

PIRL

PIRL (pretext invariant representation learning)

Notation: Dataset $\mathcal{D} = \{I_1, I_2 \dots I_D\}$

$$I_n \in \mathbb{R}^{W \times H \times 3}$$

Transformation set, \mathcal{T}

Network $\phi_\theta(\cdot)$

$$v_I = \phi_\theta(I)$$

Target optimization:

$$L_{inv}(\theta, \mathcal{D}) = \mathbb{E}_{t \sim P(t)} \left[\frac{1}{|\mathcal{D}|} \sum_{I \in \mathcal{D}} L(v_I, v_{I_t}) \right]$$

contrastive target:

$$L_{co}(\theta, \mathcal{D}) = \mathbb{E}_{t \sim P(t)} \left[\frac{1}{|\mathcal{D}|} \sum_{I \in \mathcal{D}} L_{co}(v_I, z(t)) \right]$$

measure properties of transformation +
Keep semantic
irrelevant info.

Loss function,

$$h(v_I, v_{I_t}) = \frac{\exp\left(\frac{s(v_I, v_{I_t})}{\tau}\right)}{\exp\left(\frac{s(v_I, v_{I_t})}{\tau}\right) + \sum_{I' \in \mathcal{D}_N} \exp\left(\frac{s(v_{I_t}, v_{I'})}{\tau}\right)}$$

$$L_{NCE}(I, I^t) = -\log[h(f(v_I), g(v_{I^t}))] \\ - \sum_{I' \in \mathcal{D}_N} \log[1 - h(g(v_{I'}), f(v_I))]$$

final loss function:

$$L(I, I^t) = \lambda L_{NCE}(m_I, g(v_{It})) + (1-\lambda) L_{NCE}(m_I, f(v_I))$$

Annotations: "step 2" points to $g(v_{It})$; "step 1" points to $f(v_I)$; a bracket on the right side of the equation is labeled "kinda two step".

- ① $f(v_I)$ similar to m_I // damping.
- ② $f(v_I), f(v_I')$ dissimilar.