1 Rarelow twin

Barlow Twin

Batch of images X (Augmentation 1)

Batch of images X (Augmentation 2)

$$Z^{A} = f_{0}(y^{A})$$
;  $Z^{B} = f_{0}(y^{B})$  // mean contined.

RET = \( \lambda \lamb

where, G. = \( \frac{\zeta}{b} \frac{\zeta}{b} \) \( \frac{\zeta}{

La summation over all the samples.

compared with others.

non parametric estimation of Enterpy of reps.

(P) Bordow twin (Appendix)

Information Bottleneck connection

(X)

Dishorted

Images

IB = I (20, 4) -BI (0, x) // close means

= [H(20) - H(20) y) As reducted to X as possible.

- B [H(20) - H(20) x)]

B conholable

- B [H(20) - H(20) x)]

- B [H(20) - H(20) x)]

 $\approx H(20) + \frac{1-B}{B}H(20)$  if B = 1 //always possible

then total positive (Entropy)

Zo re goussian constonants.

IBO = Ex log (Se) + 1-B log (Cro)

covernance

tunction

connected to IB with some modification & constraints.

( Demystrifying CL

**Demystifying Contrastive Learning** 

Contrastive loss.

exp (f(x) t (x)/e)

 $\mathcal{L}(D,D^{+}) = -\mathcal{E}$   $(2,2^{+}) \in D^{+} \quad \exp[f(x)^{T} + (x^{+})/2] + \mathcal{E} \quad \exp(f(x)^{T} + (x^{+})/2)$   $\tilde{\chi} \in D$ 2, x & D+

Measuring Invariance; transformation t

invocation h iff. h(x) = h(t(x))

formal Notion iff y(x) = y(+|x|) ; where,  $+ = x \rightarrow x$ tre  $h^{*}(x) = h(+|x|)$ 

invariant for 4(x) & label (y)

Definition of firing Unit

h (x) ∈ R ; fine y sihi (x) > +i ; si€[-1, 1]

Jubal firing reale, Giv: E [fix) // ti dependency.

ti chosen such that of G(i) = /y/ no of class.

& numbers of firing with

one dass + one section trug,

Equal party

1 Denystifying CL Local trajectory: T(x) = { + (x, x) | + 2} //set of Local firing rate is defined as below & their towns formation. fractubn of time i neuron fines. Twiget conditioned invariance  $J_y(i) = \frac{L_y(i)}{G(i)}$ Representation Invariance Score: (RIS): Nextrons commonalities in top to newrong for each dosses.

(P) Prototopical Contoartive leaving

Prototypical Contrastive learning

traliminariles

$$x = \{x_i, ---x_n\} \quad \text{in ordes}.$$

$$f \to \text{embedding function.}$$

$$x \to v = \{v_i, ---v_n\}$$

$$v_i' = f(x_i)$$

$$\text{dispance} \quad i = i \quad \text{order}$$

$$\text{dispance} \quad v_i' = f(x_i)$$

$$\text{dispance} \quad v_i' = f(x_i)$$

$$\text{dispance} \quad \text{order}$$

$$\text{dispance} \quad \text{order}$$

$$\text{dispance}$$

$$\text{dispance} \quad \text{order}$$

$$\text{dispance}$$

$$\text{dispan$$

D' - roving trug of D

II flow tooptamize this ??

$$\frac{2}{E} = \frac{E}{E} = \frac{E$$

E sep

prototype C: + centroid of the cluster.

 $\frac{M-step:}{\mathcal{E}} = \mathcal{E}(ci) \log p(xi, ci|\theta) = \mathcal{E} \mathcal{E}(cixi, \theta) \log p(xi, ci|\theta)$   $= \sum_{i=1}^{n} c_i \mathcal{E}(cixi, \theta) \log p(xi, ci|\theta)$ 

$$= \sum_{i=1}^{n} \sum_{c_i \in C} \mathbf{1}(x_i \in c_i) \log P(x_i, c_i \mid \theta)$$

$$P(x_i', c_i|\theta) = P(x_i|c_i, \theta)P(c_i|\theta) = \frac{1}{K} P(x_i|c_i, \theta)$$
uniformity Assumption

P Prototopical CL

Assuming isotopic gausstan.

$$P(x_i \mid C_i, \theta) = exp\left(\frac{-(v_i - c_s)^2}{2v_s^2}\right) \left(\frac{\kappa}{2v_s^2}\right) \left(\frac{-(v_i - c_s)^2}{2v_s^2}\right)$$
eatable format

By applying normal tration of + & c we get.

$$P(z;|c;,\theta) = \exp\left(\frac{-(z-z)^2c_s}{2c_s}\right) / \frac{z}{z} \exp\left(\frac{-(z-z)^2c_s}{zc_s}\right)$$

so maximizing by likelihood falk into.

with different number of charter ??

of what if 1 is bad??

concentrateur frimation : p (smaller means high concentration) 

scaling foctor for com