

notation: feature extractor network f_θ

$$f_\theta: \underbrace{X}_{\text{image}} \rightarrow \underbrace{Z}_{\substack{\downarrow \\ \text{embed dim } \mathbb{R}^d}}$$

classifier projector: f_ϕ

$$f_\phi: Z \rightarrow \mathbb{R}^{C_u + C_n}$$

probability score: $\hat{y} = \text{Softmax}(f_\phi \circ f_\theta(x))$

Objective to discover Novel classes.

$$L_{\text{nov}} = L_{\text{pair}} + L_{\text{CE}} + L_{\text{reg}}$$

$$L_{\text{pair}} = \sum_{i \neq j} \left(\underbrace{\text{sim}(\hat{y}_{i:}, \hat{y}_{j:})}_{f_\phi} - \overbrace{\text{sim}(z_i, z_j)}^{f_\theta} \right)^2$$

Pairwise Similarity loss. Novelty

Pairwise similarity function

$$f_{\Omega}: \mathcal{Z} \times \mathcal{Z} \rightarrow [0, 1]$$

Bi-level optimization procedure:

① $(\theta^*, \phi^*) = (\theta, \phi) - \alpha_{(\theta, \phi)} \nabla_{(\theta, \phi)} \mathcal{L}_{\text{loss}}(\theta, \phi, \Omega)$

level ① classifier & feature extractor network.

Supervised cross-entropy: $\mathcal{L}_{\text{ce}}^L = - \sum_i \sum_k y_{i,k} \log \hat{y}_{i,k}$

utilize updated parameter.

② $\Omega^* = \Omega - \alpha_{\Omega} \nabla_{\Omega} \mathcal{L}_{\text{CE}}^L(\theta^*, \phi^*)$

level ②

Swapped prediction !!

Dealing with labeled & pseudo-labeled data? weak aug.

$$S_{PL} = \left\{ (x_i^s, \hat{y}_{i,:}^w) \mid \max(\hat{y}_{i,:}^w) > \tau \right\}$$

strong augmentation

New ground truth $S = S_{PL} \cup S_L$

retrain using these.

$$L_{ce} = - \sum_{i \in S_0} \sum_{k=1}^{C_u} \tilde{y}_{i,k} \log \hat{y}_{i,k}$$

Entropy regularization

$$L_{reg} = - \sum_{k=1}^{C_u} y_k \log \hat{y}_k \quad // \text{enforce single decision.}$$

Close world setting with iterative pseudo-labeling