1 variables in step 1, we can calculate estimates of β_1 , β_2 and β_3 , with the 95% confidence intervals. In this approach the interaction variable is left outside the imputation process and calculated afterwards in the analysis model.

```
imps1 <- mice(dataex4, m=50, seed=1, printFlag = FALSE)
fits1 <- with(imps1, lm(y ~ x1 + x2 + x1*x2))
ests1 <- pool(fits1)
summary(ests, conf.int = TRUE)[, c(1,2,3,7,8)]</pre>
```

```
## term estimate std.error 2.5 % 97.5 % ## 1 (Intercept) 19.61789252 3.41003531 12.421281424 26.81450361 ## 2 age -3.55287155 1.54113006 -8.067205920 0.96146282 ## 3 hyp 2.19701748 2.10797844 -2.568707058 6.96274202 ## 4 chl 0.05378081 0.02031792 0.008646559 0.09891506
```

This shows that the estimate of β_2 is approximately true. However the estimates of β_1 and β_3 are not very good and the true values do not lie in the 95% confidence intervals.

b) Passive imputation

Another method is passive imputation. We start by calculating the interaction variable $x_{3i} = x_{1i}x_{2i}$ in the incomplete data and appending it as a variable to the dataset. Then we will use passive imputation to impute the interaction variable.

```
x1 \leftarrow dataex4x1; x2 \leftarrow dataex4x2; dataex4x3 \leftarrow x1x2
imp0 <- mice(dataex4, maxit=0)</pre>
meth <- imp0$method
meth["x3"] \leftarrow "\sim I(x1*x2)"
pred <- imp0$predictorMatrix</pre>
pred[c("x1", "x2"), "x3"] <- 0</pre>
visSeq <- imp0$visitSequence</pre>
visSeq
## [1] "y" "x1" "x2" "x3"
imps2 <- mice(dataex4, method = meth, predictorMatrix = pred, visitSequence = visSeq,
               m = 50, seed = 1, printFlag = FALSE)
ests2 <- pool(with(imps2, lm(y \sim x1 + x2 + x1*x2)))
summary(ests2, conf.int=TRUE)[,c(1,2,3,7,8)]
             term estimate std.error
##
                                              2.5 %
                                                        97.5 %
## 1 (Intercept) 1.5534782 0.08842211 1.3788626 1.7280939
               x1 1.1926170 0.09584345 1.0034980 1.3817360
## 3
               x2 1.9964402 0.04936582 1.8989468 2.0939336
## 4
           x1:x2 0.8740573 0.05678521 0.7615712 0.9865434
```

The estimates have improved slightly for β_1, β_2 and β_3 , however the true values of β_1 and β_3 still do not lie in the 95% confidence intervals.

c) Just another variable

Additionally, now that the interaction variable has been appended to the dataset, we can impute it just like another variable and use this variable for the interaction term in step 2.

```
imps3 <- mice(dataex4, m = 50, seed = 1, printFlag = FALSE)
fits3 <- with(imps3, lm(y ~ x1 + x2 + x3))
ests3 <- pool(fits3)
summary(ests3, conf.int=TRUE)[, c(1,2,3,7,8)]</pre>
```

```
## term estimate std.error 2.5 % 97.5 % ## 1 (Intercept) 1.499714 0.07821436 1.3452011 1.654227 ## 2 x1 1.003930 0.08228372 0.8414967 1.166363 ## 3 x2 2.026180 0.04371605 1.9398113 2.112548 ## 4 x3 1.017793 0.04428071 0.9303479 1.105238
```

This method has improved the estimates greatly. All the estimates are approximately equal to the true values of the parameters and they all lie in the 95% confidence intervals.

d)

The most obvious conceptual drawback of the *just another variable* approach for imputing interactions is that because x_3 is the last column it is imputed using the x_1 and x_2 from the original dataset.

Question 5

The dataset NHANES2.Rdata is a subset of data from the National Health and Nutrition Examination Survey (NHANES), where the goal is to assess the health and nutrition status of adults and children in the United States. The variables in the dataset are the following:

- wgt: weight in kg,
- gender: male vs female,
- bili: bilirubin concentration in mg/dL,
- age: in years,
- chol: total serum cholesterol in mg/dL,
- HDL: High-density lipoprotein cholesterol in mg/dL,
- hgt: height in metres,
- educ: educational status; 5 ordered categories,
- race: 5 unordered categories,
- SBP: systolic blood pressure in mmHg,
- hypten: hypertensive; binary,
- smoke: smoking status; 3 ordered categories,
- DM: diabetes mellitus status; binary,
- WC: waist circumference in cm.

The analysis of interest is the linear model:

$$wgt = \beta_0 + \beta_1 gender + \beta_2 age + \beta_3 hgt + \beta_4 WC + \epsilon, \quad \epsilon \sim \mathcal{N}(0, \sigma^2). \tag{1}$$

We can start by looking at the data, and by using the command dim, we see there are 500 rows (individuals), and 12 variables.

```
load("NHANES2.Rdata")
dim(NHANES2)
```

```
## [1] 500 12
```

Using the command str we can inspect the nature of our variables and check they are coded correctly.

```
str(NHANES2)
```

```
## 'data.frame':
                    500 obs. of 12 variables:
##
                  78 78 75.3 90.7 112 ...
   $ wgt
            : num
   $ gender: Factor w/ 2 levels "male", "female": 1 1 2 1 2 1 2 2 1 1 ...
                  1.1 0.7 0.5 0.8 0.6 0.7 1.1 0.8 0.8 0.5 ...
##
            : num
##
   $ age
            : num
                  67 39 64 36 33 62 56 63 55 20 ...
##
           : num 6.13 4.65 4.14 3.47 6.31 4.47 6.41 5.51 7.01 3.75 ...
   $ chol
                  1.09 1.14 1.29 1.37 1.27 0.85 1.81 2.38 2.79 1.03 ...
   $ HDL
            : num
##
   $ hgt
            : num 1.75 1.78 1.63 1.93 1.73 ...
           : Ord.factor w/ 5 levels "Less than 9th grade"<...: 5 3 5 4 4 3 4 5 4 2 ...
##
   $ educ
           : Factor w/ 5 levels "Mexican American",..: 5 3 5 3 4 5 4 5 3 3 ...
##
   $ race
   $ SBP
            : num 139 103 NaN 115 107 ...
    $ hypten: Factor w/ 2 levels "no","yes": 2 1 2 2 1 2 NA 1 2 1 ...
##
            : num 91.6 84.5 91.6 95.4 119.6 ...
```

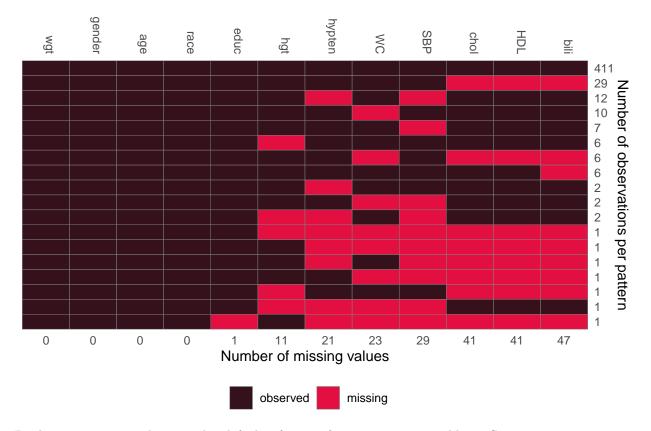
Additionally, by using the summary command we can get an idea of the min/max/mean/quantiles of the observed data in each variable, as well as the number of missing values.

summary(NHANES2)

```
##
                         gender
                                          bili
                                                                             chol
         wgt
                                                            age
##
    Min.
                      male :252
                                            :0.2000
                                                              :20.00
                                                                               : 2.07
           : 39.01
                                    Min.
                                                                        Min.
                                                       Min.
    1st Qu.: 65.20
                      female:248
                                    1st Qu.:0.6000
                                                       1st Qu.:31.00
                                                                        1st Qu.: 4.27
##
    Median : 76.20
                                    Median :0.7000
                                                       Median :43.00
                                                                        Median: 4.86
    Mean
           : 78.25
                                    Mean
                                            :0.7404
                                                       Mean
                                                              :45.02
                                                                        Mean
                                                                               : 5.00
                                    3rd Qu.:0.9000
                                                                        3rd Qu.: 5.64
##
    3rd Qu.: 86.41
                                                       3rd Qu.:58.00
           :167.38
                                            :2.9000
                                                              :79.00
                                                                               :10.68
##
    Max.
                                    Max.
                                                       Max.
                                                                        Max.
##
                                    NA's
                                            :47
                                                                        NA's
                                                                               :41
         HDL
##
                          hgt
                                                          educ
##
    Min.
            :0.360
                     Min.
                             :1.397
                                      Less than 9th grade: 31
##
    1st Qu.:1.110
                     1st Qu.:1.626
                                      9-11th grade
                                                            : 69
                                      High school graduate:115
##
    Median :1.320
                     Median :1.676
            :1.395
                             :1.687
                                      some college
##
    Mean
                     Mean
                                                            :148
##
    3rd Qu.:1.590
                     3rd Qu.:1.753
                                      College or above
                                                            :136
##
    Max.
            :3.130
                     Max.
                             :1.930
                                      NA's
                                                               1
    NA's
##
            :41
                     NA's
                             :11
##
                                    SBP
                                                                    WC
                                                  hypten
                     race
##
    Mexican American
                       : 52
                               Min.
                                      : 81.33
                                                 no :354
                                                             Min.
                                                                     : 61.90
##
    Other Hispanic
                       : 58
                               1st Qu.:109.00
                                                 yes :125
                                                             1st Qu.: 84.80
    Non-Hispanic White: 182
                               Median :118.67
                                                 NA's: 21
                                                             Median: 95.00
    Non-Hispanic Black:112
                                                                     : 96.07
##
                               Mean
                                      :120.05
                                                             Mean
##
    other
                       : 96
                               3rd Qu.:128.67
                                                             3rd Qu.:104.80
##
                                      :202.00
                                                                     :154.70
                               Max.
                                                             Max.
##
                               NA's
                                       :29
                                                             NA's
                                                                     :23
```

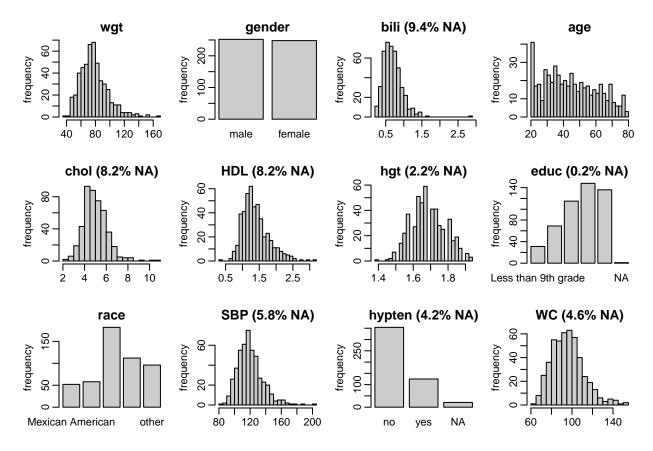
I have used the JointAI package to inspect the missing data patterns. JointAI performs (Bayesian) multiple imputation and has useful visualisation functions.

```
md_pattern(NHANES2, pattern = FALSE, color = c('#34111b', '#e30f41'))
```



Predictive mean matching is the default of mice for continuous variables. Since we want to use a normal linear regression model for imputing the missing values, we need to inspect whether the normality assumption is approximately met. The package <code>JointAI</code> allows us to visualise how the observed parts of the incomplete variables are distributed.

```
par(mar = c(3, 3, 2, 1), mgp = c(2, 0.6, 0))
plot_all(NHANES2, breaks = 30, ncol = 4)
```



We are now ready to start the imputation procedure. I will start by doing a dry run of mice(), without any iterations, which will create the default versions of everything that needs to be specified. These default settings can then be adapted to this dataset.

```
imp0 <- mice(NHANES2, maxit = 0)
imp0

## Class: mids</pre>
```

```
## Number of multiple imputations:
##
   Imputation methods:
##
                 gender
                                                                 HDL
                              bili
                                                    chol
                                                                                     educ
                                           age
                                                                           hgt
         wgt
                                            11 11
                             "pmm"
##
                                                   "pmm"
                                                              "pmm"
                                                                         "pmm"
                                                                                   "polr"
                    SBP
                                            WC
##
                            hypten
        race
                  "pmm"
##
                                        "pmm"
##
   PredictorMatrix:
                gender bili age chol HDL
##
            wgt
                                               hgt
                                                    educ
## wgt
              0
                       1
                                  1
                                        1
                                             1
                                                  1
                                                        1
                                                              1
                                                                               1
                             1
                                                                   1
                       0
                                  1
                                             1
                                                                               1
##
   gender
              1
                             1
                                        1
                                                  1
                                                        1
                                                              1
                                                                   1
## bili
              1
                       1
                             0
                                  1
                                        1
                                             1
                                                  1
                                                        1
                                                              1
                                                                   1
                                                                            1
                                                                               1
                       1
                                  0
                                        1
                                             1
                                                              1
   age
              1
                             1
                                                  1
                                                        1
                                                                   1
   chol
              1
                       1
                                  1
                                        0
                                             1
                                                  1
                                                        1
                                                              1
                                                                   1
                                                                            1
                                                                               1
##
                             1
##
   HDL
              1
                       1
                                        1
                                             0
                                                  1
                                                        1
                                                              1
                                                                   1
```

By assessing the plots, using a normal distribution for the hgt is not an unreasonable idea. Let us change the default imputation method from pmm to norm for the variable hgt.

```
meth <- imp0$method
meth["hgt"] <- "norm"
meth</pre>
```

```
##
                gender
                                                             HDL
         wgt
                             bili
                                         age
                                                  chol
                                                                        hgt
                                                                                 educ
##
                            "pmm"
                                                 "pmm"
                                                           "pmm"
                                                                     "norm"
                                                                               "polr"
                                          WC
##
                   SBP
                          hypten
        race
##
                 "pmm" "logreg"
                                      "mmmg"
```

We do not want to impute negative values of height so we can use the function post() to specify functions that modify the imputed values. With the below syntax all imputed values of hgt that are outside the interval (1.35, 1.95) will be set to those limiting values.

```
post <- imp0$post
post["hgt"] <- "imp[[j]][,i] <- squeeze(imp[[j]][,i], c(1.35, 1.95))"</pre>
```

We can now begin the imputation.

```
imp <- mice(NHANES2, method = meth, maxit = 20, m = 30, seed = 1, printFlag = FALSE)</pre>
```

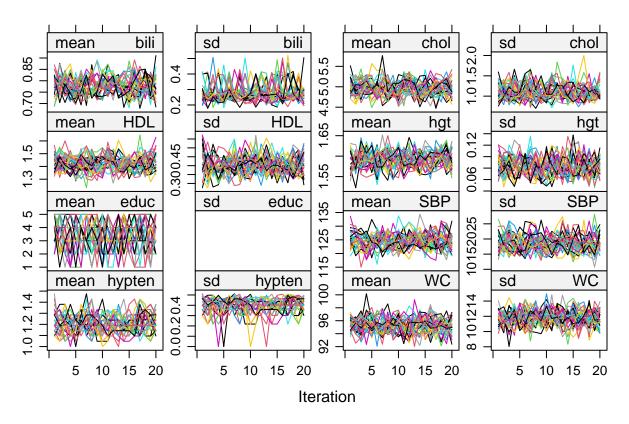
mice() does some pre-processing and removes incomplete variables that are not imputed but act as predictors in other imputation models, it also removes constant variables and variable that are collinear. Checking the loggedEvents contained in our object imp allows us to know if mice() detected any problems during the imputation.

```
imp$loggedEvents
```

NULL

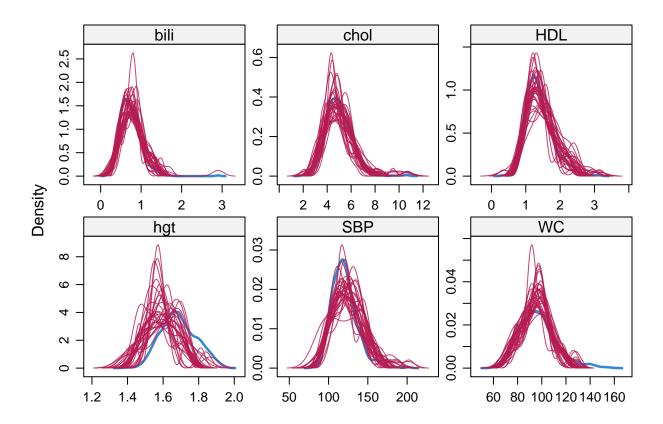
The mean and variance of the imputed values and variable are stored in the elements chainMean and chainVar of the mids object imp. To check that the mice() algorithm has converged, we can plot our object and visualize the trace plots. If the algorithm hasn't converged then there is no guarantee that the results obtained are correct.

```
plot(imp, layout = c(4,4))
```



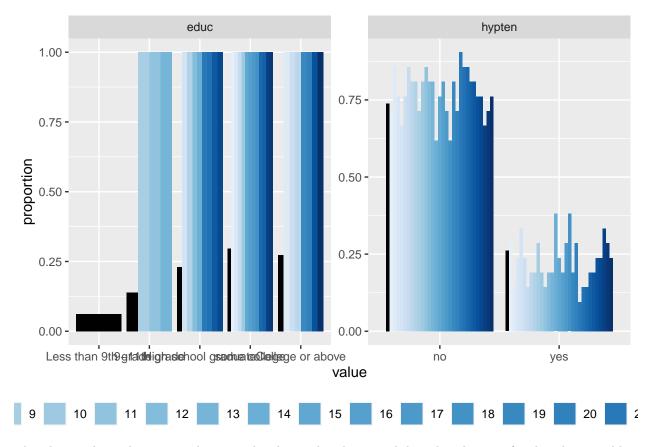
We can see that the iterative algorithm appears to have converged for all variables that were imputed. We can compare the distribution of the imputed values against the distribution of the observed values. For the continuous variables we can use the command densityplot().

densityplot(imp)



We used M=30, and since the density of the observed values are plotted first (blue line), it is difficult to see. The plot which are most different are the ones for SBP and hgt. With regard to categorical variables, we can compare the proportion of values in each category. We can use propplot, implemented by Nicole Erler and available on her github.

propplot(imp)

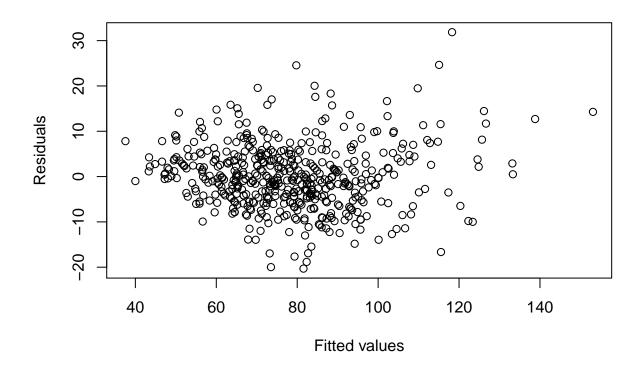


This shows a large discrepancy between the observed and imputed data distributions for the educ variables. However there is only 0.2% of data missing for this variable.

The imputation step was successful, so we can continue to the analysis of the imputed data. The model of interest is (1).

```
fit <- with(imp, lm(wgt ~ gender + age + hgt + WC))

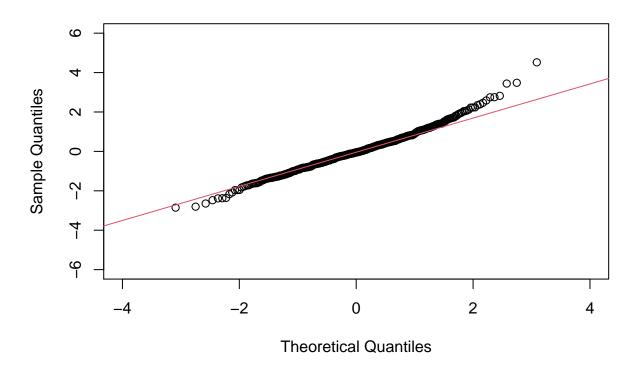
comp1 <- complete(imp, 1)
plot(fit$analyses[[1]]$fitted.values, residuals(fit$analyses[[1]]),
xlab = "Fitted values", ylab = "Residuals")</pre>
```



Doing a QQplot, we can see that nothing looks suspicious.

```
qqnorm(rstandard(fit$analyses[[1]]), xlim = c(-4, 4), ylim = c(-6, 6))
qqline(rstandard(fit$analyses[[1]]), col = 2)
```

Normal Q-Q Plot



Now we can pool the results.

pooled_ests <- pool(fit)</pre>

43.7286611

0.9818873

4

5

```
summary(pooled_ests, conf.int = TRUE)
##
                      estimate std.error
                                                           df
             term
                                           statistic
                                                                    p.value
      (Intercept) -100.6455031 7.61471595 -13.217237 460.5355 0.000000e+00
## 2 genderfemale
                                          -1.652068 458.3258 9.920548e-02
                   -1.3873860 0.83978725
## 3
              age
                    -0.1576518 0.02159588 -7.300087 433.7302 1.384448e-12
## 4
                    52.3207670 4.37203661 11.967138 450.7310 0.000000e+00
              hgt
## 5
               WC
                     1.0258588 0.02237817 45.841943 478.8476 0.000000e+00
##
            2.5 %
                       97.5 %
## 1 -115.6093979 -85.6816083
## 2
       -3.0376968
                    0.2629248
       -0.2000974
## 3
                   -0.1152062
```

```
pool.r.squared(pooled_ests, adjusted = TRUE)
```

```
## est lo 95 hi 95 fmi
## adj R^2 0.8557788 0.8300365 0.8779047 NaN
```

60.9128729

1.0698304