

Homework 9

Data Structures II

Kruskal's method for finding a minimal spanning tree of a weighted undirected graph – Implementation

Here is the algorithm

```
function Kruskal( $G = \langle N, A \rangle$ : graph; length:  $A \rightarrow \mathbb{R}^+$ ): set of edges
    {initialization}
    Sort  $A$  by increasing length
     $n \leftarrow$  the number of nodes in  $N$ 
     $T \leftarrow \emptyset$  {will contain the edges of the minimum spanning tree}
    Initialize  $n$  sets, each containing a different element of  $N$ 
    {greedy loop}
    repeat
         $e \leftarrow \{u, v\} \leftarrow$  shortest edge not yet considered
         $ucomp \leftarrow find(u)$ 
         $vcomp \leftarrow find(v)$ 
        if  $ucomp \neq vcomp$  then
             $merge(ucomp, vcomp)$ 
             $T \leftarrow T \cup \{e\}$ 
    until  $T$  contains  $n - 1$  edges
    return  $T$ 
```

Here is what you are given.

1. A single connected component graph : artist_edges.txt with 819,306 edges and 50,515 vertices.
2. A list of weights for each edge given in weights.txt . Each weight in the text file goes with the edge at the corresponding line number in artist_edges.txt
3. You will use Java's PriorityQueue and union-find algorithms to determine the minimum spanning tree.
4. Your code will return an ArrayList of edges comprising the minimum spanning tree and a double value equal to the sum of the weights of the edges on the minimum spanning tree.
5. For union- find, you will reuse the code we had for HW8 (the third algorithm) and a new algorithm using path-compression. Basically you will do this in two different ways. One is straightforward and the other requires implementation. See chapter 8.