# PRÁCTICA 1

Pablo Baeyens Antonio Checa Iñaki Madinabeitia José Manuel Muñoz Darío Sierra Algorítmica

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# EJERCICIO 1: EFICIENCIA EMPÍRICA

| Tamaño | Antonio  | Darío     | Iñaki     | José Manuel | Pablo      |
|--------|----------|-----------|-----------|-------------|------------|
| 2000   | 0,011413 | 0,0146897 | 0,0140894 | 0,00961352  | 0,00950047 |
| 10000  | 0,285049 | 0,292014  | 0,317834  | 0,319125    | 0,256134   |
| 18000  | 0,9231   | 0,957501  | 1,05149   | 1,12075     | 0,893985   |
| 26000  | 1,93603  | 2,30372   | 2,1866    | 2,41593     | 1,91995    |
| 34000  | 3,31074  | 3,46101   | 3,72809   | 4,20884     | 3,42199    |
| 42000  | 5,26566  | 5,59224   | 5,69877   | 6,46732     | 5,13279    |
| 50000  | 8,1269   | 7,95426   | 8,08572   | 9,2569      | 7,48556    |

| Tamaño | Antonio    | Darío     | Iñaki     | José Manuel | Pablo     |
|--------|------------|-----------|-----------|-------------|-----------|
| 2000   | 0,00515467 | 0,0188928 | 0,0056981 | 0,00642196  | 0,0100637 |
| 10000  | 0,121217   | 0,121786  | 0,133457  | 0,158756    | 0,126158  |
| 18000  | 0,410265   | 0,393202  | 0,436515  | 0,515545    | 0,409696  |
| 26000  | 0,872412   | 0,817823  | 0,902801  | 1,07721     | 0,853734  |
| 34000  | 1,50895    | 1,62408   | 1,5385    | 1,84905     | 1,46012   |
| 42000  | 2,35229    | 2,29655   | 2,34051   | 2,81587     | 2,22564   |
| 50000  | 3,40647    | 3,47501   | 3,3125    | 3,98744     | 3,15386   |

| Tamaño | Antonio   | Darío      | Iñaki      | José Manuel | Pablo     |
|--------|-----------|------------|------------|-------------|-----------|
| 2000   | 0,0044917 | 0,00745713 | 0,00500529 | 0,00545271  | 0,0136858 |
| 10000  | 0,107932  | 0,107475   | 0,119386   | 0,139938    | 0,106441  |
| 18000  | 0,368311  | 0,345483   | 0,394836   | 0,43881     | 0,344915  |
| 26000  | 0,760331  | 0,903855   | 0,816444   | 0,903978    | 0,711269  |
| 34000  | 1,33726   | 1,76733    | 1,35952    | 1,53781     | 1,21549   |
| 42000  | 2,08887   | 2,29417    | 2,09879    | 2,34337     | 1,84894   |
| 50000  | 3,02904   | 3,52064    | 2,92835    | 3,32697     | 2,62017   |

#### **ALGORITMOS CÚBICOS**

| Tamaño | Antonio     | Darío       | Iñaki       | José Manuel | Pablo       |
|--------|-------------|-------------|-------------|-------------|-------------|
| 30     | 0,000224592 | 0,000625181 | 0,000280424 | 0,000377972 | 0,000661632 |
| 150    | 0,0186866   | 0,0403935   | 0,0211072   | 0,024806    | 0,0200893   |
| 270    | 0,104221    | 0,106563    | 0,119058    | 0,141979    | 0,110954    |
| 390    | 0,314773    | 0,390241    | 0,358154    | 0,445757    | 0,328791    |
| 510    | 0,692464    | 0,847743    | 0,790683    | 0,965839    | 0,735368    |
| 630    | 1,30571     | 1,40966     | 1,47915     | 1,82847     | 1,37284     |
| 750    | 2,27876     | 2,69492     | 2,48584     | 3,03609     | 2,3061      |

| Tamaño   | Antonio  | Darío    | Iñaki    | José Manuel | Pablo    |
|----------|----------|----------|----------|-------------|----------|
| 1000000  | 0,140354 | 0,184352 | 0,158862 | 0,201315    | 0,151376 |
| 5000000  | 0,768809 | 0,958429 | 0,87572  | 1,10639     | 0,834242 |
| 9000000  | 1,43536  | 2,0214   | 1,63635  | 2,06708     | 1,57758  |
| 13000000 | 2,12925  | 2,98066  | 2,39937  | 3,06728     | 2,30709  |
| 17000000 | 2,81701  | 4,44071  | 3,17474  | 4,04963     | 3,04674  |
| 21000000 | 3,69781  | 5,38552  | 3,95077  | 5,0512      | 3,77894  |
| 25000000 | 4,59738  | 6,59753  | 4,77483  | 6,07513     | 4,53331  |

| Tamaño   | Antonio | Darío   | Iñaki    | José Manuel | Pablo    |
|----------|---------|---------|----------|-------------|----------|
| 1000000  | 0,22421 | 0,29581 | 0,252793 | 0,305145    | 0,298779 |
| 5000000  | 1,54404 | 1,77557 | 1,66226  | 2,03485     | 1,52638  |
| 9000000  | 3,20945 | 3,38923 | 3,30651  | 4,05931     | 2,98857  |
| 13000000 | 5,0709  | 5,08649 | 5,06756  | 6,19867     | 4,54708  |
| 17000000 | 7,11513 | 6,95513 | 6,93151  | 8,42371     | 6,22592  |
| 21000000 | 9,14739 | 8,49386 | 8,85375  | 10,7763     | 7,98279  |
| 25000000 | 11,2477 | 11,9356 | 10,7142  | 13,1053     | 9,69064  |

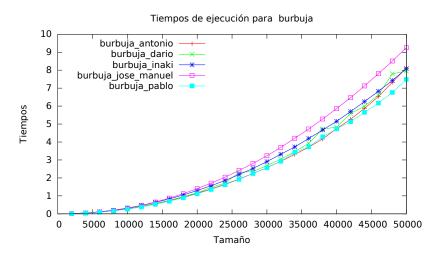
| Tamaño   | Antonio  | Darío   | Iñaki    | José Manuel | Pablo    |
|----------|----------|---------|----------|-------------|----------|
| 1000000  | 0,217543 | 0,41989 | 0,245436 | 0,301188    | 0,260094 |
| 5000000  | 1,35111  | 2,59677 | 1,42201  | 1,74213     | 1,32955  |
| 9000000  | 2,41358  | 4,73714 | 2,56327  | 3,17912     | 2,40275  |
| 13000000 | 3,73061  | 6,84617 | 4,03523  | 5,08856     | 3,76172  |
| 17000000 | 4,85593  | 7,76039 | 4,95366  | 6,13015     | 4,61115  |
| 21000000 | 6,56725  | 10,9268 | 6,45905  | 7,96927     | 6,0763   |
| 25000000 | 8,30719  | 12,8678 | 8,11788  | 10,0094     | 7,57097  |

| Tamaño | Antonio     | Darío       | Iñaki       | José Manuel | Pablo       |
|--------|-------------|-------------|-------------|-------------|-------------|
| 1      | 1,44e-07    | 4,62e-07    | 1,79e-07    | 4,47e-007   | 4,14e-07    |
| 5      | 3,51e-07    | 6,73e-07    | 2,61e-07    | 4,46e-007   | 3,79e-07    |
| 9      | 8,29e-07    | 1,998e-06   | 1,131e-06   | 8,92e-007   | 1,149e-06   |
| 13     | 2,937e-06   | 5,269e-06   | 3,612e-06   | 2,678e-006  | 2,959e-06   |
| 17     | 1,1107e-05  | 2,4038e-05  | 1,7977e-05  | 1,428e-005  | 1,658e-05   |
| 21     | 9,3336e-05  | 0,000151545 | 0,000132759 | 9,4604e-005 | 0,000106961 |
| 25     | 0,000630981 | 0,000971833 | 0,000675111 | 0,00063992  | 0,000665583 |

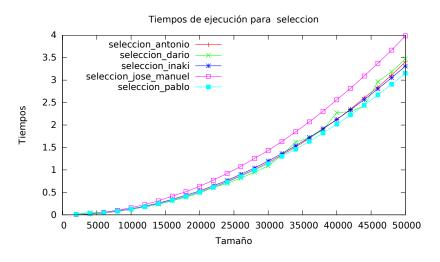
| Tamaño | Antonio     | Darío       | Iñaki       | José Manuel | Pablo       |
|--------|-------------|-------------|-------------|-------------|-------------|
| 1      | 1,79e-07    | 1,42e-07    | 1,85e-07    | 4,46e-007   | 1,62e-07    |
| 5      | 6,54e-07    | 6,14e-07    | 5,96e-07    | 8,93e-007   | 5,04e-07    |
| 9      | 4,721e-06   | 4,856e-06   | 5,639e-06   | 3,57e-006   | 4,151e-06   |
| 13     | 6,5735e-05  | 4,9866e-05  | 7,8102e-05  | 4,998e-005  | 5,3298e-05  |
| 17     | 0,000772841 | 0,000963856 | 0,000988963 | 0,000784504 | 0,000884214 |
| 21     | 0,0121097   | 0,0145301   | 0,0136331   | 0,0125967   | 0,0131647   |
| 25     | 0,19084     | 0,205991    | 0,214262    | 0,201252    | 0,203966    |

# EJERCICIO 2: ELABORACIÓN DE GRÁFICAS

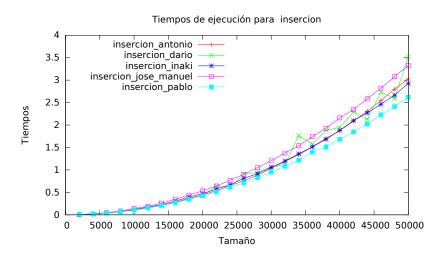
## **BURBUJA**



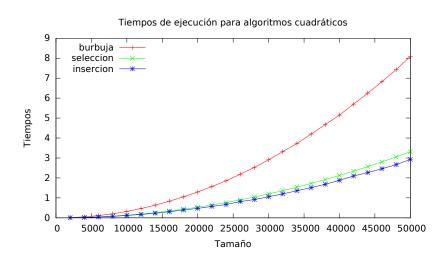
#### **SELECCIÓN**



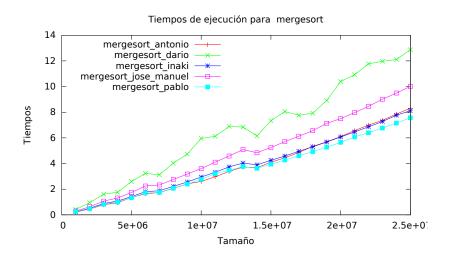
### **INSERCIÓN**



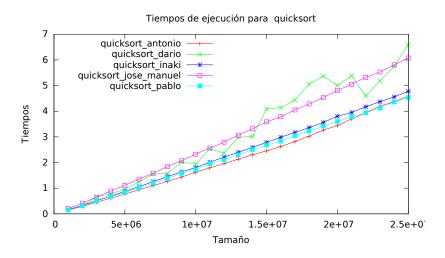
## COMPARATIVA: ALGORITMOS CUADRÁTICOS



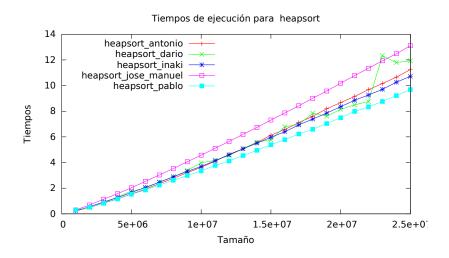
#### **MERGESORT**



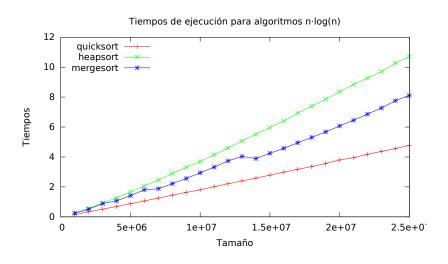
## **QUICKSORT**



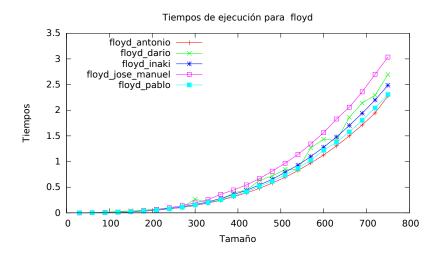
#### **HEAPSORT**



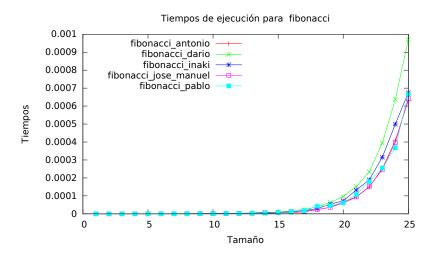
# COMPARATIVA: ALGORITMOS O(nlog(n))



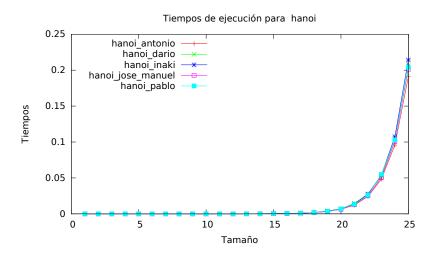
#### **ALGORITMO DE FLOYD**



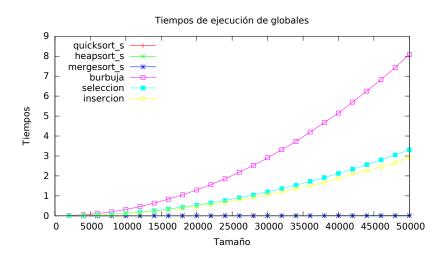
#### **FIBONACCI**



## **HANÓI**



#### COMPARATIVA GLOBAL DE LOS ALGORITMOS



# EJERCICIO 3: EFICIENCIA HÍBRIDA

| Persona     | Eficiencia híbrida de Burbuja   | r    |
|-------------|---|------|
| Antonio     | $3.67 \cdot 10^{-9}n^2 - 3.02 \cdot 10^{-5}n + 0.189$                       | 0.99 |
| Darío       | $89 \cdot 10^{-3} - 1.62 \cdot 10^{-5} \cdot n + 3 \cdot 10^{-9} \cdot n^2$ | 0.99 |
| José Manuel | $3.85 \cdot 10^{-9} n^2 - 7.88 \cdot 10^{-6} n + 0.013$                     | 0.99 |
| Pablo       | $3 \cdot 10^{-9}n^2 - 6 \cdot 10^{-6}n + 0{,}015$                           | 0.99 |
| Iñaki       | $3.23 \cdot 10^{-9} n^2 + 1.36 \cdot 10^{-7} n - 2.52 \cdot 10^{-5}$        | 0.99 |

| Persona     | Eficiencia híbrida de Inserción   | r    |
|-------------|---|------|
| Antonio     | $1.21 \cdot 10^{-9} n^2 - 5.77 \cdot 10^{-6} n + 0{,}003$                       | 0.99 |
| Darío       | $89 \cdot 10^{-3} + -1.62 \cdot 10^{-5} \cdot n + 1.68 \cdot 10^{-9} \cdot n^2$ | 0.99 |
| José Manuel | $1.32 \cdot 10^{-9} n^2 + 4.95 \cdot 10^{-7} n - 0.0024$                        | 0.99 |
| Pablo       | $10^{-9}n^2 + 4 \cdot 10^{-7}n + 0{,}002$                                       | 0.99 |
| Iñaki       | $1.18 \cdot 10^{-9}n^2 + 1.36 \cdot 10^{-7}n - 2.5 \cdot 10^{-5}$               | 0.99 |

| Persona     | Eficiencia híbrida de Selección   | r    |
|-------------|---|------|
| Antonio     | $1.459 \cdot 10^{-9}n^2 - 5.7 \cdot 10^{-6}n + 0{,}002$                         | 1    |
| Darío       | $89 \cdot 10^{-3} - 1.616 \cdot 10^{-5} \cdot n + 1.59 \cdot 10^{-9} \cdot n^2$ | 0.99 |
| José Manuel | $1.59 \cdot 10^{-9} n^2 + 2.93 \cdot 10^{-7} n - 0.0022$                        | 0.99 |
| Pablo       | $10^{-9}n^2 - 2 \cdot 10^{-7}n + 0{,}004$                                       | 1    |
| Iñaki       | $1.31 \cdot 10^{-9}n^2 + 5.81 \cdot 10^{-7} - 0.002$                            | 0.99 |

| Persona     | Eficiencia híbrida de Heapsort                      | r     |
|-------------|---|-------|
| Antonio     | $2.72 \cdot 10^{-8} n \log(n) - 0.55$               | 0.999 |
| Darío       | $2.56 \cdot 10^{-8} n \log(n) - 0.005$              | 0.99  |
| José Manuel | $3.13 \cdot 10^{-8} n \log(n) - 0.37$               | 0.99  |
| Pablo       | $1.8 \cdot 10^{-8} n \log(n) - 1.9 \cdot 10^{-7}$   | 0.995 |
| Iñaki       | $2.46 \cdot 10^{-8} n \log(n) + 1.36 \cdot 10^{-7}$ | 0.99  |

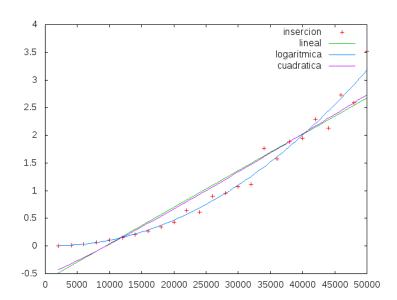
| Persona     | Eficiencia híbrida de Mergesort                 | r     |
|-------------|---|-------|
| Antonio     | $1.918 \cdot 10^{-8} n \log(n) - 0.305$         | 0.996 |
| Darío       | $3.03 \cdot 10^{-8} n \log(x) - 0.004$          | 0.99  |
| José Manuel | $2.29 \cdot 10^{-8} n \log(n) - 0.08$           | 0.99  |
| Pablo       | $2 \cdot 10^{-8} n \log(n) - 1.9 \cdot 10^{-7}$ | 0.997 |
| Iñaki       | $1.48 \cdot 10^{-8} n \log(n) + 1$              | 0.99  |

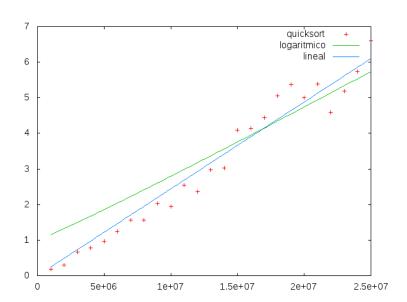
| Persona     | Eficiencia híbrida de Quicksort                     | r     |
|-------------|---|-------|
| Antonio     | $1.06 \cdot 10^{-8} n \log(n) - 0.083$              | 0.999 |
| Darío       | $1.46 \cdot 10^{-8} \cdot n \log(n) - 0.005$        | 0.99  |
| José Manuel | $1.42 \cdot 10^{-8} n \log(n) + 0.02$               | 0.99  |
| Pablo       | $1.3 \cdot 10^{-8} n \log(n) - 1.9 \cdot 10^{-7}$   | 0.999 |
| Iñaki       | $1.12 \cdot 10^{-8} n \log(n) + 1.36 \cdot 10^{-7}$ | 0.99  |

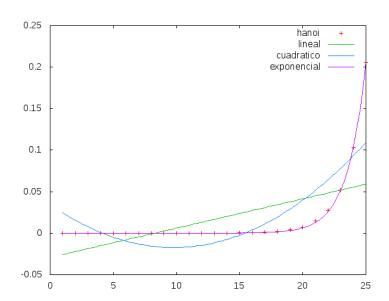
| Persona     | Eficiencia híbrida de Floyd  | r     |
|-------------|--|-------|
| Antonio     | $6 \cdot 10^{-9}n^3 - 7.9 \cdot 10^{-7}n^2 - 2.17 \cdot 10^{-4}n + 0.012$              | 0.999 |
| Darío       | $6.98 \cdot 10^{-9} \cdot n^3 - 7.66 \cdot 10^{-7} \cdot n^2 + 0.0002 \cdot n - 0.005$ | 0.999 |
| José Manuel | $6.88 \cdot 10^{-9}n^3 + 2.89 \cdot 10^{-7}n^2 - 4.44 \cdot 10^{-5}n + 0.001$          | 0.999 |
| Pablo       | $5.1 \cdot 10^{-9} n^3 + 3.8 \cdot 10^{-7} n^2 - 8.3 \cdot 10^{-5} n + 0.005$          | 1     |
| Iñaki       | $5.76 \cdot 10^{-9}n^3 + 1.36 \cdot 10^{-7}n^2 - 2.52 \cdot 10^{-5}n + 0.002$          | 0.999 |

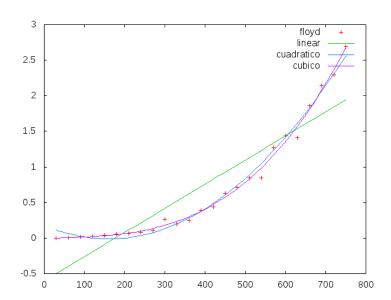
| Persona     | Eficiencia híbrida de Fibonacci                     | r     |
|-------------|---|-------|
| Antonio     | $3.81 \cdot 10^{-9} \varphi^n + 7.21 \cdot 10^{-7}$ | 0.999 |
| Darío       | $0.002 \cdot \varphi^n - 0.004$                     | 0.999 |
| José Manuel | $3.81 \cdot 10^{-9} \varphi^n + 9.68 \cdot 10^{-7}$ | 0.999 |
| Pablo       | $6.4 \cdot 10^{-9} \varphi^n - 1.8 \cdot 10^{-8}$   | 0.997 |
| Iñaki       | $4.29 \cdot 10^{-9} \varphi^n + 5.6 \cdot 10^{-6}$  | 0.995 |

| Persona     | Eficiencia híbrida de Hanoi                   | r     |
|-------------|---|-------|
| Antonio     | $5.69 \cdot 10^{-9} 2^n + 1.1 \cdot 10^{-4}$  | 1     |
| Darío       | $6.38 \cdot 10^{-9} \cdot 2^n - 0.005$        | 0.984 |
| José Manuel | $6.00 \cdot 10^{-9} 2^n + 9.3 \cdot 10^{-6}$  | 0.999 |
| Pablo       | $6.1 \cdot 10^{-9} 2^n + 1.1 \cdot 10^{-9}$   | 0.998 |
| Iñaki       | $6.39 \cdot 10^{-9}2^n + 9.48 \cdot 10^{-13}$ | 0.999 |



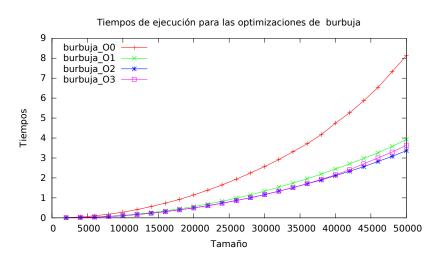




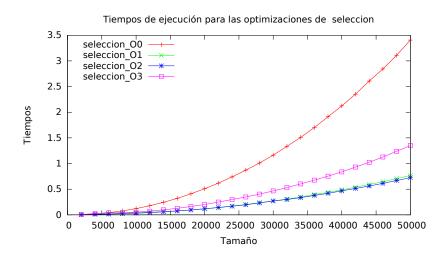


## EJERCICIO 4: EFICIENCIA SEGÚN LA OPTIMIZACIÓN

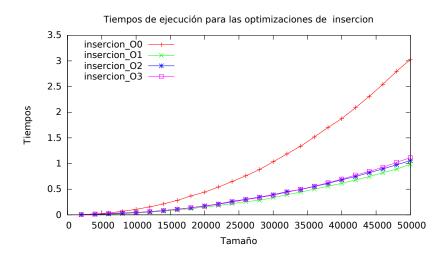
| Tamaño | O0       | O1         | O2         | O3         |
|--------|----------|------------|------------|------------|
| 2000   | 0,011413 | 0,00767027 | 0,00729825 | 0,00886811 |
| 10000  | 0,285049 | 0,124228   | 0,109425   | 0,10953    |
| 18000  | 0,9231   | 0,450813   | 0,402396   | 0,400231   |
| 26000  | 1,93603  | 0,983933   | 0,869556   | 0,865144   |
| 34000  | 3,31074  | 1,74399    | 1,51139    | 1,51782    |
| 42000  | 5,26566  | 2,70633    | 2,3327     | 2,40839    |
| 50000  | 8,1269   | 3,92439    | 3,36591    | 3,64032    |



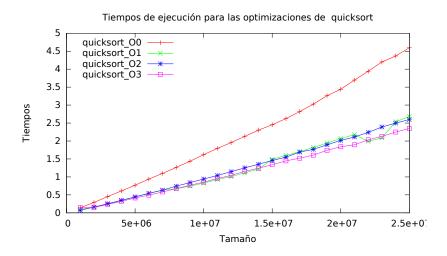
| Tamaño | O0         | O1         | O2         | O3         |
|--------|------------|------------|------------|------------|
| 2000   | 0,00515467 | 0,00518568 | 0,00295874 | 0,00781173 |
| 10000  | 0,121217   | 0,0446664  | 0,0325282  | 0,0535996  |
| 18000  | 0,410265   | 0,0952006  | 0,0954893  | 0,162643   |
| 26000  | 0,872412   | 0,202472   | 0,197149   | 0,347695   |
| 34000  | 1,50895    | 0,347973   | 0,335636   | 0,602817   |
| 42000  | 2,35229    | 0,538412   | 0,513721   | 0,930382   |
| 50000  | 3,40647    | 0,766349   | 0,725693   | 1,3503     |



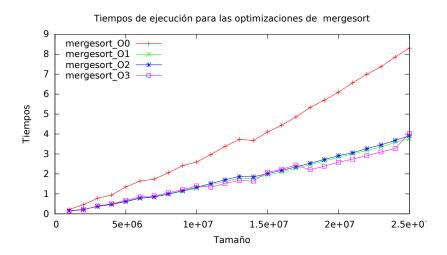
| Tamaño | O0        | O1         | O2         | O3         |
|--------|-----------|------------|------------|------------|
| 2000   | 0,0044917 | 0,00195844 | 0,00468466 | 0,00632375 |
| 10000  | 0,107932  | 0,037316   | 0,0457049  | 0,0458144  |
| 18000  | 0,368311  | 0,120639   | 0,138311   | 0,137761   |
| 26000  | 0,760331  | 0,257764   | 0,301838   | 0,295198   |
| 34000  | 1,33726   | 0,444824   | 0,492365   | 0,497819   |
| 42000  | 2,08887   | 0,679748   | 0,747116   | 0,773843   |
| 50000  | 3,02904   | 0,987499   | 1,05693    | 1,11367    |



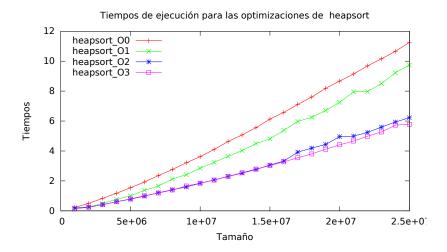
| Tamaño   | O0       | O1       | O2        | O3       |
|----------|----------|----------|-----------|----------|
| 1000000  | 0,140354 | 0,108984 | 0,0723194 | 0,145934 |
| 5000000  | 0,768809 | 0,4443   | 0,444097  | 0,413716 |
| 9000000  | 1,43536  | 0,744798 | 0,842272  | 0,768711 |
| 13000000 | 2,12925  | 1,11231  | 1,2527    | 1,15554  |
| 17000000 | 2,81701  | 1,70221  | 1,69107   | 1,52156  |
| 21000000 | 3,69781  | 2,17781  | 2,11261   | 1,8951   |
| 25000000 | 4,59738  | 2,68214  | 2,59766   | 2,34848  |



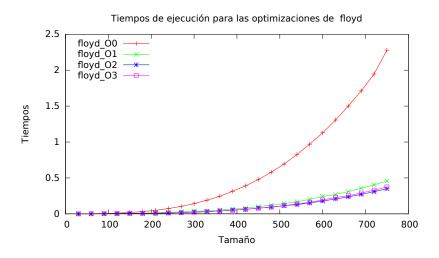
| Tamaño   | O0       | O1       | O2       | O3       |
|----------|----------|----------|----------|----------|
| 1000000  | 0,217543 | 0,14913  | 0,155871 | 0,142481 |
| 5000000  | 1,35111  | 0,605842 | 0,626561 | 0,673165 |
| 9000000  | 2,41358  | 1,12709  | 1,15498  | 1,21198  |
| 13000000 | 3,73061  | 1,76984  | 1,86878  | 1,66805  |
| 17000000 | 4,85593  | 2,28211  | 2,35156  | 2,44318  |
| 21000000 | 6,56725  | 3,00782  | 3,05882  | 2,74309  |
| 25000000 | 8,30719  | 3,76735  | 3,90997  | 4,03064  |



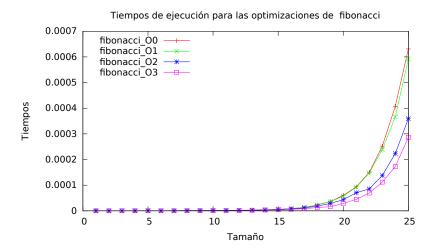
| Tamaño   | O0      | O1       | O2       | O3       |
|----------|---------|----------|----------|----------|
| 1000000  | 0,22421 | 0,162612 | 0,189088 | 0,124874 |
| 5000000  | 1,54404 | 0,996273 | 0,776043 | 0,797603 |
| 9000000  | 3,20945 | 2,41538  | 1,59403  | 1,65914  |
| 13000000 | 5,0709  | 4,02955  | 2,52116  | 2,54731  |
| 17000000 | 7,11513 | 5,97832  | 3,9232   | 3,5468   |
| 21000000 | 9,14739 | 7,9527   | 4,99053  | 4,66293  |
| 25000000 | 11,2477 | 9,74256  | 6,22192  | 5,78521  |



| Tamaño | O0          | O1         | O2         | O3         |
|--------|-------------|------------|------------|------------|
| 30     | 0,000224592 | 0,00011651 | 5,3519e-05 | 8,2696e-05 |
| 150    | 0,0186866   | 0,00662406 | 0,00634183 | 0,00455262 |
| 270    | 0,104221    | 0,029449   | 0,0166624  | 0,0174797  |
| 390    | 0,314773    | 0,0663636  | 0,052403   | 0,0504283  |
| 510    | 0,692464    | 0,14376    | 0,114807   | 0,115598   |
| 630    | 1,30571     | 0,269596   | 0,207239   | 0,227301   |
| 750    | 2,27876     | 0,456356   | 0,349434   | 0,374203   |



| Tamaño | O0          | O1          | O2          | O3          |
|--------|-------------|-------------|-------------|-------------|
| 1      | 1,44e-07    | 3,74e-07    | 4,1e-07     | 4,05e-07    |
| 5      | 3,51e-07    | 6,09e-07    | 4,66e-07    | 3,84e-07    |
| 9      | 8,29e-07    | 1,177e-06   | 9,62e-07    | 7,74e-07    |
| 13     | 2,937e-06   | 3,159e-06   | 2,467e-06   | 2,21e-06    |
| 17     | 1,1107e-05  | 1,4243e-05  | 1,1615e-05  | 8,258e-06   |
| 21     | 9,3336e-05  | 9,188e-05   | 7,0517e-05  | 4,4614e-05  |
| 25     | 0,000630981 | 0,000592224 | 0,000359381 | 0,000286624 |



**HANÓI** 

| Tamaño | O0          | O1          | O2          | O3          |
|--------|-------------|-------------|-------------|-------------|
| 1      | 1,79e-07    | 2,03e-07    | 3,96e-07    | 3,6e-07     |
| 5      | 6,54e-07    | 4,43e-07    | 1,256e-06   | 6,19e-07    |
| 9      | 4,721e-06   | 2,48e-06    | 4,946e-06   | 3,05e-06    |
| 13     | 6,5735e-05  | 2,4637e-05  | 5,0217e-05  | 2,3284e-05  |
| 17     | 0,000772841 | 0,000387059 | 0,000577299 | 0,000286237 |
| 21     | 0,0121097   | 0,00643389  | 0,00811653  | 0,00335663  |
| 25     | 0,19084     | 0,0969232   | 0,0829641   | 0,0535821   |

**HANÓI** 

