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Fakultät VII Wirtschaft & Management  
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## Bachelorarbeit

Title

Subtitle

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Berlin, Sunday 3<sup>rd</sup> February, 2019

## **Statutory declaration**

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As of the date of submission, this piece of document and its content have not been submitted anywhere else but to our supervisors.

Berlin, Sunday 3<sup>rd</sup> February, 2019

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MAXIMILIAN EISSLER

## **Abstract**

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# 1 Introduction

In this document the topic, motivation and approach of my bachelor's thesis shall be outlined. The aim is to give the reader an idea of what I try to accomplish with the choice of topic and methods, as well as a look at the first iteration of the mathematical model I am aiming to build.

## 1.1 Motivation

As the technological requirements for a decentralized energy system increasingly mature, the importance of understanding smaller units within the electricity system grows. There is a possibility of increasing reliance on small, partially autonomous grid units (microgrids) in the future. This calls for a better understanding of how such systems might operate. Especially the possible efficiency gains over a centralised system and the circumstances on which these efficiency gains might depend should be of interest to science and will be the focus of thesis.

more here,  
definition  
microgrid,  
more topic  
introduction, definitions of words, pv, distributed generation

## 1.2 Research Question

In my thesis I want to create a model of a small electricity grid with a single point of access to the main grid. The microgrid will contain 25 households of different types that will aim to reduce their total electricity costs. To attain this goal there will be two possible courses of action available:

1. First, the option to invest in electricity generation and storage facilities, in this case only solar pv and battery storage.
2. Secondly, the possibility of unrestricted trade within the microgrid, meaning there will be no variable transaction costs, as they would usually occur in the form of fees and levies on electricity being transferred.

The aim of this approach is to determine the cost-saving potential in comparison to pure electricity consumption from the main grid in subject to the characteristics of the main parameter types to this model, which are:

more here,  
GER-MANY,  
capacity  
building,  
distribute  
technological  
know-how

what is  
a linear  
model, theory, MILP,  
different  
optimisation methods

1. The environmental conditions, primarily pertaining to the availability of renewable resources - in this case, solar irradiation - as well as temperature and changing seasonal energy demand.
2. The 'behaviour' of the participants in this microgrid, primarily their willingness to shift or avoid loads depending on the current price of electricity within the microgrid or the main grid.
3. The price of power from the main grid as a function of the time of day and season, as well as the price of power generated by the households themselves.

### **1.3 Methods**

To model the outlined situation I want to use the computational modelling language 'Julia' and construct a linear optimisation model which can be solved with it. The goal is to minimise the cost of electricity for the households in the microgrid. It is notable at this point, that the non-consumption of electricity as well as the delay of consumption will be seen as a cost to the actor forgoing her demand. There will be an investment opportunity at the beginning of the examined timeframe of 20 years. The number of timeslices considered in the optimisation will be depending on performance of the model and can therefore not be determined yet.

As a case study for this thesis I want to apply the model to the example of a community in Northrhine-Westfalia. With environmental variables set, I will then construct a number of scenarios with variations in electricity price and actor behaviour parameters.

Another goal of this project is to make this a functional piece of research by reducing performance requirements as far as possible and creating an intuitive user interface that enables the user to 'play' with different scenarios. I prefer this approach over a few detailed and rigid scenarios because the future external factors are presently highly uncertain, which drives me to the conviction that an understanding of the dynamics involved in the examined system is of greater value than an exact solution to an unlikely scenario.

### **1.4 Expected Results**

The result should be a tool that enables an intuitive understanding of the characteristics and the potentials of microgrids, even to non-economists. I intend an exemplary application of the model to the case of a Northrhine-Westfalian community. From this application I expect an insight into the efficiency gains achievable by microgrids in the German context. Also the required external factors for these efficiency gains to materialise should become evident. Under the right conditions I expect a double digit percentage drop in electricity costs compared to a purely consumption-based system. I

hope to arrive at practical conclusions regarding present use cases for microgrids and required future regulation.

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of all main  
chapters

## 2 Literature Review

In this section I shall attempt to give an overview over the current status quo regarding the optimization of microgrids and more especially the tools available to do so. I will pursue this by answering a number of broad questions, which I think are crucial regarding my subject. The procedure will be structured by utilizing a consistent and reproducible methodology described in detail below. In addition to scientific literature other sources will also be taken into account at my discretion if they are necessary or helpful in answering a question.

### 2.1 Key Questions

This literature review will attempt to answer the following key questions in the context of my subject:

1. What are the most eminent scientific standards for modelling a microgrid allocation and dispatch?
2. What is usually within the scope of such a model (what types of generation assets, only electricity or also thermal energy and so on)?
3. What are the common methods used to determine some of the key variables required in such a model such as interest rates, CAPEX and OPEX of assets and so on?
4. What are the most commonly used (commercial) tools for optimizing a microgrid? Are there any free or open source solutions?

### 2.2 Methodology

To arrive at a dataset of scientific literature that is reproducible I use the methodology described in :

1. Define a search string
2. Choose scientific databases to which to apply that search string
3. Due to the possibly large amount of papers brought up by this kind of search I am only considering the 100 most relevant papers from each database.
4. Define keywords, which have to occur in the abstracts of the publications. All publications that

add reference to  
papers  
here

lack a keyword are discarded.

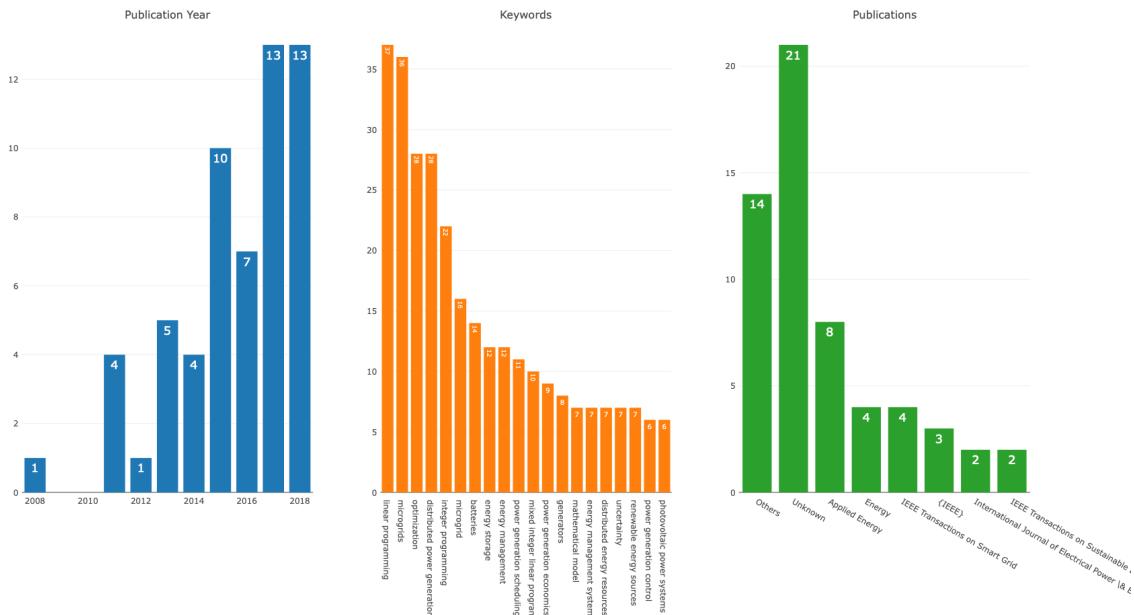
5. Define Inclusion as well as Exclusion criteria. A publication must satisfy all inclusion criteria as well as none of the exclusion criteria to be included in the literature review.

Due to the nature of some of the questions I am trying to answer in my literature review it is additionally necessary to include further non-scientific sources at my discretion. The search strings, used databases, as well as the dataset of literature at each step will be included in the appendix.

## 2.3 Descriptive Analysis

After filtering the original dataset of 275 unique publications in the way described in the last chapter, I arrive at a set of 61 publications. The publication year, as can be observed in Figure 1 is for most publications quite recently: 27 out of 61 papers were published 2017 and after. This could indicate a rising interest in the subject, but is probably at least partly due to the way the different search engines employed compute relevancy.

include  
info and  
datasets  
in the ap-  
pendix



**Figure 1: Results of an automated Descriptive Analysis**

Source: Own illustration.

Looking at the keywords used to describe the publication shows that, unsurprisingly, the most often occurring keywords are the ones used in conducting the search: 'linear programming', 'microgrids' and 'optimization'. 'distributed energy generation' and 'distributed energy resources' are mentioned 37 times.

'batteries' and 'energy storage' a total of 28 times, and 'renewable energy sources' and 'generators' a total of 16 times. This illustrates the focus on decentralized energy sources and storage, more specifically renewables and small scale combined heat and power generation that prevails throughout the literature.

The publication chart is not very enlightening. This is due to the fact 28 out of 61 publications are conference papers which either appear under others because there is only one instance of that particular conference or unknown. From a more general point of view though almost all papers are published either by Elsevier or IEEE, with very few exceptions.

## 2.4 Literature Overview

The first question in need of an answer in optimizing a microgrids design and dispatch is the question of the modelling approach itself. Although the dataset of literature derived from the methodology described in 2.2 is biased towards Linear Programming, which was one of the search and filter criteria, it contains multiple employed methodologies. For example, [21] employ both a Mixed Integer Linear Programming (MILP) model and a Genetic Algorithm (GA) and come to the conclusion that while both deliver accurate and robust results the MILP model is faster. [30] mostly concur. While in this case, the results of the GA were better in two scenarios, it was outperformed by the MILP model in the remaining three. A key problem of MILP however seems to be its deterministic nature, which anticipates perfect knowledge of all the parameters involved. Especially for optimisation problems regarding a short timeframe, such as day-ahead scheduling this is a significant problem, since actual parameters may be different. Several methods addressing this problem can be found in literature. One such method are rolling time horizons. This approach optimizes the dispatch of a microgrid for a fixed time horizon based on steadily updated forecasts of the uncertain parameters. The optimization is repeated periodically to reflect the updated forecasts [32] [42] and increase dispatch accuracy in the nearer future. Rolling Horizon Optimization is however unfit to optimize investment, since it is not possible to adapt investment decisions ex post to changed conditions.

While the rolling time horizon method helps to limit uncertainty by reacting to changes of input parameters, Robust Optimization and Stochastic Optimization try to proactively account for a variety of possible scenarios. Robust Optimization achieves this by optimizing for a number of scenarios deemed equally likely, as in [8] using ensemble weather forecasts or in [16] and [54] using upper and lower boundaries for uncertain parameters. Stochastic Optimization on the other hand uses detailed probability distributions to weigh the probability of each scenario occurring as explained in [28]. To arrive at these distributions secondary tools are usually needed. Shams et al use a simple Gaussian randomization to make their demand data reflect uncertainty, as well as more specific distributions for irradiation and wind speeds. A number of other methodologies appear in literature such as employing

a Monte Carlo simulation [57] or deriving multiple scenarios and corresponding realization probabilities from historical data [31].

The scope of the microgrid models found in literature varies greatly. A constant however is the definition of a microgrid as bounded, operating in a small geographical zone and with a clear electrical boundaries [44][25][18]; managing local loads [52] [56]; possibly containing various generation units and storage [42][23] and possibly being able to exchange power with the main grid [30][10], from whose perspective it is seen as a single entity [19].

While most of the selected literature consider cases where a grid connection exists and can be used at all times, there is a number of publications that consider either completely islanded microgrids [53][32] [39][38] or microgrids that can sustain themselves in islanded mode for extended periods for example in case of natural disasters [44].

The clearest distinctions between microgrid models, after the object and applied methodology is properly defined, is based on the aspect or aspects that the model is supposed to optimize. The literature can be split in two groups, either optimizing only dispatch or both investment (e.g. the planning phase) and dispatch. The former group is definitely the larger, with only 12 out of 61 publications considering investment. Notably only one of these [28] uses any of the methods to model uncertainty discussed above.

There is also significant diversity in literature when it comes to the technologies considered in modelling. Modelling dispatchable (eg. non-renewable) as well as non-dispatchable (eg. renewable) generation is rather common, but the specifics differ: While most models consider PV or Wind as well as a CHP generator, the included generation technologies are as diverse as geothermal generators [21] and gas turbines [45] [30]. In addition to modelling electricity, some publications also consider heat generation and transmission [20][49]. This is valuable, because the economic performance of a non-renewable generation unit (usually CHP) present in most models depends heavily on if and how the heat is used, as [7] point out.

The types of storage used in literature also vary. Although battery storage [2][45][50] or an abstract storage device [33][51] are the most common choices, there are a number of papers modeling heat storage [52][54][20][49], and some with more exotic technology choices such as flywheels [37] or an electrolyzer [13].

In addition to these generation and storage technologies some publications also model the network topology [24][6][41] and some even consider electrical phenomena such as active and reactive power losses [23][25] and voltage deviation [23].

Demand side management, which some models implement is usually represented by dividing loads into different categories. [6] distinguish between 'critical loads', meaning loads that absolutely have to be satisfied, 'shiftable loads', meaning loads that have to be satisfied, although there is a time window, rather than an exact point in which they can be serviced, and 'adjustable' loads, which can be dropped

if needed. Although the terms may vary, and many publications do not introduce the 'shiftable loads' category altogether, these conceptual distinctions are made by a number of other authors [42][54][55]. The model results depend almost as much on the given input parameters used in case studies as on the modelling approach itself. There is however only a limited number of publications with detailed documentation of the parameters used. The used parameters can be broadly categorized as either economic parameters, such as capital and operation and maintenance cost for the technologies used, generation related parameters such as irradiation and wind speeds, and load data, representing consumer behaviour.

In publications documenting cost parameters there is a clear trend towards a split of technology cost into investment and maintenance cost. However, whereas [20] define maintenance cost as a fixed cost per unit of time, [49] define it as a function of kilowatthours produced, a measurement which [20] call 'fuel costs'. [2] choose a definition closer aligned with the former, they however define yearly maintenance cost simply as a flat percentage of the units' investment cost.[19] seem to neglect maintenance costs altogether focusing only on investment costs. While some models document economic paramters such as discount rates [2], many don't and it is unclear if future flows of value are properly discounted in these models. Furthermore many of the publications declare cost parameters as assumptions rather than trying to derive them from sources, although a few such as [20] and [49] do so.

The selected literature offers multiple ways of obtaining input parameters of metereological data. [14] use historical metereological data while [32] build a prediction model for forecasting irridiation and wind speeds. Similarly there are authors who use historical data for load parameters such as [14] and ones who generate synthetic data based on appliance use and probabilistic models [52][51][54] or neural networks using empirical data [32].

When it comes to modelling tools DER-CAM [20][57][24] and HOMER [1][57][20] are the most often referenced. DER-CAM or Distributed Energy Resources Customer Adoption Model is an optimizatioon tool developed at Berkeley Labs and uses Mixed Integer Linear Programming to optimize portfolio, placement, sizing and dispatch of Microgrid Energy Systems [9]. HOMER Grid is a commercial optimization tool for behind the meter systems. Its main advantage is it's large database of components and tariff rates in the United States and Canada [15]. The most often mentioned solver is the CPLEX commercial solver [40][30][46][23]... . Most of the models are written in GAMS [42][46][8]..., although many are written in MATLAB [23][6]... .

Open source tools seem scarcely available. A search of 'microgrid optimization' on [github.com](https://github.com), the major open source software platform, brings up only 3 items with more than one star, none of them has more than ten (popular libraries might have thousands)[12]. The most up-to-date one has not been updated for a year and none features a graphical user interface.

### 3 Model

#### 3.1 Time

The range of scenarios and complexity the model can handle is, among other things, dependant on its implementation of discrete time. More and smaller timesteps and a representative sample of diverse expectable conditions regarding the parameters leads to higher model accuracy. Of course the amount of timesteps is limited by processing power and therefore by model complexity. To enable both diverse and therefore potentially discontinuous parameter sets and a reasonable length for each set, the length of 1 hour is chosen for the basic timestep  $t; t \in [1, T]; T \in \mathbb{N}$ .  $T$  denotes the number of hours in each discontinuous sets of supply and demand parameters. Furthermore the ability of including multiple discontinuous sets of supply and demand parameters of the same length in one scenario is gained by introducing a second iterator  $s; s \in [1, S]; S \in \mathbb{N}$ .  $S$  denotes the number of discontinuous sets of supply and demand parameters.

#### 3.2 Households

To properly conduct trading and for the future possibility of adding voltage and topological constraints to the model, the households are modelled as independent entities, each with its own demand, generation and storage. Therefore a third iterator  $u; u \in [1, U]; U \in \mathbb{N}$ ; is introduced.  $U$  denotes the number of households modelled. An abstract household  $H$  is defined as a tuple of storage and generation devices as well as demand curves. For discrete storage and generation devices two separate sets of positive integers define how much of each option available in the scenario was installed. Additionally each household has a price  $shiftP$  and  $curtP$  at which they are willing to shift or curtail a unit of their load respectively.

$$H := (GEN, ST, dGEN, dST, DEM, shiftP, curtP) \quad (1)$$

A concrete household  $H_u$  implements these values:

$$GEN \in \mathbb{R}^K; GEN_k \geq 0 \forall k; k \in [0, K] \quad (2)$$

$$ST \in \mathbb{R}^L; ST_l \geq 0 \forall l; l \in [0, L] \quad (3)$$

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$$dGEN \in \mathbb{N}^M \quad (4)$$

$$dST \in \mathbb{N}^N \quad (5)$$

with

$k, l$  in  $\mathbb{N}$

and

$K, L, M, N \in \mathbb{N}$

and

$shiftP, curtP \geq 0$

$K$  and  $L$  denote the amount of generation and storage devices in household  $H_u$ . This, in practice, is equal to the amount of linear scaling investment options for each category, since a zero capacity device is still modelled as a device.  $M$  and  $N$  denote the amount of discrete investment options in their respective category.  $GEN_k$  and  $ST_l$  are the capacities installed of the  $k$ -th and  $l$ -th linear investment option respectively.  $GEN_m$  and  $dST_n$  are the amount installed of the  $m$ -th and  $n$ -th discrete investment option available.  $DEM$  is further defined in the subsection demand.

A list of instances of the structure  $H$  and its length  $U$  are both model parameters.

### 3.3 Internal Variables

The objective of the model is to find optimal investment, dispatch and trade. Therefore, the following sets of internal parameters are introduced:

$\forall u, s, t$ :

$$toTR_{u,s,t}, fromTR_{u,s,t} \geq 0 \quad (6)$$

The trade supply variables  $toTR_{u,s,t}$  and  $fromTR_{u,s,t}$  reflect the amount of traded power, to the trading pool and from the trading pool, respectively. They are defined for each household at each timestep.

$\forall u, k, m, s, t$ :

$$genS_{u,k,s,t}, dgenS_{u,m,s,t} \geq 0 \quad (7)$$

The generation supply variables  $genS_{u,k,s,t}$  and  $dgenS_{u,m,s,t}$  describe the amount of energy produced by each linear or discrete generation option respectively. They are defined for each generation option in each household and at each timestep. It is useful to keep in mind though, that not every household needs to implement all the generation options. In case of zero instances of the discrete generation option  $dGEN_2$  installed in household  $H_5$ , for example,  $dgenS_{5,2,s,t} = 0$  for all  $s$  and  $t$ .

$\forall u, l, n, s, t:$

$$fromST_{u,l,s,t}, toST_{u,l,s,t}, fromDST_{u,n,s,t}, toDST_{u,n,s,t} \geq 0 \quad (8)$$

The storage supply variables  $fromST_{u,l,s,t}$  and  $toST_{u,l,s,t}$  indicate the amount of power fed into or withdrawn from a linear storage investment option. They are defined for each linear investment option and each household at each timestep. The variables  $fromDST_{u,n,s,t}$  and  $toDST_{u,n,s,t}$  have the equivalent function for all discrete storage investment options.

$\forall u, s, t:$

$$toSC_{u,s,t}, fromSC_{u,s,t}, ncS_{u,s,t} \geq 0 \quad (9)$$

The shifted consumption supply variable  $toSC_{u,s,t}$  represents the amount of power consumption shifted by each household at each timestep.  $fromSC_{u,s,t}$  indicates the amount of power consumption that has previously been shifted and is now consumed. The non-consumption supply variable  $ncS_{u,s,t}$  designates the amount of power consumption curtailed for each household at each timestep.

$\forall u, s, t:$

$$fromGR_{u,s,t}, toGR_{u,s,t} \geq 0 \quad (10)$$

Finally, the grid supply variables  $fromGR_{u,s,t}$  and  $toGR_{u,s,t}$  denote the amount of power supplied by and to the respectively by each household at each timestep. Only power flowing out of and into the microgrid included in this definition, power traded internally, while using the (micro)grid, is reflected in the trade variables. (see formula (6))

$\forall u, k:$

$$H_u \hookrightarrow GEN_k \geq 0 \quad (11)$$

$\forall u, l:$

$$H_u \hookrightarrow ST_l \geq 0 \quad (12)$$

$\forall u, m$

$$H_u \hookrightarrow dGEN_m \in \mathbb{N} \quad (13)$$

$\forall u, n$

$$H_u \hookrightarrow dST_n \in \mathbb{N} \quad (14)$$

$H_u \hookrightarrow GEN_k$ ,  $H_u \hookrightarrow ST_l \geq 0$ ,  $H_u \hookrightarrow dGEN_m$ ,  $H_u \hookrightarrow dST_n$  are variables describing the realized capacities of each linear and discrete investment option in each household. They are explained in more

detail in section 3.2.

### 3.4 Generation

For a model, explicitly built to optimize decentralized generation in microgrids, a robust and flexible mathematical representation of generation options is required. Therefore an abstract linear generation device  $GEN$  and an abstract discrete generation device  $dGEN$ , which can represent a range of technology options, are defined:

$$GEN := (C_{Cap}, C_{OpFix}, C_{OpVar}, T_{Life}, EFF_{el}, PR, maxFl) \quad (15)$$

$$dGEN := (CAP, C_{Cap}, C_{OpFix}, C_{OpVar}, T_{Life}, EFF_{el}, PR, maxFl) \quad (16)$$

$CAP \geq 0$ , which is only required for discrete investments, defines the generation capacity of the discrete investment option.  $C_{Cap} \geq 0$  defines the total investment cost for discrete generation devices. For linear generation devices the investment cost is expressed in terms of one unit of capacity.  $C_{OpFix} \geq 0$  expresses the fixed maintenance cost per unit of time. In the case of linear generation they expressed in proportion to capacity, while for discrete generation they express the maintenance cost of one discrete device.  $C_{OpVar} \geq 0$  expresses the variable maintenance cost per unit of input consumed.  $T_{Life} \in \mathbb{N}$  defines the life expectancy of a generation device, e.g. the time before it is replaced.  $EFF_{el} \in [0, 1]$  defines the ratio of supplied energy, for example sunlight or gas, to produced electricity.  $PR \in [0, 1]$  is another definable penalty to electricity production, which can, for example, express the degradation of solar cells.  $maxFl \in \mathbb{R}^{S \times T}$ ,  $maxFL \geq 0 \forall s, t$  denotes the maximal possible flow of input energy, e.g. sunlight in case of solar pv or gas in case of a fuel cell. This enables the representation of intermittent availability for wind and solar. It could nevertheless be used to model any condition that would restrict a conventional generation device from running at capacity at certain times, for example air quality regulation.

All instances of the  $GEN$  structure are collected in one list. The same is true for all instances of the  $dGEN$  structure. These lists and their sizes  $K$  and  $M$  are parameters. The model uses the iterators  $k$  and  $m$  to represent individual instances of these structures. (see section 3.2)

In addition, to model generation appropriately, several sets of constraints need to be defined:

$\forall u, k, s, t:$

$$\begin{aligned} genS_{u,k,s,t} &\leq \min\left(\frac{GEN_k \hookrightarrow EFF_{el} * GEN_k \hookrightarrow maxFl_{s,t}}{H_u \hookrightarrow GEN_k}, 1\right) \\ &* H_u \hookrightarrow GEN_k * GEN_k \hookrightarrow PR \end{aligned} \quad (17)$$

$\forall u, m, s, t:$

$$dgenS_{u,m,s,t} \leq \min\left(\frac{GEN_m \hookrightarrow EFF_{el} * GEN_m \hookrightarrow maxFl_{s,t}}{H_u \hookrightarrow dGEN_m * dGEN_m \hookrightarrow CAP}, 1\right) * H_u \hookrightarrow dGEN_m * dGEN_m \hookrightarrow CAP * dGEN_k \hookrightarrow PR \quad (18)$$

The capacity constraints restrict the use of any linear generation device  $GEN_k$  or any discrete generation device  $dGEN_m$  to its capacity rating and the maximum flow of input energy supplied to it. The constraints differ due to the capacity of linear generator devices being stored in the household structure directly, while for discrete generation devices the household structure only contains an integer representing the amount implemented. This value is then multiplied with the capacity of one unit of the concerned discrete generation device to compute the total installed capacity. In both cases the result is multiplied with the performance ratio  $PR$  of the concerned device, which acts as a penalty to capacity(see above). The minimized term calculates the ratio of maximum output achievable with the available maximum input to the capacity of the device. If the input suffices for running at capacity the term returns a maximum of 1, not restricting supply further, otherwise it restricts capacity to the maximum possible under current resource input.

### 3.5 Storage

The introduction of the concept of energy storage is necessary if the use of a large proportion of intermittent power production while maintaining intermittent power demand is to be seriously explored. Therefore an abstract linear storage device  $ST$  and an abstract discrete storage device  $dST$ , which can represent a range of technology options, are defined:

$$ST := (C_{Cap}, T_{Life}, EFF_{+-}, maxP_+, maxP_-) \quad (19)$$

$$dST := (CAP, C_{Cap}, T_{Life}, EFF_{+-}, maxP_+, maxP_-) \quad (20)$$

$CAP \geq 0$ , which is only required for discrete investments, defines the usable capacity of the discrete investment option.  $C_{Cap} \geq 0$  defines the total investment cost for discrete storage devices. For linear storage investment options the investment cost is expressed in terms of one unit of capacity.  $T_{Life} \in \mathbb{N}$  defines the life expectancy of a storage device, e.g the time before it is replaced. To be able to better estimate this value it is assumed, that storage is, on average, cycled once per day.  $EFF_{+-} \in [0, 1]$  defines the roundtrip efficiency, e.g. what proportion of one unit of power is left after charging and discharging inefficiencies. It is used to compute the charge and discharge efficiencies. The charge efficiency  $EFF_+$  is defined as  $EFF_+ = \sqrt{EFF_{+-}}$  and the discharge efficiency  $EFF_-$  as  $EFF_- = 1/EFF_+$ .[20]

$\max P_+ \geq 0$  and  $\max P_- \in [0, 1]$  denote the maximum charge rate and discharge rate respectively, relative to the devices capacity. All instances of the  $ST$  structure are collected in one list. The same applies for all instances of  $dST$ . The two lists and their sizes  $L$  and  $N$  are model parameters. The model uses the iterators  $l$  and  $n$  to represent individual instances of these structures. (see section 3.2) To model storage appropriately several sets of constraints need to be specified:

$\forall u, l, s, t:$

$$toST_{u,l,s,t} \leq ST_l \hookrightarrow \max P_+ * H_u \hookrightarrow ST_l \quad (21)$$

$$fromST_{u,l,s,t} \leq ST_l \hookrightarrow \max P_- * H_u \hookrightarrow ST_l \quad (22)$$

The flow constraints for linear storage constrain the maximum in- and outflow for each linear storage device to its maximum in- and outflow rate relative to capacity.

$\forall u, n, s, t:$

$$toDST_{u,n,s,t} \leq dST_n \hookrightarrow \max P_+ * H_u \hookrightarrow dST_n * dST_n \hookrightarrow CAP \quad (23)$$

$$fromDST_{u,n,s,t} \leq dST_n \hookrightarrow \max P_- * H_u \hookrightarrow dST_n * dST_n \hookrightarrow CAP \quad (24)$$

The flow constraints for discrete storage work similar to the linear ones, with the slight distinction of how capacity is computed. Rather than stored directly in the  $H_u$  structure, it is stored as an attribute of the discrete storage device structure  $dST_n$  and is multiplied by the integer amount of units implemented stored in  $H_u$ . (see 3.2)

$\forall u, l, s:$

$$\sum_{t=1}^T (ST_l \hookrightarrow EFF_+ * toST_{u,l,s,t'} - ST_l \hookrightarrow EFF_- * fromST_{u,l,s,t'}) = 0 \quad (25)$$

$\forall u, n, s:$

$$\sum_{t=1}^T (dST_n \hookrightarrow EFF_+ * toDST_{u,n,s,t'} - dST_n \hookrightarrow EFF_- * fromDST_{u,n,s,t'}) = 0 \quad (26)$$

The model assumes the storage to be full at the start of each simulated discontinuous period  $s$  and requires it to be full at the end of each period. This means inflows minus outflows weighted by the respective efficiencies need to sum up to zero for the entirety of each period  $s$ .

$\forall u, l, s, t:$

$$begin{aligned} & toST_{u,l,s,t} * ST_l \hookrightarrow EFF_+ \leq \\ & \sum_{t'=1}^{t-1} (-ST_l \hookrightarrow EFF_+ * toST_{u,l,s,t'} + ST_l \hookrightarrow EFF_- * fromST_{u,l,s,t'}) \end{aligned} \quad (27)$$

$\forall u, n, s, t:$

$$\begin{aligned} & toDST_{u,n,s,t} * dST_n \hookrightarrow EFF_+ \leq \\ & \sum_{t'=1}^{t-1} (dST_n \hookrightarrow EFF_+ * toDST_{u,n,s,t'} - dST_n \hookrightarrow EFF_- * fromDST_{u,n,s,t'}) \end{aligned} \quad (28)$$

The storage capacity constraints prohibit storage usage beyond the storage devices capacity. The remaining storage capacity at time  $(s, t)$  is in theory calculated as the capacity minus current storage level, which is the sum of all inflows and outflows weighted by in- and outflow efficiency. Since the storage at each timestep  $(s, 0)$  is required to be full, the capacity is subtracted once, which eliminates it and leaves only the sum. The constraint is implemented equivalently for discrete storage.

$\forall u, l, s, t:$

$$\begin{aligned} & fromST_{u,l,s,t} * ST_l \hookrightarrow EFF_- \leq H_u \hookrightarrow ST_l + \\ & \sum_{t'=1}^{t-1} (ST_l \hookrightarrow EFF_+ * toST_{u,l,s,t'} - ST_l \hookrightarrow EFF_- * fromST_{u,l,s,t'}) \end{aligned} \quad (29)$$

$\forall u, n, s, t:$

$$\begin{aligned} & fromDST_{u,n,s,t} * dST_n \hookrightarrow EFF_- \leq H_u \hookrightarrow dST_n * dST_n \hookrightarrow CAP+ \\ & \sum_{t'=1}^{t-1} (dST_n \hookrightarrow EFF_+ * toDST_{u,n,s,t'} - dST_n \hookrightarrow EFF_- * fromDST_{u,n,s,t'}) \end{aligned} \quad (30)$$

Finally, the storage level constraints prohibit the storage level to fall below zero. This means there can be no more power withdrawn, weighted by outflow efficiency, than is currently stored in the device. Because we assume the storage to be full at the start of each period  $s$ , the current charge amounts to one full charge (storage capacity) plus the sum of all transactions during the current period up to the current timestep  $t$ . The only distinction for discrete storage devices is the way capacity is calculated. (see 3.2)

### 3.6 Trade

Trade is implemented as an exchange platform, which sums up deposits and withdrawals of power at each timestep and always needs to be balanced. This approach has the advantage of reducing the number of constraints and therefore complexity greatly, although it is not very well suited to handle grid topology constraints which might be added in the future.

The trade constraint is defined as:

$\forall s, t:$

$$\sum_{u=1}^U (toTR_{u,s,t} - fromTR_{u,s,t}) = 0 \quad (31)$$

### 3.7 Demand

Abstract demand data  $DEM$  is defined as a set of the size  $S$  of demand profile sets of the size  $T$ :

$$DEM := \{DEM_s | s \in [1, S]; s \in \mathbb{N}; \forall DEM_s, DEM_s := \{DEM_{s,t} | t \in [0, T]; t \in \mathbb{N}\}\} \quad (32)$$

As frequently applied in literature,  $DEM_{s,t}$  is not a demand value, but rather a tuple of three demand values, critical demand, shiftable demand and curtailable demand [42][54][55][6] :

$$DEM_{s,t} := (critDEM_{s,t}, shiftDEM_{s,t}, curtDEM_{s,t}) \quad (33)$$

$\forall u, s, t:$

$$H_u \hookrightarrow critDEM_{s,t}, H_u \hookrightarrow shiftDEM_{s,t}, H_u \hookrightarrow curtDEM_{s,t}, t \geq 0$$

Critical demand will be met by the model as it is seen as a constraint. Shiftable demand can be shifted by one hour at a fixed rate defined for each household. Curtailable demand can be dropped at a fixed rate defined for each household. The restrictions on shiftable and curtailable demand is expressed by the following sets of constraints:

$\forall u, s, t:$

$$scS_{u,s,t} \leq H_u \hookrightarrow shiftDEM_{s,t} \quad (34)$$

$$ncS_{u,s,t} \leq H_u \hookrightarrow curtDEM_{s,t} \quad (35)$$

### 3.8 Grid

The modelled microgrid is connected to the grid via a common point of coupling. The grid is defined as:

$$GRID := (maxS, maxD, gridC, feedC) \quad (36)$$

with

$$maxS, maxD, gridC, feedC \in \mathbb{R}^{S \times T}$$

and  $\forall s, t$ :

$$maxS_{s,t}, max_{s,t}, gridC_{s,t}, feedC_{s,t} \geq 0$$

$maxS$  describes the maximum amount of power supplied by the grid at each timestep  $(s, t)$ , while  $gridC_{s,t}$  expresses the price at which this power can be bought.  $maxD$  describes the maximum amount power that can be fed into the the grid at timestep  $(s, t)$ , while  $feedC_{s,t}$  expresses the price at which the grid buys this power.

To model the expected behaviour of the grid several sets of constraints need to be introduced:

$\forall s, t$ :

$$\sum_{u=1}^U (fromGR_{u,s,t} - toGR_{u,s,t}) \leq maxS_{s,t} \quad (37)$$

The first grid constraint, restricts the sum of each households "trade balance" with the grid to the maximum power the grid can supply at each timestep.

$\forall s, t$

$$\sum_{u=1}^U (toGR_{u,s,t} - fromGR_{u,s,t}) \leq maxD_{s,t} \quad (38)$$

The second grid constraint does the reverse, in that it restricts the sum of each households "trade balance" with the grid to the maximum power the microgrid can feed into the grid at each timestep.

### 3.9 Power Balance

The power balance constraints describe the need for a balance between supply and demand at each node at each timestep:

$\forall u, s, t$ :

$$H_u \hookrightarrow critDEM_{s,t} + H_u \hookrightarrow shiftDEM_{s,t} + H_u \hookrightarrow curtDEM_{s,t}$$

=

$$\begin{aligned} & fromGR_{u,s,t} - toGR_{u,s,t} + \sum_{k=1}^K genS_{u,k,s,t} + \sum_{m=1}^M dgenS_{u,m,s,t} \\ & + fromTR_{u,s,t} - toTR_{u,s,t} + scS_{u,s,t} - scS_{i,s,t-1} + ncS_{u,s,t} \\ & + \sum_{l=1}^L fromST_{u,l,s,t} - toST_{u,l,s,t} + \sum_{n=1}^N fromDST_{u,n,s,t} - toDST_{u,n,s,t} \end{aligned} \quad (39)$$

The power balance constraint requires electricity supply and demand to be balanced for each household at each timestep. On the demand side the three types of demand of the concerned household and the current timestep are summed up. The supply side is made up of several terms:

$fromGR_{u,s,t} - toGR_{u,s,t}$  expresses the momentary trade balance with the grid, while  $fromTR_{u,s,t} - toTR_{u,s,t}$  denotes the momentary trade balance with the microgrid's trading pool.  $scS_{u,s,t} - scS_{i,s,t-1}$  is the balance of consumption shifted from the current timestep into the future and past shifted demand realized now.  $ncS_{u,s,t}$  reflects loads dropped in the current timestep. Finally the power generated by all linear and discrete generation devices is summed up, as well as the balance of storage use for all linear and discrete storage devices.

### 3.10 Cost Minimisation Formula

The cost minimisation formula calculates the cost of all investment and dispatch decisions made:

$$\min C_{total} = C_{Investment} + C_{Operation} + C_{Dispatch} \quad (40)$$

The total cost can be broken down into investment, operation and dispatch costs.

$$\begin{aligned} C_{Investment} = & \sum_{u=1}^U [\sum_{k=1}^K (GEN_k \rightarrow C_{Cap} * H_u \rightarrow GEN_k) \\ & + \sum_{l=1}^L (ST_l \rightarrow C_{Cap} * H_u \rightarrow ST_l) \\ & + \sum_{m=1}^M (dGEN_m \rightarrow C_{Cap} * H_u \rightarrow dGEN_m) \\ & + \sum_{n=1}^N (dST_n \rightarrow C_{Cap} * H_u \rightarrow dST_n)] \end{aligned} \quad (41)$$

The investment costs consist of all investment into generation and storage devices throughout the microgrid. In the context of the model this means for linear investment options the installed capacity times the costs of capital per unit of capacity and for discrete investment options the costs of capital for a single instance of a device multiplied with the number of instances installed.

$$\begin{aligned} C_{Operation} = & \sum_{u=1}^U [\sum_{k=1}^K (GEN_k \rightarrow C_{OpFix} * H_u \rightarrow GEN_k * S * T) \\ & + \sum_{m=1}^M (dGEN_m \rightarrow C_{opFix} * H_u \rightarrow GEN_m * S * T)] \end{aligned} \quad (42)$$

The operation costs are the sum of all fixed operation costs of all generation devices deployed. They are calculated for each investment option in each household by multiplying its fixed operation costs with the installed capacity (or pieces in the case of discrete investment options) and the total number of timesteps. The sum over all of these investment options are the total maintenance costs for generation in the microgrid. Since there is no fixed maintenance cost defined for storage this value is equal to all the maintenance costs incurred.

$$\begin{aligned}
 C_{Dispatch} = & \sum_{s=1}^S \sum_{t=1}^T \sum_{u=1}^U [gridC_{s,t} * fromGR_{u,s,t} - feedC_{s,t} * toGR_{u,s,t} \\
 & + H_u \hookrightarrow curtP * ncS_{u,s,t} + H_u \hookrightarrow shiftP * scS_{u,s,t} \\
 & + \sum_{k=1}^K (GEN_k \hookrightarrow C_{OpVar} * genS_{u,k,s,t}) \\
 & + \sum_{m=1}^M (dGEN_m \hookrightarrow C_{OpVar} * dgenS_{u,m,s,t})]
 \end{aligned} \tag{43}$$

The dispatch cost consist of the fuel costs (or variable operation costs  $C_{OpVar}$ ) incurred by the use of all deployed generation devices as well as the value of all shifted and curtailed loads. In addition all transactions with the main grid are valued at the power and feed-in rates for their respective timestep and summed up.

## 4 Implementation

The performance of a modeling tool depends as much on its implementation, as on mathematical soundness. In this section the choices made implementing the model described in the previous section are outlined.

The implementation of the modeling tool pursues multiple objectives:

- Performance: The ability to solve the problem adequately fast.
- Scalability: The ability for the system to potentially be used by many users concurrently, without encountering performance issues.
- Flexibility: The ability to receive a wide range of differently formatted input data and still function adequately. Sparse, or otherwise lacking input data is preprocessed, and can be supplemented by default values.
- User-Friendliness: The tool offers a user-friendly way of inputting data and of viewing computation results, possibly through a graphical interface.

### 4.1 Architecture

To address these objectives the modeling tool was designed to work as a multi-layer architecture, with each layer performing a distinct part of the work flow. It is important to note however, that, while these layers can run on separate machines to provide scalability, they do not have to. In the setup used for conducting the case study all layers were run on a single machine.

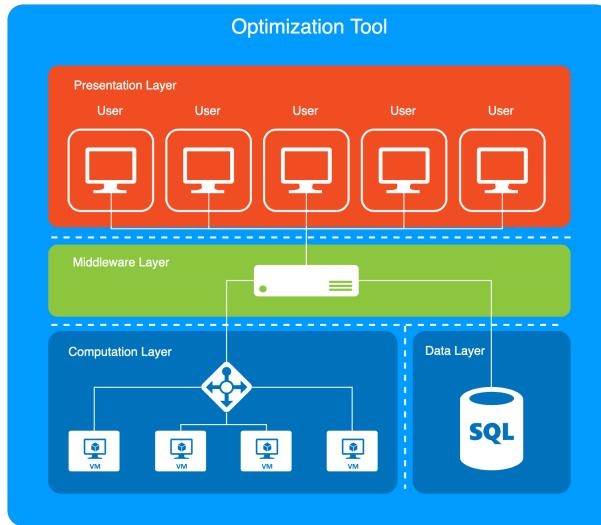


Figure 2: The proposed architecture for scaling the optimization tool

Source: Own Illustration.

The computation layer is where the actual model is built and solved. It ideally consist of several worker units, possibly virtualized or containerized, which run the model code and a load balancing server queueing and assigning tasks received from the middleware layer via messages and relaying the returned solutions. It is currently implemented only rudimentary as shell script, that relays input and output data and launches the model code. The model code is written in the Julia programming language, which was chosen for its high performance [and its focus on scientific computing](#). The model code also includes the data preprocessing code, which grants the user higher flexibility regarding the form and quality of her input data. It is integrated directly with the model itself, so the model can be used with different interfaces without the need to implement data preprocessing first (see 4.2). This does however impact performance, as preprocessing in the presentation layer would be distributed. The data layer should ideally consist of an SQL database which allows the implementation of features in the presentation layer, that require a persistent state, such as user authentication or saved requests and solutions. It is accessed via the middleware layer. For all but the largest scale implementations there is no need to physically separate it from the middleware layer. The data layer and corresponding functionality are currently not implemented.

The middleware layer coordinates communication between the users and the layers below. It is currently implemented as a simple node.js server [exposing a REST API to the presentation layer](#).

The presentation layer handles all user input and presents the results of the calculations conducted by the computation layer. It also handles all data processing required for presenting the data tu the user. It is currently implemented as a Web Application using the React.js framework .

[reference](#)

[reference](#)

[reference](#)

[reference](#)

## 4.2 Workflow

When the user enters data in the presentation layer, basic type checks are conducted. The input is then encoded as a JSON string , which is sent as the payload of an HTML GET-Request to the middleware layer. The middleware layer transfers the JSON string into the environment the model code is run in and launches the model code. The model preprocesses the received input. The preprocessing is configured with option parameters which are included in the input. Currently the model supports a number of preprocessing options:

- Filling vector parameters, such as electricity prices or shiftable demand with a constant.
- Adjusting the length of a number of vector parameters by cutting, if too long and looping, if too short.
- Adding noise to a number of vector parameters, by multiplying each value with a random number out of a normal distribution with a mean of 1.0. A variance can additionally be supplied.
- Normalizing the weights given to the discontinuous periods  $s_i$ .

The model is then constructed and solved. For construction the Julia library "JuMP" is used, for solving the Gurobi commercial solver. The model results are saved and transferred to the presentation layer via the middleware layer in a response to the GET-Request sent earlier. In the presentation layer the results are interactively visualized using the plotly visualization library. Currently a dispatch chart for each modeled household as well as two charts showing the generation and storage investment of each household are generated. In addition Key Performance Indicators (KPIs) such as the the levels of autarky and self-consumption or the average cost per KWh consumed are calculated to make different result easier to compare.

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## 5 Case Study

### 5.1 Overview

To demonstrate the viability of the designed model and of local microgrids, a limited case study is conducted. The location chosen is the small village of Morschenich in Northrhine-Westphalia, which is located in immediate proximity to the lignite surface mine of Hambach. According to current plans of RWE, the owner and operator of the mine and the state of Northrhine-Westphalia, the village is due to be razed and the population resettled by the year 2024, when the mining activities are expected to reach the village. [35][26]



**Figure 3: The village of Morschenich**

Source: Google Maps.

Although the resettlement process has already begun and the village 'Morschenich-Neu' is under construction several kilometers away, there are as of the date of writing still several hundred inhabitants remaining in Morschenich, including some Syrian war refugees, who have been accommodated in abandoned houses of families already been resettled.[3]

The case study will focus on the northern part of Morschenich, where several housing- and two commercial units are located in block as indicated by the white line in Figures 2 and 3.



**Figure 4: A detailed view of the chosen location.**

Source: Google Maps.

In figure 3 all buildings in the area designated for the case studies proposed microgrid have been marked with coloured boxes. Blue boxes represent small residential units, while green boxes indicate larger residential and red boxes commercial units.

The case study will examine the business case of the establishment of an autonomous microgrid in the selected area. Therefore we model investment decisions and dispatch for three discontinuous periods of one week each to reflect the different conditions encountered throughout the year. The buildings designated will be assumed to be the participants of the considered microgrid. The different classes of buildings are modelled with different parameters to accurately represent their distinct sizes and uses.

The following sections will document the assumed input parameters the model requires for the calculation of a base scenario and how they were derived. To properly function the model requires meteorological data for constraints on intermittent power generation, as well as data on investment options, household demand and grid supply. The final section will introduce a number of further scenarios in which some of the assumptions are changed.

## 5.2 Meteorological Data

An hourly profile of solar the capacity factor for a pv installation in Morschenich is sourced from [34]. From the profile, which includes an entire year of data, three samples are extracted: One 144 hour sample representing the transitional season, e.g. spring and fall and two 72 hour samples representing summer and winter. The difference in length is not relevant for use in the model, as the data preprocessing only uses these profiles as input for generating the profiles used in the optimization itself (see section 4). The resulting vector of values is used as the parameter  $GEN_1 \hookrightarrow maxFl$ , which is interpreted as the maximum input flow for the solar pv installation. In addition the parameter  $EFF_{el}$  is set to 1.0, which makes the model effectively treat the vector as a capacity factor.

## 5.3 Investment Options

To test the different implementations of discrete and linear investment options the case study incorporates two linear-scaling generation devices as possible investments, as well as two discretely-scaling storage devices. The generation devices consist of a photovoltaic system as a renewable option and a combined heat and power fuel cell, as a conventional, though decentralised and highly efficient option. It is further capable of using biofuels, which can be expressed through higher fuel prices.

**Table 1: Parameters describing the generation technologies**

Parameter	Name	Unit	Value	Reference
<i>Photovoltaic System</i>	$GEN_1$			
Installation Cost	$C_{Cap}$	$\text{€}K\text{W}^{-1}$	1200	Estimate based on [48], [43], [27]
Maintenance Cost	$C_{OpFix}$	$\text{€}K\text{W}^{-1}\text{yr}^{-1}$	50	Estimate
Fuel Cost	$C_{OpVar}$	$\text{€}K\text{Wh}^{-1}$	0.0	no sun taxes ... yet
Lifetime	$T_{Life}$	yr	25	[48]
Electric Efficiency	$EFF_{el}$	%	100	included in $maxFl$
Performance Ratio	$PR$	%	85	[48]
Maximum Input Flow	$maxFl$	KW	see section 5.2	based on insolation
<i>CHP Micro Fuel Cell</i>	$GEN_2$			
Installation Cost	$C_{Cap}$	$\text{€}K\text{W}^{-1}$	3500	Estimate based on [20]
Maintenance Cost	$C_{OpFix}$	$\text{€}K\text{W}^{-1}\text{yr}^{-1}$	175	Estimate based on [20]
Fuel Cost	$C_{OpVar}$	$\text{€}K\text{Wh}^{-1}$	0.0608	[29]
Lifetime	$T_{Life}$	yr	15	[20]
Electric Efficiency	$EFF_{el}$	%	60	[5]
Performance Ratio	$PR$	%	100	no additional penalties
Maximum Input Flow	$maxFl$	KW	999	no restrictions

The storage investment options given are two differently sized Lithium Ion batteries: A 4 KWh option manufactured by Victron Energy and a 13.5 KWh option manufactured by Tesla. While the two generation devices are hypothetical, these storage devices can actually be bought, which leads to lower

error due to false assumptions and linearisation of non-linear relationships (such as storage size and price). This the main advantage discrete modelling of investment options has over linear modelling.

**Table 2: Parameters describing the storage technologies**

Parameter	Name	Unit	Value	Reference
<i>Li-Ion Battery 1</i>	$dST_1$			<i>Tesla Powerwall</i>
Usable Capacity	$CAP$	KWh	13.5	[36]
Installation Cost	$C_{Cap}$	€	10000	Estimate based on [36]
Lifetime	$T_{Life}$	yr	10	Estimate based on [36]
Roundtrip Efficiency	$EFF_{+-}$	%	90	[36]
Max. charging power	$maxP_+$	kW	4.6	[36]
Max. discharging power	$maxP_-$	kW	4.6	[36]
Initial State of Charge	—	%	100	Assumption
Terminal State of Charge	—	%	100	Assumption
<i>Li-Ion Battery 2</i>	$dST_2$			<i>Victron Energy Lithium HE Batterie</i>
Usable Capacity	$CAP$	KWh	4	based on [22] considering depth of discharge
Installation Cost	$C_{Cap}$	€	5000	Estimate based on [47]
Lifetime	$T_{Life}$	yr	10	Estimate based on [22]
Roundtrip Efficiency	$EFF_{+-}$	%	92	[20]
Max. charging power	$maxP_+$	KW	4.8	[22]
Max. discharging power	$maxP_-$	KW	7.2	[22]
Initial State of Charge	—	%	100	Assumption
Terminal State of Charge	—	%	100	Assumption

## 5.4 Demand

As the case study distinguishes between three types of buildings, three demand profiles where compiled. Each profile is made up of three hourly load vectors spanning one or several days. Demand vectors for the two types of residential units are sourced from [17]. The choice was made because these profiles are specifically created for optimization of decentralized generation. They are samples of measurements taken on several houses and therefore feature a much higher variability than standard profiles, which usually are averages of many measurements. In the context of this case study it is critical to accurately reflect this high variability, which a microgrid can do a lot to manage. For the commercial units profiles where sourced from the association of the German power industry (BDEW) [11][4]. These are standard profiles specifically from commercial consumers. The samples were of varying sizes of one to several days, to reflect the approximate ratios of occurrences of the different model days provided for our particular meteorological region. They were further preprocessed by the model itself. The noise filter of the model was provided with a variance value of 0.25 for the smaller residential households and a variance of 0.15 for the larger residential and commercial buildings (see 4). This additional noise is crucial in distinguishing the demands of different instances of one household type from one another, as would occur in reality. Furthermore it makes the load profile more realistic, when scaled beyond its original length, since it makes the repeated profile differ notably.(see 4)

For the residential buildings it is assumed that at any time 10 percent of loads can be curtailed at a flat renumeration rate of 0.35€per KwH. A further 20 percent of total loads are assumed to be shiftable at a flat rate of 0.15€per KwH per hour shifted. The remaining 70 percent of loads are deemed essential. The commercial units can also shift up to 20 percent of their load for 0.15€per KwH per hour, but no curtailment is allowed.

The profiles are scaled for the total yearly demand of the smaller residential buildings to be around 5000 KWh. The multi-family residential and commercial buildings' profiles are scaled to a yearly demand of approximately 10000 KWh and 16000 KWh respectively.

## 5.5 Grid Supply

For the base scenario the grid supply is assumed to be capped at a constant value of 500KW, which guarantees that all supply can be met solely by the grid. It is further assumed that the price of this energy is set at 0.3€at any time. The feed in tariff is assumed to be constant at 0.08€and the feed-in is capped at a constant 20KW.

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## 5.6 Further Assumptions

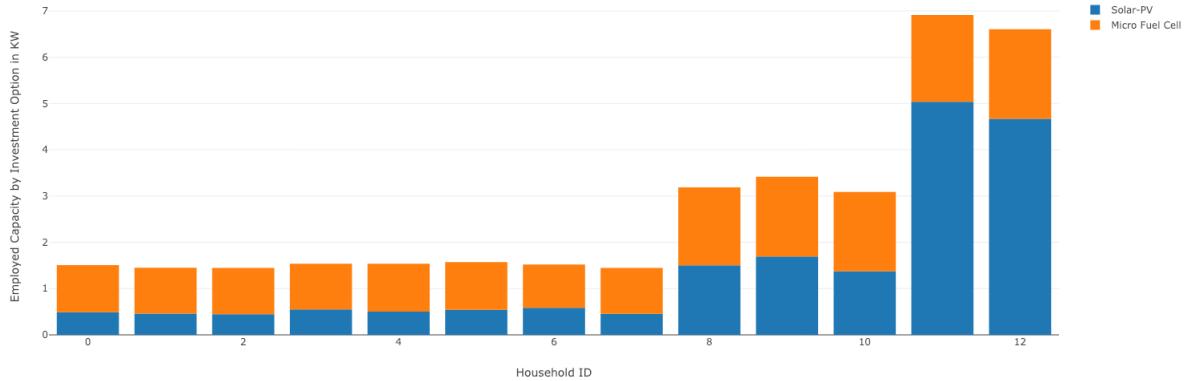
To keep the model from trading randomly inside the microgrid, a trade fee of 0.001€per KWh is imposed on all trade within the microgrid.

To accurately reflect the prevalence of the weather conditions and demand profiles represented by the three seasonal periods modelled the summer, winter and transitional period have been weighed with the factors 169, 81 and 115, respectively. These factors are normalized during preprocessing (see 4) and all cost incurred during each period is multiplied with the normalized corresponding weight. The weights have been chosen according to the prevalence of different weather conditions in the meteorological region of Morschenich [17].

## 5.7 Results

Surprisingly, even in the base scenario, the microgrid seems to be commercially viable, as an autarky level of 94 percent is reached. Investment is heavily biased towards Fuel Cells (see figure 4), which are installed at a smaller capacity than pv installations but operate at a capacity factor of up to 100 percent versus around 12 for pv. Therefore, most power is generated by flexible gas fuel cells (dark blue), only supplemented by a small amount of pv generation (light blue), mostly installed by the commercial consumers, which have higher loads throughout the day, and therefore are less

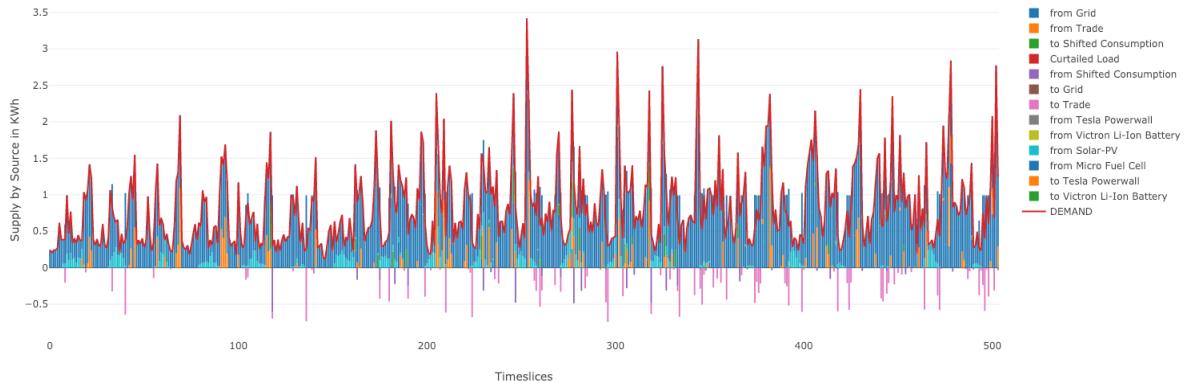
disadvantaged by the intermittency of pv. With this setup the model stays at a self-consumption rate of 100 percent, as feed-in renumeration seems to be insufficient. Furthermore no storage is needed to achieve these levels of autarky and self-sufficiency.



**Figure 5: Generation Investment in the base setup of the case study**

Source: Own Model User Interface

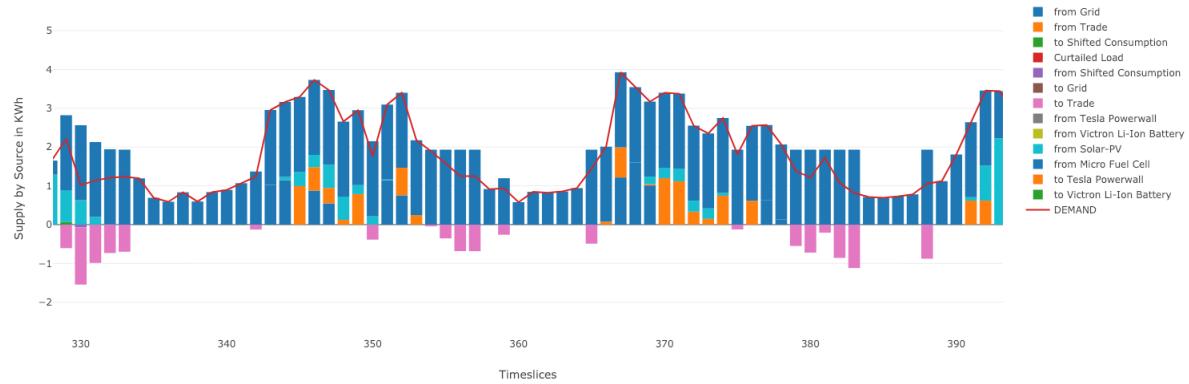
As can be observed in figures 5 and 6 trading (orange and pink) is heavily utilised for balancing, as the load profiles of participants differ enough to enable this. Also load shifting (green and purple) is sporadically used (see figures 5 and 6), but rarely loads are shifted for more than one hour.



**Figure 6: The dispatch of a residential building in the base setup of the case study**

Source: Own Model User Interface

The only use of the use of grid energy (also dark blue, but below orange and light blue) occurs during the winter week (the last third of the dispatch chart), when generation and internal dispatch are insufficient to meet peak demand, most likely due to a lack of irradiation (see figure 6).



**Figure 7: The dispatch of a commercial building in detail for two winter days**

Source: Own Model User Interface

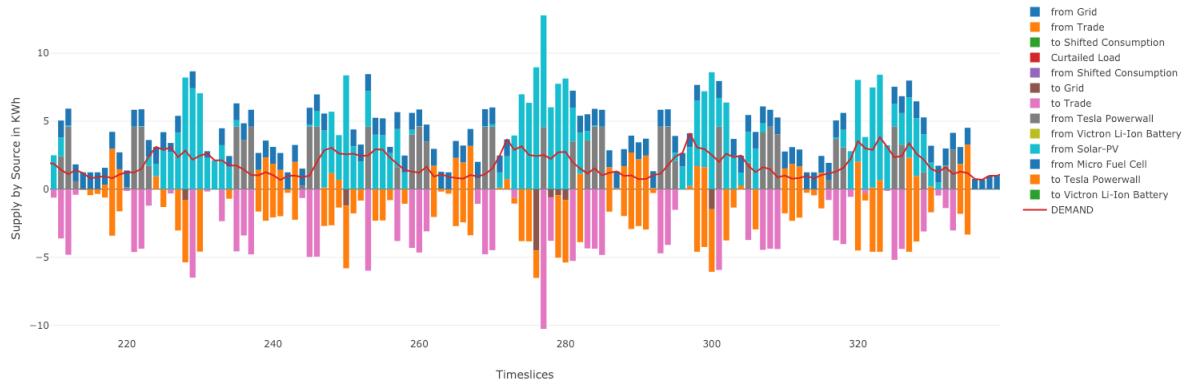
Overall the result is surprisingly cheap, with the average cost per KWh being at about 0.164 € and the total cost at approximately 1259.624 €.

The model solves in approx. 4-6 minutes on a macOS 10.14 system with the Gurobi Commercial Solver and a 3.3Ghz Quad-Core Intel Core i5 processor with 24GB of 1867MHz DDR3 RAM.

## 5.8 Sensitivity Analysis

To test the validity and robustness of the solution obtained above, a sensitivity analysis is conducted.

To test the importance of the use of fuel cells for the result and its robustness, first the price of gas is raised by 50 percent. This could reflect the  $CO^2$  neutral use of more expensive biogas or the insecurity of the price of fossile fuels in general, as the investment horizon considered in the case study is up to 25 years.



**Figure 8: Effects of a gas price increase of 50 percent**

Source: Own Model User Interface

The increased gas price results in a drop of installed fuel cell capacity by around a quarter. Pv deployment consequently increases by over 300 percent. One of thee commercial buildings, in addition to 17.7 KWp of pv is equipped with a Tesla Powerwall, which is utilized heavily to store solar energy which is traded to the microgrid during the evening (see figure 7). Autarky remains high at 92 percent, while self consumption drops slightly to 96 percent. The grid is still not utilized a lot since the average price per KWh at 0.199 €is still well below grid power prices. Still the objective value rises approx. 20 percent to 1524.547 €.

Another factor which seems critical to the base result is the reliance on trading. To test the robustness of trading, the price per traded KWh of electricity is raised from a merely symbolic 0.001€to 0.03€. This could be considered the cost of maintaining the infrastructure of the grid, or the energy lost in cross-microgrid transactions.

This has only a negligible effect, as the objective value is only raised by about 10 €. Raising the fee to 0.06 €. per KWh has a similarly small effect, raising the objective value by another 18 €. Another increase to 0.09 €fails to have a much greater impact at an objective value of approx. 1293 €.

Another possibility is a change in the price of pv panels and batteries in the coming years. To test the effect these changes could have on the optimal result, the base case is altered by reducing the investment price of pv installations by 25 percent and the investment price of storage by 35 percent. This has a simnilar effect to increased gas prices, in that fuel cell deployment falls, whereas pv installations increase. Additionally, as before, one Tesla Powerwall is installed by a commercial entity. The effect on the objective value however is not significant, as it is only decreased by 46€or 0.005€per KWh. Adding the 50 percent increased gas prices to alterations results in a total of 64 KWp pv

installation, but only a single Powerwall, which seems to suffice, as self-consumption is still at 92 percent. The average electricity price rises to 0.19 €. Decreasing battery prices by 50 percent relative to the base case results in the installation of a second Powerwall in one of the multi-family residential buildings. The solution however, is hardly superior at 0.188 € per KWh.

Finally, a major weakness of the base cases result is the linear scaling of the price of generation technology, which leads to installation of small capacities throughout the microgrid. In reality this would be very expensive, since the prices do not in fact scale linearly. To test the robustness to non-linear generation options, we convert both generation options to discrete investments. The pv installation will only be available in increments of 5 KWp and the Fuel Cell in increments of 2.5 KWp.

The test is run with a 15 min time limit, as it does not terminate in a reasonable amount of time otherwise. The gap to optimality after this period is at 0.31 percent or approx. 4 €.

## **6 Discussion and Conclusion**

## 7 Appendix

### 7.1 Literature Review

The used search String was: [microgrid AND (optimization OR optimisation) AND linear programming]

The used databases are ScienceDirect, IEEE Xplore and Google Scholar.

The original dataset consists of 300 publications of which 275 remained after duplicates were merged.

The search string for the Abstract Keyword Search was [(microgrid OR micro-grid OR off-grid) AND (optimization OR optimisation OR optimise OR optimal OR optimally) AND (linear programming OR linear program OR mixed integer)]

After the abstract keyword search was conducted 106 publications remained.

The inclusion criteria were:

1. An optimization model is employed.
2. There is some discussion about the design of the model.
3. The objective of the model is the optimization of design or dispatch of a single microgrid.
4. There is some sort of case study conducted.

The exclusion criteria were:

1. The publication is not in English language.
2. The full text is not obtainable for this author with reasonable effort.
3. The publication is a Work-In-Progress / Conference Paper version of a publication published in a journal and also included in this dataset.
4. The mathematical model designed is non-linear.
5. The mathematical model designed only considers a specific aspect of dispatch or design, not the entirety.
6. The mathematical model is mostly focused on heat generation/distribution rather than electricity.

After the filtering by inclusion and exclusion criteria 58 publications remained.

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