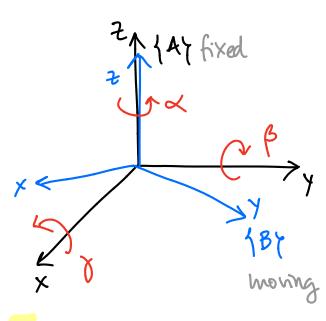
1) Fixed Angle Representation



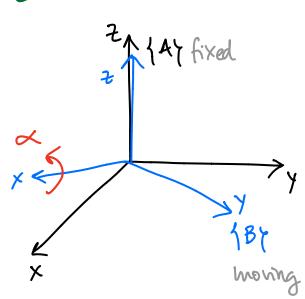
- When noing a fixed angle
 representation, each rotation tales
 place about a fixed (not moring)
 reference frame
- We rotate a frame (By nong the axes of a fixed frame (Ay

$$A$$
 $B \approx XYZ (8, \beta, \alpha) = R_2(\alpha) R_Y(\beta) R_X(8)$
 X,Y,Z

We apply backwards

Note that each of the elementary Rx (0), Ry (0), Rz (0) are the same for fixed/monny rotation of a around axis 2 of fixed frame (A)

2) Euler Angle Representation (Moving)



- With this representation, each notation takes place about the exis of the moning system

ellmentary Rx (0), Ry(0), Rz(0) are the same for fixed/moning

(3) Comparing rotation representations

All representations yield the same rotation. We need 3 values for describing the orientation, but the order M which they're applied is relevant - that's why re have rotation representation conventions.

There is a set of 24 angle representation conventions, depending on:

- fixed / moving (Enler)
- order: XYZ, ZYZ, ZYX ...

(4) Example: Find Enter angles

$$H_{K} = \begin{bmatrix} 1 & 0 & 0 & | & 2 \\ 0 & 0 & 0 & | & 5 \\ 0 & 1 & 0 & | & 9 \\ \hline 0 & 0 & 0 & | & 1 \end{bmatrix}, W_{B} = \begin{bmatrix} 0 & -1 & 0 & | & 3 \\ 1 & 0 & 0 & | & -3 \\ 0 & 0 & 1 & | & 1 \\ \hline 0 & 0 & 0 & | & 1 \end{bmatrix}$$

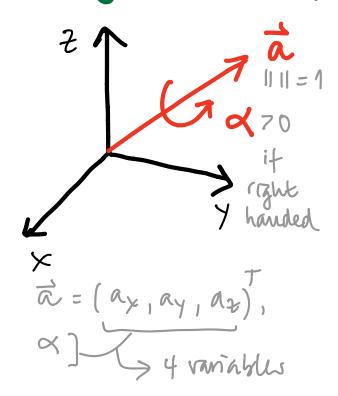
Enler angles Z-X-Z of BH6?

$$\begin{array}{lll}
\mathsf{BH}_{\mathsf{G}} &= \begin{pmatrix} \mathsf{M}_{\mathsf{H}_{\mathsf{B}}} \end{pmatrix}^{-1} & \mathsf{M}_{\mathsf{G}} &= \begin{bmatrix} 0 & 1 & 0 & 3 \\ -1 & 0 & 0 & 3 \\ 0 & 0 & 1 & -1 \\ \hline 0 & 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & 0 & 2 \\ 0 & 0 & -1 & 5 \\ 0 & 1 & 0 & 0 \\ \hline 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\begin{array}{lll}
\mathsf{RT}_{\mathsf{C}} &= \mathsf{RT}_{\mathsf{C}} & \mathsf{C}_{\mathsf{C}} &$$

By comparing the developed matrix with the values, we can isolate/solve for $\angle 13, \delta$.

) Angle-Axis Representation



It is possible to represent a rotation, orientation with an. axis a and an angle & around it.

Interpretation: we attach a to a fame/ostect and notate around it.

the moerse tansformatin is also possible, book at the Wikipedral

$$Q = a \cos \left(\frac{11 + 12 + 133 - 1}{2} \right)$$

Note that it 15 undefined for a = 0, 180.

6 Unit quaternions = Euler parameters
Unit quaternions are 4D constructs that describe
rotations as a vector:

$$\vec{q} = (q_1, q_2, q_3, q_4)^T$$
, $||\vec{q}|| = \sqrt{q_1^2 + q_2^2 + q_3^2 + q_4^2} = 1$
They are related to the angle-axis representation:

$$\vec{\alpha} = (\alpha_x, \alpha_y, \alpha_z)^T, \alpha$$

$$94 = \cos(\alpha/2)$$

(7) Rodrignes Formula

A notation on 3D space belongs to the rotation group of all possible rotations in Enclidean space R2, denoted as 50(3). Exponental maps can be noted to compute rotations in that group. The Rodrigues' formula shows how to rotate a rector around an axis without computny its exponential map.

thus, it can be used to rotate the 3 axus of of frame without computing the notation matrix!

Giren

- A vector it e IR3
- A unit rector K of rotation
- An angle θ for notation (0>0 right handed) The notated vector \mathcal{T}_{rot} is:

Jot = J. ωsθ + (KxJ). smθ + K. (K.+) (1-ωsθ)