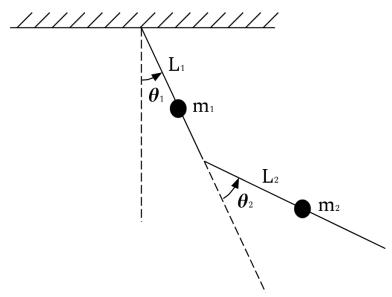
Arm Motion Modeling

System Description

A double-pendulum system hanging in gravity is shown in the figure above. $q = [\theta_1, \theta_2]$ are the system configuration variables. We assume the z-axis is pointing out from the screen/paper, thus the positive direction of rotation is counter-clockwise. The solution steps are:

- 1. Computing the Lagrangian of the system.
- 2. Computing the Euler-Lagrange equations, and solve them for $\ddot{\theta}_1$ and $\ddot{\theta}_2$.
- 3. Numerically evaluating the solutions for τ_1 and τ_2 , and simulating the system for θ_1 , θ_2 , $\dot{\theta}_1$, $\dot{\theta}_2$, $\ddot{\theta}_1$ and $\ddot{\theta}_2$.
- 4. Animating the simulation.





Import Libraries and Define System Constants

Import libraries:

```
In [7]: # Imports required for data processing
        import os
        import csv
        import pandas as pd
        # Imports required for dynamics calculations
        import sympy
        from sympy.abc import t
        from sympy import symbols, Eq, Function, solve, sin, cos, Matrix, Subs, substitution, Derivative,
        import math
        from math import pi
        import numpy as np
        import matplotlib.pyplot as plt
        # Imports required for animation
        from plotly.offline import init_notebook_mode, iplot
        from IPython.display import display, HTML
        import plotly.graph_objects as go
```

```
In [8]: # Masses, length and center-of-mass positions (calculated using the lab measurements)
          # Mass calculations (mass unit is kg)
          # m body = 90.6
                                                            # Average weights for American adult male
                                                            # from "Anthropometric Reference Data for Children and Ad
                                                            # United States, 2015—2018"
         m_body_dict = {'ID': 51, 'JD': 79.5, 'JR': 76, 'KS': 59.3, 'KW': 63.8, 'LC': 61.2,
                            'LD': 97.3, 'LS': 82.2, 'MK': 93.5, 'MV': 98.5, 'SM': 68.5, 'TD': 70,
                            'TM': 66.2}
          \# m_upper_arm = 0.028 * m_body
                                                            # Average upper arm weights relative to body weight, from
                                                            # and Motor Control of Human Movement" by David Winter (2
          m_upper_arm_dict = \{'ID': 0.028 * m_body_dict['ID'], 'JD': 0.028 * m_body_dict['JD'], 
                                   'JR': 0.028 * m_body_dict['JR'], 'KS': 0.028 * m_body_dict['KS'],
                                  'KW': 0.028 * m_body_dict['KW'], 'LC': 0.028 * m_body_dict['LC'], 'LD': 0.028 * m_body_dict['LD'], 'LS': 0.028 * m_body_dict['LS'], 'MK': 0.028 * m_body_dict['MK'], 'MV': 0.028 * m_body_dict['MV'], 'SM': 0.028 * m_body_dict['SM'], 'TD': 0.028 * m_body_dict['TD'],
                                   'TM': 0.028 * m_body_dict['TM']}
          m_lower_arm = 0.7395
                                                         # Average lower prosthetics weights, calculated using lab n
          # Arm length calculations (length unit is m)
          # H body = 1.769
                                                            # Average height for American adult male, from "Height ar
          #
                                                            # index trajectories of school-aged children and adolesce
         #
                                                            # 1985 to 2019 in 200 countries and territories: a pooled
                                                            # of 2181 population-based studies with 65 million partid
         H body dict = {'ID': 1.62, 'JD': 1.76, 'JR': 1.77, 'KS': 1.64, 'KW': 1.62, 'LC': 1.58,
                             'LD': 1.875, 'LS': 1.635, 'MK': 1.78, 'MV': 1.805, 'SM': 1.79, 'TD': 1.69,
                            'TM': 1.735}
          \# L upper arm = 0.186 * H body
                                                            # Average upper arm length relative to body height
                                                            # from "Biomechanics and Motor Control of Human Movement"
                                                            # Winter (2009), 4th edition
         L_upper_arm_dict = {'ID': 0.186 * H_body_dict['ID'], 'JD': 0.186 * H_body_dict['JD'], 

'JR': 0.186 * H_body_dict['JR'], 'KS': 0.186 * H_body_dict['KS'], 

'KW': 0.186 * H_body_dict['KW'], 'LC': 0.186 * H_body_dict['LC'], 

'LD': 0.186 * H_body_dict['LD'], 'LS': 0.186 * H_body_dict['LS'],
                                  'MK': 0.186 * H_body_dict['MK'], 'MV': 0.186 * H_body_dict['MV'],
                                  'SM': 0.186 * H_body_dict['SM'], 'TD': 0.186 * H_body_dict['TD'],
                                   'TM': 0.186 * H body dict['TM']}
          L lower arm = 0.42
                                                         # Average lower prosthetics length, calculated using lab me
          # Arm center of mass length calculations (length unit is m)
          # L_upper_arm_COM = 0.436 * L_upper_arm  # Average upper arm length from shoulder to center of mas
                                                            # to upper arm length, from "Biomechanics and Motor Conti
                                                            # Movement" by David Winter (2009), 4th edition
         'KW': 0.436 * L_upper_arm_dict['KW'], 'LC': 0.436 * L_upper_arm_dict['LC']
'LD': 0.436 * L_upper_arm_dict['LD'], 'LS': 0.436 * L_upper_arm_dict['LS']
'MK': 0.436 * L_upper_arm_dict['MK'], 'MV': 0.436 * L_upper_arm_dict['MV']
'SM': 0.436 * L_upper_arm_dict['SM'], 'TD': 0.436 * L_upper_arm_dict['TD']
                                       'TM': 0.436 * L_upper_arm_dict['TM']}
          L_lower_arm_COM = 0.2388
                                                         # Average lower prosthetics length from elbow to center of
                                                         # calculated using lab measurements
```

Extracting Data

Extracting angles data and computing angular velocities and angular accelerations from the angles:

```
In [10]: def calculate_Vel(Ang_list, time_list, index):
             return ((Ang_list[index + 1] - Ang_list[index])
                   / (time_list[index + 1] - time_list[index]))
         def calculate_Acc(Vel_list, time_list, index):
             return ((Vel_list[index + 1] - Vel_list[index])
                   / (time_list[index + 1] - time_list[index]))
         data_csv_dir = '../../data/control_data/CSV Converted Files'
         frame_frequency = 120
         print("current directory: ", os.getcwd())
         participants_list = []
         time_list = []
         Elbow_Ang_list = []
         Shl_Flex_Ang_list = []
         Elbow_Vel_list = []
         Shl_Flex_Vel_list = []
         Elbow_Acc_list = []
         Shl Flex Acc list = []
         for file in os.listdir(data csv dir):
             file_name = file.split(".")[0]
             participant_name = file.split("_")[0]
             if file.endswith(".csv"):
                 frame = 0
                 file_time_list = []
                 file R Elbow Ang list = []
                 file_R_Shl_Flex_Ang_list = []
                 file_L_Elbow_Ang_list = []
                 file_L_Shl_Flex_Ang_list = []
                 file_R_Elbow_Vel_list = []
                 file_R_Shl_Flex_Vel_list = []
                 file_L_Elbow_Vel_list = []
                 file_L_Shl_Flex_Vel_list = []
                 file_R_Elbow_Acc_list = []
                 file R Shl Flex Acc list = []
                 file L Elbow Acc list = []
                 file_L_Shl_Flex_Acc_list = []
                 data_path = os.path.join(data_csv_dir, file)
                 # Cutting out weird data behavior on data edges
                 if file == 'TD WN7.csv':
                     data_rows = open(data_path).read().strip().split("\n")[40:]
                 elif file == 'TD WN4.csv':
                     data rows = open(data path).read().strip().split("\n")[24:-12]
                 elif file == 'TD_WN11.csv':
                     data rows = open(data path).read().strip().split("\n")[24:-3]
                 else:
                     data rows = open(data_path).read().strip().split("\n")[24:]
                 # Extract time [sec], elbow angles [rad], and shoulder angles [rad] from data
                 for row in data rows:
                     splitted row = row.strip().split("\t")
                     # Check if loop finished all data
                     if len(splitted row) < 80:</pre>
                         break
                     file time list.append(frame/frame frequency)
                     file_R_Elbow_Ang_list.append(float(splitted_row[9]) * 2*pi/360)
                     file R Shl Flex Ang list.append(float(splitted row[11]) * 2*pi/360)
                     file L Elbow Ang list.append(float(splitted row[21]) * 2*pi/360)
                     file_L_Shl_Flex_Ang_list.append(float(splitted_row[23]) * 2*pi/360)
                     frame += 1
```

```
# Extract elbow and shoulder velocities [rad/sec] from angles
for i in range(len(file time list) - 1):
   R_Elbow_Vel = calculate_Vel(file_R_Elbow_Ang_list, file_time_list, i)
   R_Shl_Flex_Vel = calculate_Vel(file_R_Shl_Flex_Ang_list, file_time_list, i)
   L Elbow_Vel = calculate_Vel(file_L_Elbow_Ang_list, file_time_list, i)
   L Shl Flex Vel = calculate Vel(file L Shl Flex Ang list, file time list, i)
   file_R_Elbow_Vel_list.append(R_Elbow_Vel)
   file_R_Shl_Flex_Vel_list.append(R_Shl_Flex_Vel)
   file L Elbow Vel list.append(L Elbow Vel)
   file_L_Shl_Flex_Vel_list.append(L_Shl_Flex_Vel)
# Extract elbow and shoulder Accelerations [rad/sec^2] from velocities
for i in range(len(file time list) - 2):
   R Elbow Acc = calculate Acc(file R Elbow Vel list, file time list, i)
   R_Shl_Flex_Acc = calculate_Acc(file_R_Shl_Flex_Vel_list, file_time_list, i)
   L_Elbow_Acc = calculate_Acc(file_L_Elbow_Vel_list, file_time_list, i)
   L_Shl_Flex_Acc = calculate_Acc(file_L_Shl_Flex_Vel_list, file_time_list, i)
   file R Elbow Acc list.append(R Elbow Acc)
   file R Shl Flex Acc list.append(R Shl Flex Acc)
   file L Elbow Acc list.append(L Elbow Acc)
   file_L_Shl_Flex_Acc_list.append(L_Shl_Flex_Acc)
# Adjust lists length
file_time_list = file_time_list[:-2]
file_R_Elbow_Ang_list = file_R_Elbow_Ang_list[:-2]
file_R_Shl_Flex_Ang_list = file_R_Shl_Flex_Ang_list[:-2]
file_L_Elbow_Ang_list = file_L_Elbow_Ang_list[:-2]
file L Shl Flex Ang list = file L Shl Flex Ang list[:-2]
file_R_Elbow_Vel_list = file_R_Elbow_Vel_list[:-1]
file R Shl Flex Vel list = file R Shl Flex Vel list[:-1]
file_L_Elbow_Vel_list = file_L_Elbow_Vel_list[:-1]
file_L_Shl_Flex_Vel_list = file_L_Shl_Flex_Vel_list[:-1]
participants_list.append(participant_name)
participants_list.append(participant_name)
time_list.append(file_time_list)
time_list.append(file_time_list)
Elbow_Ang_list.append(file_R_Elbow_Ang_list)
Shl_Flex_Ang_list.append(file_R_Shl_Flex_Ang_list)
Elbow_Ang_list.append(file_L_Elbow_Ang_list)
Shl_Flex_Ang_list.append(file_L_Shl_Flex_Ang_list)
Elbow_Vel_list.append(file_R_Elbow_Vel_list)
Shl_Flex_Vel_list.append(file_R_Shl_Flex_Vel_list)
Elbow_Vel_list.append(file_L_Elbow_Vel_list)
Shl Flex Vel list.append(file L Shl Flex Vel list)
Elbow Acc list.append(file R Elbow Acc list)
Shl Flex Acc list.append(file R Shl Flex Acc list)
Elbow_Acc_list.append(file_L_Elbow_Acc_list)
Shl_Flex_Acc_list.append(file_L_Shl_Flex_Acc_list)
```

current directory: /home/yael/Documents/MSR_Courses/ME499-Final_Project/Motorized-Prosthetic-Ar m/motor_control/arm_pendulum_modeling

System Modeling

Computing the Lagrangian of the system:

```
In [11]: m1, m2, g, R1, R1_COM, R2, R2_COM = symbols(r'm1, m2, g, R1, R1_COM, R2, R2_COM')
         # The system torque variables as function of t
         tau1 = Function(r'tau1')(t)
         tau2 = Function(r'tau2')(t)
         # The system configuration variables as function of t
         theta1 = Function(r'theta1')(t)
         theta2 = Function(r'theta2')(t)
         # The velocity as derivative of position wrt t
         theta1_dot = theta1.diff(t)
         theta2_dot = theta2.diff(t)
         # The acceleration as derivative of velocity wrt t
         theta1_ddot = theta1_dot.diff(t)
         theta2_ddot = theta2_dot.diff(t)
         # Converting the polar coordinates to cartesian coordinates
         x1 = R1 COM*sin(theta1)
         x2 = R1*sin(theta1) + R2_COM*sin(theta1 + theta2)
         y1 = -R1 COM*cos(theta1)
         y2 = -R1*cos(theta1) - R2_COM*cos(theta1 + theta2)
         # Calculating the kinetic and potential energy of the system
         KE = \frac{1}{2}m1*((x1.diff(t))**2 + (y1.diff(t))**2) + \frac{1}{2}m2*((x2.diff(t))**2 + (y2.diff(t))**2)
         PE = m1*g*y1 + m2*g*y2
         # Computing the Lagrangian
         L = simplify(KE - PE)
         print('L: ')
         display(L)
         L:
```

 $0.5R_{1COM}^{2}m_{1}\left(\frac{d}{dt}\theta_{1}(t)\right)^{2}+R_{1COM}gm_{1}\cos(\theta_{1}(t))+gm_{2}\left(R_{1}\cos(\theta_{1}(t))+R_{2COM}\cos(\theta_{1}(t)+\theta_{2}(t))\right)$

 $+0.5m_2\left(R_1^2\left(\frac{d}{dt}\theta_1(t)\right)^2+2R_1R_{2COM}\cos\left(\theta_2(t)\right)\left(\frac{d}{dt}\theta_1(t)\right)^2+2R_1R_{2COM}\cos\left(\theta_2(t)\right)\frac{d}{dt}\theta_1(t)\frac{d}{dt}\theta_2(t)+R_{2COM}^2\left(\frac{d}{dt}\theta_1(t)\right)^2\right)$

Computing the Euler-Lagrange equations:

```
In [12]: # Define the derivative of L wrt the functions: x, xdot
         L_dtheta1 = L.diff(theta1)
         L_dtheta2 = L.diff(theta2)
         L_dtheta1_dot = L.diff(theta1_dot)
         L_dtheta2_dot = L.diff(theta2_dot)
         # Define the derivative of L_dxdot wrt to time t
         L_dtheta1_dot_dt = L_dtheta1_dot.diff(t)
         L_dtheta2_dot_dt = L_dtheta2_dot.diff(t)
         # Define the left hand side of the the Euler-Lagrange as a matrix
         lhs = Matrix([simplify(L_dtheta1_dot_dt - L_dtheta1),
                       simplify(L_dtheta2_dot_dt - L_dtheta2)])
         # Define the right hand side of the the Euler-Lagrange as a Matrix
         rhs = Matrix([tau1, tau2])
         # Compute the Euler-Lagrange equations as a matrix
         EL_eqns = Eq(lhs, rhs)
         print('Euler-Lagrange matrix for this systems:')
         display(EL_eqns)
```

Euler-Lagrange matrix for this systems:

$$\begin{bmatrix} 1.0R_{1COM}^2m_1\frac{d^2}{dt^2}\theta_1(t) + R_{1COM}gm_1\sin\left(\theta_1(t)\right) + gm_2\left(R_1\sin\left(\theta_1(t)\right) + R_{2COM}\sin\left(\theta_1(t)\right) + \theta_2(t)\right) \\ + m_2\left(R_1^2\frac{d^2}{dt^2}\theta_1(t) - 2R_1R_{2COM}\sin\left(\theta_2(t)\right)\frac{d}{dt}\theta_1(t)\frac{d}{dt}\theta_2(t) - R_1R_{2COM}\sin\left(\theta_2(t)\right)\left(\frac{d}{dt}\theta_2(t)\right)^2 + 2R_1R_{2COM}\cos\left(\theta_2(t)\right)\frac{d^2}{dt^2}\theta_2(t) \\ + R_{2COM}\frac{d^2}{dt^2}\theta_1(t) + R_{2COM}^2\frac{d^2}{dt^2}\theta_1(t) + R_{2COM}^2\frac{d^2}{dt^2}\theta_2(t)\right) \\ R_{2COM}m_2\left(R_1\sin\left(\theta_2(t)\right)\left(\frac{d}{dt}\theta_1(t)\right)^2 + R_1\cos\left(\theta_2(t)\right)\frac{d^2}{dt^2}\theta_1(t) + R_{2COM}\frac{d^2}{dt^2}\theta_1(t) + R_{2COM}\frac{d^2}{dt^2}\theta_2(t) + g\sin\left(\theta_1(t)\right)\right) \\ R_{2COM}m_2\left(R_1\sin\left(\theta_2(t)\right)\left(\frac{d}{dt}\theta_1(t)\right)^2 + R_1\cos\left(\theta_2(t)\right)\frac{d^2}{dt^2}\theta_1(t) + R_{2COM}\frac{d^2}{dt^2}\theta_1(t) + R_{2COM}\frac{d^2}{dt^2}\theta_2(t) + g\sin\left(\theta_1(t)\right)\right) \\ R_{2COM}m_2\left(R_1\sin\left(\theta_2(t)\right)\left(\frac{d}{dt}\theta_1(t)\right)^2 + R_1\cos\left(\theta_2(t)\right)\frac{d^2}{dt^2}\theta_1(t) + R_{2COM}\frac{d^2}{dt^2}\theta_1(t) + R_{2COM}\frac{d^2}{dt^2}\theta_2(t) + g\sin\left(\theta_1(t)\right)\right) \\ R_{2COM}m_2\left(R_1\sin\left(\theta_2(t)\right)\left(\frac{d}{dt}\theta_1(t)\right)^2 + R_1\cos\left(\theta_2(t)\right)\frac{d^2}{dt^2}\theta_1(t) + R_{2COM}\frac{d^2}{dt^2}\theta_1(t) + R_{2COM}\frac{d^2}{dt^2}\theta_2(t) + g\sin\left(\theta_1(t)\right)\right) \\ R_{2COM}m_2\left(R_1\sin\left(\theta_2(t)\right)\left(\frac{d}{dt}\theta_1(t)\right)^2 + R_1\cos\left(\theta_2(t)\right)\frac{d^2}{dt^2}\theta_1(t) + R_{2COM}\frac{d^2}{dt^2}\theta_1(t) + R_{2COM}\frac{d^2}{dt^2}\theta_2(t) + g\sin\left(\theta_1(t)\right)\right) \\ R_{2COM}m_2\left(R_1\sin\left(\theta_2(t)\right)\left(\frac{d}{dt}\theta_1(t)\right)^2 + R_1\cos\left(\theta_2(t)\right)\frac{d^2}{dt^2}\theta_1(t) + R_{2COM}\frac{d^2}{dt^2}\theta_1(t) + R_{2COM}\frac{d^2}{dt^2}\theta_2(t) + g\sin\left(\theta_1(t)\right)\right) \\ R_{2COM}m_2\left(R_1\sin\left(\theta_2(t)\right)\left(\frac{d}{dt}\theta_1(t)\right)^2 + R_1\cos\left(\theta_2(t)\right)\frac{d^2}{dt^2}\theta_1(t) + R_2\cos\left(\theta_2(t)\right)\frac{d^2}{dt^2}\theta_1(t) + R_2\cos\left(\theta_2(t)$$

Solve the equations for τ_1 and τ_2 :

```
In [13]: # Solve the Euler-Lagrange equations for the shoulder and elbow torques
    T = Matrix([tau1, tau2])
    soln = solve(EL_eqns, T, dict=True)

# Initialize the solutions
    solution = [0, 0]
    i = 0

for sol in soln:
    for v in T:
        solution[i] = simplify(sol[v])
        display(Eq(T[i], solution[i]))
        i =+ 1
```

$$\tau_{1}(t) = R_{1}^{2}m_{2}\frac{d^{2}}{dt^{2}}\theta_{1}(t) - 2.0R_{1}R_{2COM}m_{2}\sin(\theta_{2}(t))\frac{d}{dt}\theta_{1}(t)\frac{d}{dt}\theta_{2}(t) - R_{1}R_{2COM}m_{2}\sin(\theta_{2}(t))\left(\frac{d}{dt}\theta_{2}(t)\right)^{2} + 2.0R_{1}R_{2COM}m_{2}\sin(\theta_{2}(t))\frac{d^{2}}{dt^{2}}\theta_{1}(t) + R_{1}R_{2COM}m_{2}\cos(\theta_{2}(t))\frac{d^{2}}{dt^{2}}\theta_{2}(t) + R_{1}gm_{2}\sin(\theta_{1}(t)) + R_{1COM}^{2}m_{1}\frac{d^{2}}{dt^{2}}\theta_{1}(t) + R_{1COM}gm_{1}\sin(\theta_{1}(t)) + R_{2COM}m_{2}\frac{d^{2}}{dt^{2}}\theta_{2}(t) + R_{2COM}gm_{2}\sin(\theta_{1}(t) + \theta_{2}(t))$$

$$\tau_{2}(t) = R_{2COM} m_{2} \left(R_{1} \sin{(\theta_{2}(t))} \left(\frac{d}{dt} \theta_{1}(t) \right)^{2} + R_{1} \cos{(\theta_{2}(t))} \frac{d^{2}}{dt^{2}} \theta_{1}(t) + R_{2COM} \frac{d^{2}}{dt^{2}} \theta_{1}(t) + R_{2COM} \frac{d^{2}}{dt^{2}} \theta_{2}(t) + g \sin{(\theta_{1}(t))} \theta_{2}(t) + g \sin{(\theta_{2}(t))} \theta_{2}(t) + g \sin{(\theta_{1}(t))} \theta_{2}(t) + g \sin{(\theta_{2}(t))} \theta_{2}(t) + g \sin{(\theta_$$

4 ∥



```
In [14]: # Substitute the derivative variables with a dummy variables and plug-in the constants
         solution_0_subs = solution[0]
         solution_1_subs = solution[1]
         theta1 dot dummy = symbols('dtheta1')
         theta2_dot_dummy = symbols('dtheta2')
         theta1_ddot_dummy = symbols('ddtheta1')
         theta2_ddot_dummy = symbols('ddtheta2')
         solution_0_subs = solution_0_subs.subs([(g, 9.81)])
         solution_1_subs = solution_1_subs.subs([(g, 9.81)])
         solution_0\_subs = solution_0\_subs.subs([((thetal.diff(t)).diff(t), thetal_ddot_dummy), thetal_ddot_dummy))
         ((theta2.diff(t)).diff(t), theta2_ddot_dummy)])
solution_1_subs = solution_1_subs.subs([((theta1.diff(t)).diff(t), theta1_ddot_dummy),
                                                   ((theta2.diff(t)).diff(t), theta2_ddot_dummy)])
         solution_0_subs = solution_0_subs.subs([(thetal.diff(t), thetal_dot_dummy),
                                                   (theta2.diff(t), theta2_dot_dummy)])
         solution_1_subs = solution_1_subs.subs([(theta1.diff(t), theta1_dot_dummy),
                                                   (theta2.diff(t), theta2_dot_dummy)])
         # Lambdify the thetas and its derivatives
         func1 = lambdify([theta1, theta2, theta1_dot_dummy, theta2_dot_dummy, theta1_ddot_dummy,
                            theta2_ddot_dummy, m1, m2, R1, R2, R1_COM, R2_COM], solution_0_subs, modules = $
         func2 = lambdify([theta1, theta2, theta1_dot_dummy, theta2_dot_dummy, theta1_ddot_dummy,
                            theta2_ddot_dummy, m1, m2, R1, R2, R1_COM, R2_COM], solution_1_subs, modules = $
         # Initialize the torque and power lists
         Shl_Flex_tau_list, Elbow_tau_list = [], []
         Shl_Flex_power_list, Elbow_power_list = [], []
         for i in range(len(time_list)):
             # Initialize the torque and power lists
             tau1_list, tau2_list = [], []
             power1_list, power2_list = [], []
             t_list = time_list[i]
             theta1_list = Shl_Flex_Ang_list[i]
             theta2_list = Elbow_Ang_list[i]
             dtheta1 list = Shl Flex Vel list[i]
             dtheta2 list = Elbow Vel list[i]
             ddtheta1_list = Shl_Flex_Acc_list[i]
             ddtheta2_list = Elbow_Acc_list[i]
             # Plug-in the angles, angular velocities and angular accelerations for every time step to find
             for j in range(len(t list)):
                 taul_list.append(func1(thetal_list[j], theta2_list[j], dtheta1_list[j], dtheta2_list[j],
                                         ddtheta1_list[j], ddtheta2_list[j], m_upper_arm_dict[participants_l
                                         m_lower_arm, L_upper_arm_dict[participants_list[i]], L_lower_arm,
                                         L_upper_arm_COM_dict[participants_list[i]], L_lower_arm_COM))
                 tau2_list.append(func2(theta1_list[j], theta2_list[j], dtheta1_list[j], dtheta2_list[j],
                                         ddtheta1_list[j], ddtheta2_list[j], m_upper_arm_dict[participants_l
                                         m_lower_arm, L_upper_arm_dict[participants_list[i]], L_lower_arm,
                                         L_upper_arm_COM_dict[participants_list[i]], L_lower_arm_COM))
                 # Calculate the power required to reach the required angular velocities and joints torques
                 power1 list.append(dtheta1 list[j] * tau1 list[j])
                 power2_list.append(dtheta2_list[j] * tau2_list[j])
             Shl_Flex_tau_list.append(tau1_list)
             Elbow_tau_list.append(tau2_list)
             Shl_Flex_power_list.append(power1_list)
             Elbow power list.append(power2 list)
             print(f"Trial {i}/{len(time_list)-1} finished \t maximum torque is {format(max(tau2_list),
```

```
Trial 0/203 finished
                         maximum torque is 1.929 [Nm]
                                                          maximum power is 0.968 [W]
Trial 1/203 finished
                         maximum torque is 2.216 [Nm]
                                                          maximum power is 2.258 [W]
Trial 2/203 finished
                         maximum torque is 3.126 [Nm]
                                                          maximum power is 3.431 [W]
Trial 3/203 finished
                         maximum torque is 3.753 [Nm]
                                                          maximum power is 2.448 [W]
Trial 4/203 finished
                         maximum torque is 2.113 [Nm]
                                                          maximum power is 2.634 [W]
Trial 5/203 finished
                         maximum torque is 2.409 [Nm]
                                                          maximum power is 4.074 [W]
Trial 6/203 finished
                         maximum torque is 1.745 [Nm]
                                                          maximum power is 2.063 [W]
Trial 7/203 finished
                         maximum torque is 2.379 [Nm]
                                                          maximum power is 1.769 [W]
Trial 8/203 finished
                         maximum torque is 2.085 [Nm]
                                                          maximum power is 1.952 [W]
Trial 9/203 finished
                         maximum torque is 2.202 [Nm]
                                                          maximum power is 1.177 [W]
Trial 10/203 finished
                         maximum torque is 2.498 [Nm]
                                                          maximum power is 2.797 [W]
Trial 11/203 finished
                         maximum torque is 3.138 [Nm]
                                                          maximum power is 3.980 [W]
Trial 12/203 finished
                         maximum torque is 1.827
                                                          maximum power is 2.661 [W]
                                                  [Nm]
Trial 13/203 finished
                         maximum torque is 1.831
                                                  [Nm]
                                                          maximum power is 1.548 [W]
Trial 14/203 finished
                         maximum torque is 2.643
                                                  [Nm]
                                                          maximum power is 2.506 [W]
Trial 15/203 finished
                         maximum torque is 1.949 [Nm]
                                                          maximum power is 1.771 [W]
Trial 16/203 finished
                         maximum torque is 2.293 [Nm]
                                                          maximum power is 2.658 [W]
Trial 17/203 finished
                         maximum torque is 2.320 [Nm]
                                                          maximum power is 4.121 [W]
Trial 18/203 finished
                         maximum torque is 1.781 [Nm]
                                                          maximum power is 2.715 [W]
Trial 19/203 finished
                         maximum torque is 2.058 [Nm]
                                                          maximum power is 3.501 [W]
Trial 20/203 finished
                         maximum torque is 2.971 [Nm]
                                                          maximum power is 1.741 [W]
Trial 21/203 finished
                         maximum torque is 2.432 [Nm]
                                                          maximum power is 3.929 [W]
Trial 22/203 finished
                         maximum torque is 2.289 [Nm]
                                                          maximum power is 2.062 [W]
Trial 23/203 finished
                         maximum torque is 1.933 [Nm]
                                                          maximum power is 1.531 [W]
Trial 24/203 finished
                         maximum torque is 2.088 [Nm]
                                                          maximum power is 1.166 [W]
Trial 25/203 finished
                         maximum torque is 2.189 [Nm]
                                                          maximum power is 2.242 [W]
Trial 26/203 finished
                         maximum torque is 1.683 [Nm]
                                                          maximum power is 2.473 [W]
Trial 27/203 finished
                         maximum torque is 1.957 [Nm]
                                                          maximum power is 1.527 [W]
                                                          maximum power is 1.911 [W]
Trial 28/203 finished
                         maximum torque is 1.939 [Nm]
Trial 29/203 finished
                                                          maximum power is 1.182 [W]
                         maximum torque is 1.862 [Nm]
Trial 30/203 finished
                         maximum torque is 1.635 [Nm]
                                                          maximum power is 2.278 [W]
Trial 31/203 finished
                         maximum torque is 1.577
                                                          maximum power is 1.567 [W]
                                                  [ Nm ]
Trial 32/203 finished
                         maximum torque is 2.348 [Nm]
                                                          maximum power is 2.592 [W]
Trial 33/203 finished
                         maximum torque is 2.109 [Nm]
                                                          maximum power is 4.635 [W]
                         maximum torque is 1.919 [Nm]
Trial 34/203 finished
                                                          maximum power is 1.520 [W]
Trial 35/203 finished
                         maximum torque is 2.203 [Nm]
                                                          maximum power is 2.940 [W]
Trial 36/203 finished
                         maximum torque is 1.815 [Nm]
                                                          maximum power is 1.817 [W]
                                                          maximum power is 1.380 [W]
Trial 37/203 finished
                         maximum torque is 1.562 [Nm]
                                                          maximum power is 1.619 [W]
Trial 38/203 finished
                         maximum torque is 1.874 [Nm]
Trial 39/203 finished
                         maximum torque is 2.076 [Nm]
                                                          maximum power is 2.065 [W]
Trial 40/203 finished
                         maximum torque is 2.057 [Nm]
                                                          maximum power is 1.557 [W]
Trial 41/203 finished
                         maximum torque is 2.135 [Nm]
                                                          maximum power is 1.611 [W]
Trial 42/203 finished
                         maximum torque is 1.656 [Nm]
                                                          maximum power is 2.253 [W]
Trial 43/203 finished
                         maximum torque is 1.767 [Nm]
                                                          maximum power is 1.735 [W]
Trial 44/203 finished
                         maximum torque is 3.006 [Nm]
                                                          maximum power is 1.578 [W]
Trial 45/203 finished
                         maximum torque is 3.526 [Nm]
                                                          maximum power is 2.605 [W]
Trial 46/203 finished
                                                          maximum power is 1.060 [W]
                         maximum torque is 2.130 [Nm]
Trial 47/203 finished
                         maximum torque is 2.309 [Nm]
                                                          maximum power is 2.922 [W]
Trial 48/203 finished
                                                          maximum power is 2.193 [W]
                         maximum torque is 2.114 [Nm]
Trial 49/203 finished
                         maximum torque is 1.601 [Nm]
                                                          maximum power is 1.672 [W]
Trial 50/203 finished
                         maximum torque is 3.968 [Nm]
                                                          maximum power is 3.813 [W]
Trial 51/203 finished
                         maximum torque is 3.439 [Nm]
                                                          maximum power is 4.145 [W]
Trial 52/203 finished
                         maximum torque is 2.384 [Nm]
                                                          maximum power is 1.641 [W]
Trial 53/203 finished
                         maximum torque is 1.807 [Nm]
                                                          maximum power is 1.430 [W]
Trial 54/203 finished
                         maximum torque is 1.781 [Nm]
                                                          maximum power is 2.892 [W]
                                                          maximum power is 2.061 [W]
Trial 55/203 finished
                         maximum torque is 1.731 [Nm]
Trial 56/203 finished
                         maximum torque is 2.325 [Nm]
                                                          maximum power is 2.868 [W]
Trial 57/203 finished
                         maximum torque is 2.276 [Nm]
                                                          maximum power is 4.228 [W]
Trial 58/203 finished
                         maximum torque is 2.123 [Nm]
                                                          maximum power is 2.077 [W]
Trial 59/203 finished
                         maximum torque is 2.041 [Nm]
                                                          maximum power is 1.953 [W]
Trial 60/203 finished
                         maximum torque is 2.244 [Nm]
                                                          maximum power is 1.126 [W]
Trial 61/203 finished
                         maximum torque is 2.346 [Nm]
                                                          maximum power is 2.143 [W]
Trial 62/203 finished
                         maximum torque is 3.548 [Nm]
                                                          maximum power is 2.410 [W]
Trial 63/203 finished
                         maximum torque is 3.619 [Nm]
                                                          maximum power is 2.826 [W]
Trial 64/203 finished
                         maximum torque is 2.534 [Nm]
                                                          maximum power is 2.340 [W]
Trial 65/203 finished
                                                          maximum power is 4.337 [W]
                         maximum torque is 2.335 [Nm]
Trial 66/203 finished
                                                          maximum power is 1.505 [W]
                         maximum torque is 1.971 [Nm]
Trial 67/203 finished
                         maximum torque is 2.061 [Nm]
                                                          maximum power is 2.517 [W]
Trial 68/203 finished
                         maximum torque is 2.376 [Nm]
                                                          maximum power is 3.009 [W]
```

```
maximum power is 4.121 [W]
Trial 69/203 finished
                         maximum torque is 2.875 [Nm]
Trial 70/203 finished
                         maximum torque is 1.904 [Nm]
                                                          maximum power is 1.072 [W]
Trial 71/203 finished
                         maximum torque is 1.942 [Nm]
                                                          maximum power is 1.714 [W]
Trial 72/203 finished
                         maximum torque is 2.201 [Nm]
                                                          maximum power is 1.443 [W]
                                                          maximum power is 1.718 [W]
Trial 73/203 finished
                         maximum torque is 2.129 [Nm]
Trial 74/203 finished
                         maximum torque is 1.974 [Nm]
                                                          maximum power is 1.706 [W]
Trial 75/203 finished
                         maximum torque is 1.978 [Nm]
                                                          maximum power is 2.523 [W]
                                                          maximum power is 1.152 [W]
Trial 76/203 finished
                         maximum torque is 2.469 [Nm]
Trial 77/203 finished
                         maximum torque is 2.401 [Nm]
                                                          maximum power is 1.364 [W]
Trial 78/203 finished
                         maximum torque is 1.861 [Nm]
                                                          maximum power is 1.752 [W]
Trial 79/203 finished
                         maximum torque is 1.875 [Nm]
                                                          maximum power is 1.706 [W]
Trial 80/203 finished
                         maximum torque is 2.243 [Nm]
                                                          maximum power is 2.217 [W]
Trial 81/203 finished
                         maximum torque is 2.522 [Nm]
                                                          maximum power is 4.007 [W]
Trial 82/203 finished
                         maximum torque is 2.391 [Nm]
                                                          maximum power is 2.629 [W]
Trial 83/203 finished
                         maximum torque is 2.542 [Nm]
                                                          maximum power is 4.609 [W]
Trial 84/203 finished
                         maximum torque is 2.741 [Nm]
                                                          maximum power is 1.506 [W]
                                                          maximum power is 1.294 [W]
Trial 85/203 finished
                         maximum torque is 2.333 [Nm]
Trial 86/203 finished
                         maximum torque is 2.170 [Nm]
                                                          maximum power is 2.756 [W]
Trial 87/203 finished
                         maximum torque is 2.589 [Nm]
                                                          maximum power is 4.681 [W]
Trial 88/203 finished
                         maximum torque is 2.358 [Nm]
                                                          maximum power is 2.869 [W]
Trial 89/203 finished
                         maximum torque is 1.987 [Nm]
                                                          maximum power is 1.439 [W]
Trial 90/203 finished
                         maximum torque is 2.278 [Nm]
                                                          maximum power is 2.368 [W]
Trial 91/203 finished
                         maximum torque is 2.525 [Nm]
                                                          maximum power is 2.188 [W]
Trial 92/203 finished
                         maximum torque is 2.173 [Nm]
                                                          maximum power is 1.750 [W]
Trial 93/203 finished
                         maximum torque is 1.912 [Nm]
                                                          maximum power is 0.842 [W]
                         maximum torque is 2.015 [Nm]
Trial 94/203 finished
                                                          maximum power is 2.232 [W]
Trial 95/203 finished
                         maximum torque is 2.040 [Nm]
                                                          maximum power is 3.430 [W]
Trial 96/203 finished
                         maximum torque is 1.774 [Nm]
                                                          maximum power is 1.637 [W]
Trial 97/203 finished
                         maximum torque is 1.556 [Nm]
                                                          maximum power is 1.528 [W]
Trial 98/203 finished
                         maximum torque is 2.215 [Nm]
                                                          maximum power is 3.812 [W]
Trial 99/203 finished
                         maximum torque is 2.002 [Nm]
                                                          maximum power is 3.090 [W]
Trial 100/203 finished
                         maximum torque is 2.126 [Nm]
                                                          maximum power is 2.131 [W]
Trial 101/203 finished
                         maximum torque is 2.360 [Nm]
                                                          maximum power is 3.469 [W]
Trial 102/203 finished
                         maximum torque is 1.947 [Nm]
                                                          maximum power is 1.375 [W]
                         maximum torque is 1.990 [Nm]
Trial 103/203 finished
                                                          maximum power is 2.304 [W]
Trial 104/203 finished
                         maximum torque is 2.212 [Nm]
                                                          maximum power is 3.225 [W]
Trial 105/203 finished
                         maximum torque is 3.599 [Nm]
                                                          maximum power is 4.341 [W]
Trial 106/203 finished
                         maximum torque is 2.234 [Nm]
                                                          maximum power is 2.158 [W]
Trial 107/203 finished
                         maximum torque is 2.002 [Nm]
                                                          maximum power is 1.892 [W]
Trial 108/203 finished
                         maximum torque is 2.106 [Nm]
                                                          maximum power is 2.203 [W]
Trial 109/203 finished
                         maximum torque is 1.893 [Nm]
                                                          maximum power is 0.919 [W]
Trial 110/203 finished
                         maximum torque is 2.191 [Nm]
                                                          maximum power is 1.887 [W]
Trial 111/203 finished
                         maximum torque is 2.268 [Nm]
                                                          maximum power is 1.469 [W]
                         maximum torque is 1.966 [Nm]
Trial 112/203 finished
                                                          maximum power is 1.381 [W]
Trial 113/203 finished
                         maximum torque is 2.072 [Nm]
                                                          maximum power is 2.131 [W]
Trial 114/203 finished
                                                          maximum power is 1.739 [W]
                         maximum torque is 2.578 [Nm]
Trial 115/203 finished
                         maximum torque is 1.988 [Nm]
                                                          maximum power is 1.013 [W]
Trial 116/203 finished
                         maximum torque is 2.339 [Nm]
                                                          maximum power is 1.967 [W]
Trial 117/203 finished
                         maximum torque is 2.146 [Nm]
                                                          maximum power is 2.601 [W]
Trial 118/203 finished
                         maximum torque is 2.098 [Nm]
                                                          maximum power is 1.906 [W]
Trial 119/203 finished
                         maximum torque is 1.820 [Nm]
                                                          maximum power is 1.798 [W]
Trial 120/203 finished
                         maximum torque is 3.030 [Nm]
                                                          maximum power is 2.246 [W]
Trial 121/203 finished
                         maximum torque is 2.473 [Nm]
                                                          maximum power is 2.025 [W]
Trial 122/203 finished
                         maximum torque is 2.410 [Nm]
                                                          maximum power is 3.457 [W]
Trial 123/203 finished
                         maximum torque is 2.514 [Nm]
                                                          maximum power is 5.727 [W]
Trial 124/203 finished
                         maximum torque is 2.730 [Nm]
                                                          maximum power is 2.621 [W]
Trial 125/203 finished
                         maximum torque is 4.763 [Nm]
                                                          maximum power is 7.720 [W]
Trial 126/203 finished
                         maximum torque is 2.091 [Nm]
                                                          maximum power is 2.594 [W]
                                                          maximum power is 3.097 [W]
Trial 127/203 finished
                         maximum torque is 2.475 [Nm]
Trial 128/203 finished
                         maximum torque is 2.455 [Nm]
                                                          maximum power is 1.926 [W]
Trial 129/203 finished
                         maximum torque is 1.996 [Nm]
                                                          maximum power is 1.769 [W]
Trial 130/203 finished
                         maximum torque is 2.532 [Nm]
                                                          maximum power is 1.744 [W]
Trial 131/203 finished
                                                          maximum power is 2.392 [W]
                         maximum torque is 2.613 [Nm]
Trial 132/203 finished
                                                          maximum power is 2.620 [W]
                         maximum torque is 2.044 [Nm]
Trial 133/203 finished
                                                          maximum power is 1.610 [W]
                         maximum torque is 1.554 [Nm]
Trial 134/203 finished
                         maximum torque is 2.198 [Nm]
                                                          maximum power is 2.649 [W]
Trial 135/203 finished
                         maximum torque is 1.966 [Nm]
                                                          maximum power is 1.637 [W]
Trial 136/203 finished
                         maximum torque is 2.294 [Nm]
                                                          maximum power is 2.665 [W]
Trial 137/203 finished
                         maximum torque is 2.576 [Nm]
                                                          maximum power is 4.996 [W]
```

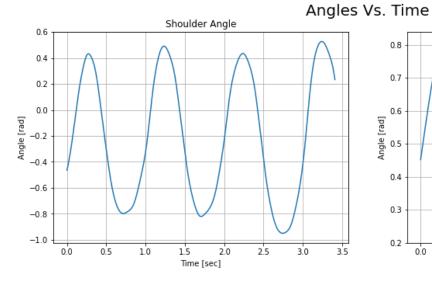
Trial 138/203	finished	maximum	torque	is	2.785	[Nm]	maximum	nower	is	2.246	ſW1
Trial 139/203		maximum	•				maximum	•			
Trial 140/203		maximum					maximum	•			
Trial 141/203		maximum					$\max_{\cdot} \max$				
Trial 142/203		maximum					maximum				
Trial 143/203	finished	maximum	torque	is	2.086	[Nm]	maximum	power	is	3.021	[W]
Trial 144/203	finished	maximum	torque	is	2.387	[Nm]	maximum	power	is	0.947	[W]
Trial 145/203	finished	maximum					maximum	•			
Trial 146/203		maximum					maximum	•			
Trial 147/203		maximum					maximum				
Trial 148/203		maximum					$\max_{\cdot} \max$	•			
Trial 149/203		maximum	•				maximum	•			
Trial 150/203	finished	maximum	torque	is	1.823	[Nm]	maximum	power	is	1.170	[W]
Trial 151/203	finished	maximum	torque	is	2.183	[Nm]	maximum	power	is	1.349	[W]
Trial 152/203	finished	maximum	torque	is	2.172	[Nm]	${\tt maximum}$	power	is	2.224	[W]
Trial 153/203		maximum					maximum				
Trial 154/203		maximum					maximum	•			
								•			
Trial 155/203		maximum					maximum	•			
Trial 156/203		maximum					maximum				
Trial 157/203		maximum					maximum				
Trial 158/203	finished	maximum	torque	is	2.351	[Nm]	maximum	power	is	1.031	[W]
Trial 159/203	finished	maximum	torque	is	2.428	[Nm]	maximum	power	is	1.585	[W]
Trial 160/203	finished	maximum					maximum	power	is	1.369	[W]
Trial 161/203		maximum	•				maximum	•			
Trial 162/203		maximum					maximum				
Trial 163/203		$\max_{\cdot} \max$					$\max_{\cdot} \max$	•			
Trial 164/203		maximum					maximum				
Trial 165/203	finished	maximum	torque	is	2.354	[Nm]	${\tt maximum}$				
Trial 166/203	finished	maximum	torque	is	2.030	[Nm]	maximum	power	is	1.526	[W]
Trial 167/203	finished	maximum	torque	is	2.073	[Nm]	${\tt maximum}$	power	is	2.896	[W]
Trial 168/203		maximum					maximum				
Trial 169/203		maximum					maximum				
Trial 170/203		maximum					maximum	•			
								•			
Trial 171/203		maximum					maximum				
Trial 172/203		maximum					maximum	•			
Trial 173/203		maximum					maximum				
Trial 174/203	finished	maximum	torque	is	2.013	[Nm]	maximum	power	is	1.113	[W]
Trial 175/203	finished	maximum	torque	is	2.360	[Nm]	maximum				
Trial 176/203		maximum					maximum	•			
Trial 177/203		maximum					maximum				
Trial 178/203		maximum					maximum				
Trial 179/203		$\max_{\cdot} \max$					$\max_{\cdot} \max$				
Trial 180/203		maximum					maximum				
Trial 181/203		maximum	torque	is	1.920	[Nm]	maximum				
Trial 182/203	finished	maximum	torque	is	2.279	[Nm]	maximum	power	is	2.805	[W]
Trial 183/203	finished	maximum	torque	is	2.452	[Nm]	${\tt maximum}$	power	is	2.878	[W]
Trial 184/203		maximum					maximum				
Trial 185/203		maximum					maximum				
Trial 186/203		maximum					maximum	-			
Trial 187/203		maximum					$\max_{\cdot} \max$				
Trial 188/203		maximum					maximum				
Trial 189/203		maximum					${\tt maximum}$				
Trial 190/203	finished	maximum	torque	is	2.553	[Nm]	maximum	power	is	2.004	[W]
Trial 191/203	finished	maximum	torque	is	1.659	[Nm]	maximum	power	is	2.123	[W]
Trial 192/203		maximum					maximum				
Trial 193/203		maximum					maximum				
Trial 194/203		maximum					maximum				
Trial 195/203		maximum					maximum				
Trial 196/203		maximum					maximum	•			
Trial 197/203		${\tt maximum}$					maximum				
Trial 198/203	finished	maximum	torque	is	1.963	[Nm]	${\tt maximum}$	power	is	3.649	[W]
Trial 199/203		maximum					maximum				
Trial 200/203		maximum					maximum				
Trial 201/203		maximum					maximum				
11146 201/203	. Initiation	GATIIIUIII	201 que		Z 1 Z 7 J	[1411]	GATIIIUIII	POWCI	_3	2.517	r **]
Trial 202/203	finished	maximum	torque	ic	1 5/16	[Nm]	maximum	nower	ic	1 621	[/]
Trial 203/203	THITSHED	maximum	corque	тЭ	T.002	[וזווו]	maximum	hower	Τ2	1.302	[M]

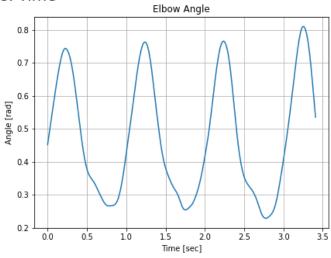
```
In [22]: # print(f"Shoulder max angular velocity:\t{format(max(dtheta1_list), '.3f')} [rad/sec]\t\t Shoulde
                   # print(f"Shoulder max angular velocity:\t{format(max(dtheta1_list)*60/(2*pi), '.3f')} [rpm]\t\t $
                   # print(f"Elbow max angular velocity:\t{format(max(dtheta2_list), '.3f')} [rad/sec]\t\t Elbow aver
                   # print(f"Elbow max angular velocity:\t{format(max(dtheta2_list)*60/(2*pi), '.3f')} [rpm]\t\t Elbo
                   # print(f"Shoulder max torque:\t\t{format(max(tau1_list), '.3f')} [Nm]\t\t Shoulder average torque
                   # print(f"Elbow max torque: \t \t {format(max(tau2_list), '.3f')} [Nm] \t \t Elbow average torque: \t \t \t \
                   # print(f"Shoulder max power:\t\t{format(max(power1_list), '.3f')} [W]\t\t Shoulder average power:
                   # print(f"Elbow max power:\t\t{format(max(power2_list), '.3f')} [W]\t\t Elbow average power:\t\t\t
                   max_Elbow_tau, max_Elbow_power, max_Elbow_Vel = 0, 0, 0
                   max_Elbow_tau_index, max_Elbow_power_index, max_Elbow_Vel_index = 0, 0, 0
                   for i in range(len(Elbow_tau_list)):
                            if max Elbow Vel < max(Elbow Vel list[i]):</pre>
                                    max_Elbow_Vel = max(Elbow_Vel_list[i])
                                    max_Elbow_Vel_index = i
                            if max_Elbow_tau < max(Elbow_tau_list[i]):</pre>
                                    max_Elbow_tau = max(Elbow_tau_list[i])
                                    max_Elbow_tau_index = i
                            if max Elbow power < max(Elbow power list[i]):</pre>
                                    max_Elbow_power = max(Elbow_power_list[i])
                                    max_Elbow_power_index = i
                   print(f"maximum elbow angular velocity is {format(max_Elbow_Vel, '.3f')} [rad/sec] ({format(max_Elbow_Vel, '.3f')}
                   print(f"maximum elbow torque is {format(max_Elbow_tau, '.3f')} [Nm], in trial {max_Elbow_tau_index
print(f"maximum elbow power is {format(max_Elbow_power, '.3f')} [W], in trial {max_Elbow_power_inc}
                   # The torque equations for the maximum power:
                   solution_0_subs = solution_0_subs.subs([(m1, m_upper_arm_dict[participants_list[max_Elbow_tau_inde
                   solution_1_subs = solution_1_subs.subs([(m1, m_upper_arm_dict[participants_list[max_Elbow_tau_inde
                   print("\nThe torque equations for the maximum torque:")
                   display(Eq(T[0], solution_0_subs))
                   display(Eq(T[1], solution_1_subs))
                   maximum elbow angular velocity is 4.143 [rad/sec] (39.560 [rpm]), in trial 69
                   maximum elbow torque is 4.763 [Nm], in trial 125
                   maximum elbow power is 7.720 [W], in trial 125
                   The torque equations for the maximum torque:
                   \tau_1(t) = 0.111020235768ddtheta_1\cos(\theta_2(t)) + 0.152055338724674ddtheta_1 + 0.055510117884ddtheta_2\cos(\theta_2(t))
                   +0.04217031288 ddtheta_2 - 0.111020235768 dtheta_1 dtheta_2 \sin(\theta_2(t)) - 0.055510117884 dtheta_2^2 \sin(\theta_2(t)) + 1.7323768 dtheta_2^2
                   (\theta_1(t) + \theta_2(t)) + 4.915563608124 \sin(\theta_1(t))
                   \tau_2(t) = 0.055510117884ddtheta_1\cos(\theta_2(t)) + 0.04217031288ddtheta_1 + 0.04217031288ddtheta_2 + 0.055510117884ddtheta_2
                   +1.732373406\sin(\theta_1(t)+\theta_2(t))
```

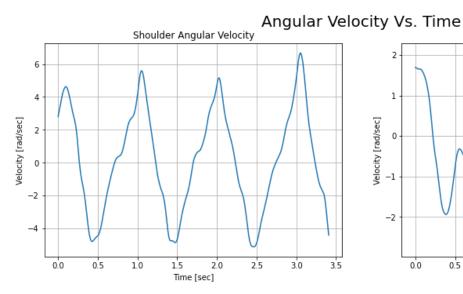
Example for the trial with the largest elbow torque & power:

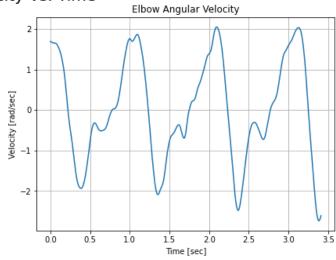
```
In [25]: index = 125
         t_list = time_list[index]
         theta1_list = Shl_Flex_Ang_list[index]
         theta2_list = Elbow_Ang_list[index]
         dtheta1 list = Shl Flex Vel list[index]
         dtheta2_list = Elbow_Vel_list[index]
         ddtheta1_list = Shl_Flex_Acc_list[index]
         ddtheta2_list = Elbow_Acc_list[index]
         tau1_list = Shl_Flex_tau_list[index]
         tau2_list = Elbow_tau_list[index]
         power1_list = Shl_Flex_power_list[index]
         power2_list = Elbow_power_list[index]
         # Compute the trajectory of the arm's motion
         N = int((max(t_list) - min(t_list))/(1/frame_frequency))
         tvec = np.linspace(min(t_list), max(t_list), N)
         traj = np.zeros((6, N))
         for i in range(N):
             traj[0, i] = theta1_list[i]
              traj[1, i] = theta2_list[i]
              traj[2, i] = dtheta1_list[i]
              traj[3, i] = dtheta2_list[i]
             traj[4, i] = ddthetal_list[i]
              traj[5, i] = ddtheta2_list[i]
         # Calculate the length difference between the time list and the trajectory lists
         diff = (len(t_list) - len(traj[0]))
         # Plot the trajectory lists (angles, velocities, accelerations, torques, and power)
         plt.figure(figsize=(15,5))
         plt.suptitle('Angles Vs. Time', fontsize=20)
         plt.subplot(121)
         plt.plot(t_list[:-diff], traj[0])
         plt.ylabel('Angle [rad]')
         plt.xlabel('Time [sec]')
         plt.grid()
         plt.title('Shoulder Angle')
         plt.subplot(122)
         plt.plot(t list[:-diff], traj[1])
         plt.ylabel('Angle [rad]')
         plt.xlabel('Time [sec]')
         plt.grid()
         plt.title('Elbow Angle')
         plt.show()
         plt.figure(figsize=(15,5))
         plt.suptitle('Angular Velocity Vs. Time', fontsize=20)
         plt.subplot(121)
         plt.plot(t_list[:-diff], traj[2])
plt.ylabel('Velocity [rad/sec]')
         plt.xlabel('Time [sec]')
         plt.grid()
         plt.title('Shoulder Angular Velocity')
         plt.subplot(122)
         plt.plot(t_list[:-diff], traj[3])
         plt.ylabel('Velocity [rad/sec]')
         plt.xlabel('Time [sec]')
         plt.grid()
         plt.title('Elbow Angular Velocity')
         plt.show()
         plt.figure(figsize=(15,5))
         plt.suptitle('Angular Acceleration Vs. Time', fontsize=20)
         plt.subplot(121)
         plt.plot(t_list[:-diff], traj[4])
plt.ylabel('Acceleration [rad/sec^2]')
         plt.xlabel('Time [sec]')
```

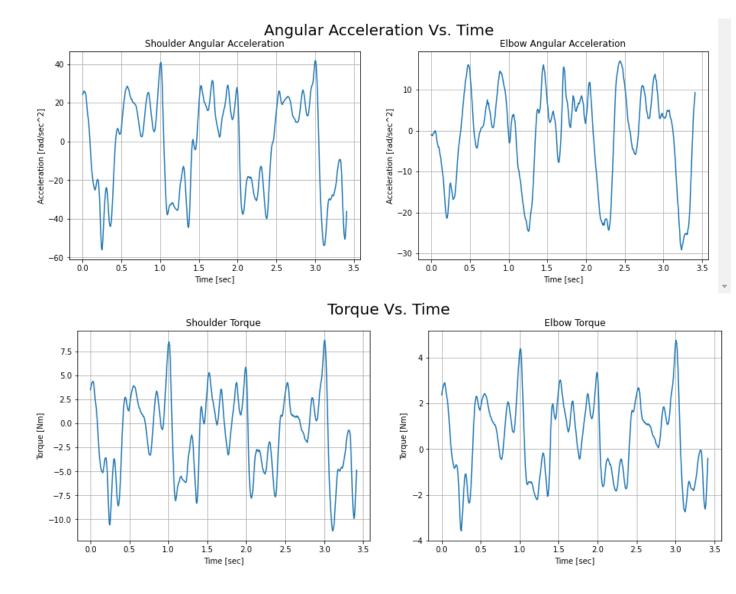
```
plt.grid()
plt.title('Shoulder Angular Acceleration')
plt.subplot(122)
plt.plot(t_list[:-diff], traj[5])
plt.ylabel('Acceleration [rad/sec^2]')
plt.xlabel('Time [sec]')
plt.arid()
plt.title('Elbow Angular Acceleration')
plt.show()
plt.figure(figsize=(15,5))
plt.suptitle('Torque Vs. Time', fontsize=20)
plt.subplot(121)
plt.plot(t list, tau1 list)
plt.vlabel('Torque [Nm]')
plt.xlabel('Time [sec]')
plt.grid()
plt.title('Shoulder Torque')
plt.subplot(122)
plt.plot(t list, tau2 list)
plt.ylabel('Torque [Nm]')
plt.xlabel('Time [sec]')
plt.grid()
plt.title('Elbow Torque')
plt.show()
plt.figure(figsize=(15,5))
plt.suptitle('Power Vs. Time', fontsize=20)
plt.subplot(121)
plt.plot(t_list, power1_list)
plt.ylabel('Power [W]')
plt.xlabel('Time [sec]')
plt.grid()
plt.title('Shoulder Power')
plt.subplot(122)
plt.plot(t_list, power2_list)
plt.ylabel('Power [W]')
plt.xlabel('Time [sec]')
plt.grid()
plt.title('Elbow Power')
plt.show()
plt.figure(figsize=(15,5))
plt.suptitle('Speed Vs. Torque', fontsize=20)
plt.subplot(121)
plt.plot(tau1_list[:-diff], traj[2])
plt.ylabel('Velocity [rad/sec]')
plt.xlabel('Torque [Nm]')
plt.grid()
plt.title('Shoulder Speed-Torque')
plt.subplot(122)
plt.plot(tau2_list[:-diff], traj[3])
plt.ylabel('Velocity [rad/sec]')
plt.xlabel('Torque [Nm]')
plt.grid()
plt.title('Elbow Speed-Torque')
plt.show()
```

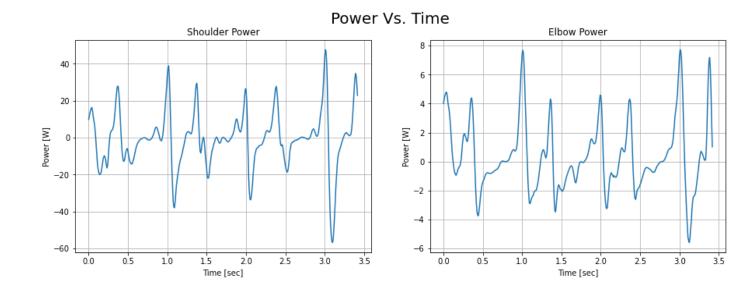


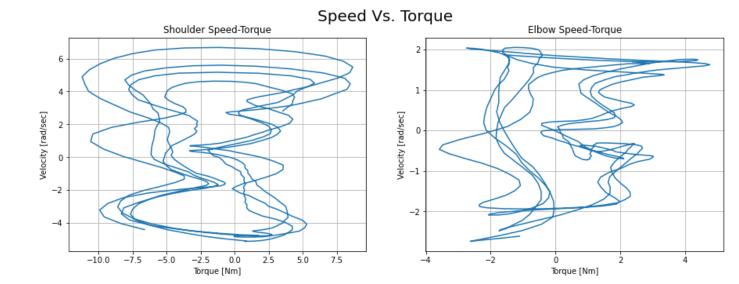










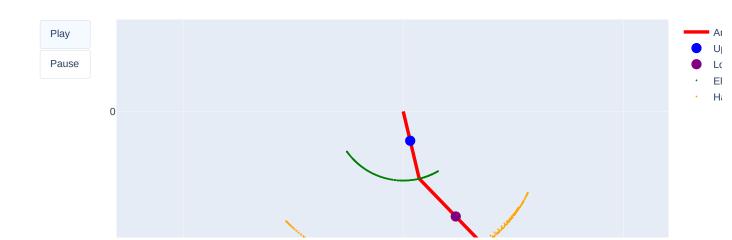


Animating the simulation:

```
In [26]: def animate double pend(traj, L1, L2, L1_COM, L2_COM, T):
             Function to generate web-based animation of double-pendulum system
             Parameters:
                 traj:
                              trajectory of thetal and theta2
                              length of the upper arm
                 L1:
                 L2:
                              length of the lower arm
                 L1 COM:
                              length of the center of mass of the upper arm from the shoulder
                 L2_COM:
                              length of the center of mass of the lower arm from the elbow
                 T:
                              length/seconds of animation duration
             Returns: None
             # Browser configuration
             def configure_plotly_browser_state():
                 import IPython
                 display(IPython.core.display.HTML('''
                     <script src="/static/components/requirejs/require.js"></script>
                       requirejs.config({
                          paths: {
                           base: '/static/base',
                           plotly: 'https://cdn.plot.ly/plotly-1.5.1.min.js?noext',
                         },
                       });
                     </script>
                     · · · ))
             configure_plotly_browser_state()
             init notebook mode(connected=False)
             # Getting data from pendulum angle trajectories
             xx1 = L1 * np.sin(traj[0])
             yy1 = -L1 * np.cos(traj[0])
             xx1_COM = L1_COM * np.sin(traj[0])
             yy1_COM = -L1_COM * np.cos(traj[0])
             xx2 = xx1 + L\overline{2} * np.sin(traj[0] + traj[1])
             yy2 = yy1 - L2 * np.cos(traj[0] + traj[1])
             xx2 COM = xx1 + L2 COM * np.sin(traj[0] + traj[1])
             yy2 COM = yy1 - L2 COM * np.cos(traj[0] + traj[1])
             N = len(traj[0])
             # Using these to specify axis limits
             xm = np.min(xx1)
             xM = np.max(xx1)
             ym = np.min(yy1) - 0.6
             yM = np.max(yy1) + 0.6
             # Defining data dictionary
             data = [dict(x=xx1, y=yy1,
                          mode='lines', name='Arm',
                          line=dict(width=5, color='blue')
                     dict(x=xx1 COM, y=yy1 COM,
                          mode='lines', name='Upper Arm Center of Mass',
                          line=dict(width=2, color='green')
                     dict(x=xx2 COM, y=yy2 COM,
                          mode='lines', name='Lower Arm Center of Mass',
                          line=dict(width=2, color='orange')
                          ),
                     dict(x=xx1, y=yy1,
                          mode='markers', name='Elbow Trajectory',
                          marker=dict(color="green", size=2)
                          ),
                     dict(x=xx2, y=yy2,
                          mode='markers', name='Hand Trajectory',
                          marker=dict(color="orange", size=2)
```

```
)
          ]
    # Preparing simulation layout
    layout = dict(xaxis=dict(range=[xm, xM], autorange=False, zeroline=False,dtick=1),
                  yaxis=dict(range=[ym, yM], autorange=False, zeroline=False, scaleanchor = "x", dti
                  title='Simulation of Arm Modeled as a Double Pendulum',
                  hovermode='closest',
                  updatemenus= [{'type': 'buttons',
                                  'buttons': [{'label': 'Play', 'method': 'animate',
                                                'args': [None, {'frame': {'duration': T, 'redraw': F
                                              {'args': [[None], {'frame': {'duration': T, 'redraw':
                                                'transition': {'duration': 0}}],'label': 'Pause', 'n
                                }]
                 )
    # Defining the frames of the simulation
    frames = [dict(data=[dict(x=[0,xx1[k],xx2[k]),
                               y=[0,yy1[k],yy2[k]],
                              mode='lines',
                               line=dict(color='red', width=4)),
                         go.Scatter(
                               x=[xx1 COM[k]],
                               y=[yy1_C0M[k]],
                              mode="markers",
                               marker=dict(color="blue", size=12)),
                         go.Scatter(
                              x=[xx2_COM[k]],
                               y=[yy2_COM[k]],
                              mode="markers",
                               marker=dict(color="purple", size=12)),
                        ]) for k in range(N)]
    # Putting it all together and plotting
    figure = dict(data=data, layout=layout, frames=frames)
    iplot(figure)
# Animate the system
L1 = L_upper_arm_dict[participants_list[index]]
L2 = L_lower_arm
L1_COM = L_upper_arm_COM_dict[participants_list[index]]
L2\_COM = L\_lower\_arm\_COM
T = 5
animate_double_pend(traj, L1, L2, L1_COM, L2_COM, T)
```

Simulation of Arm Modeled as a Double Pendulum



Motor Selection

Plotting the torque-speed curve of all trials and the torque-speed curve of some motors:

```
In [61]: # Compute the torque and speed vectors of the arm's motion for all trials
         tot_dtheta1_list = []
         tot_dtheta2_list = []
         tot_tau1_list = []
         tot_tau2_list = []
         for lst in range(len(time_list)):
             for i in range(len(time_list[lst])):
                 tot_dtheta1_list.append(Shl_Flex_Vel_list[lst][i])
                 tot_dtheta2_list.append(Elbow_Vel_list[lst][i])
                 tot_tau1_list.append(Shl_Flex_tau_list[lst][i])
                 tot_tau2_list.append(Elbow_tau_list[lst][i])
         # Compute the torque and speed vectors of some motors
         # T-Motor, GL80 (KV30):
         tau_stall_GL80_30 = 1.75
         no_load_speed_GL80_30 = 720*2*pi/60
         motor_speed_GL80_30 = [2*no_load_speed_GL80_30, no_load_speed_GL80_30, 0, -.5*no_load_speed_GL80_3
         motor_torque_GL80_30 = [-tau_stall_GL80_30, 0, tau_stall_GL80_30, 1.5*tau_stall_GL80_30]
         # T-Motor, GL80 (KV60):
         tau stall GL80 60 = 2.9
         no_load_speed_GL80_60 = 1440*2*pi/60
         motor_speed_GL80_60 = [2*no_load_speed_GL80_60, no_load_speed_GL80_60, 0, -.5*no_load_speed_GL80_6
         motor_torque_GL80_60 = [-tau_stall_GL80_60, 0, tau_stall_GL80_60, 1.5*tau_stall_GL80_60]
         # T-Motor, G80 (KV30):
         tau stall G80 30 = 2.9
         no_load_speed_G80_30 = 700*2*pi/60
         motor speed G80 30 = [2*no\ load\ speed\ G80\ 30,\ no\ load\ speed\ G80\ 30,\ 0,\ -.5*no\ load\ speed\ G80\ 30]
         motor_torque_G80_30 = [-tau_stall_G80_30, 0, tau_stall_G80_30, 1.5*tau_stall_G80_30]
         # T-Motor, G80 (KV60):
         tau_stall_G80_60 = 2.9
         no_load_speed_G80_60 = 1400*2*pi/60
         motor_speed_G80_60 = [2*no_load_speed_G80_60, no_load_speed_G80_60, 0, -.5*no_load_speed_G80_60]
         motor_torque_G80_60 = [-tau_stall_G80_60, 0, tau_stall_G80_60, 1.5*tau_stall_G80_60]
         # T-Motor, GL60 (KV25):
         tau stall GL60 25 = 1.75
         no load speed GL60\ 25 = 600*2*pi/60
         motor_speed_GL60_25 = [2*no_load_speed_GL60_25, no_load_speed_GL60_25, 0, -.5*no_load_speed_GL60_2
         motor_torque_GL60_25 = [-tau_stall_GL60_25, 0, tau_stall_GL60_25, 1.5*tau_stall_GL60_25]
         # T-Motor, GL60 (KV55):
         tau stall GL60 55 = 1.75
         no_load_speed_GL60_55 = 1200*2*pi/60
         motor_speed_GL60_55 = [2*no_load_speed_GL60_55, no_load_speed_GL60_55, 0, -.5*no_load_speed_GL60_5
         motor_torque_GL60_55 = [-tau_stall_GL60_55, 0, tau_stall_GL60_55, 1.5*tau_stall_GL60_55]
         # T-Motor, GL100 (KV10):
         tau_stall_GL100 = 7.7
         no\_load\_speed\_GL100 = 250*2*pi/60
         motor_speed_GL100 = [2*no_load_speed_GL100, no_load_speed_GL100, 0, -.5*no_load_speed_GL100]
         motor torque GL100 = [-tau stall GL100, 0, tau stall GL100, 1.5*tau stall GL100]
         # T-Motor, G100 (KV10):
         tau stall G100 = 7.7
         no load speed G100 = 250*2*pi/60
         motor_speed_G100 = [2*no_load_speed_G100, no_load_speed_G100, 0, -.5*no_load_speed_G100]
         motor torque G100 = [-tau stall G100, 0, tau stall G100, 1.5*tau stall G100]
         # T-Motor, R60 (KV115):
         tau_stall_R60 = 16.96
         no load speed R60 = 5520*2*pi/60
         motor speed R\overline{60} = [2*no load speed R60, no load speed R60, 0, -.5*no load speed R60]
         motor_torque_R60 = [-tau_stall_R60, 0, tau_stall_R60, 1.5*tau_stall_R60]
```

```
# T-Motor, R80 (KV110):
tau_stall_R80 = 17.73
no load speed R80 = 5280*2*pi/60
motor_speed_R80 = [2*no_load_speed_R80, no_load_speed_R80, 0, -.5*no_load_speed_R80]
motor_torque_R80 = [-tau_stall_R80, 0, tau_stall_R80, 1.5*tau_stall_R80]
# T-Motor, AK60-6:
tau_stall_AK60_6 = 37.49
no load speed AK60 6 = 560*2*pi/60
motor_speed_AK60_6 = [2*no_load_speed_AK60_6, no_load_speed_AK60_6, 0, -.5*no_load_speed_AK60_6]
motor_torque_AK60_6 = [-tau_stall_AK60_6, 0, tau_stall_AK60_6, 1.5*tau_stall_AK60_6]
# T-Motor, AK80-6:
tau stall AK80 6 = 80.888
no load speed AK80 6 = 460*2*pi/60
motor speed AK80 6 = [2*no load speed AK80 6, no load speed AK80 6, 0, -.5*no load speed AK80 6]
motor_torque_AK80_6 = [-tau_stall_AK80_6, 0, tau_stall_AK80_6, 1.5*tau_stall_AK80_6]
# Maxon, 614949:
tau stall 614949 = 4.3
no_load_speed_614949 = 4300*2*pi/60
motor speed 614949 = [2*no load speed 614949, no load speed 614949, 0, -.5*no load speed 614949]
motor torque 614949 = [-tau stall 614949, 0, tau stall 614949, 1.5*tau stall 614949]
# E-S Motor, 28PG-385SP-19-EN:
tau_stall_28PG = 3.73
no load speed 28PG = 310*2*pi/60
motor_speed_28PG = [2*no_load_speed_28PG, no_load_speed_28PG, 0, -.5*no_load_speed_28PG]
motor torque 28PG = [-tau stall 28PG, 0, tau stall 28PG, 1.5*tau stall 28PG]
# E-S Motor, 36GP-555PM-51-EN 24V:
tau stall 36GP 51 = 4.90
no_load_speed_36GP_51 = 230*2*pi/60
motor\_speed\_36GP\_51 = [2*no\_load\_speed\_36GP\_51, no\_load\_speed\_36GP\_51, 0, -.5*no\_load\_speed\_36GP\_51, 0, -.5*no\_speed\_36GP\_51, 0, -.5*no\_load\_speed\_36GP\_51, 0, -.5*no\_load\_speed\_36GP\_51
motor_torque_36GP_51 = [-tau_stall_36GP_51, 0, tau_stall_36GP_51, 1.5*tau_stall_36GP_51]
# E-S Motor, 36GP-555PM-100-EN 24V:
tau_stall_36GP_100 = 4.90
no_{load\_speed\_36GP\_100} = 120*2*pi/60
motor_speed_36GP_100 = [2*no_load_speed_36GP_100, no_load_speed_36GP_100, 0, -.5*no_load_speed_36GP_100, 0, -.5*no_load_speed_36GP_100
motor_torque_36GP_100 = [-tau_stall_36GP_100, 0, tau_stall_36GP_100, 1.5*tau_stall_36GP_100]
# E-S Motor, 36GP-555PM-139-EN 24V:
tau_stall_36GP_139 = 4.90
no_load_speed_36GP_139 = 85*2*pi/60
motor_speed_36GP_139 = [2*no_load_speed_36GP_139, no_load_speed_36GP_139, 0, -.5*no_load_speed_36GP_139
motor_torque_36GP_139 = [-tau_stall_36GP_139, 0, tau_stall_36GP_139, 1.5*tau_stall_36GP_139]
# Pololu, 150:1 Metal Gearmotor 37Dx73L mm 12V with 64 CPR Encoder (Helical Pinion):
tau_stall_37D_12V_150 = 4.805
no_load_speed_37D_12V_150 = 67*2*pi/60
motor_speed_37D__12V_150 = [2*no_load_speed_37D__12V_150, no_load_speed_37D__12V_150, 0, -.5*no_load_speed_37D__12V_150 = [2*no_load_speed_37D__12V_150, no_load_speed_37D__12V_150, 0, -.5*no_load_speed_37D__12V_150 = [2*no_load_speed_37D__12V_150, no_load_speed_37D__12V_150, no_loa
motor_torque_37D__12V_150 = [-tau_stall_37D__12V_150, 0, tau_stall_37D__12V_150, 1.5*tau_stall_37D_
# Pololu, 131:1 Metal Gearmotor 37Dx73L mm 12V with 64 CPR Encoder (Helical Pinion):
tau_stall_37D__12V_131 = 4.41
no_load_speed_37D_12V_131 = 76*2*pi/60
motor_speed_37D__12V_131 = [2*no_load_speed_37D__12V_131, no_load_speed_37D__12V_131, 0, -.5*no_ld
motor_torque_37D__12V_131 = [-tau_stall_37D__12V_131, 0, tau_stall_37D__12V_131, 1.5*tau_stall_37D_
# Pololu, 150:1 Metal Gearmotor 37Dx73L mm 24V with 64 CPR Encoder (Helical Pinion):
tau_stall_37D_24V_150 = 5.49
no_load_speed_37D_24V_150 = 68*2*pi/60
motor_speed_37D__24V_150 = [2*no_load_speed_37D__24V_150, no_load_speed_37D__24V_150, 0, -.5*no_ld
motor_torque_37D__24V_150 = [-tau_stall_37D__24V_150, 0, tau_stall_37D__24V_150, 1.5*tau_stall_37D_
```

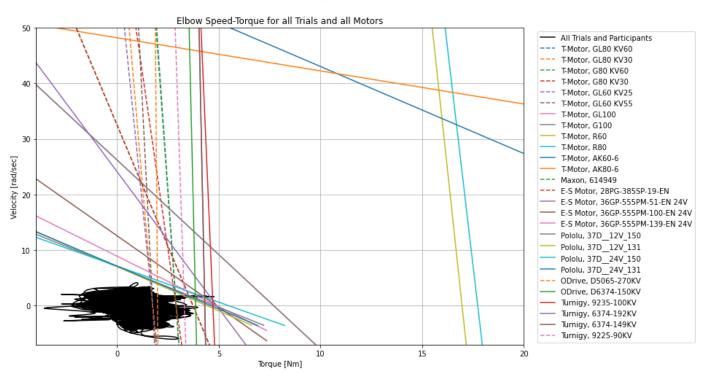
Pololu, 131:1 Metal Gearmotor 37Dx73L mm 24V with 64 CPR Encoder (Helical Pinion):

```
tau_stall_37D_24V_131 = 4.61
no_load_speed_37D_24V_131 = 79*2*pi/60
motor_speed_37D__24V_131 = [2*no_load_speed_37D__24V_131, no_load_speed_37D__24V_131, 0, -.5*no_load_speed_37D__24V_131, 
motor_torque_37D__24V_131 = [-tau_stall_37D__24V_131, 0, tau_stall_37D__24V_131, 1.5*tau_stall_37D
# ODrive, DUAL SHAFT MOTOR - D5065 270KV:
tau stall D5065 = 1.99
no_load_speed_D5065 = 8640*2*pi/60
motor_speed_D5065 = [2*no_load_speed_D5065, no_load_speed_D5065, 0, -.5*no_load_speed_D5065]
motor_torque_D5065 = [-tau_stall_D5065, 0, tau_stall_D5065, 1.5*tau_stall_D5065]
# ODrive, DUAL SHAFT MOTOR - D6374 150KV:
tau stall D6374 = 3.86
no_load_speed_D6374 = 5760*2*pi/60
motor speed D6374 = [2*no load speed D6374, no load speed D6374, 0, -.5*no load speed D6374]
motor torque D6374 = [-tau stall D6374, 0, tau stall D6374, 1.5*tau stall D6374]
# Turnigy, 9235-100KV Brushless Multi-Rotor Motor:
tau stall 9235 = 4.71
no load speed 9235 = 3840*2*pi/60
motor_speed_9235 = [2*no_load_speed_9235, no_load_speed_9235, 0, -.5*no_load_speed_9235]
motor torque 9235 = [-tau stall 9235, 0, tau stall 9235, 1.5*tau stall 9235]
# Turnigy, SK8 6374-192KV Sensored Brushless Motor (14P):
tau stall 6374\ 192KV = 4.31
no_load_speed_6374_192KV = 7373*2*pi/60
motor_speed_6374_192KV = [2*no_load_speed_6374_192KV, no_load_speed_6374_192KV, 0, -.5*no_load_spe
motor_torque_6374_192KV = [-tau_stall_6374_192KV, 0, tau_stall_6374_192KV, 1.5*tau_stall_6374_192KV
# Turnigy, SK8 6374-149KV Sensored Brushless Motor (14P):
tau stall 6374\ 149KV = 4.31
no_load_speed_6374_149KV = 7373*2*pi/60
motor_speed_6374_149KV = [2*no_load_speed_6374_149KV, no_load_speed_6374_149KV, 0, -.5*no_load_speed_6374_149KV, 0, -.5*no_load_spee
motor_torque_6374_149KV = [-tau_stall_6374_149KV, 0, tau_stall_6374_149KV, 1.5*tau_stall_6374_149K
# Turnigy, 9225-90KV Turnigy Multistar Brushless Multi-Rotor Motor:
tau_stall_9225 = 3.31
no_load_speed_9225 = 3456*2*pi/60
motor_speed_9225 = [2*no_load_speed_9225, no_load_speed_9225, 0, -.5*no_load_speed_9225]
motor_torque_9225 = [-tau_stall_9225, 0, tau_stall_9225, 1.5*tau_stall_9225]
# Plotting the torque-speed curves of the arm's motion and the motors
plt.figure(figsize=(12,8))
plt.plot(tot_tau2_list, tot_dtheta2_list, color='black', label='All Trials and Participants')
plt.plot(motor_torque_GL80_60, motor_speed_GL80_60, '--', label='T-Motor, GL80 KV60')
plt.plot(motor_torque_GL80_30, motor_speed_GL80_30, '--', label='T-Motor, GL80 KV30')
plt.plot(motor_torque_G80_60, motor_speed_G80_60, '--', label='T-Motor, G80 KV60')
plt.plot(motor_torque_G80_30, motor_speed_G80_30, '--', label='T-Motor, G80 KV30')
plt.plot(motor_torque_G80_30, motor_speed_G80_30, '--', label='T-Motor, G80 KV30')
plt.plot(motor_torque_GL60_25, motor_speed_GL60_25, '--', label='T-Motor, GL60 KV25')
plt.plot(motor_torque_GL60_55, motor_speed_GL60_55, '--', label='T-Motor, GL60_KV55')
plt.plot(motor torque GL100, motor speed GL100, label='T-Motor, GL100')
plt.plot(motor_torque_G100, motor_speed_G100, label='T-Motor, G100')
plt.plot(motor_torque_R60, motor_speed_R60, label='T-Motor, R60')
plt.plot(motor_torque_R80, motor_speed_R80, label='T-Motor, R80')
plt.plot(motor_torque_AK60_6, motor_speed_AK60_6, label='T-Motor, AK60-6')
plt.plot(motor_torque_AK80_6, motor_speed_AK80_6, label='T-Motor, AK80-6')
plt.plot(motor_torque_28PG, motor_speed_28PG, '--', label='Maxon, 614949')
plt.plot(motor_torque_28PG, motor_speed_28PG, '--', label='E-S Motor, 28PG-385SP-19-EN')
plt.plot(motor_torque_36GP_51, motor_speed_36GP_51, label='E-S Motor, 36GP-555PM-51-EN 24V')
plt.plot(motor_torque_36GP_100, motor_speed_36GP_100, label='E-S Motor, 36GP-555PM-100-EN 24V') plt.plot(motor_torque_36GP_139, motor_speed_36GP_139, label='E-S Motor, 36GP-555PM-139-EN 24V')
plt.plot(motor_torque_37D__12V_150, motor_speed_37D__12V_150, label='Pololu, 37D__12V_150')
plt.plot(motor_torque_37D__12V_131, motor_speed_37D__12V_150, label='Pololu, 37D__12V_131') plt.plot(motor_torque_37D__24V_150, motor_speed_37D__24V_150, label='Pololu, 37D__24V_150') plt.plot(motor_torque_37D__24V_131, motor_speed_37D__24V_150, label='Pololu, 37D__24V_131')
plt.plot(motor_torque_D5065, motor_speed_D5065, '--', label='ODrive, D5065-270KV')
plt.plot(motor_torque_D6374, motor_speed_D6374, label='ODrive, D6374-150KV')
plt.plot(motor_torque_9235, motor_speed_9235, label='Turnigy, 9235-100KV')
plt.plot(motor torque 6374 192KV, motor speed 6374 192KV, label='Turnigy, 6374-192KV')
plt.plot(motor_torque_6374_149KV, motor_speed_6374_149KV, label='Turnigy, 6374-149KV')
```

```
plt.plot(motor_torque_9225, motor_speed_9225, linestyle='--', label='Turnigy, 9225-90KV')

plt.ylabel('Velocity [rad/sec]')
plt.xlabel('Torque [Nm]')
plt.xlim([-4, 20])
plt.ylim([-7, 50])
plt.grid()
plt.legend(loc='upper left', bbox_to_anchor=(1.02,1))
plt.suptitle('Elbow Speed-Torque', fontsize=20)
plt.title('Elbow Speed-Torque for all Trials and all Motors')
plt.show()
```

Elbow Speed-Torque



In []: