⑧ Neural turing machine — Neural Turing Machine

Reading: memory $M_t \rightarrow (N) \times [M]$ matrix
- N: memory location
- M: vector size at each location
- t: time

Attention weights $0 \le w_t(i) \le 1$; $i \in \{1 \dots N\}$ with constraint $\sum_i w_t(i) = 1$

read memory r_t ($1 \times M$ size) $\leftarrow \sum_i w_t(i) M_t(i)$
- i: ith row
- convex combination, weighted sum of rows
- differentiable

Writing:

$$\tilde{M}_t(i) \leftarrow M_{t-1}(i) \left[1 - w_t(i) e_t \right]$$

- e_t: erase vector ($1 \times M$), $[0 \dots 1]$
- $M_{t-1}(i)$ and $w_t(i) e_t$: pointwise multiply
- both differentiable

After erase add:

$$M_t(i) \leftarrow \tilde{M}_t(i) + w_t(i) a_t$$

Constructing weight vector:

focusing by content

$$w_t^c(i) \leftarrow \frac{\exp\left(\beta_t K\left[k_t, M_t(i)\right]\right)}{\sum_j \exp\left(\beta_t K\left[k_t, M_t(j)\right]\right)}$$

- β_t: key strength
- K: cosine sim
- k_t: key vector ($1 \times M$)

focusing by location:

interpolation gate (0, 1)

$$\underline{w}_t^g \leftarrow g_t \underline{w}_t^c + (1 - g_t)\underline{w}_{t-1}$$

$$\tilde{w}_t(i) \leftarrow \sum_{j=0}^{N-1} w_t^g(j)\, s(i-j)$$

shift weight,

$$w_t(i) \leftarrow \frac{\tilde{w}_t(i)^{\gamma_t}}{\sum_j \tilde{w}_t(j)^{\gamma_t}}$$

→ sharpening & normalization.