

MX automation: few perspectives from ESRF

MXCUBE UI

Present	Future
Unique interface (user/BL scientist)	
Manual puck assignment	Auto puck assignment

SHIPMENT ASSIGNMENT

Shipment is always linked to a session with date

Immutable session date is part of the folders structure

89 shipments candidates for FX89								
Shipment			Experiment					
Name	Status	Created on	Start on	beamline				
ESRF FX23 15...	PROCESSING	08-11-2024	15-11-2024	ID30A-1	1 parcels / 2 containers (25 samples)			
ESRF FX23 8 ...	SENT TO USER	01-11-2024	08-11-2024	ID30A-1	1 parcels / 4 containers (62 samples)			
ESRF FX23 25...	SENT TO USER	17-10-2024	25-10-2024	ID30A-1	1 parcels / 3 containers (38 samples)			
ESRF FX23 4 ...	AT_ESRF	26-09-2024	04-10-2024	ID30A-1	2 parcels / 3 containers (16 samples)			
ESRF FX23 13...	SENT TO USER	05-09-2024	13-09-2024	ID30A-1	1 parcels / 2 containers (20 samples)			
ESRF FX23 6 ...	SENT TO USER	29-08-2024	06-09-2024	ID30A-1	1 parcels / 2 containers (32 samples)			
ESRF FX23 30...	SENT TO USER	22-08-2024	30-08-2024	ID30A-1	1 parcels / 5 containers (64 samples)			
ESRF FX23 26...	SENT TO USER	18-07-2024	26-07-2024	ID30A-1	1 parcels / 1 containers (6 samples)			
ESRF FX23 28...	SENT TO USER	20-06-2024	28-06-2024	ID30A-1	1 parcels / 3 containers (69 samples)			
ESRF FX23 21...	SENT TO USER	13-06-2024	21-06-2024	ID30A-1	1 parcels / 2 containers (32 samples)			
ESRF FX23 14...	SENT TO USER	06-06-2024	14-06-2024	ID30A-1	1 parcels / 3 containers (39 samples)			
ESRF FX23 7 ...	SENT TO USER	30-05-2024	07-06-2024	ID30A-1	1 parcels / 7 containers (112 samples)			
ESRF FX23 12...	SENT TO USER	04-04-2024	12-04-2024	ID30A-1	1 parcels / 3 containers (33 samples)			
ESRF FX23 5 ...	SENT TO USER	26-03-2024	06-04-2024	ID30A-1	1 parcels / 2 containers (18 samples)			
ESRF FX23 28...	SENT TO USER	22-03-2024	29-03-2024	ID30A-1	1 parcels / 6 containers (81 samples)			
ESRF FX23 4 ...	SENT TO USER	27-02-2024	08-03-2024	ID30A-1	1 parcels / 3 containers (48 samples)			
ESRF FX23 16...	SENT TO USER	09-02-2024	16-02-2024	ID30A-1	1 parcels / 1 containers (12 samples)			
ESRF FX23 5 ...	SENT TO USER	01-02-2024	09-02-2024	ID30A-1	1 parcels / 3 containers (48 samples)			

PUCK ASSIGNMENT

89 shipments candidates for FX89

Display only shipments scheduled for future sessions or in processing status

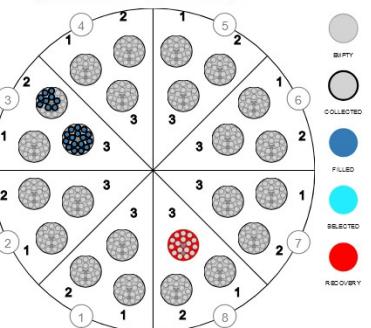
Shipment			Experiment	
Name	Status	Created on	Start on	beamline
ESRF FX23 15...	PROCESSING	08-11-2024	15-11-2024	ID30A-1
ESRF FX23 8 ...	SENT TO USER	01-11-2024	08-11-2024	ID30A-1
ESRF FX23 25 ...	SENT TO USER	17-10-2024	25-10-2024	ID30A-1
ESRF FX23 4 ...	AT_ESRF	26-09-2024	04-10-2024	ID30A-1
ESRF FX23 13...	SENT TO USER	05-09-2024	13-09-2024	ID30A-1
ESRF FX23 6 ...	SENT TO USER	29-08-2024	06-09-2024	ID30A-1
ESRF FX23 30...	SENT TO USER	22-08-2024	30-08-2024	ID30A-1
ESRF FX23 26...	SENT TO USER	18-07-2024	26-07-2024	ID30A-1
ESRF FX23 28...	SENT TO USER	20-06-2024	28-06-2024	ID30A-1
ESRF FX23 21...	SENT TO USER	13-06-2024	21-06-2024	ID30A-1
ESRF FX23 14...	SENT TO USER	06-06-2024	14-06-2024	ID30A-1
ESRF FX23 7 ...	SENT TO USER	30-05-2024	07-06-2024	ID30A-1
ESRF FX23 12...	SENT TO USER	04-04-2024	12-04-2024	ID30A-1
ESRF FX23 5 ...	SENT TO USER	26-03-2024	06-04-2024	ID30A-1
ESRF FX23 28...	SENT TO USER	22-03-2024	29-03-2024	ID30A-1
ESRF FX23 4 ...	SENT TO USER	27-02-2024	08-03-2024	ID30A-1
ESRF FX23 16...	SENT TO USER	09-02-2024	16-02-2024	ID30A-1
ESRF FX23 5 ...	SENT TO USER	01-02-2024	09-02-2024	ID30A-1

Loaded or to be Loaded on MxCube

Shipment	Parcel	Container	Container type	Beamline	Cell	Position
ESRF FX23 15 Nov 2024	dewer1	gsk1007 (16 samples)	UNIPUCK	ID30A-1	3	3
ESRF FX23 15 Nov 2024	dewer1	cps0801 (9 samples)	UNIPUCK	ID30A-1	3	2

Unload all

ID30A-1
(FlexHCDUnipuckPlate)

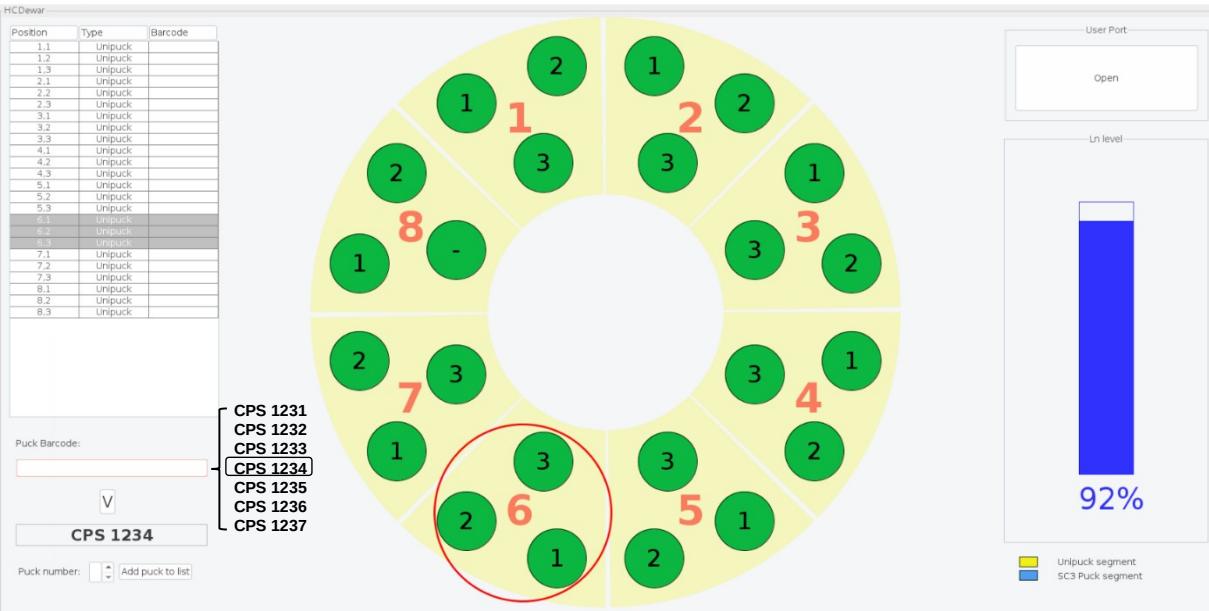


AUTOMATED SESSION/PUCK ASSIGNMENT

Barcode reader for the dewar

Connection between sample changer and LIMS

Puck detection



Barcode reader for the dewar

Puck detection

Connection between sample changer and DRAC



Present	Future
Unique interface (user/BL scientist)	
Manual puck assignment	Auto puck assignment
Single user	Unique operator (SSO)

SINGLE SIGN-ON

On-time and early/late session selection

The screenshot shows the MXCuBE-Web interface for the European Synchrotron. On the left, there's a large preview window showing a diffraction pattern with a scale bar of 50 μm. To the right of the preview are various control panels and status indicators. At the top, it shows beam parameters: Energy: 12.8420 KeV, Resolution: 2.000 Å, Transmission: 100.0 %, Cryo: 100.02 k, Wavelength: 0.97 Å, Detector: 388.6 mm, and Flux: 2.71e+11 ph/s. Status indicators include Sensor Changer (READY), Detector (UNKNOWN), Capillary (IN), Fast Shutter (CLOSED), Spill shutter (OPEN), and Ring Current (153.85 mA). Below these are controls for Phase Control (DataCollection selected), Beam size (A30), Omega (360.00), Kappa (0.0), Kappa Phi (0.0), and Sample alignment. A 'Beamsline Actions' dropdown is also present. The main workspace has tabs for Samples, Data collection, Equipment, and System log. In the center, a 'Select a session' dialog is open, listing scheduled sessions (5) and non-scheduled ones (84). The sessions listed are:

ID	User/Project	Description	Date	Start Time	End Time	Actions
MX-2644	ID30A-1	Swiss consortium in macromolecular X-ray crystallography structure determination for academic researchers: EPFL, UNIL, UNIGE, Zurich and SL	29-11-2024	09:30:00	29-11-2024 17:00:00	Reschedule Cancel Select
FX-75	ID30A-1	Mail-in	20-11-2024	09:30:00	21-11-2024 01:00:00	Reschedule Cancel Select
MX-2647	ID30A-1	Coordinated user access to HTX lab – MASSIF-1 facilities for fragment screening and new structures. With funding through iNEXT Discovery, In	19-11-2024	09:30:00	20-11-2024 01:00:00	Reschedule Cancel Select
FX-23	ID30A-1	MXpress for GSK	15-11-2024	09:30:00	15-11-2024 17:00:00	Reschedule Cancel Select
FX-66	ID30A-1	Mail-in Ligand screening	14-11-2024	09:30:00	15-11-2024 01:00:00	Reschedule Cancel Select
MX-2647	ID30A-1	Coordinated user access to HTX lab – MASSIF-1 facilities for fragment screening and new structures. With funding through iNEXT Discovery, In	13-11-2024	17:00:00	14-11-2024 01:00:00	Reschedule Cancel Select
MX-2654	ID30A-1	Structural Biology at EMBL Grenoble, IBS-CIBB and IAB	13-11-2024	17:00:00	14-11-2024 01:00:00	Reschedule Cancel Select

At the bottom of the dialog, there are buttons for [16:32:14] Diffractometer phase changed to DataCollection, Reschedule, Cancel, and Select FX-23. A note indicates '13-3run_01_MXPressAI'.

MXCUBE UI

Present	Future
Unique interface (user/BL scientist)	
Manual puck assignment	Auto puck assignment
Single user	Unique operator (SSO)
Single session	Multiple sessions

MULTIPLE SESSIONS

MXCuBE-Web (OSC)

Samples Data collection Equipment System log Help Remote Proposal (1965749388) Sign out (Didier NURIZZO)

Synchronize with Create new sample Clear sample list View Mode Filter : Filter options Add Task to Samples Settings Stop queue

Cell 5

Cell 5 | Code : AD044A

- AP2B2 - CD041908_D08-1.x1
- AP2B2 - CD041908_D08-1.x2
- AP2B2 - CD041908_E10-1.x1
- AP2B2 - CD041908_E10-1.x2
- AP2B2 - CD041908_E10-3

Cell 5 | Code : AD022A

- AP2B2 - CD041773_C10-3
- AP2B2 - CD041881_B09-1
- AP2B2 - CD041809_A07-1.x1 (MOUNTED)
- AP2B2 - CD041809_A07-1.x2
- AP2B2 - CD041809_A07-1.x3
- AP2B2 - CD041809_A07-3.x1
- AP2B2 - CD041809_A07-3.x2
- AP2B2 - CD041809_A07-3.x3
- AP2B2 - CD041809_B03-1.x1
- AP2B2 - CD041809_B03-1.x2
- AP2B2 - CD041774_D06-1.x1
- AP2B2 - CD041774_D06-1.x2
- AP2B2 - CD041903_H01-1
- AP2B2 - CD041904_C08-3.x1
- AP2B2 - CD041904_C08-3.x2
- AP2B2 - CD041904_C09-3

MXCuBE-Web (OSC)

Samples Data collection Equipment System log Help Remote Proposal (1965749388) Sign out (Didier NURIZZO)

Phase Control Beam size A20 Omega 200.00 Kappa Kappa Phi Sample alignment Show motors

Energy: 12.8420 KeV Resolution: 2.009 Å Transmission: 100.0 % Cryo: 100.02 K Wavelength: 0.97 Å Detector: 308.6 mm Flux: 2.71e+11 ph/s

50 μm

MXPressA
Path: ..\RAW_DATA\AP2B2\AP2B2-CD041773_C10-3
MESH (mesh-AP2B2-CD041773_C10-3_1_2_4656.h5)

Log messages:

- [16:33:43]: Workflow: Checking that images have been written to disk
- [16:33:40]: Workflow: Data collection finished
- [16:33:39]: Workflow: ISP/B path to first image: ..\data\visitors\mx254\ds0\120241114\RAW\run_01_02_meshmesh-AP2B2-CD041773_C10-3_1_2_0001.cbf
- [16:33:39]: Collection finished
- [16:32:14]: Diffractometer phase changed to DataCollection

A single operator runs multiple session in one go

Present	Future
Unique interface (user/BL scientist)	
Manual puck assignment	Auto puck assignment
Single user	Unique operator (SSO)
Single session	Multiple sessions
Immutable queue	On-the-fly mutable (+/-) queue order

MX-CUBE QUEUING

Diffracton Plan including the processing plan in LIMS

The screenshot displays the MXCuBE Web interface for MX-Cube Queuing. The main window is divided into three vertical sections representing Cells 1, 2, and 3. Each section shows a grid of sample slots, some of which are occupied by samples with labels like "Levit-V3SC R7B8_KK_Aus". Below the grid, a "Collect Queue?" dialog box is open, asking if the user wants to collect 8 tasks on 8 samples. It includes checkboxes for "Auto loop centring", "Auto mount next sample", and "Crystal snapshots (1)". The "Data Root" is set to `data/visitor/rbx66/d30a1/20241114/RAW_DATA`. A table below the grid lists the sample details: Type (MXPressA), Sample (e.g., b12p10 - C08BE), Path (e.g., `..data/visitor/rbx2649/d30a1/20241110/RAW DATA/TnmS3/W59BpByAia_b10p1C08BE-b12p10_0_0004d.cbf`), and # Images (100). To the right of the cells, there is a "Cell 3" panel showing a list of tasks: "Collect - C08EC-b12p1", "Collect - C08EC-b12p2", and "Collect - C08EC-b12p3". At the bottom right, a processing status bar shows "MXPressA - C08EC-b12p1" with progress bars for "Scan" (~80%), "Process" (~40%), and "Reduce" (~10%). The status bar also indicates "Data reduction in progress" and "Data reduction completed".

Present	Future
Unique interface (user/BL scientist)	
Manual puck assignment	Auto puck assignment
Single user	Unique operator (SSO)
Single session	Multiple sessions
Immutable queue	On-the-fly mutable (+/-) queue order
Per sample queuing list	Sample changer / Puck queuing overview

MX-CUBE QUEUING

Design a Sample Changer overview / Puck overview

The screenshot displays the MXCuBE-Web interface, specifically the 'Samples' tab, which provides a detailed overview of three sample changers (Cell 2, Cell 3, and Cell 4) and a beamline camera view.

Sample Changer Overview:

- Cell 2:** Contains two sample changers, each with 12 positions. The first changer is labeled "Puck 1 | Code : RUGX-008" and the second is "Puck 2 | Code : RUGX-008". Both changers show various sample types, including "Lure-V3SC_R7B8_KK_Au2" and "RaeNB_V3SC_R7B8_KK_Au2".
- Cell 3:** Contains one sample changer labeled "Puck 1 | Code : RUGX-012", which also shows samples from the same categories.
- Cell 4:** Contains one sample changer labeled "Puck 1 | Code : RUGX-013", which shows samples from the same categories.

Beamline Camera View:

A central window shows a beamline camera view with a bright spot on a dark background. The camera parameters are displayed as follows:

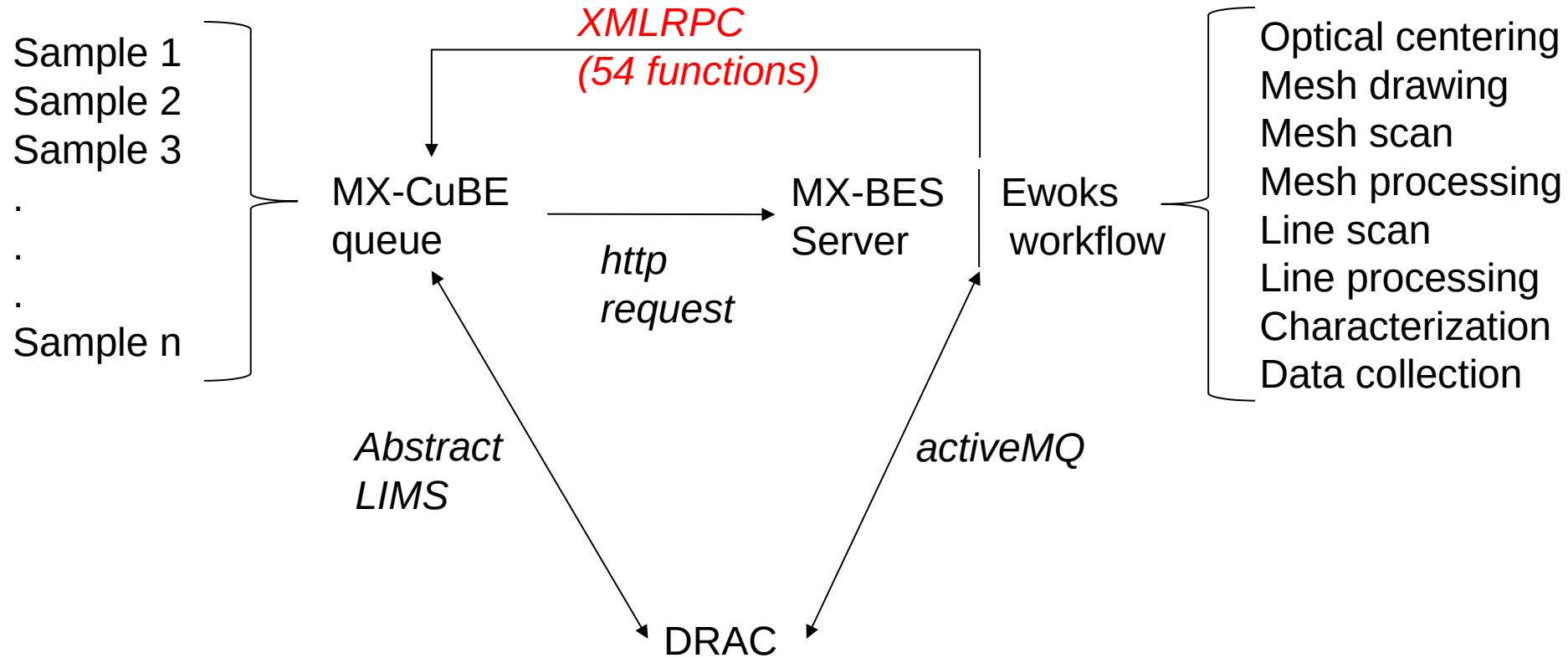
- Energy: 19.626 keV
- Resolution: 2048 x 2048
- Pixel size: 0.160 μm
- Exposure time: 1.00 ms
- Frame rate: 1.000 Hz
- Image type: 16-bit grayscale

Beamline Control Panel:

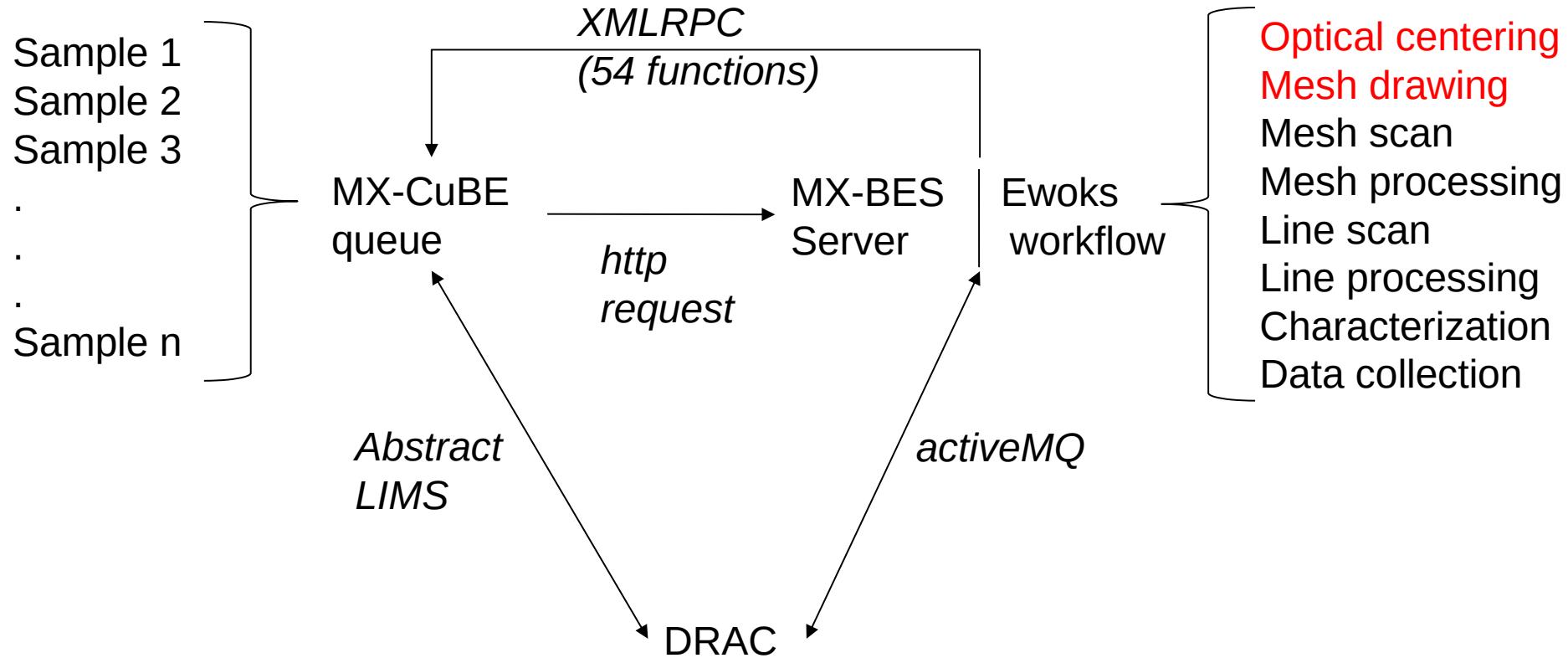
The right side of the interface features a control panel with several tabs and status indicators:

- General:** Shows the beamline status as "Ready".
- Motor Control:** Displays current values for various motors.
- Detector Control:** Shows current values for the detector.
- Sample Changer Control:** Shows current values for the sample changers.
- Beamline Control:** Shows current values for the beamline.
- Log messages:** A list of log messages including "10/11/2024 10:00:00: Beamline opening is successful", "10/11/2024 10:00:00: Beamline opening is successful", and "10/11/2024 10:00:00: Beamline opening is successful".

WORKFLOW / MXCUBE REFURBISHMENT

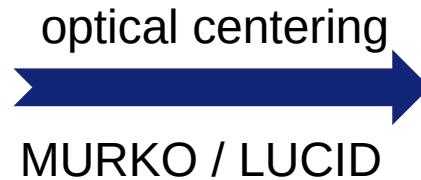


SOFTWARE REFURBISHMENT

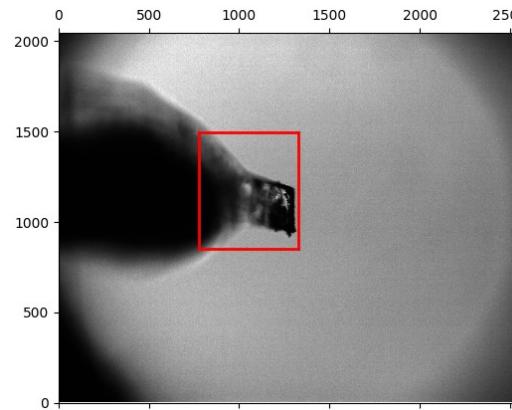
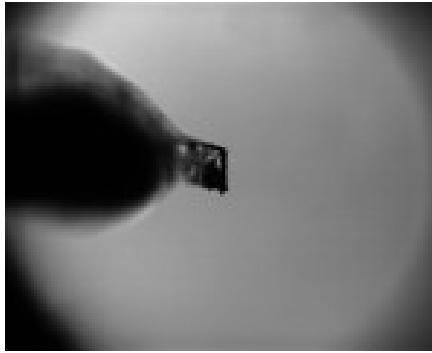


OPTICAL ANALYSIS

A set of optical images

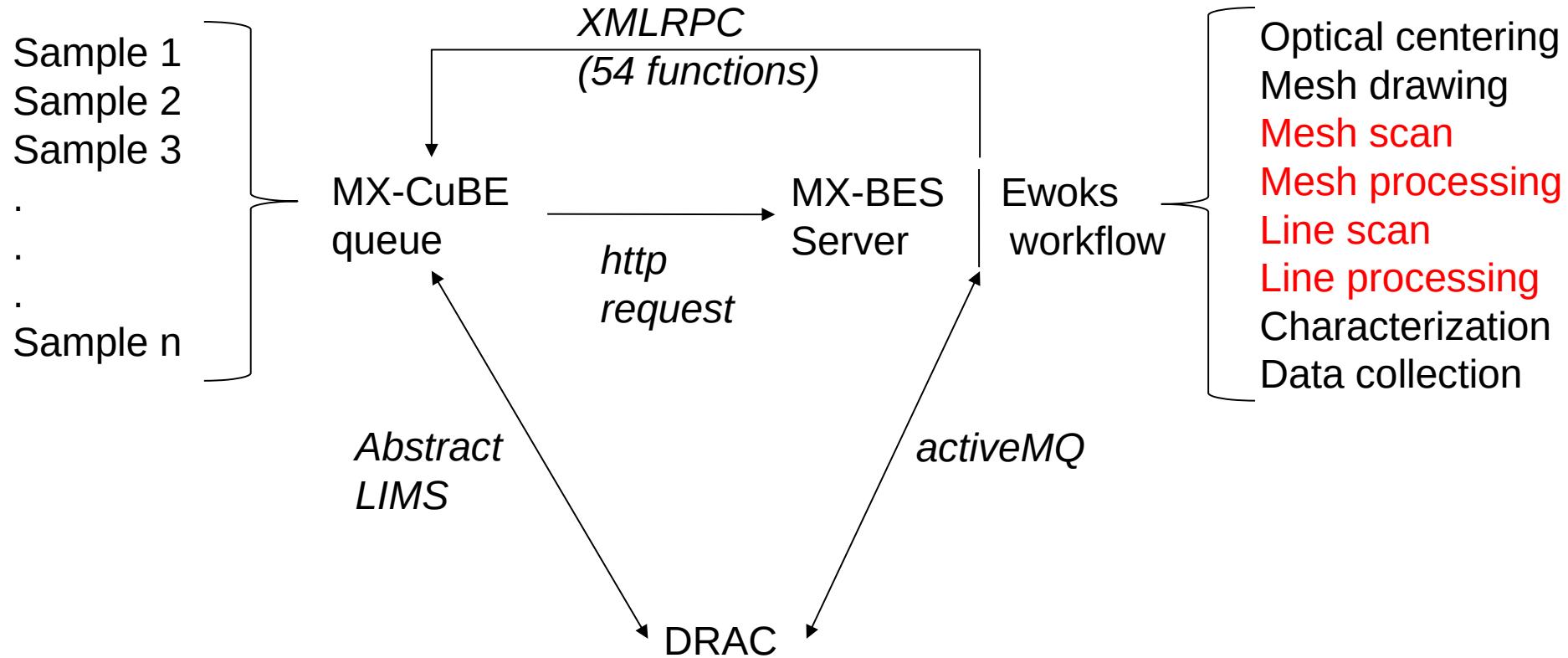


- Loop centering
- Crystal recognition
- Mesh drawing



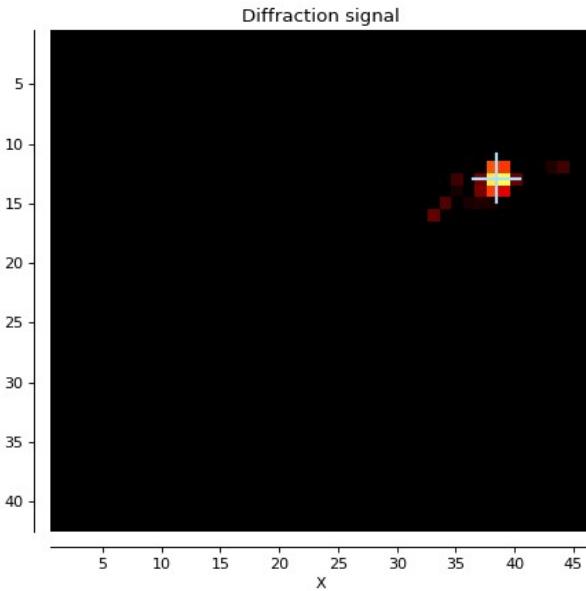
Single object returning the optical features of the crystal inside the loop
(center of mass, position of the crystal, size of the loop, etc...)

SOFTWARE REFURBISMENT

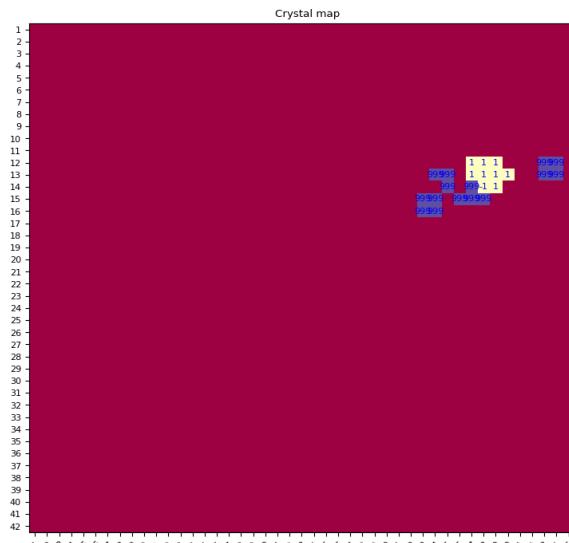


X-RAY CENTERING

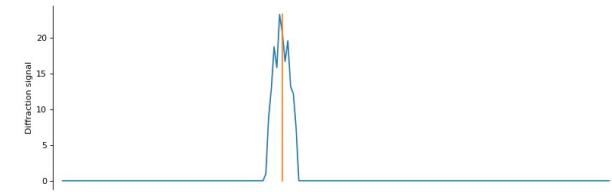
A set of diffraction images



Diffraction alignment



- Best diffraction centering
- Crystal size
- Crystal homogeneity
- Resolution limit



Single object returning the diffraction features of the crystal
(best diffracting volume and position, size of the crystal, , etc...)

ACKNOWLEDGEMENTS

Thoroughly discussed :

During our bi-weekly Automation Task

Force meetings

and

In our MXCuBE automation WG:

Matthew Bowler

Antonia Beteva

Marcus Oskarsson

Estelle Mossou

Daniele de Sanctis

Andrew McCarthy

Johannes

Kamps

Max Nanao

Ludovic Broche

Romain Talon

Wout de Nolf

Yan Welsh

And many
more

Questions still under discussion:

- Common definition of automated/unattended DC
- Long term perspective for the DC model
- Granularity of the abstraction



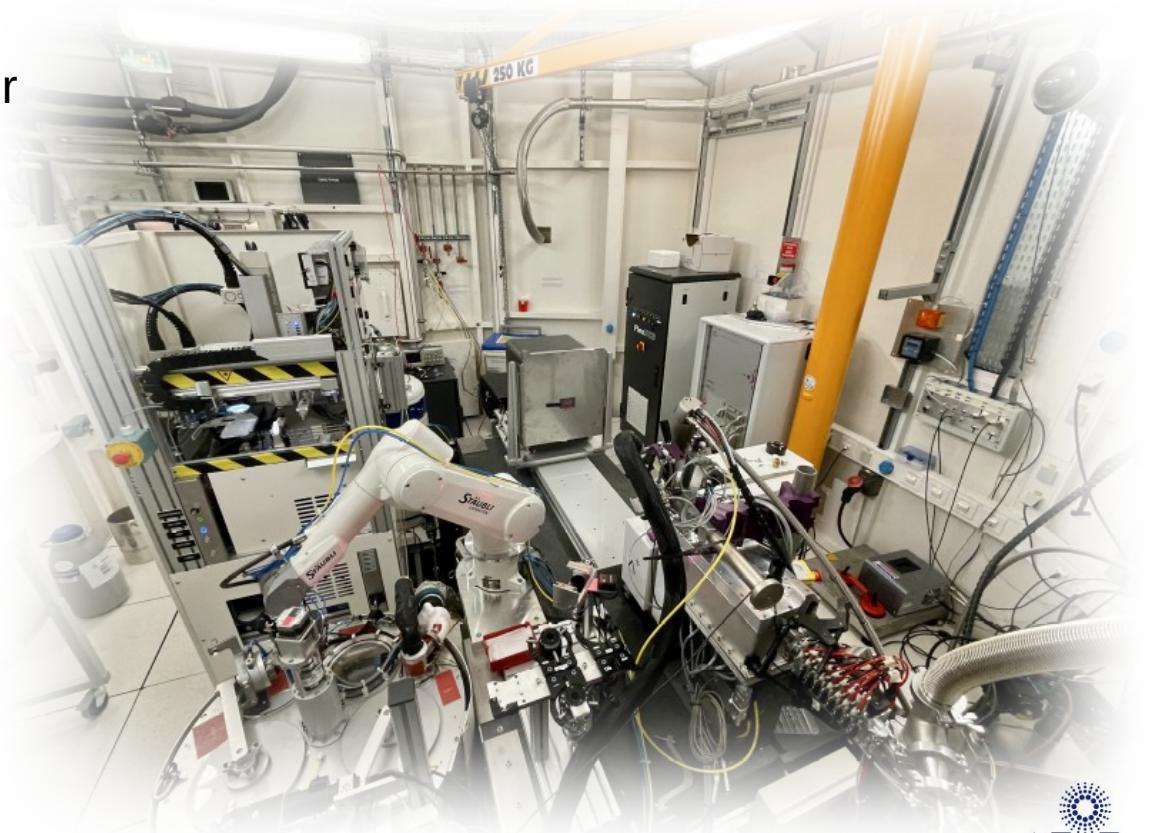


Macromolecular Crystallography And Structural Biology at synchrotron

MASSIF-1 AUTOMATED DATA COLLECTION

Automation for Room Temperature experiments

- Crystal Direct Harvester
- In-Situ data collection



MASSIF-1 AUTOMATED DATA COLLECTION

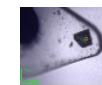
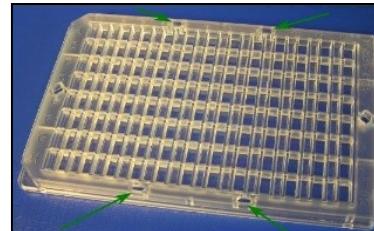
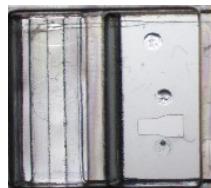
Automation for Room Temperature experiments

- Crystal Direct Harvester



- In-Situ data collection

MiTegen



Crystal Direct technology

MASSIF-1 AUTOMATED DATA COLLECTION

Automation for Room Temperature experiments

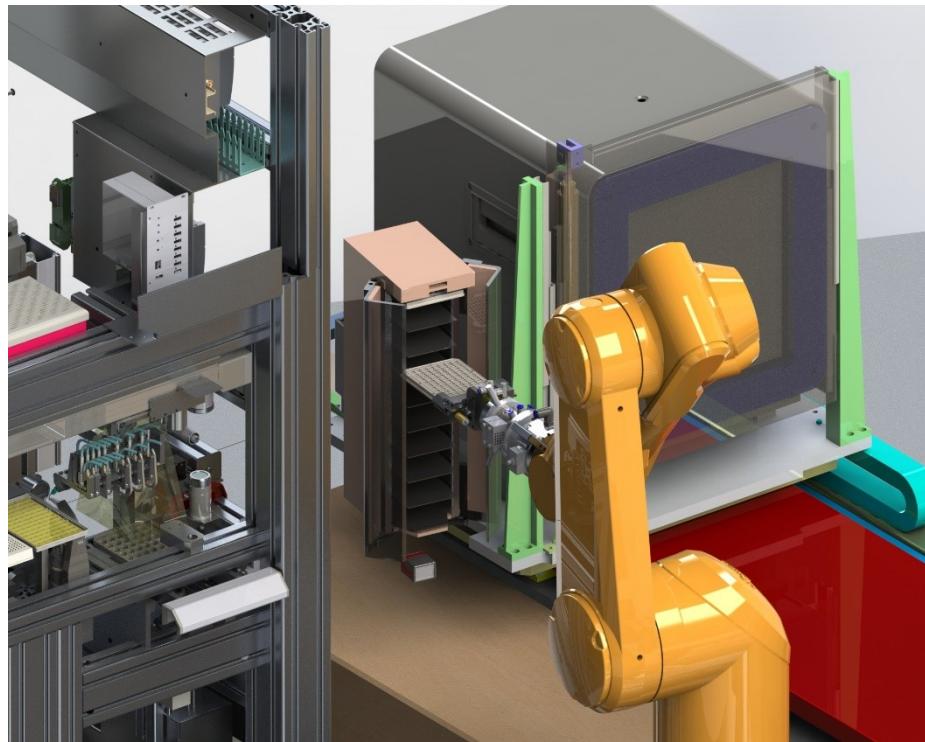
- Crystal Direct Harvester
- In-Situ data collection



MASSIF-1 AUTOMATED DATA COLLECTION

Automation for Room Temperature experiments

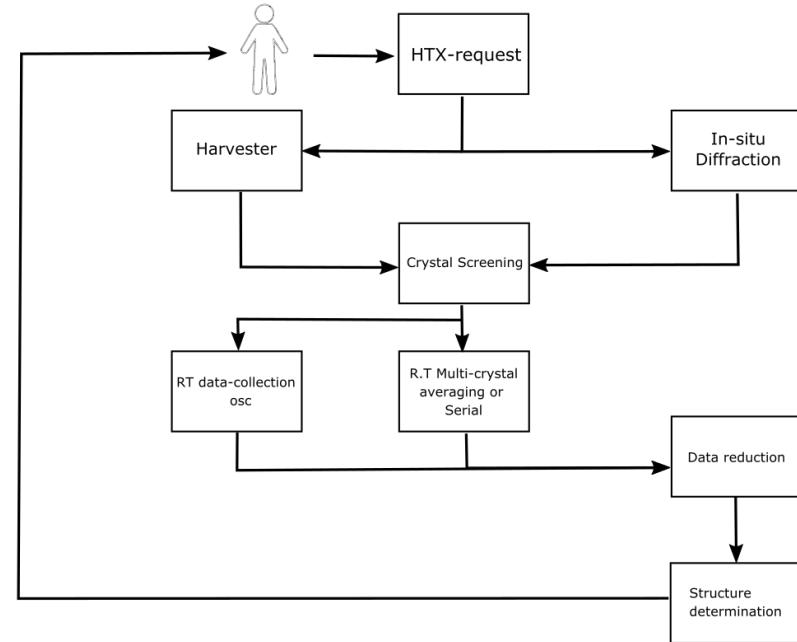
- Crystal Direct Harvester
- In-Situ data collection



MASSIF-1 AUTOMATED DATA COLLECTION

Automation for Room Temperature experiments

- Crystal Direct Harvester
- In-Situ data collection



CURRENT FEATURES

Main:

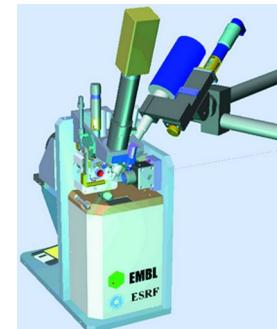
Ω axis (SOC<1μm)
Centering table
Alignment table
Apertures
Capillary
Beamstop
smartMagnet
OAV camera
Scintillator
Fluo det translation



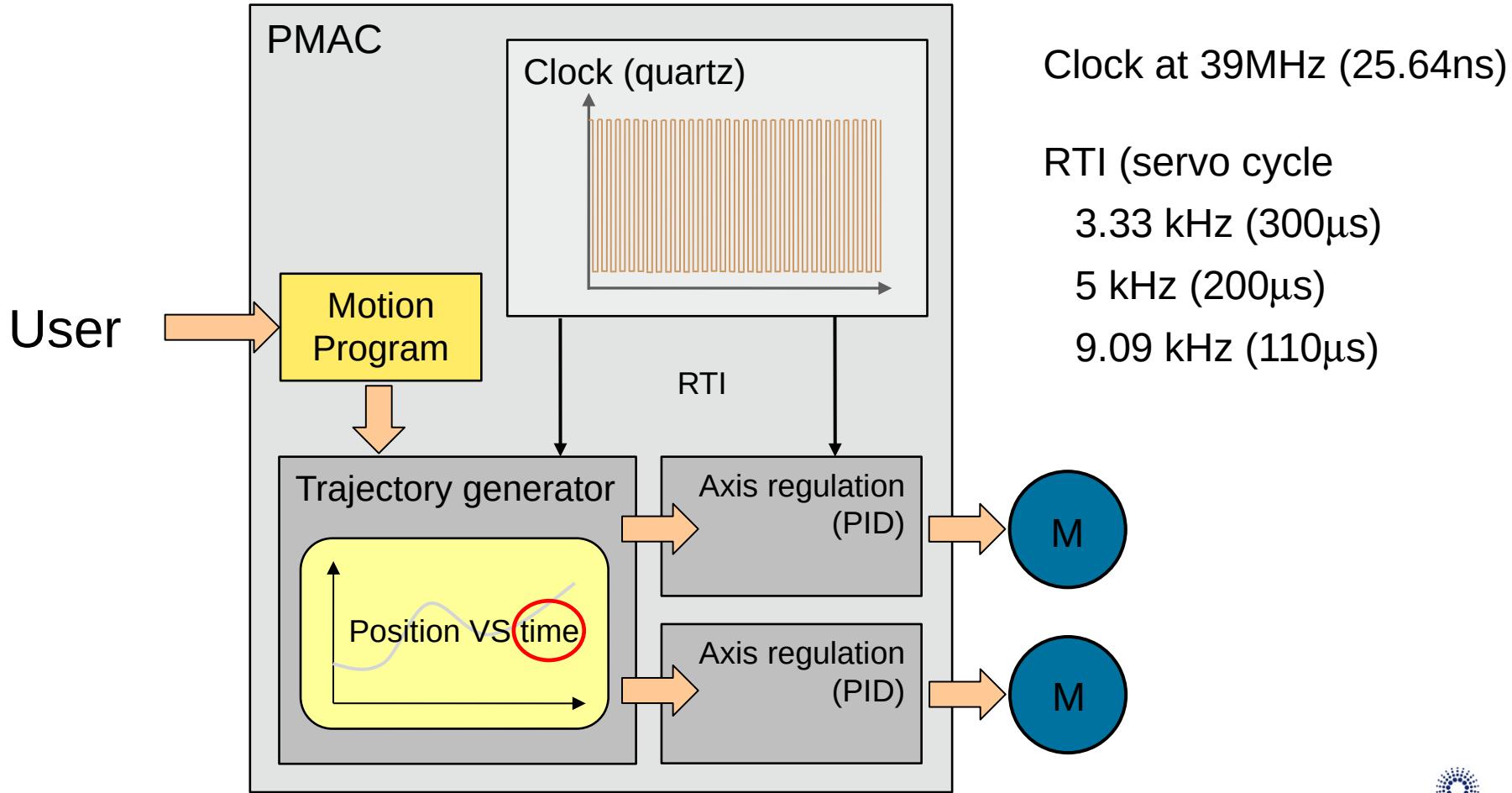
Protein microcrystals and the design of a microdiffractometer: current experience and plans at EMBL and ESRF/ID13
Perrakis, A., Cipriani, F., Castagna, J.-C., Claustre, L., Burghammer, M., Riekel, C. & Cusack, S. (1999). Acta Cryst. D55, 1765-1770.

Ancillary:

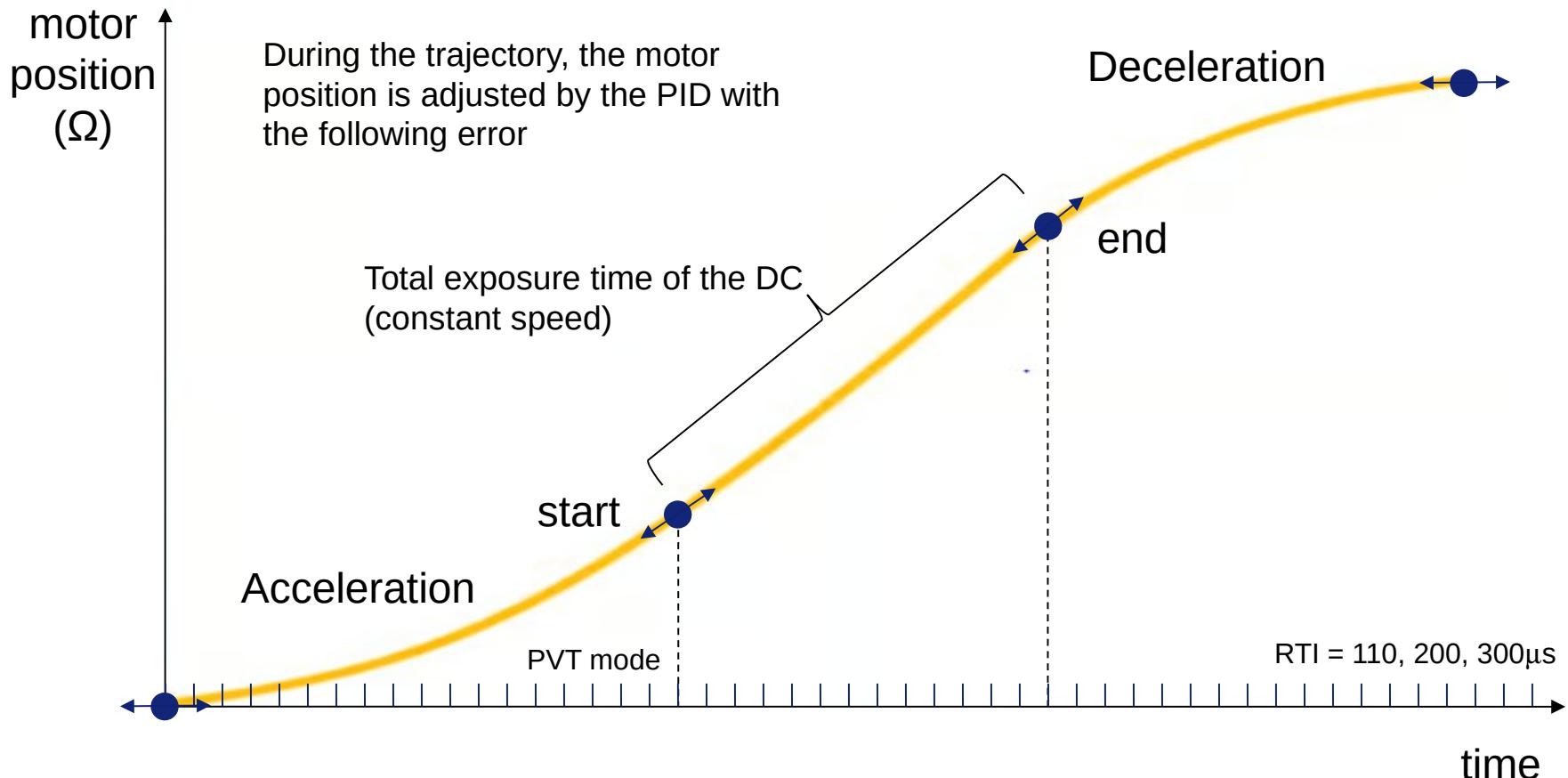
Mini-Kappa
Plate manipulator
Fluo det translation
Luciole control
REX control
Shutter control
Flex communication



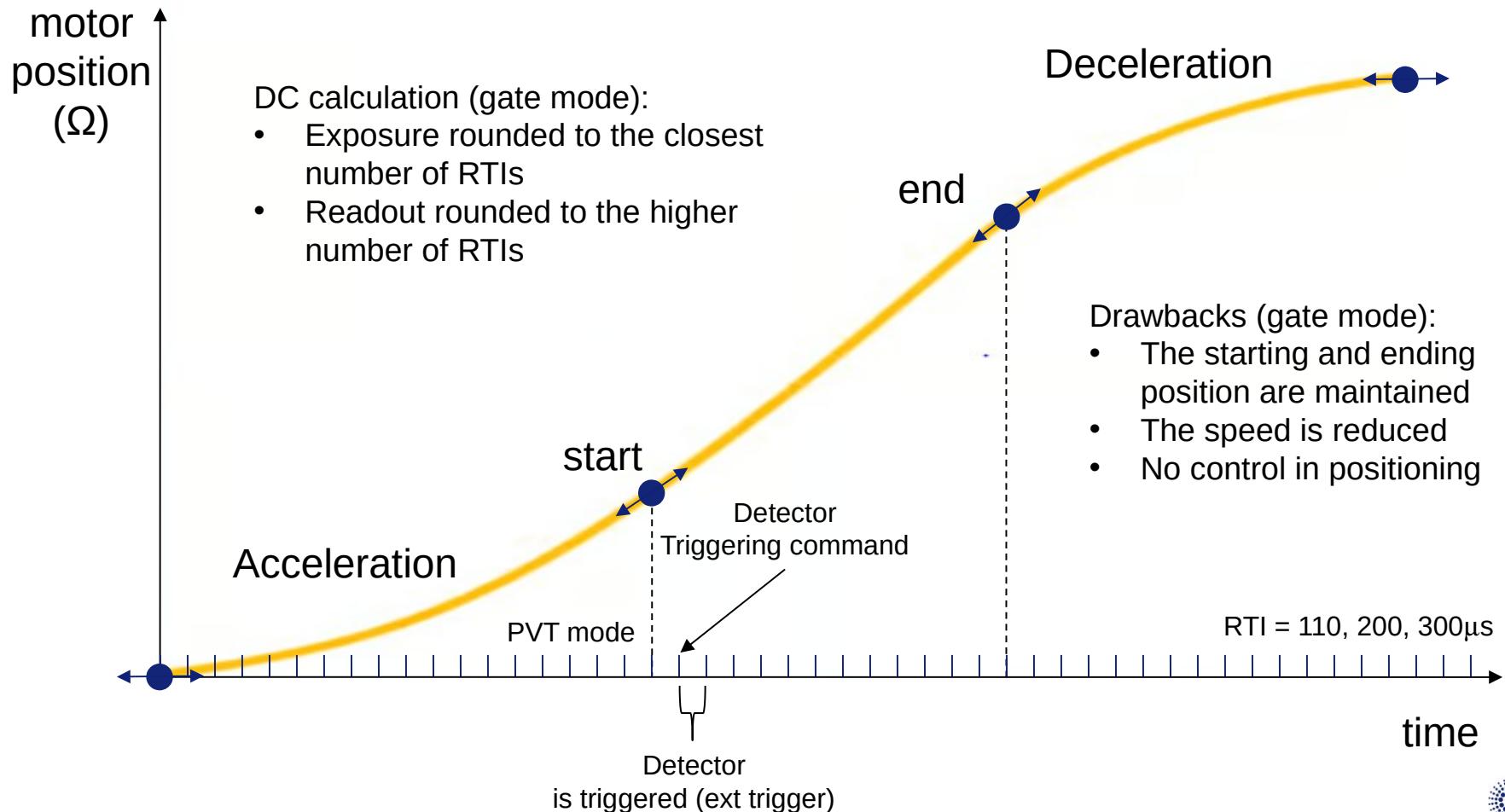
PMAC – DELTA TAU



MOTION PROGRAMME

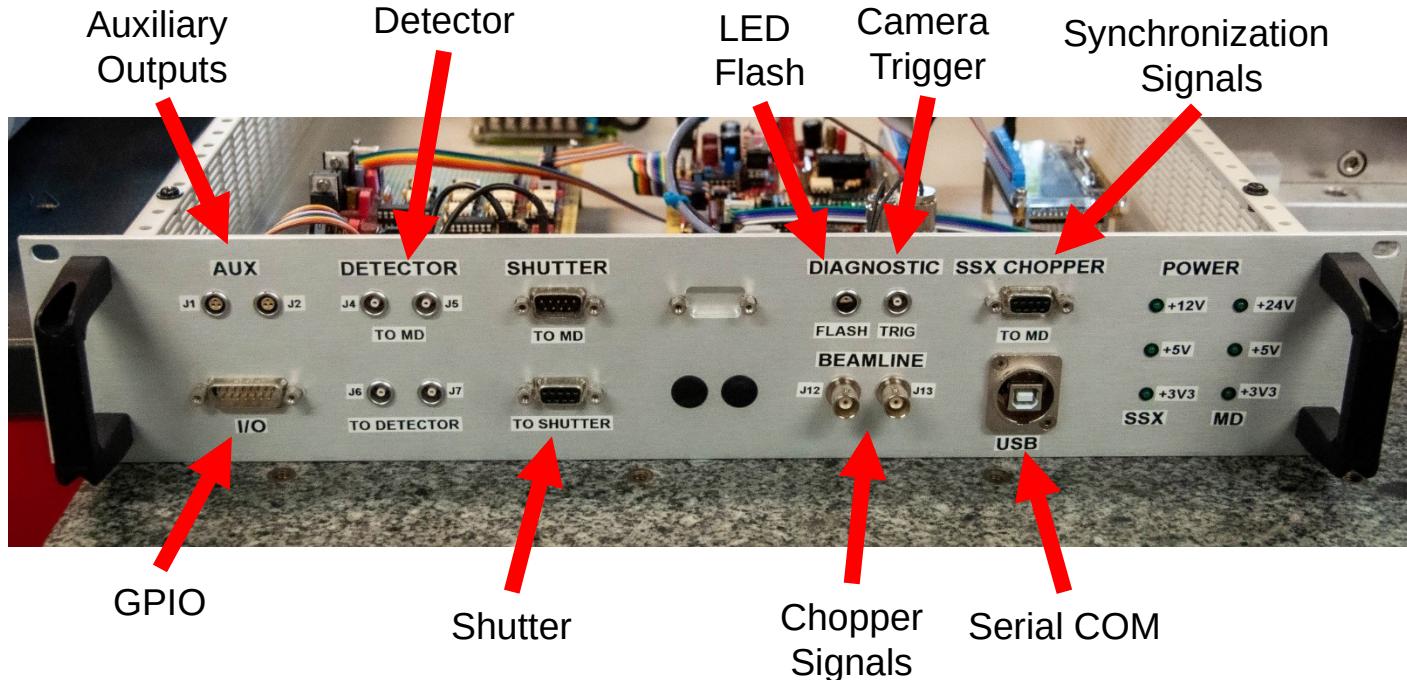


MOTION PROGRAMME

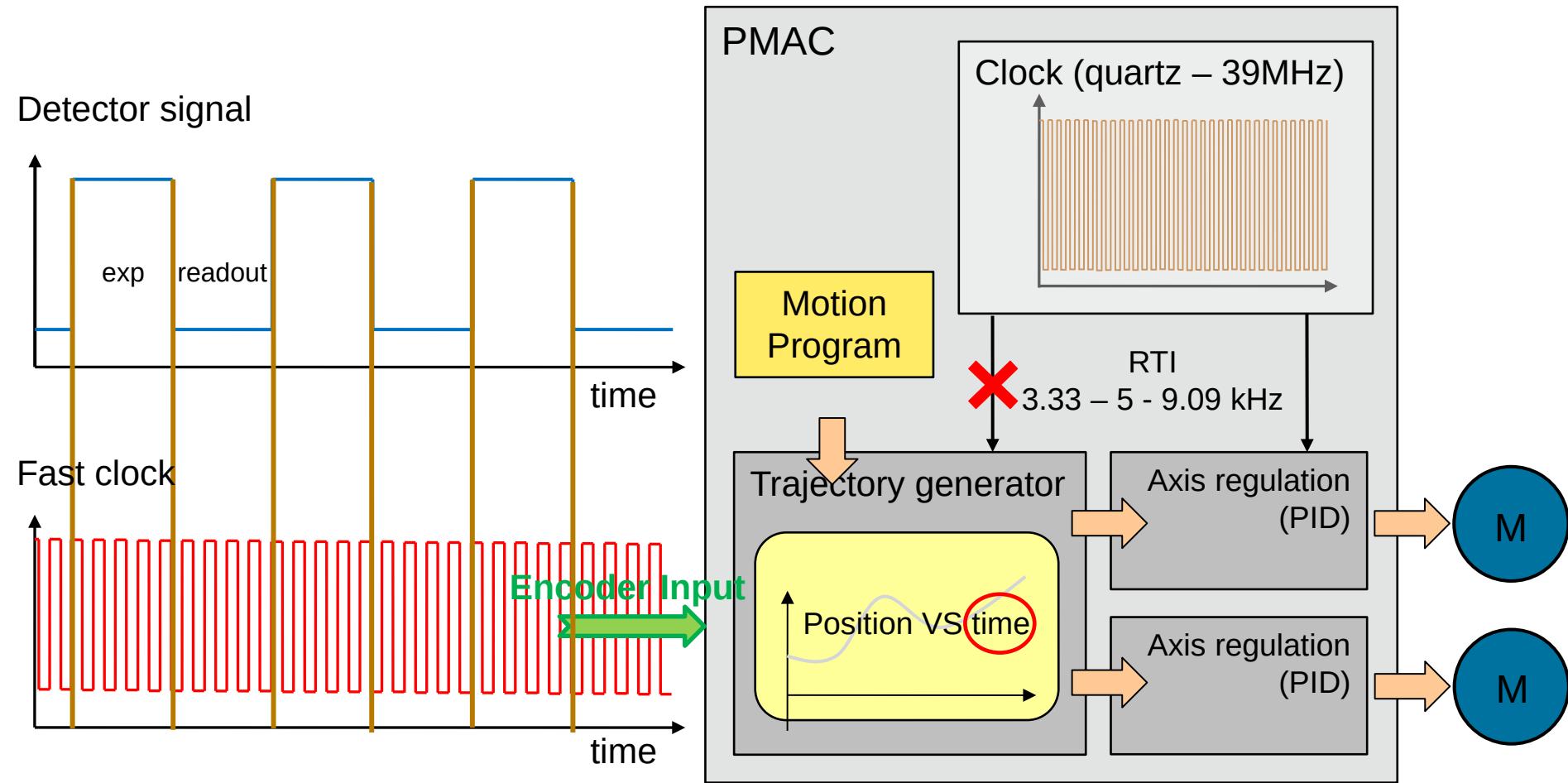


SSX CONTROL UNIT ON ID29 (FPGA)

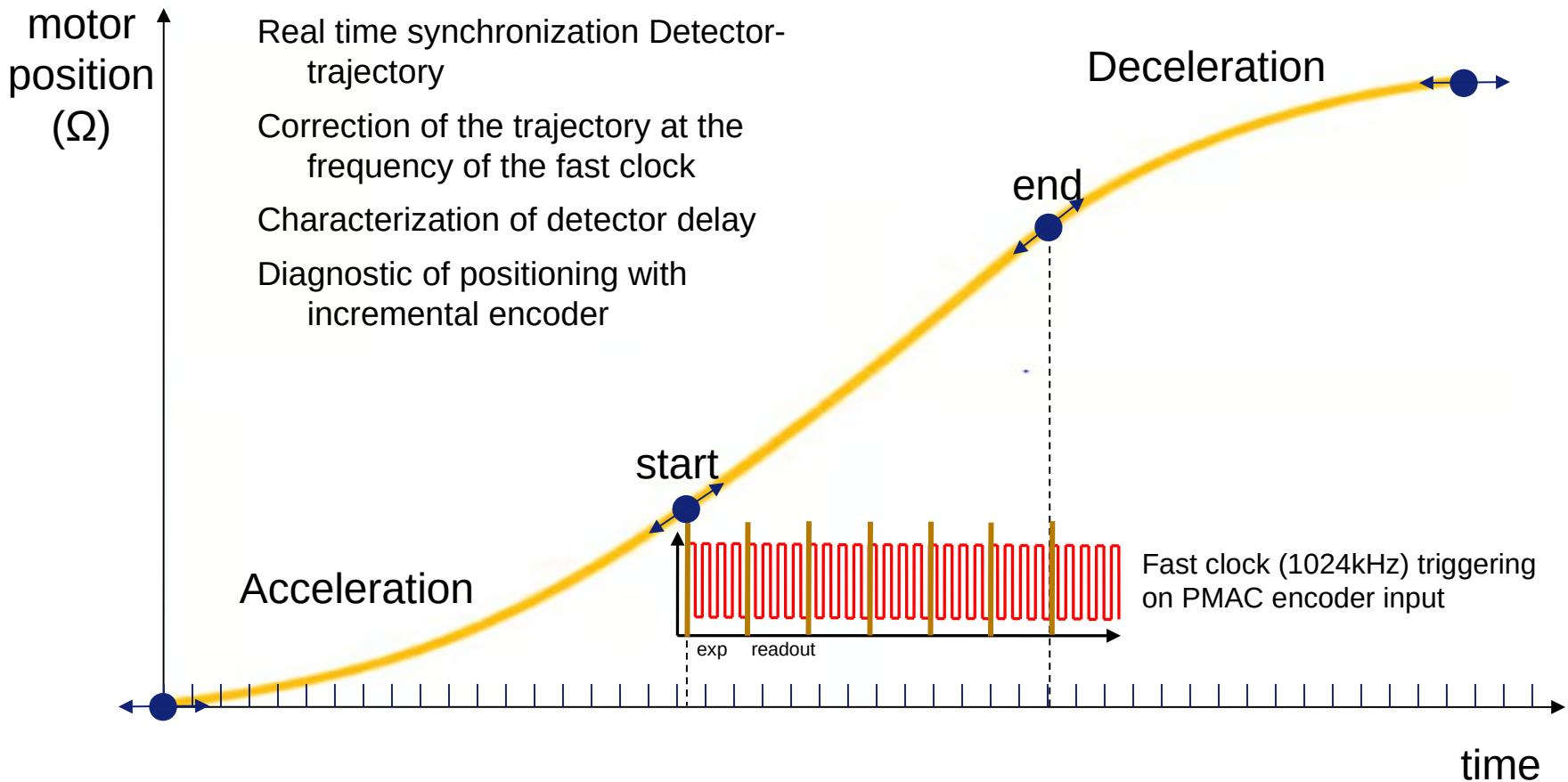
Clock at 50MHz (20-ns)



TRIGGERED TIME BASE



TRIGGERED TIME BASE



Macromolecular Crystallography And Structural Biology at synchrotron

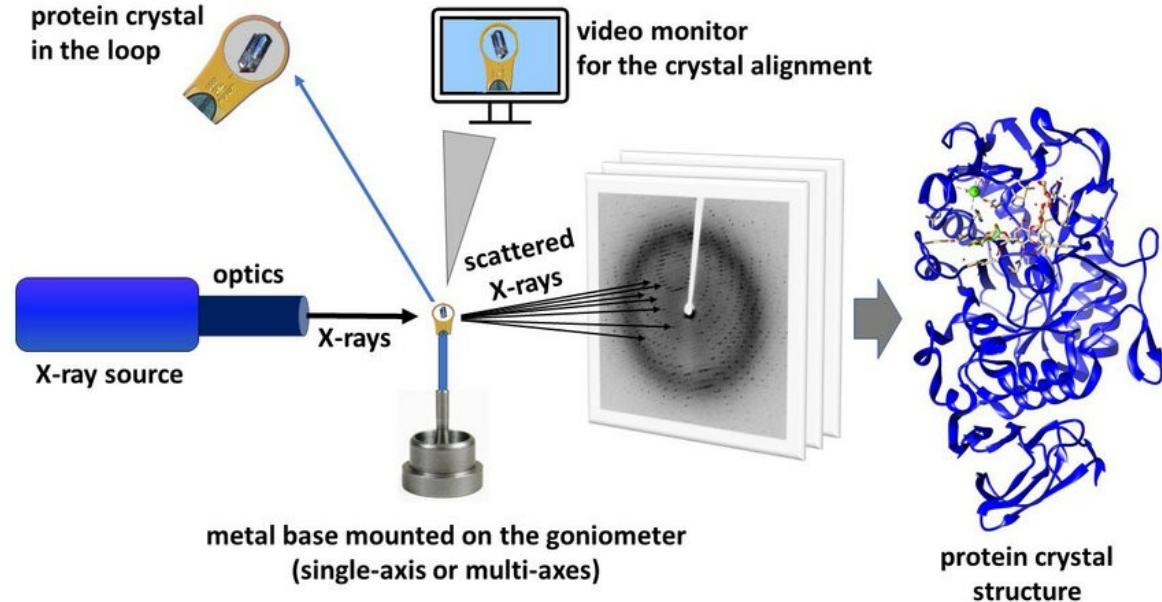
CONTENTS

Theory

1. *Crystallogenesis*
2. *Crystal symmetries*
3. *X-rays*
4. *Diffraction*
5. *Phase problem*

Practice

6. *Crystal harvesting*
7. *Data collection*
8. *Data processing*
9. *Solving structures*
10. *Examples*



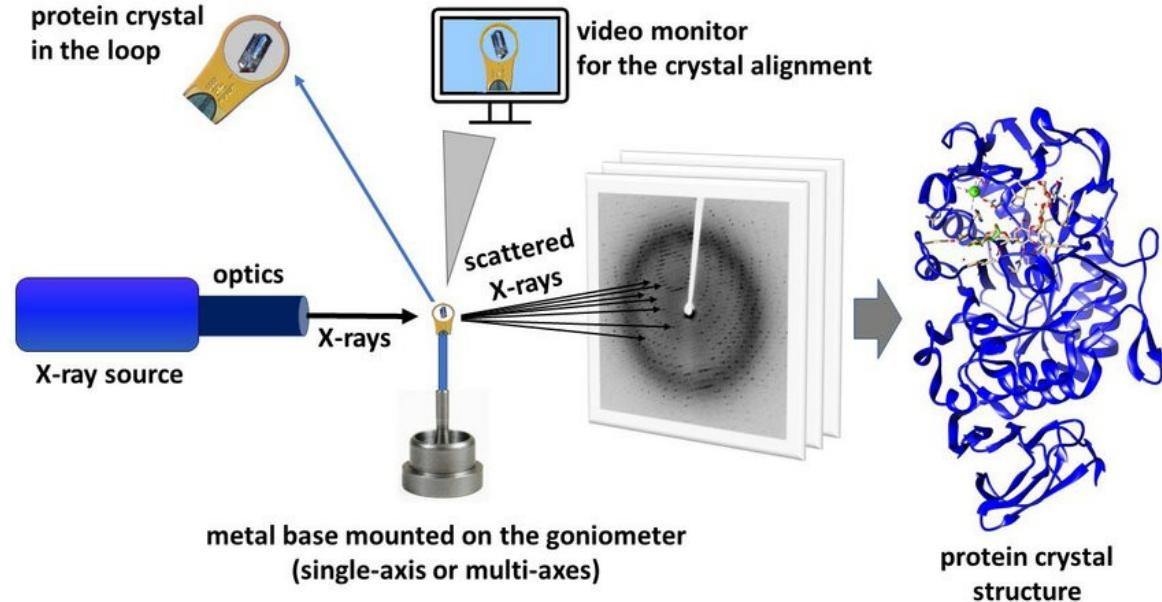
CONTENTS

Theory

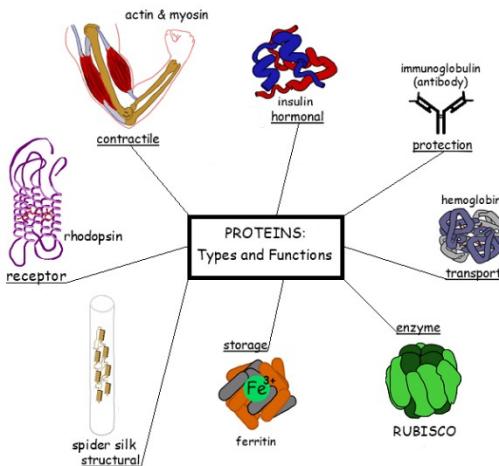
1. *Crystallogenesis*
2. *Crystal symmetries*
3. *X-rays*
4. *Diffraction*
5. *Phase problem*

Practice

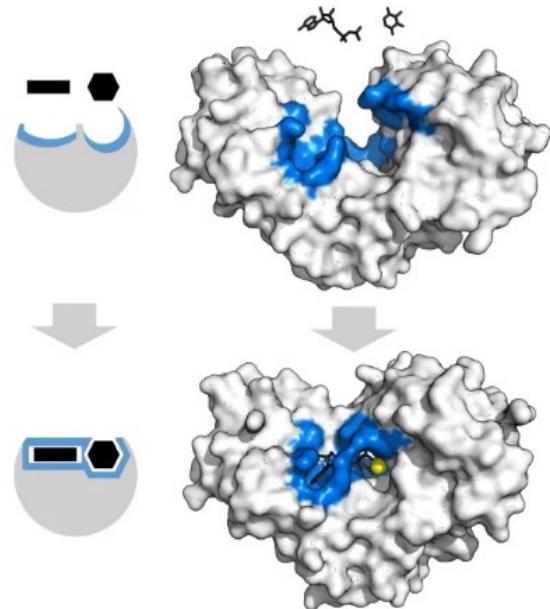
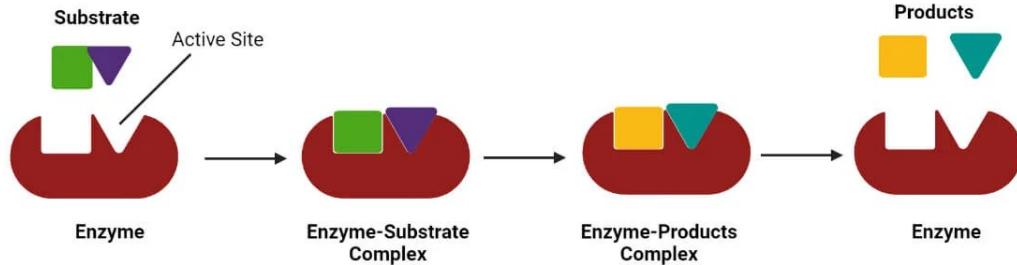
6. *Crystal harvesting*
7. *Data collection*
8. *Data processing*
9. *Solving structures*
10. *Examples*



LOCK-AND-KEY MODEL (1894)



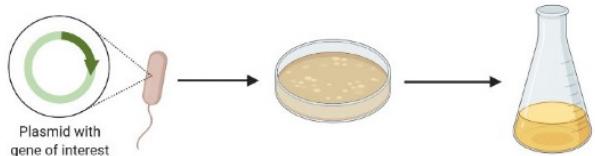
Emil Fischer (1852-1919)
Nobel prize in Chemistry(1902)



PURIFICATION

Molecular biology

- ① Transformation
- ② Selection
- ③ Cell growth and protein production
- ④ Cell lysis



- ⑧ Fluorescence analysis



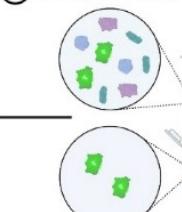
- ⑦ SDS-PAGE



- ⑥ Dialysis

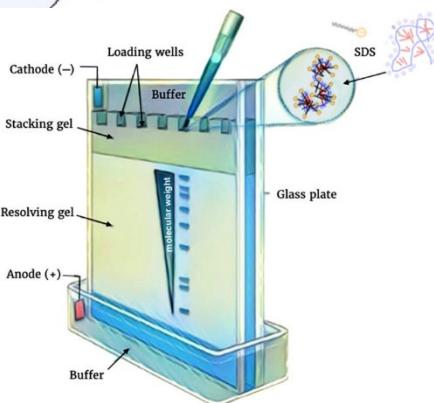


- ⑤ Affinity chromatography

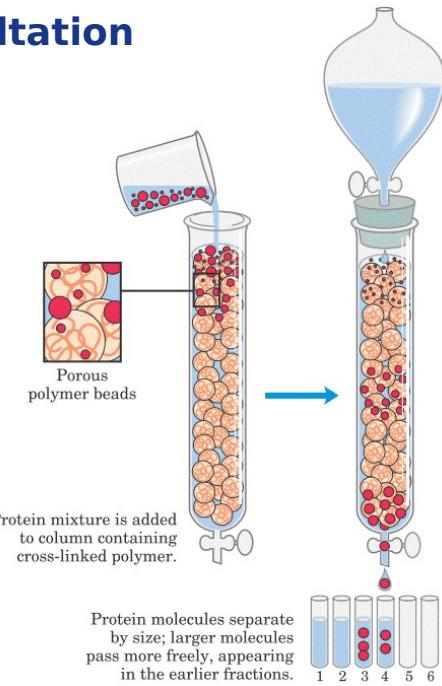


SDS-PAGE electrophoresis

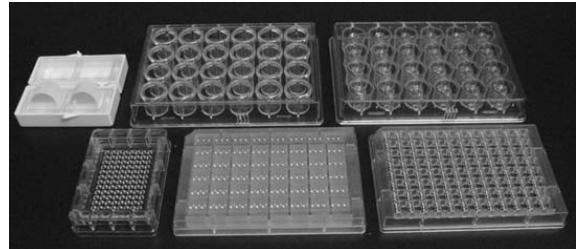
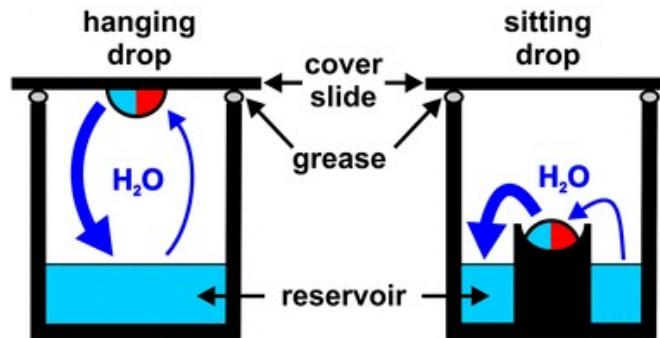
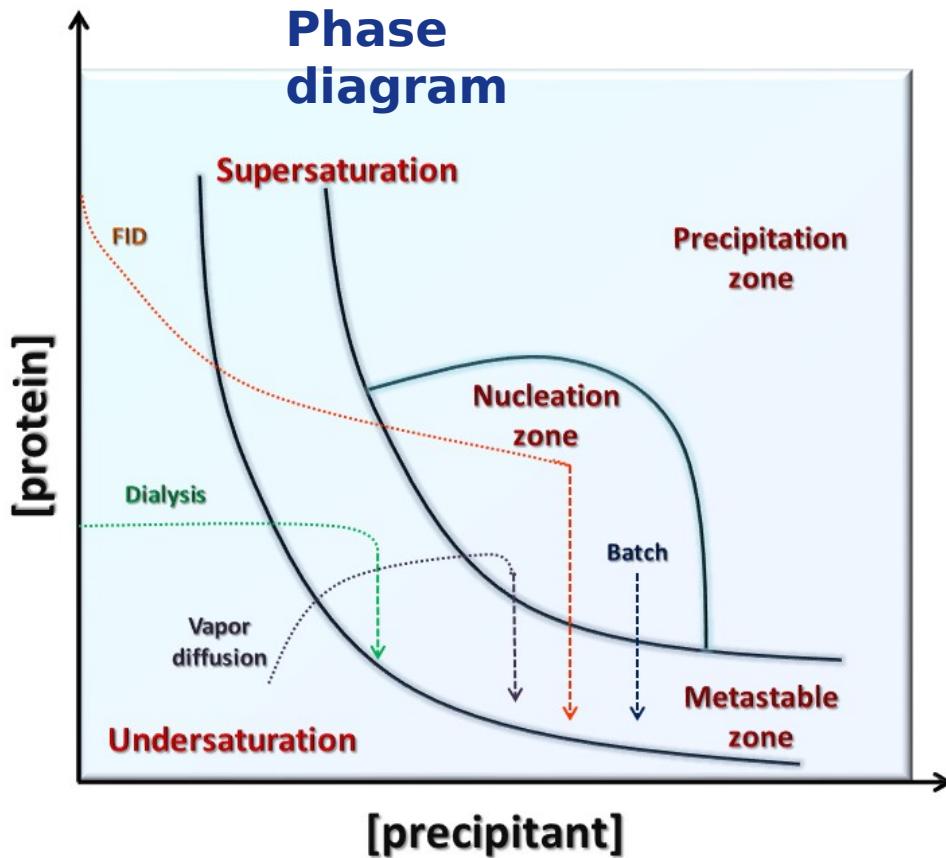
Protein migration



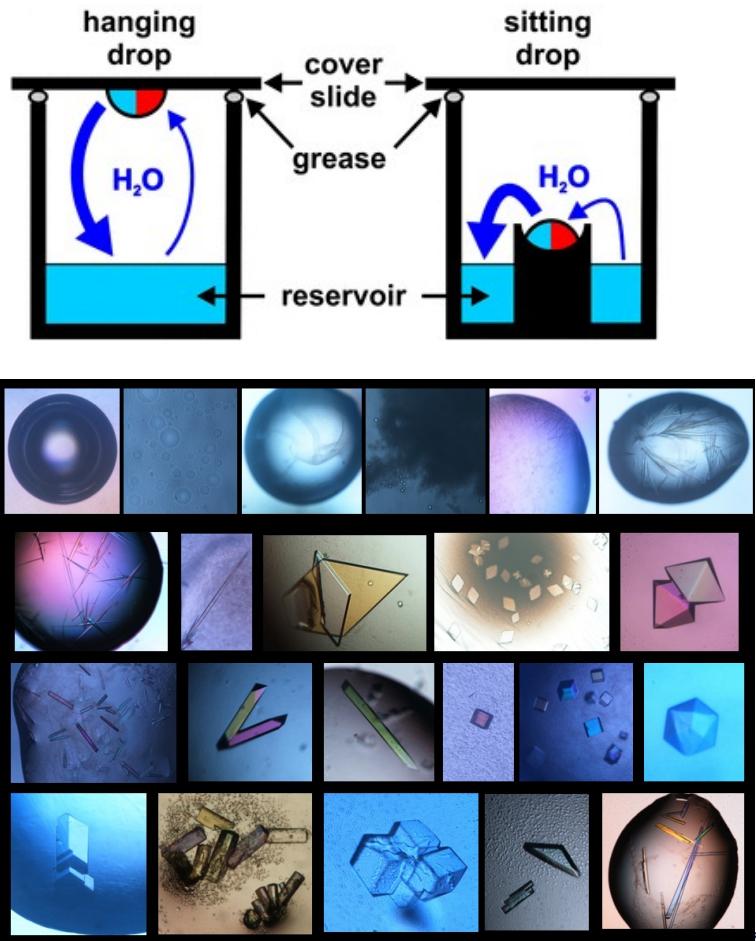
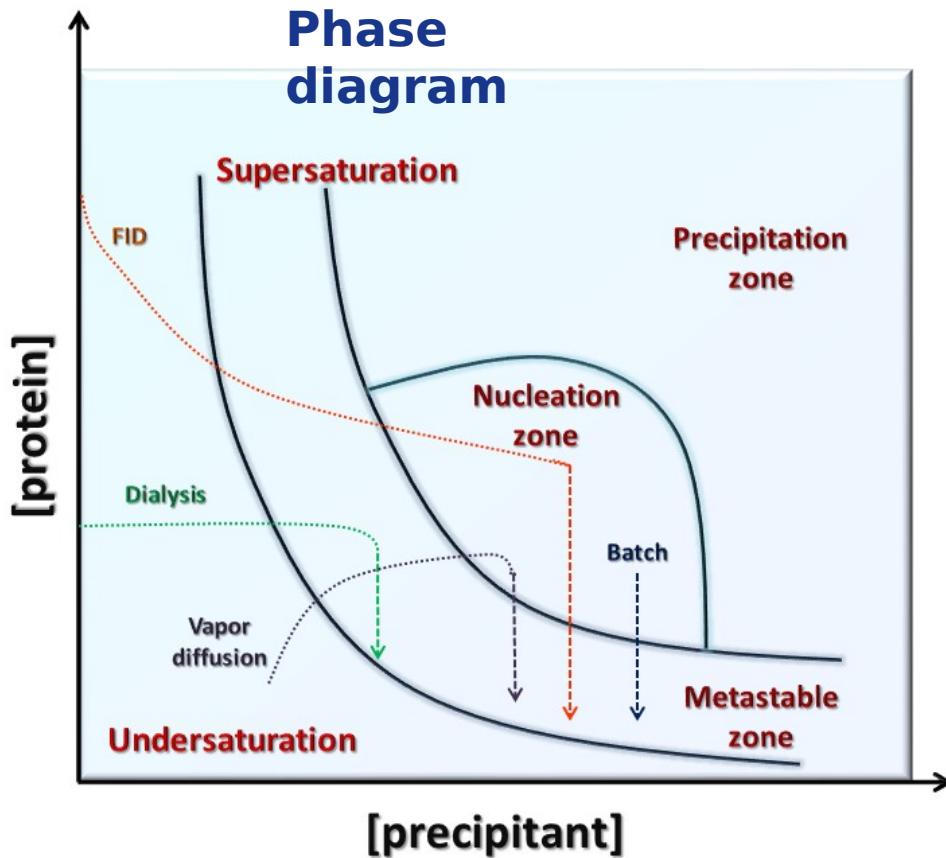
Gel filtration HPLC



CRYSTALLOGENESIS



CRYSTALLOGENESIS



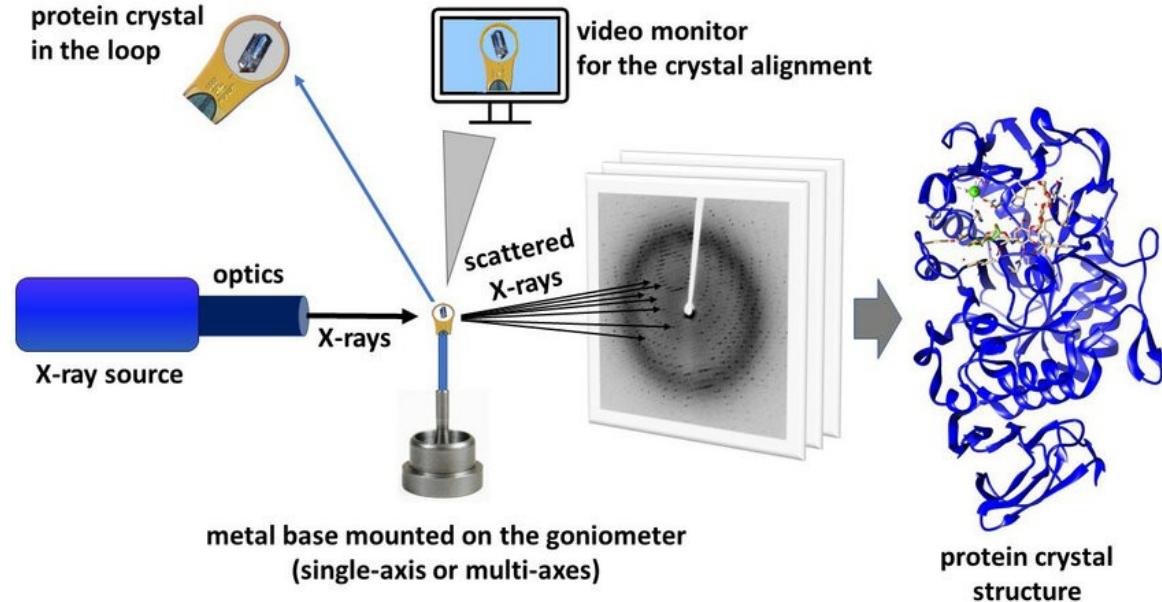
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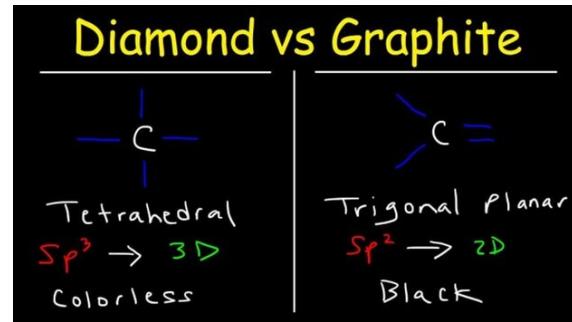
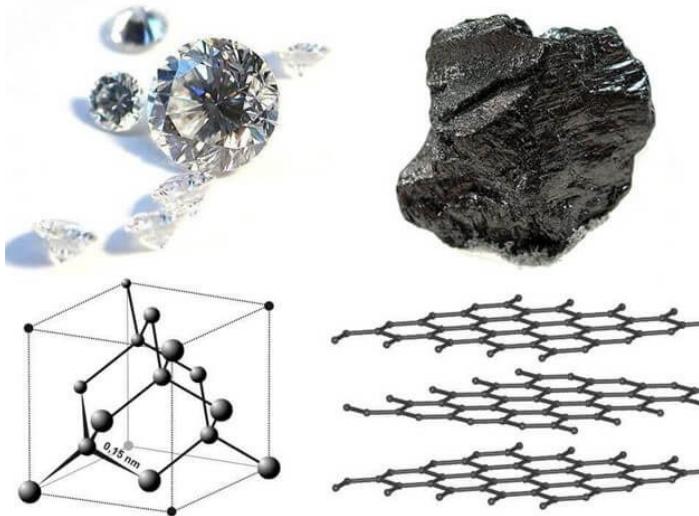
1. *Crystallogenesis*
2. *Crystal symmetries*
3. *X-rays*
4. *Diffraction*
5. *Phase problem*

Practice

6. *Crystal harvesting*
7. *Data collection*
8. *Data processing*
9. *Solving structures*
10. *Examples*



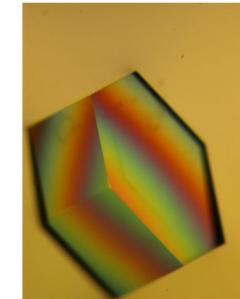
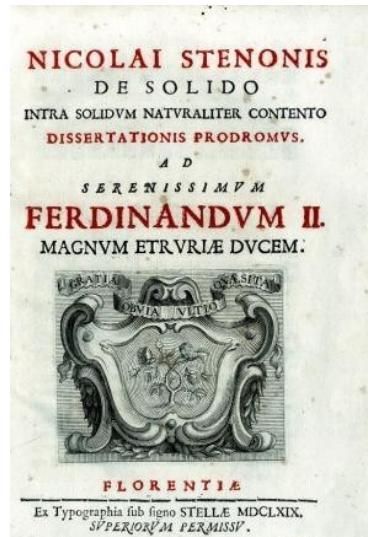
CRYSTALS



Steno's Law (1669)

The angles between corresponding faces on crystals of any solid chemical or mineral species are constant and are characteristic of the species. The interfacial angle is measured between face normals.

The law constant of interfacial angles holds for any crystals of a given species, whether they are natural or hand-made, regardless of size or provenance.



7 LATTICE SYSTEMS

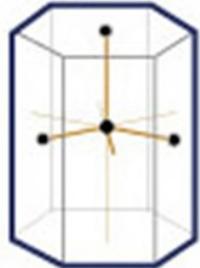
© AllAboutGemstones.com



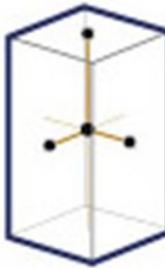
Cub
ic



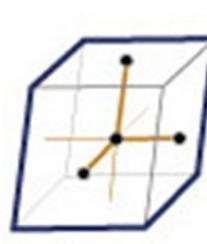
Hexago
nal



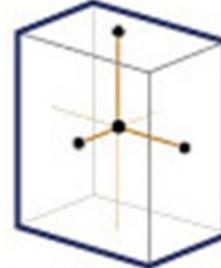
Tetrago
nal



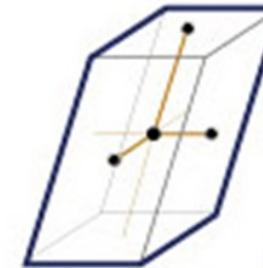
Rhombohe
dral
(or
trigonal)



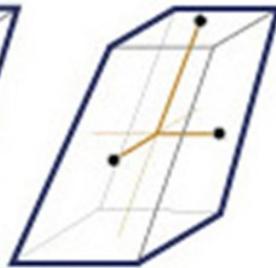
Orthorho
mbic



Monocli
nic

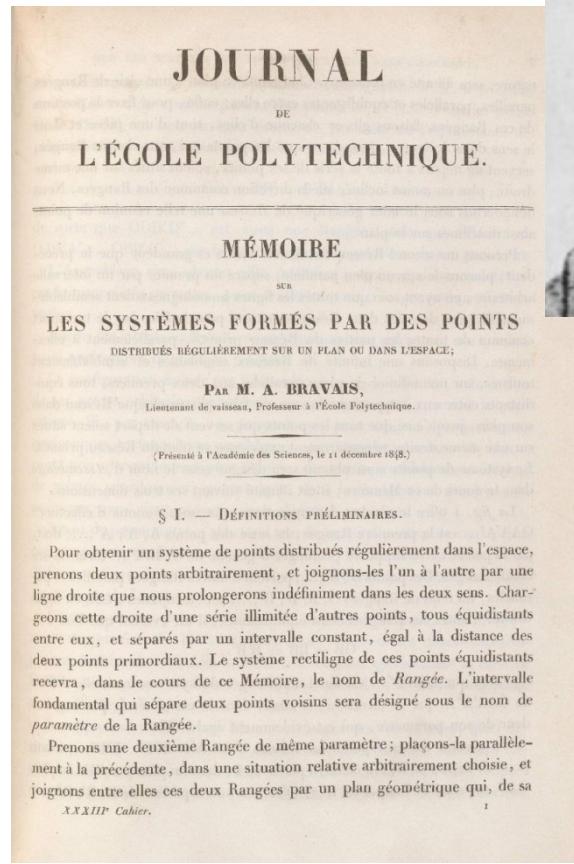


Tricli
nic



14 BRAVAIS LATTICES

Crystal family	Lattice system	Point group (Schönhflies notation)	14 Bravais lattices			
			Primitive (P)	Base-centered (S)	Body-centered (I)	Face-centered (F)
Triclinic (a)		C ₁				
Monoclinic (m)		C _{2h}				
Orthorhombic (o)		D _{2h}				
Tetragonal (t)		D _{4h}				
Hexagonal (h)	Rhombohedral	D _{3d}				
	Hexagonal	D _{6h}				
Cubic (c)		O _h				



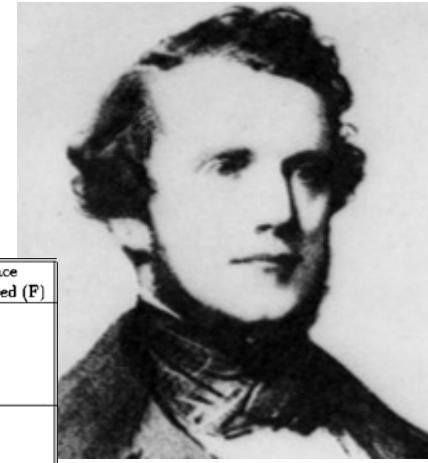
Auguste Bravais(1811-1863)

14 BRAVAIS LATTICES

$$\mathbf{R} = n_1 \mathbf{a}_1 + n_2 \mathbf{a}_2 + n_3 \mathbf{a}_3$$

Crystal family	Lattice system	Point group (Schönhflies notation)	14 Bravais lattices			
			Primitive (P)	Base-centered (S)	Body-centered (I)	Face-centered (F)
Triclinic (a)		C ₁				
Monoclinic (m)		C _{2h}				
Orthorhombic (o)		D _{2h}				
Tetragonal (t)		D _{4h}				
Rhombohedral		D _{3d}				
Hexagonal (h)	Hexagonal	D _{6h}				
Cubic (c)		O _h				

Bravais lattice	Parameters	Simple (P)	Volume centered (I)	Base centered (C)	Face centered (F)
Triclinic	$a_1 \neq a_2 \neq a_3$ $\alpha_{12} \neq \alpha_{23} \neq \alpha_{31}$				
Monoclinic	$a_1 \neq a_2 \neq a_3$ $\alpha_{23} = \alpha_{31} = 90^\circ$ $\alpha_{12} \neq 90^\circ$				
Orthorhombic	$a_1 \neq a_2 \neq a_3$ $\alpha_{12} = \alpha_{23} = \alpha_{31} = 90^\circ$				
Tetragonal	$a_1 = a_2 \neq a_3$ $\alpha_{12} = \alpha_{23} = \alpha_{31} = 90^\circ$				
Trigonal	$a_1 = a_2 = a_3$ $\alpha_{12} = \alpha_{23} = \alpha_{31} < 120^\circ$				
Cubic	$a_1 = a_2 = a_3$ $\alpha_{12} = \alpha_{23} = \alpha_{31} = 90^\circ$				
Hexagonal	$a_1 = a_2 \neq a_3$ $\alpha_{12} = 120^\circ$ $\alpha_{23} = \alpha_{31} = 90^\circ$				



Auguste Bravais(1811-1863)

32 POINT GROUPS

A group of point symmetry operations leave at least one point unmoved. Lattice translation is not considered in point group.

Crystal family	Crystal system	Group names						
	Cubic	23	$m\bar{3}$		432	$\bar{4}3m$	$m\bar{3}m$	
Hexagonal	Hexagonal	6	$\bar{6}$	$6/m$	622	6mm	$\bar{6}m2$	6/mmm
	Trigonal	3	$\bar{3}$		32	3m	$\bar{3}m$	
	Tetragonal	4	$\bar{4}$	$4/m$	422	4mm	$\bar{4}2m$	4/mmm
	Orthorhombic				222		$mm2$	mmm
	Monoclinic	2		$2/m$		m		
	Triclinic	1	$\bar{1}$					



Johann Hessel (1796-1872)

230 SPACE GROUPS

Hermann-Mauguin symbol
(internat. Table vol. A)

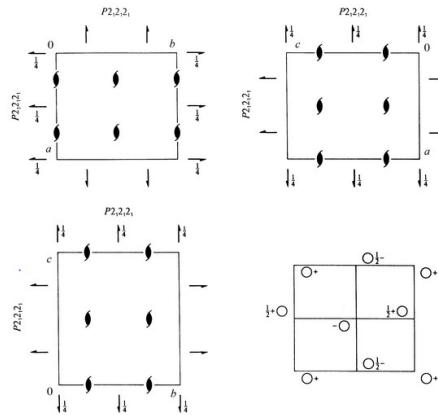
$P_{2_1}2_12_1$

D_2^4

222

No. 19

$P_{2_1}2_12_1$



Origin at midpoint of three non-intersecting pairs of parallel 2-fold axes

Symmetric unit $0 \leq x \leq 1/2; 0 \leq y \leq 1/2; 0 \leq z \leq 1$

Symmetry operations

(1) 1 (2) $2(0, 0, 1/2) \quad 1/4, 0, z$ (3) $2(0, 1/2, 0) \quad 0, y, 1/4$ (4) $2(1/2, 0, 0) \quad x, 1/4, 0$

Generators selected (1); $\langle 1, 0, 0 \rangle; \langle 0, 1, 0 \rangle; \langle 0, 0, 1 \rangle; \langle 2 \rangle; \langle 3 \rangle$

Positions

Multiplicity, Wyckoff letter, Site symmetry	Coordinates	Reflection conditions
4 α 1 (1) x, y, z (2) $x + 1/2, -y, z + 1/2$ (3) $x, y + 1/2, -z + 1/2$ (4) $x + 1/2, -y + 1/2, -z$		General: $h00: h = 2n$ $0k0: k = 2n$ $00l: l = 2n$

Orthorhombic

Patterson symmetry $Pmmm$

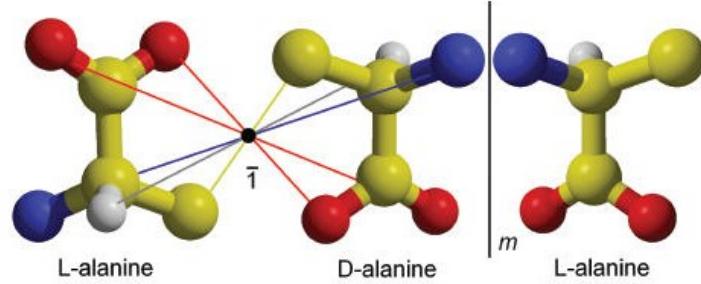


Evgraf Fedorov (1853-1919)

Triclinic	None		
Monoclinic*	$[010]$ ('unique axis b') $[001]$ ('unique axis c')		
Orthorhombic	$[100]$	$[010]$	$[001]$
Tetragonal	$[001]$	$\left\{ \begin{matrix} [100] \\ [010] \end{matrix} \right\}$	$\left\{ \begin{matrix} [1\bar{1}0] \\ [\bar{1}10] \end{matrix} \right\}$
Hexagonal	$[001]$	$\left\{ \begin{matrix} [100] \\ [010] \\ [\bar{1}\bar{1}0] \end{matrix} \right\}$	$\left\{ \begin{matrix} [1\bar{1}0] \\ [\bar{1}20] \\ [\bar{2}\bar{1}0] \end{matrix} \right\}$
Rhombohedral (hexagonal axes)	$[001]$	$\left\{ \begin{matrix} [100] \\ [010] \\ [\bar{1}\bar{1}0] \end{matrix} \right\}$	
Rhombohedral (rhombohedral axes)	$[111]$	$\left\{ \begin{matrix} [\bar{1}\bar{1}0] \\ [011] \\ [\bar{1}01] \end{matrix} \right\}$	
Cubic	$\left\{ \begin{matrix} [100] \\ [010] \\ [001] \end{matrix} \right\}$	$\left\{ \begin{matrix} [111] \\ [\bar{1}\bar{1}\bar{1}] \\ [\bar{1}\bar{1}\bar{1}] \end{matrix} \right\}$	$\left\{ \begin{matrix} [\bar{1}\bar{1}0] \\ [110] \\ [011] \\ [011] \\ [\bar{1}01] \\ [101] \end{matrix} \right\}$

SPACE GROUPS IN MX

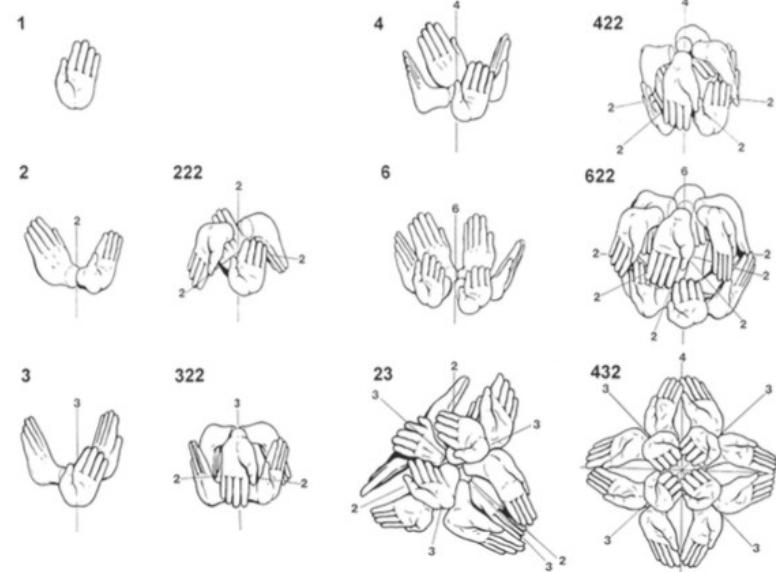
11 point group in proteins



Combination of all point symmetry operations generates **32 point groups** but for proteins, only 11 are allowed

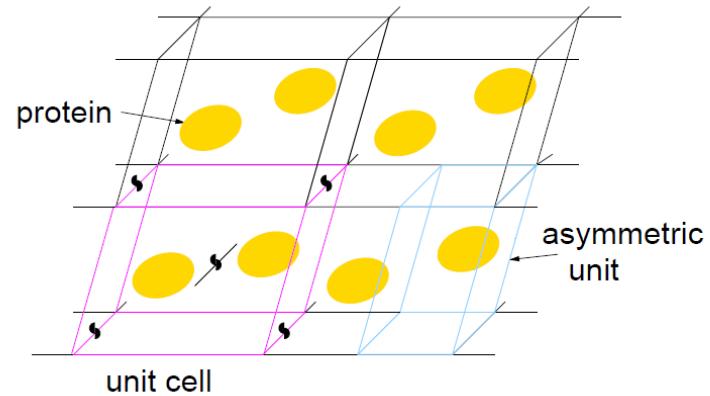
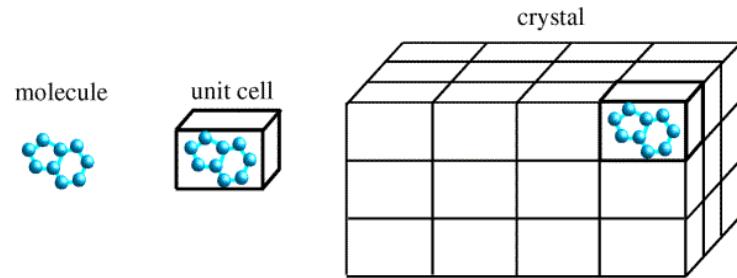
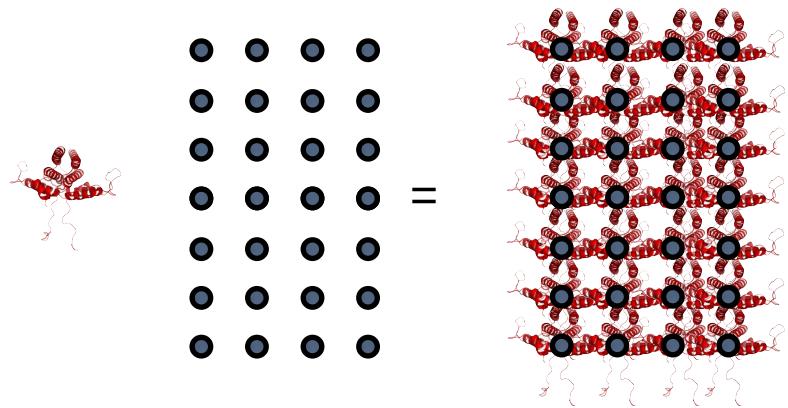
Crystal family	Crystal system	Group names						
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Hexagonal	Hexagonal	6	$\bar{6}$	$\bar{6}/m$	622	6mm	$\bar{6}m2$	6/mmm
	Trigonal	3	$\bar{3}$		32	3m	$\bar{3}m$	
Tetragonal		4	$\bar{4}$	$4/m$	422	4mm	$\bar{4}2m$	4/mmm
Orthorhombic					222		mm2	mmm
Monoclinic		2		$2/m$		m		
Triclinic		1	$\bar{1}$					

Combination of point groups and Bravais lattices leaves **65 space groups** for protein crystals (chiral objects)



PROTEIN CRYSTAL

Crystal is a convolution of the molecule over the lattice



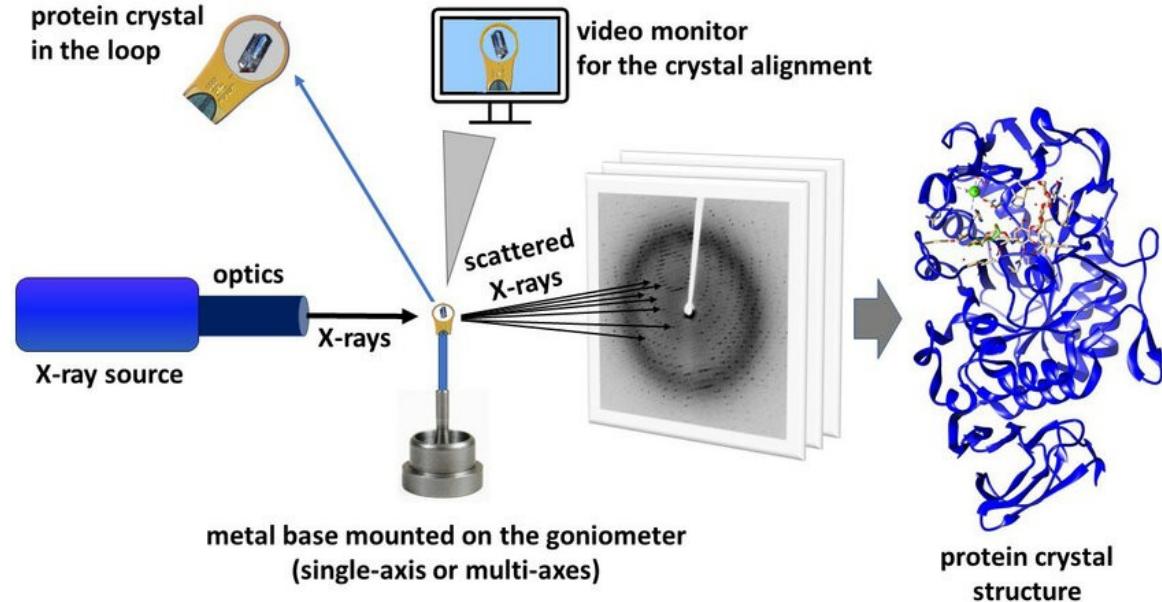
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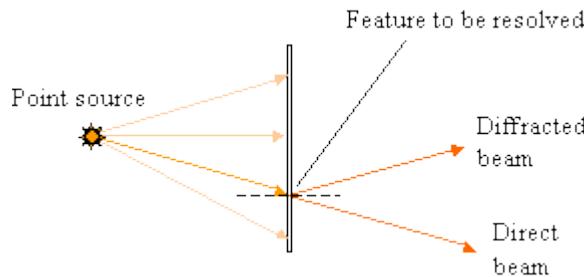
1. *Crystallogenesis*
2. Crystal symmetries
3. *X-rays*
4. *Diffraction*
5. *Phase problem*

Practice

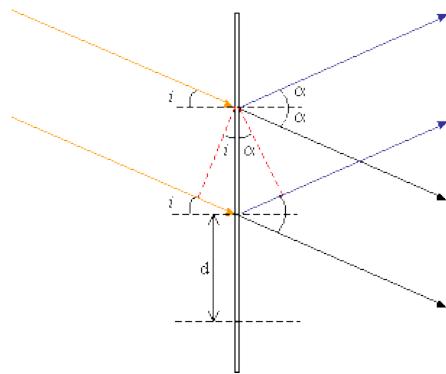
6. *Crystal harvesting*
7. *Data collection*
8. *Data processing*
9. *Solving structures*
10. *Examples*



HOW TO PROBE A CRYSTAL?

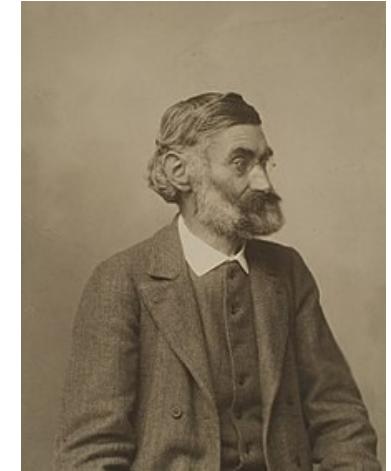


$$d_{min}$$



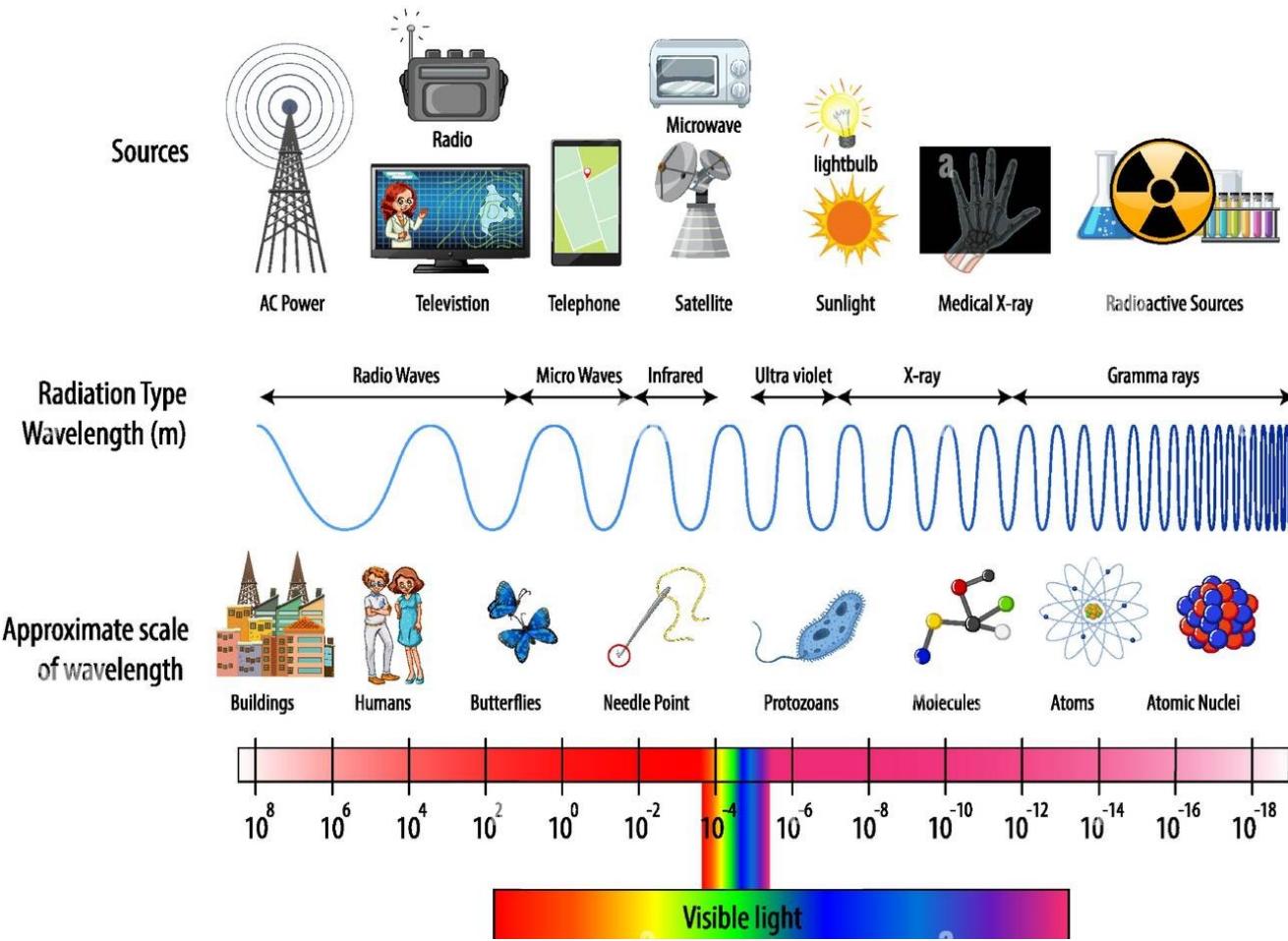
The limit of resolution (or resolving power) is a measure of the ability of the objective lens to separate in the image, adjacent details of the object.

n is the refractive index.

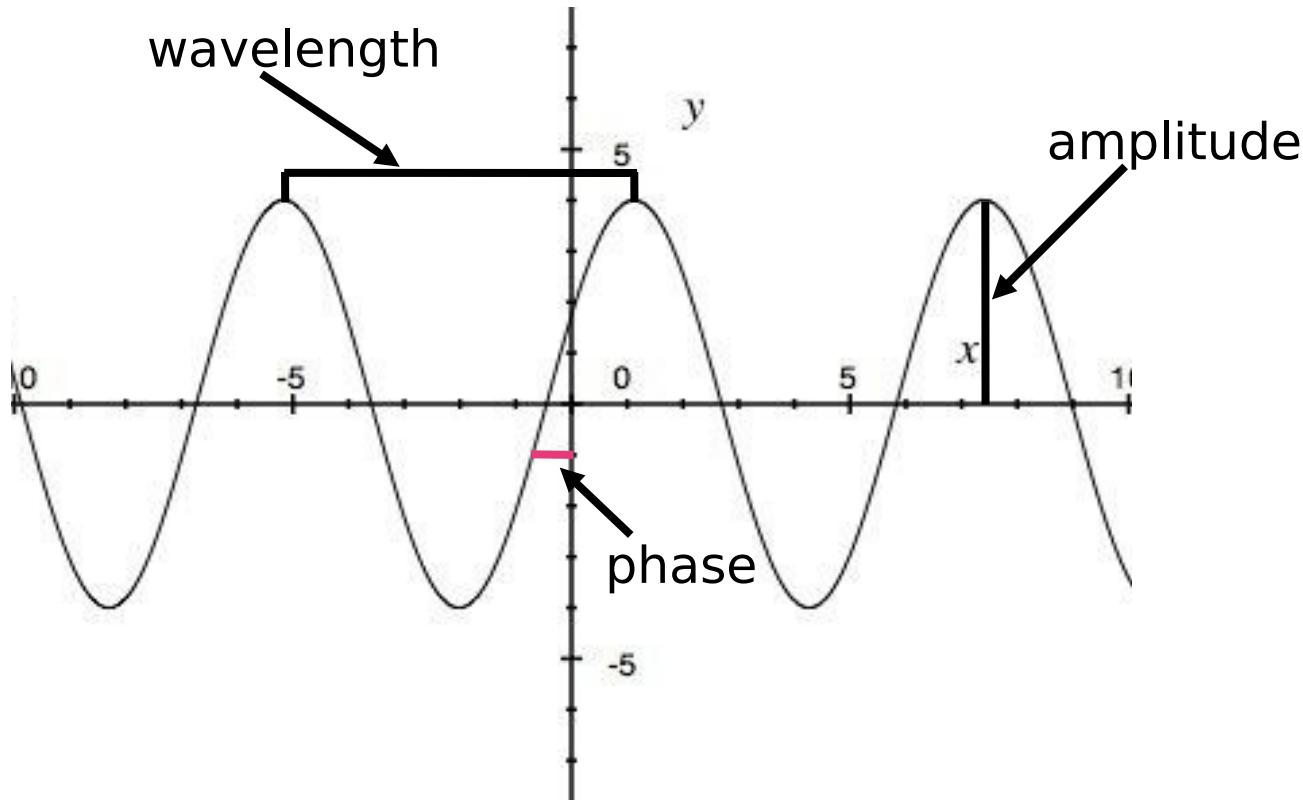


Ernst Abbe (1840-1905)

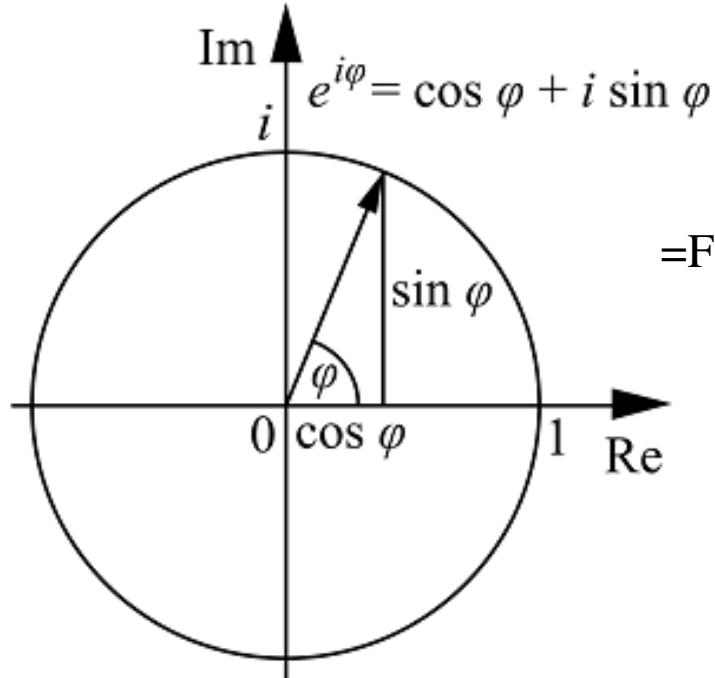
HOW TO PROBE A CRYSTAL?



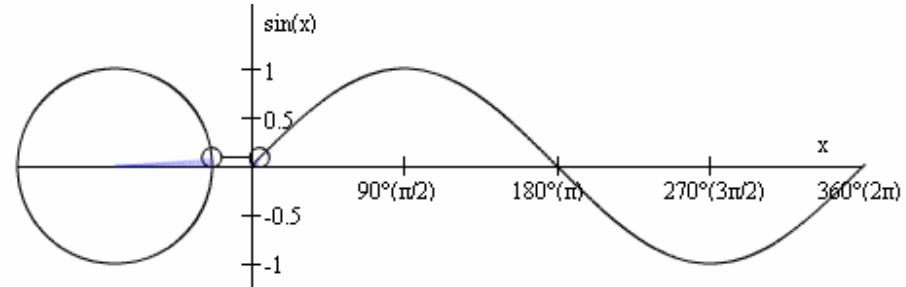
X-RAY AS A WAVE



XRAY AS A WAVE



A complex number may represent a wave, defined by an Amplitude and a Phase (Euler and trigonometric functions)

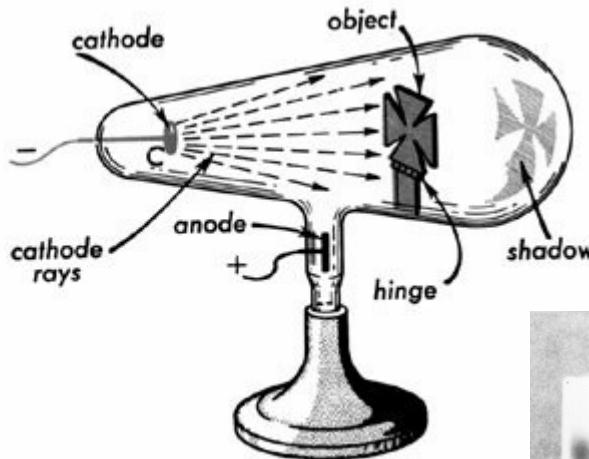


X-RAY PRODUCTION

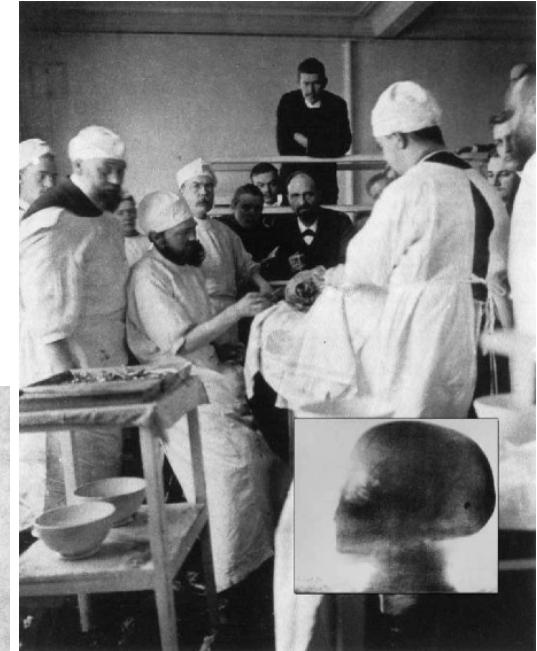
Vacuum tube



William Crookes
(1832-1919)



Wilhelm Röntgen is usually credited as the discoverer of X-rays in 1895

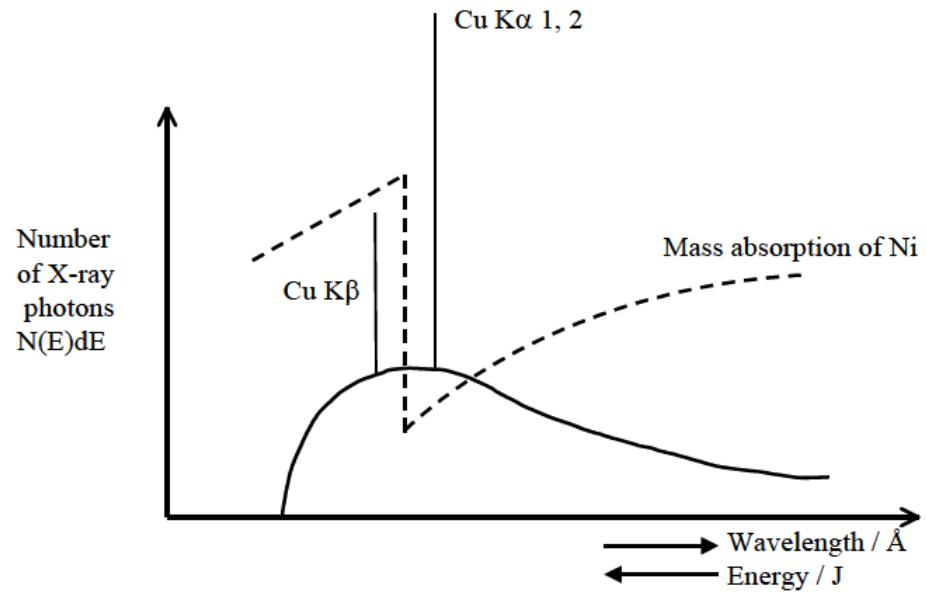
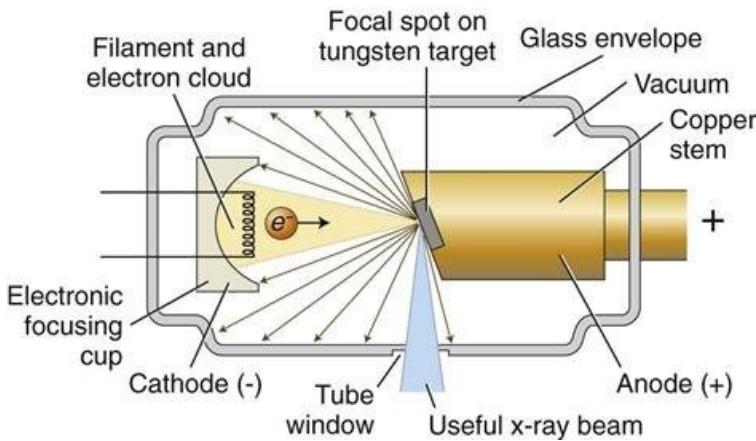


Medical applications of X-rays

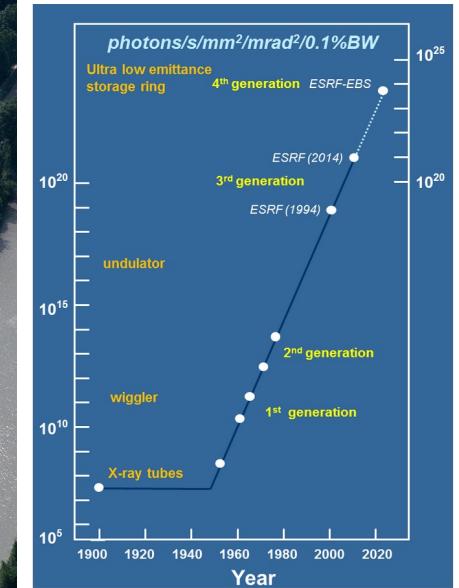
MONOCHROMATIC BEAM

Rotating anode

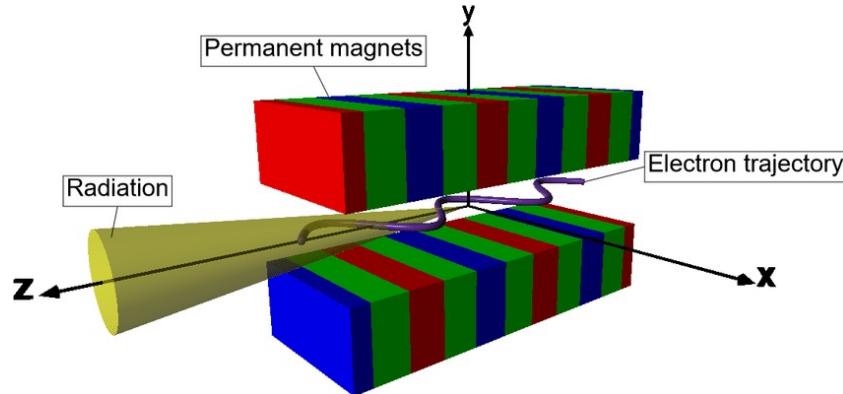
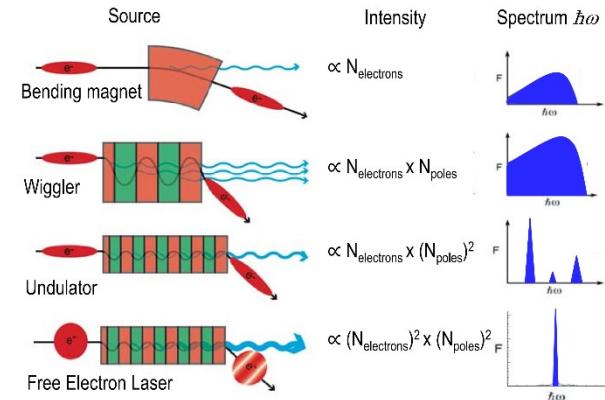
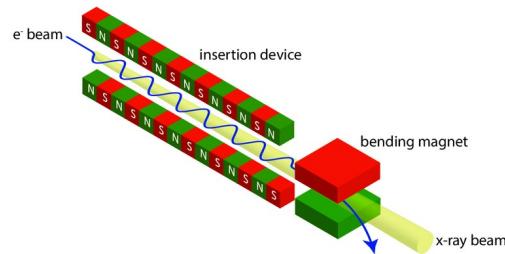
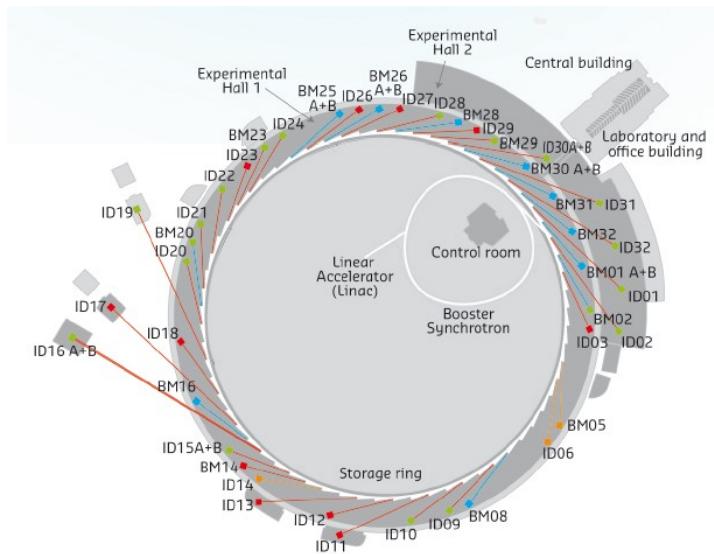
~50% of the Cu K α is transmitted
(~ 10^{10} ph/s/mm 2)



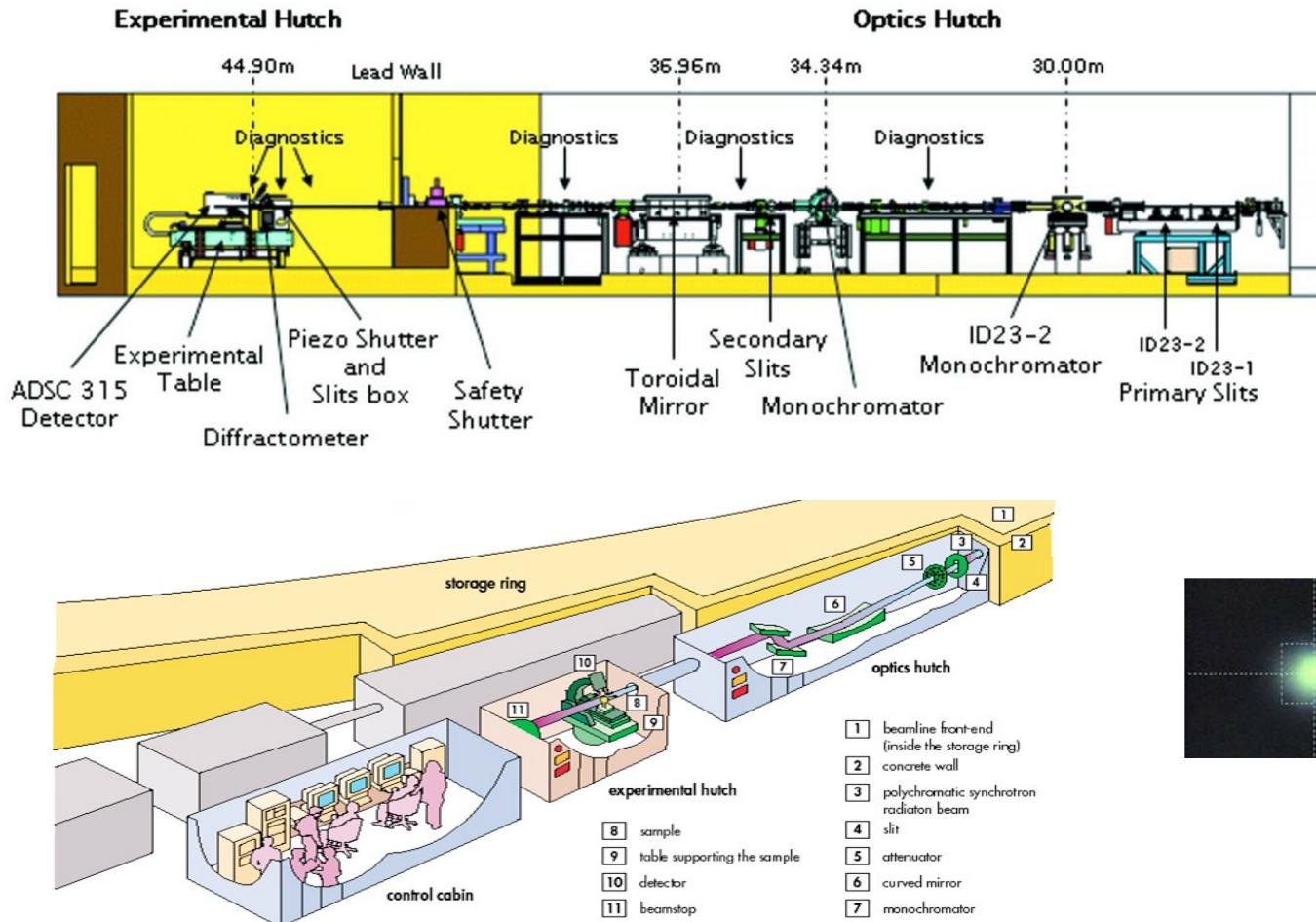
WHAT IS A SYNCHROTRON ?



HOW DOES IT WORK?



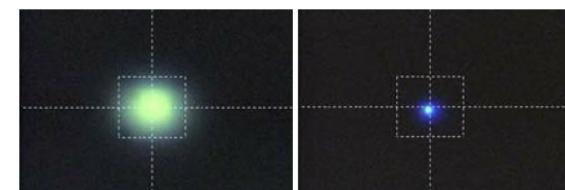
WHAT IS A BEAMLINE?



Size
 $<30\mu\text{m} \varnothing$

Flux
 $> 10^{12} \text{ ph/s}$

Energy resolution



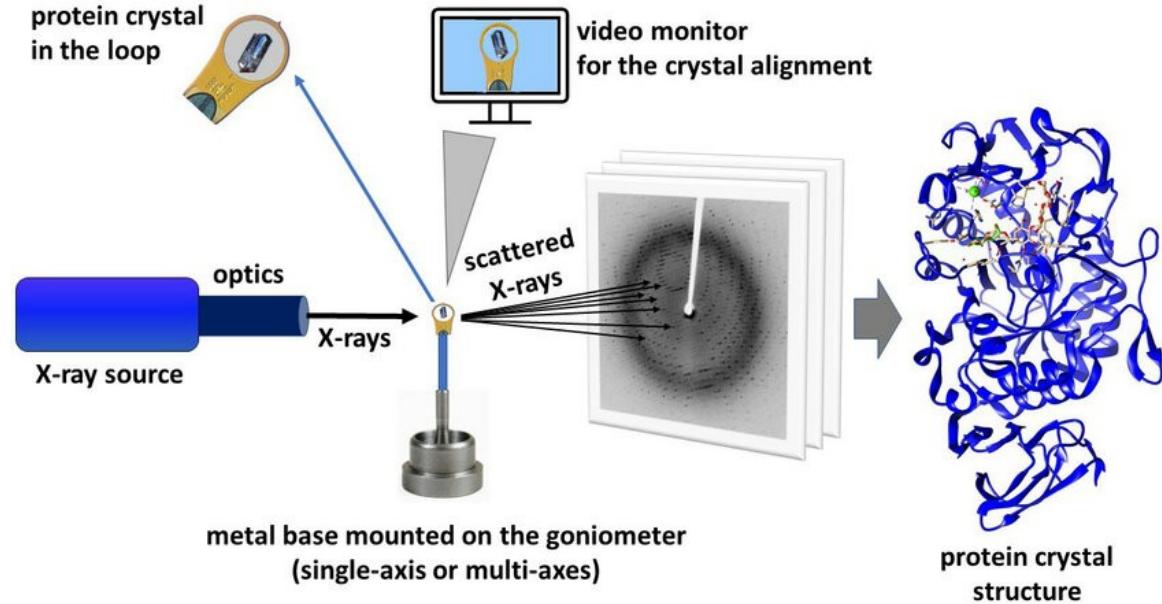
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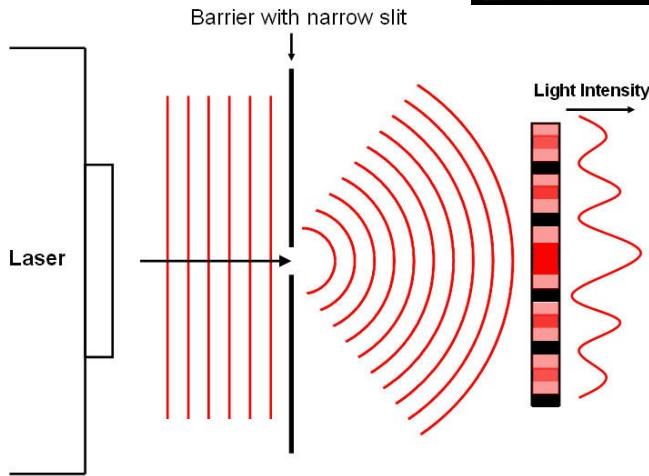
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DIFFRACTION

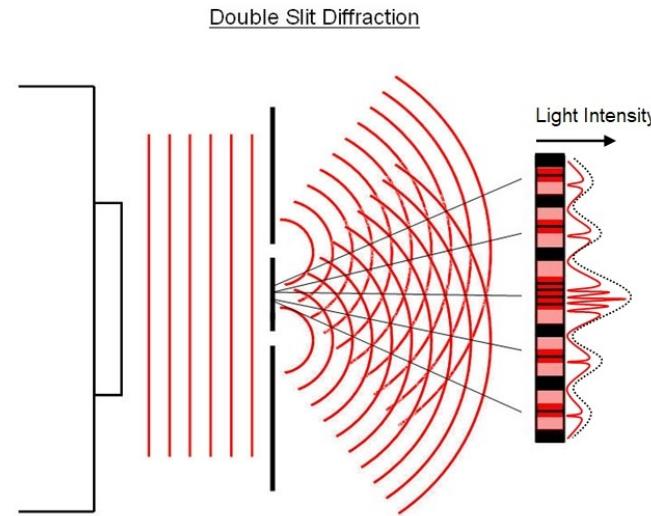


Single Slit Diffraction



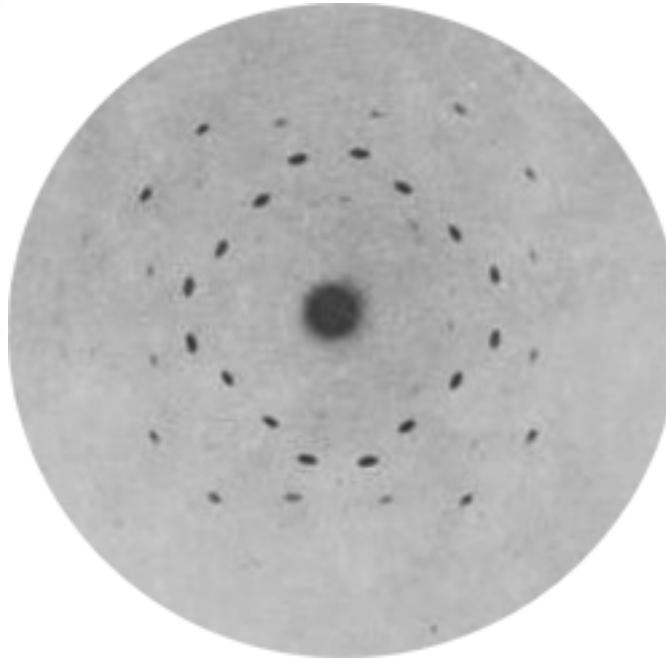
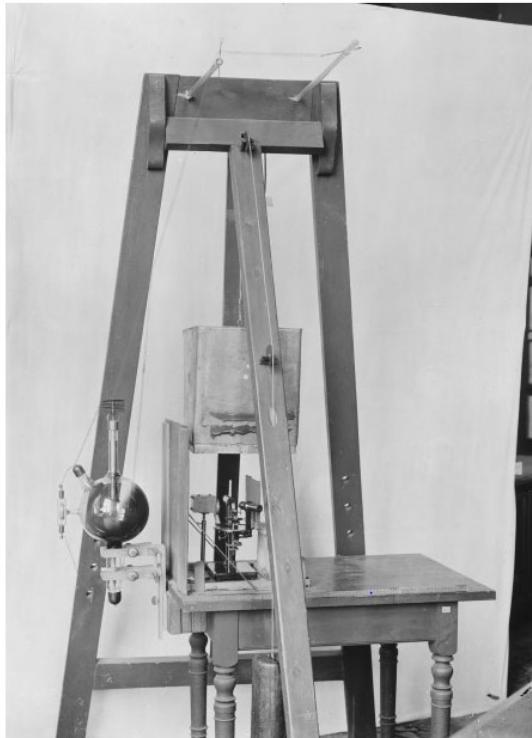
Plane waves through a slit -
slit becomes source of spherical waves

Waves interfere constructively in specific directions

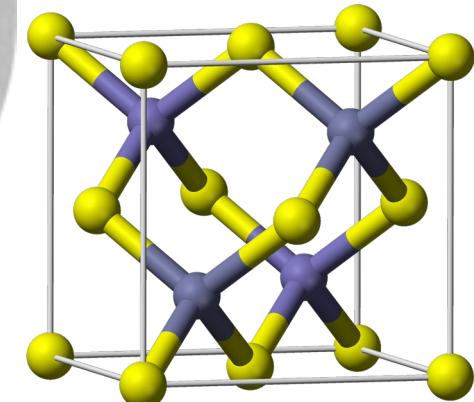


X-RAY DIFFRACTION

Max Laue's photo of X-ray diffraction from Zinc blende ZnS (Zn sulphide) cubic face centered (F3m)

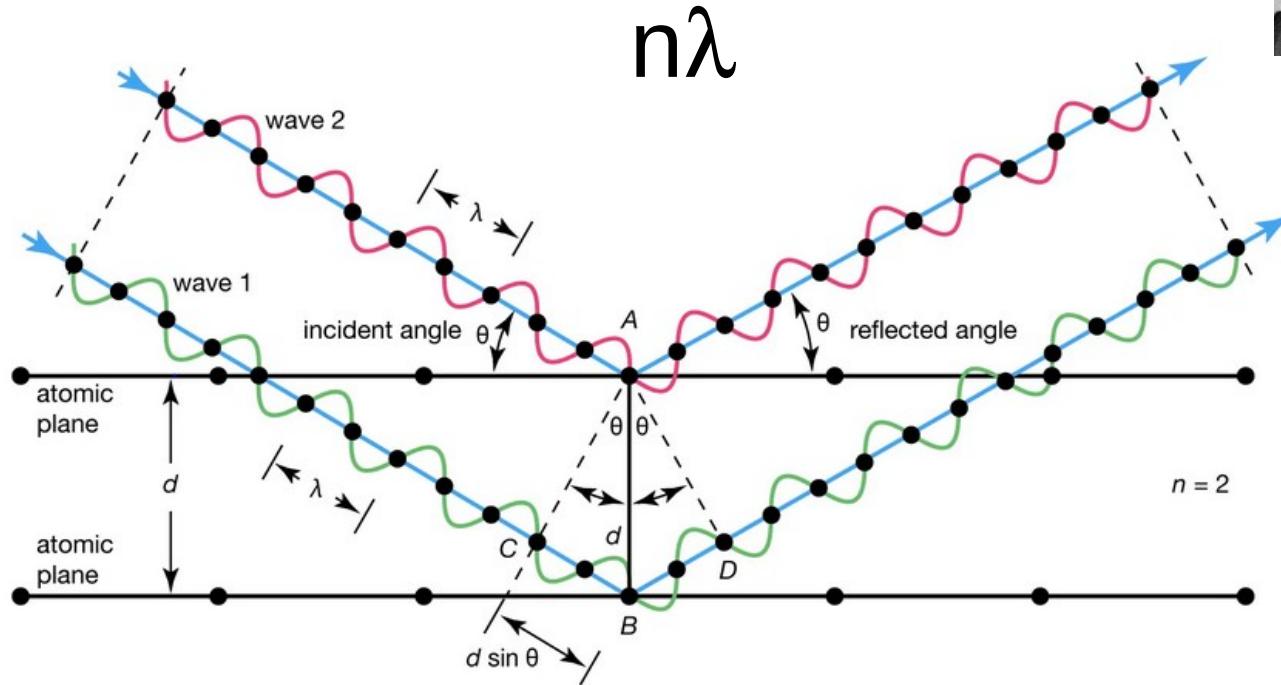
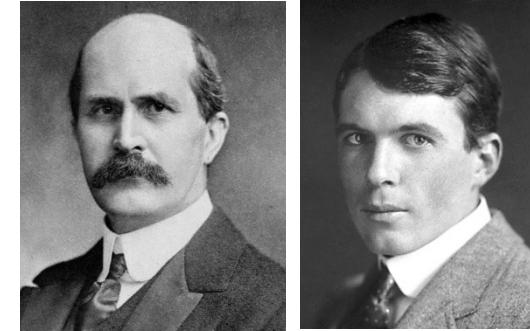


Max von Laue (1879-1960)
Nobel Prize 1914



BRAGG'S LAW

Bragg diffraction describes the condition for constructive interference from **monochromatic** waves, with amplitude and phase, reflected by planes in the crystalline material

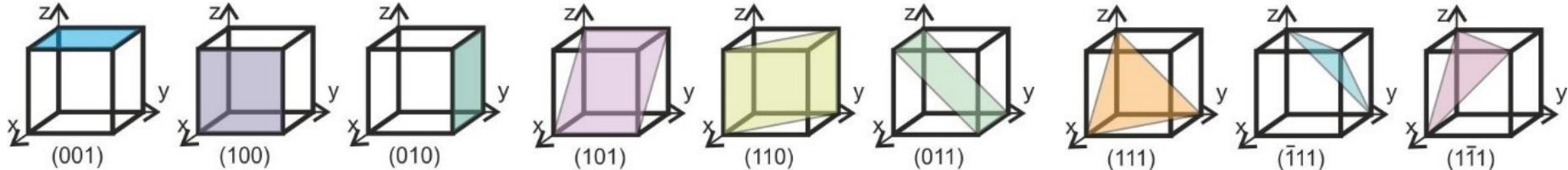
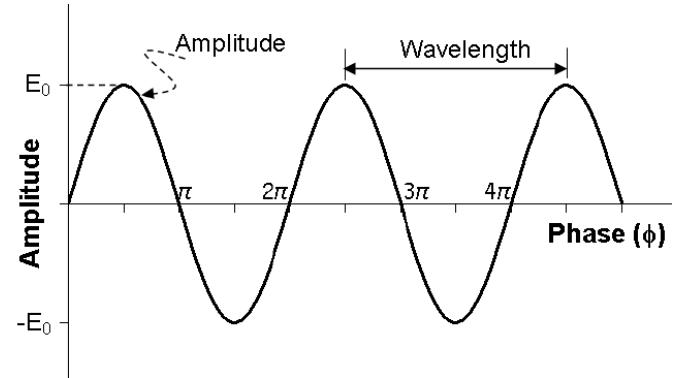


W. H & W. L Bragg
(1862-1942) – (1890-1971)
Nobel prize 1915

BRAGG'S LAW

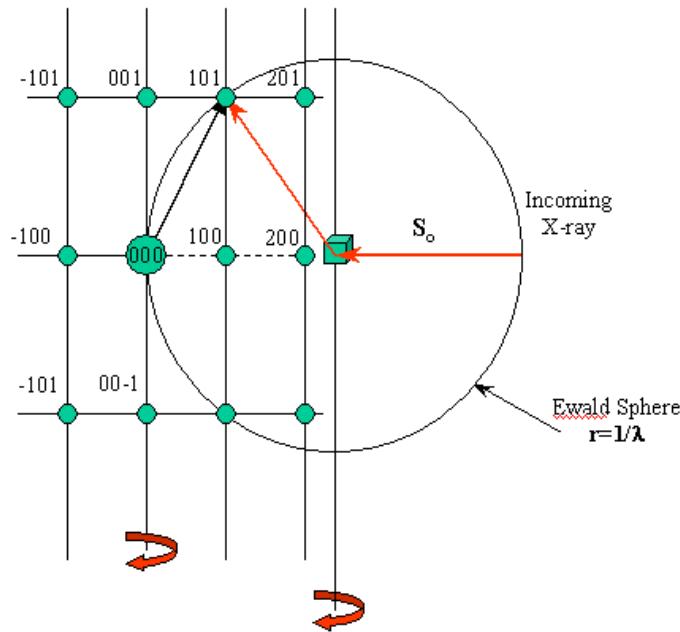
Bragg diffraction describes the condition for constructive interference from **monochromatic** waves, with amplitude and phase, reflected by planes in the crystalline material

$$n\lambda$$

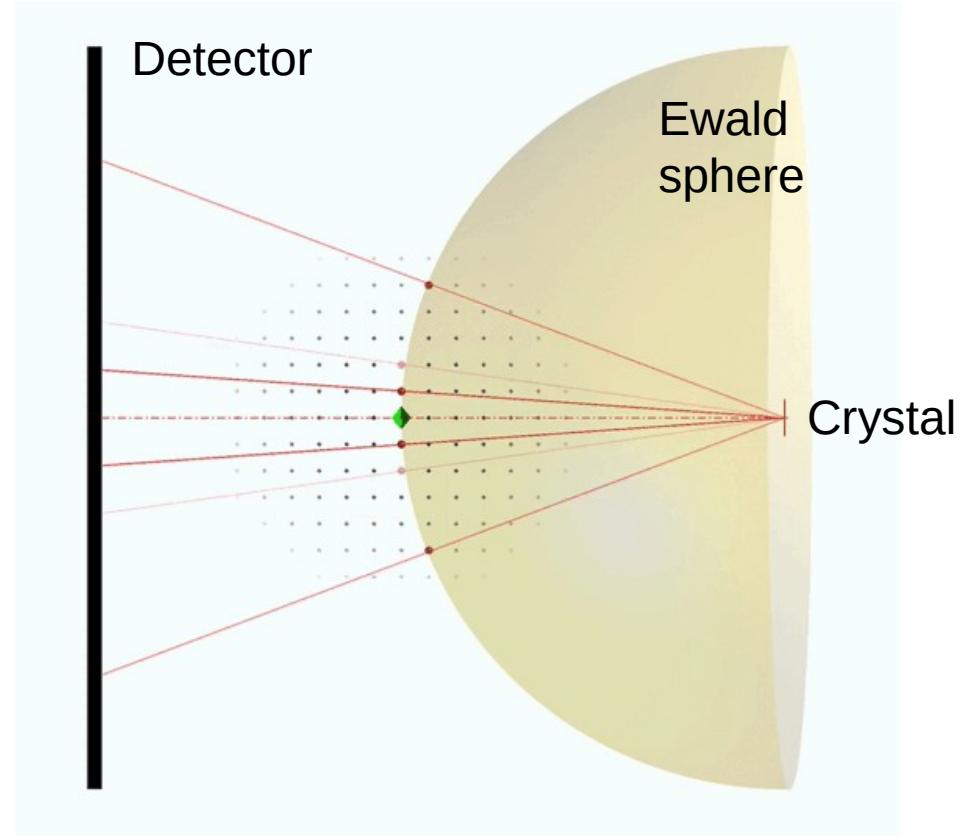


Each plane gives a spot of diffraction and this spot is defined by a triplet of integer hkl (Miller indices) in the reciprocal space

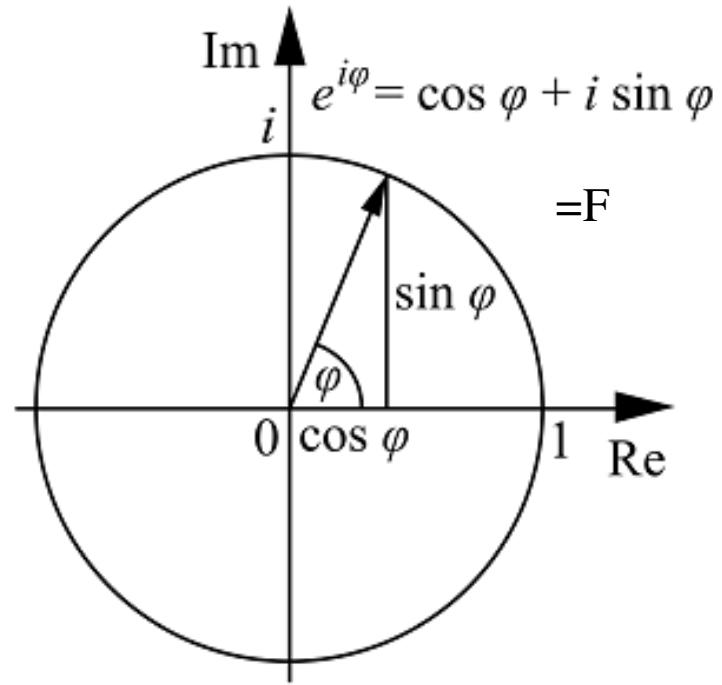
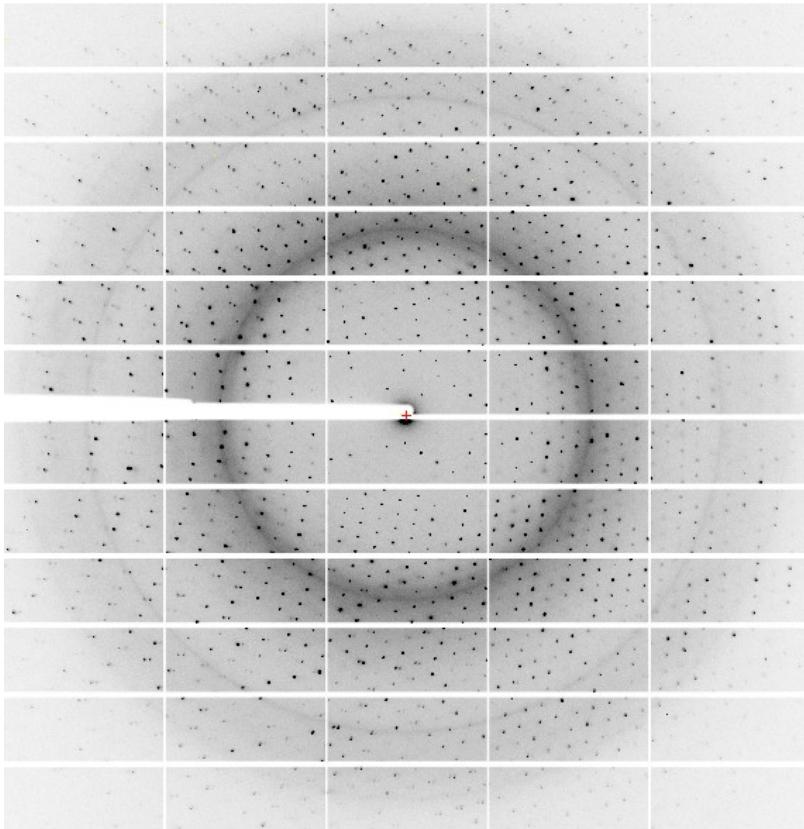
EWALD SPHERE



Each diffraction plane is represented as node



CRYSTAL DIFFRACTION



The 2D detector measures
Intensities of the diffraction peaks
BUT

DATASET STATISTICS

	Overall	Inner shell	Outer shell
Resolution (Å)	50-1.40	50 - 5.7	1.47 – 1.40
R _{merge}	0.052	0.022	1.047
R _{meas}	0.065	0.027	1.314
R _{pim}	0.038	0.015	0.785
CC _{1/2}	0.997	0.995	0.474
# observations	571512	9792	43402
# unique	127131	2224	9827
<I>/σ(I)	12.8	50.8	1.2
Completeness	0.929	0.88	0.745
Multiplicity	4.5	4.4	4.4

CC_{1/2} the intensities of two randomly sets of reflections correlates

<I>/σ(I) Intensity of the reflection over the error

Completeness, ratio between the # of unique observations and the total # theoretical reflections

Multiplicity, ratio between # of observed and unique reflections

$$R_{merge} = \frac{\sum_{hkl} \sum_{i=1}^n |I_i(hkl) - \bar{I}(hkl)|}{\sum_{hkl} \sum_{i=1}^n I_i(hkl)}$$

$$R_{meas} = \frac{\sum_{hkl} \sqrt{\frac{n}{n-1}} \sum_{i=1}^n |I_i(hkl) - \bar{I}(hkl)|}{\sum_{hkl} \sum_{i=1}^n I_i(hkl)}$$

$$R_{pim} = \frac{\sum_{hkl} \sqrt{1/n-1} \sum_{i=1}^n |I_i(hkl) - \bar{I}(hkl)|}{\sum_{hkl} \sum_{i=1}^n I_i(hkl)}$$

merged data

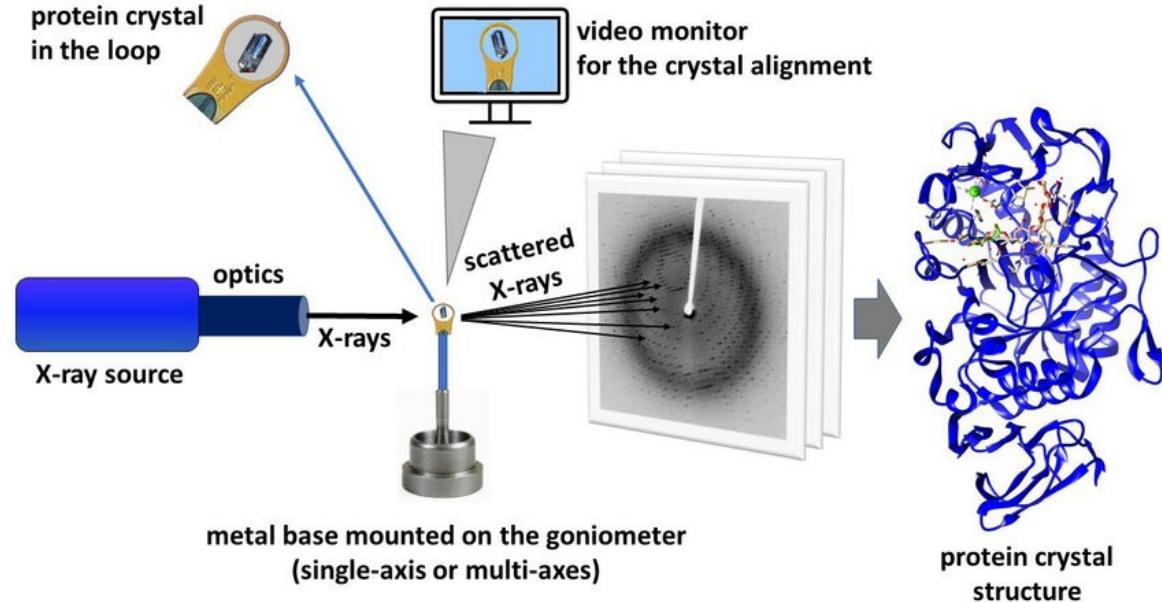
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1. *Crystallogenesis*
2. Crystal symmetries
3. *X-rays*
4. *Diffraction*
5. *Phase problem*
 1. *SAD*
 2. *MR*

Practice

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8. *Data processing*
9. *Solving structures*
10. *Examples*

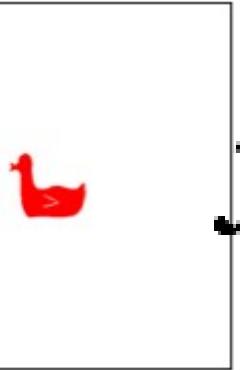
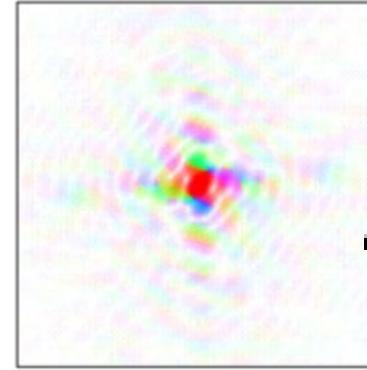
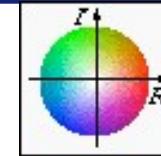
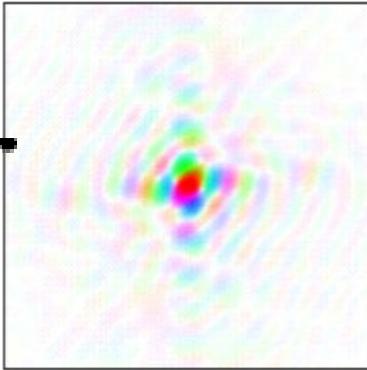
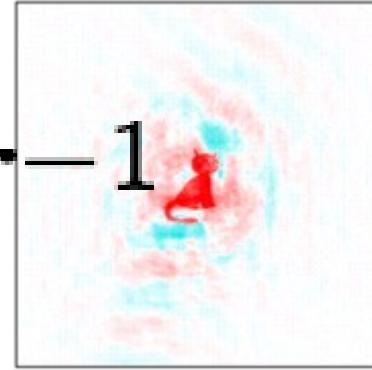


WHY RETRIEVING PHASES

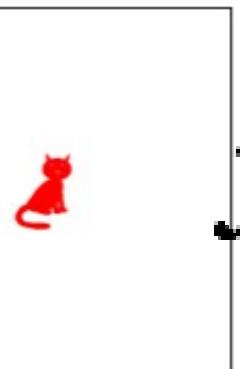
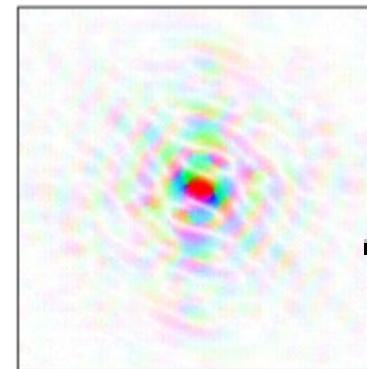
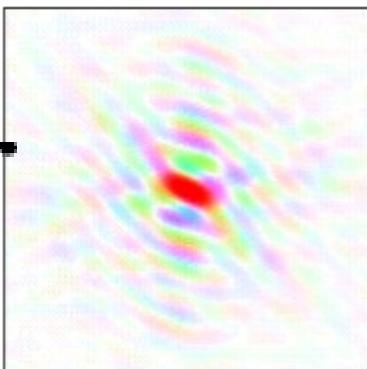
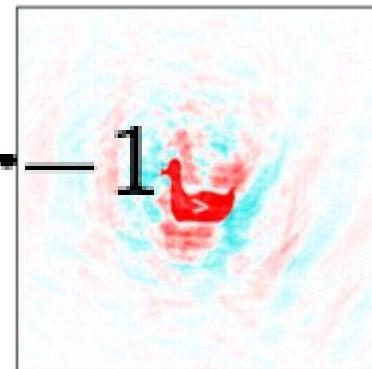
the electron density over the volume of the cell
(Fourier transform)



WHY RETRIEVING PHASES

 \mathcal{F}  \mathcal{F}^{-1} 

Phases are the most important information to obtain

 \mathcal{F}  \mathcal{F}^{-1} 

THE PHASE PROBLEM

The electron density over the volume of the cell:

How to retrieve the phase?

Method

Direct (< 1000 non hydrogen / ua)

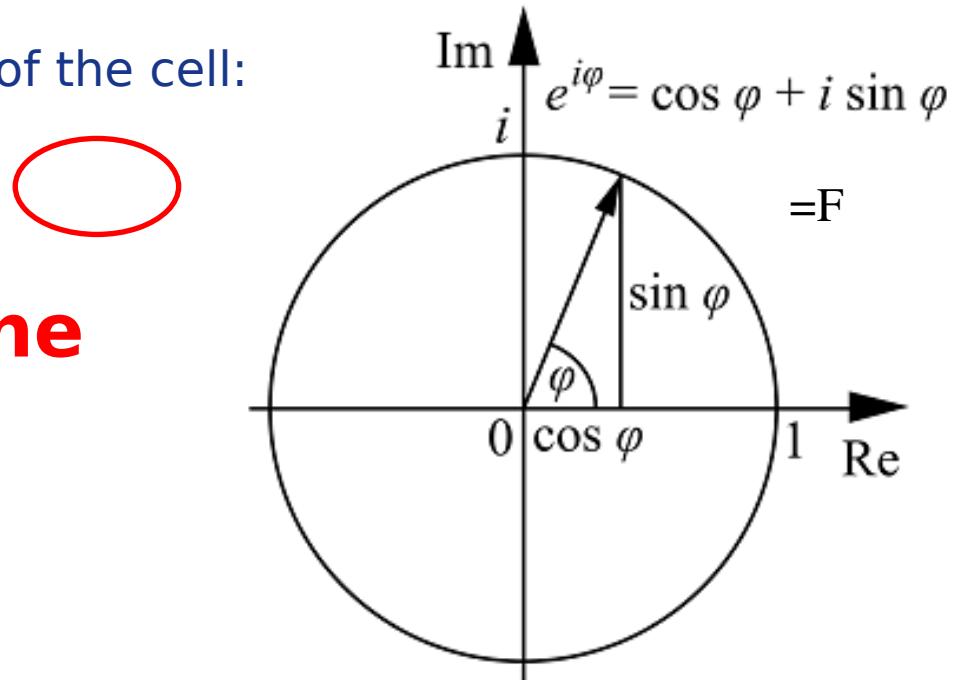
SIR, MIR

SIRAS, MIRAS

MAD, SAD

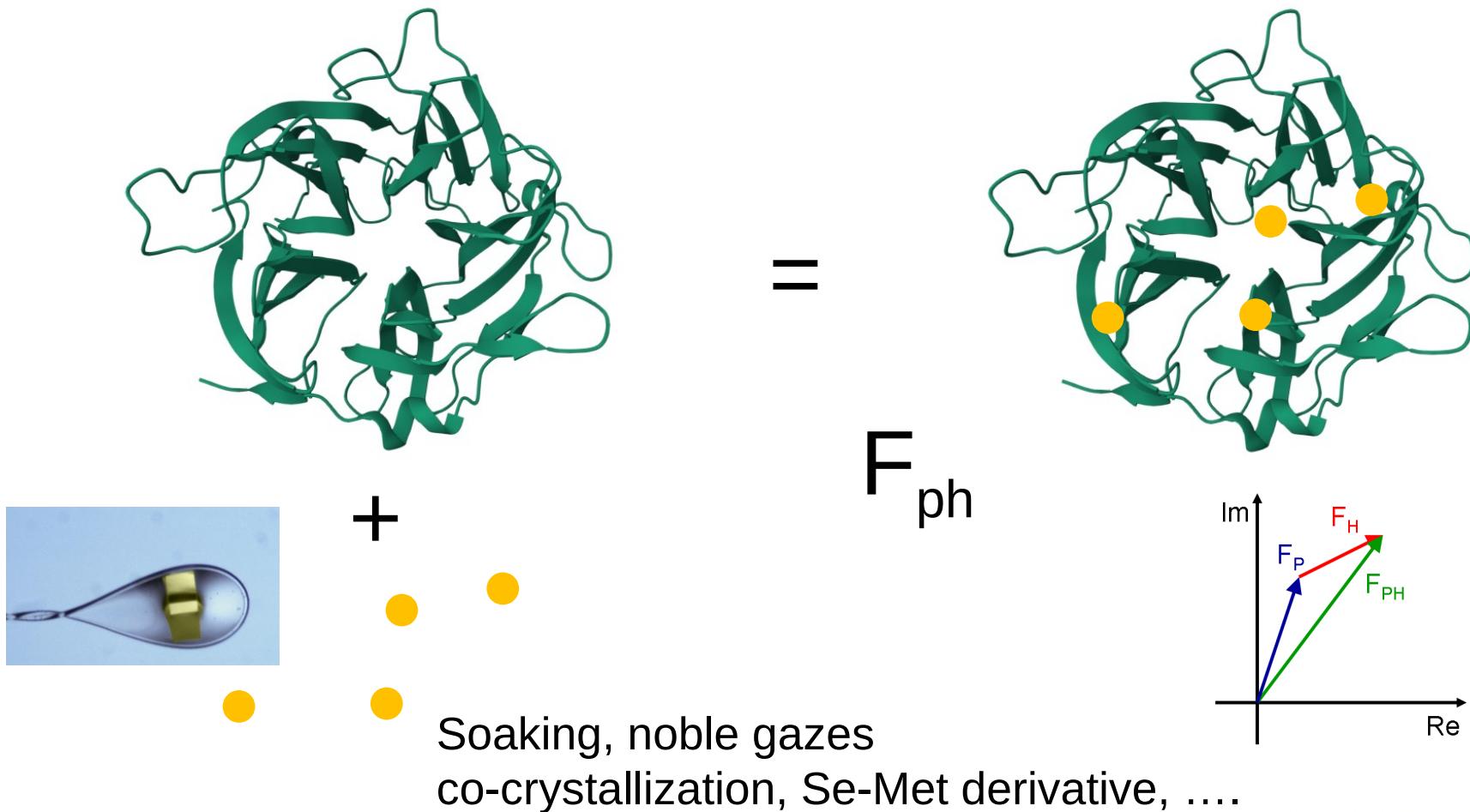
Molecular Replacement

*Isomorphous
Replacement*

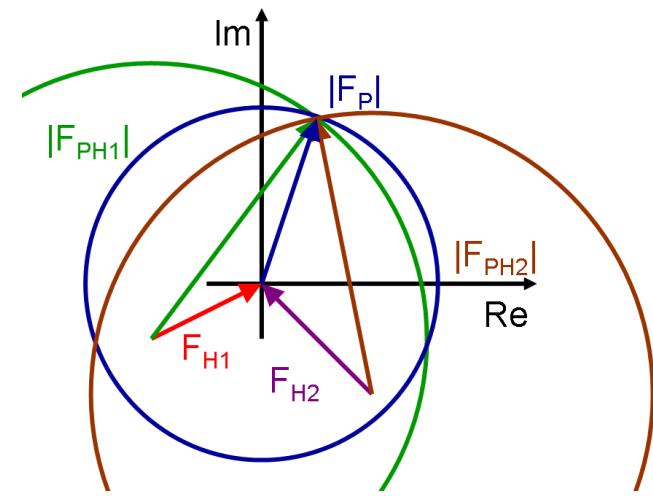
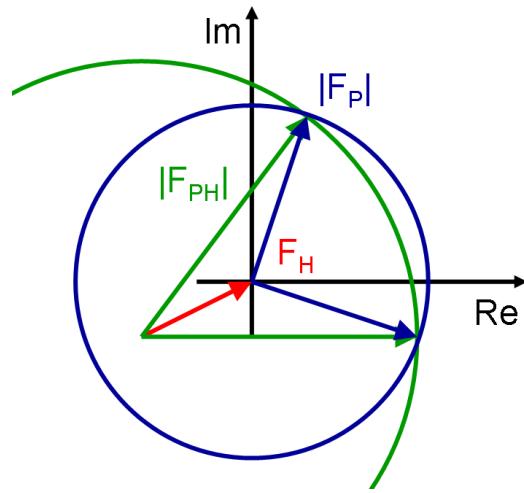
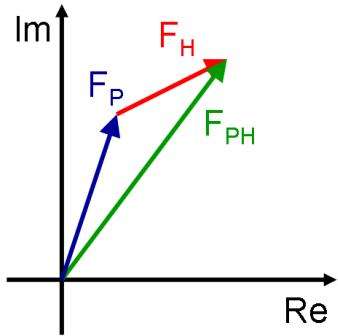


The 2D detector measures
Intensities of the diffraction peaks
BUT

HEAVY ATOM DERIVATIVE



HARKER CONSTRUCTION



THE PHASE PROBLEM

The electron density over the volume of the cell:

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Direct (< 1000 non hydrogen / ua)

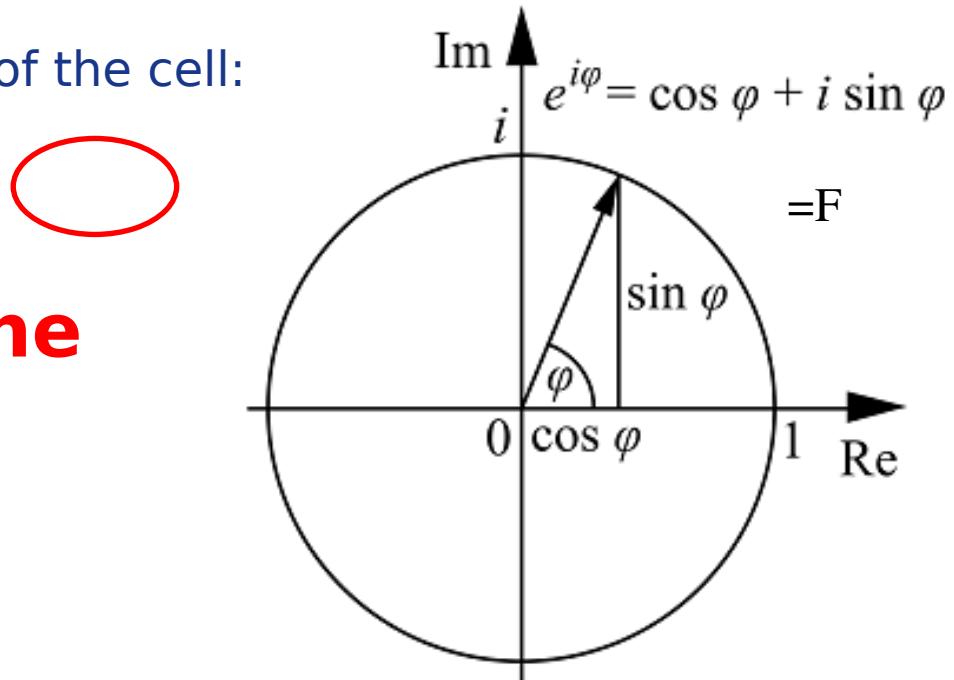
SIR, MIR

SIRAS, MIRAS

MAD, SAD

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} ***Isomorphous Replacement***

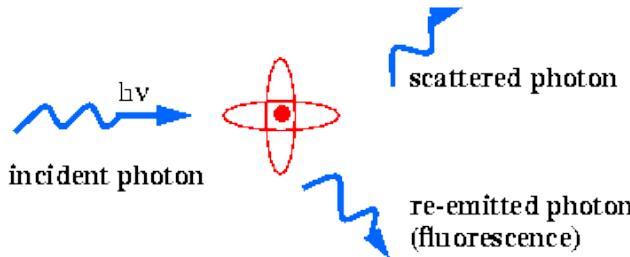


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Intensities of the diffraction peaks
BUT

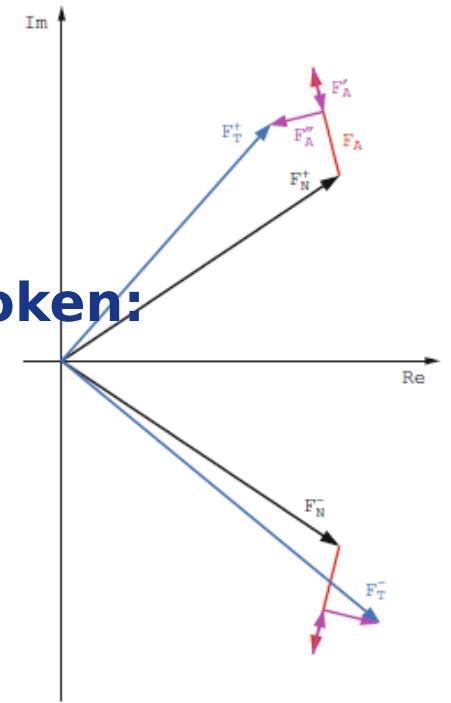
FRIEDEL'S LAW

When incident X-ray energy matches the binding energy of the electrons of the heavy atom, the absorption of X-rays increases.

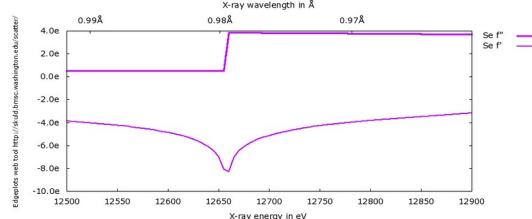
The scattering factor of the HA takes the form of :



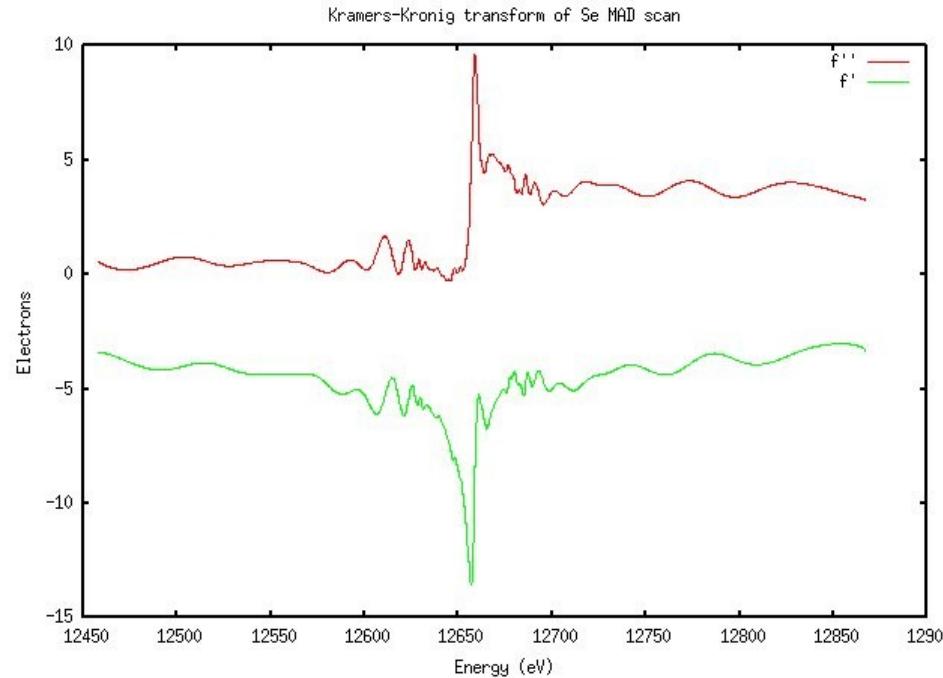
Friedel's law is broken:
 $F(hkl) \neq F(-h-k-l)$



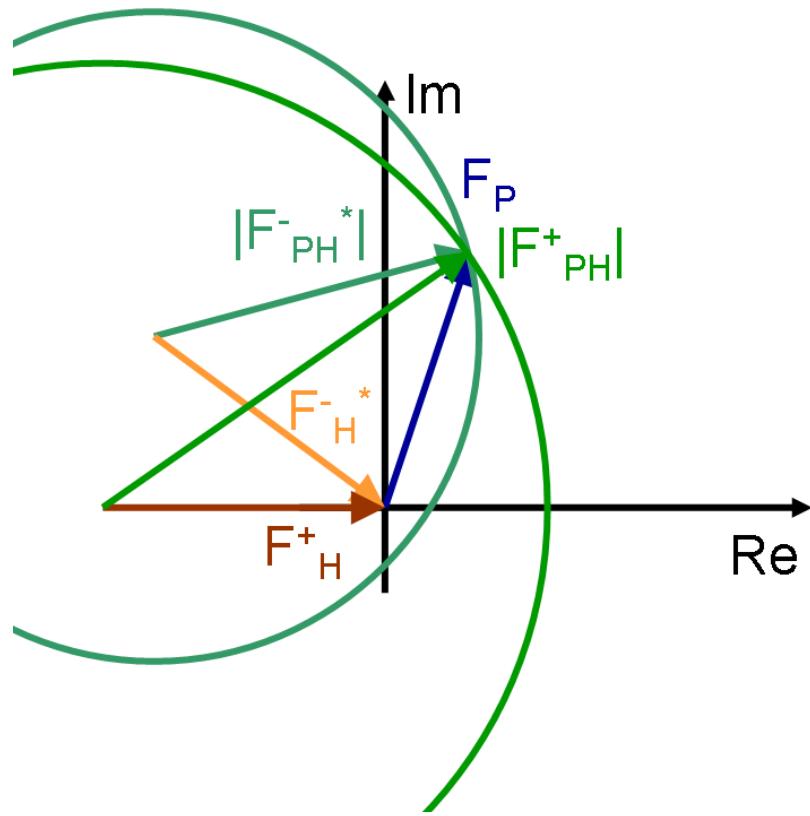
ENERGY SCAN



SAD is a single wavelength data collection (high E remote, peak or inflection)
MAD is a 3 or 4 wavelength data collection



SOLVING THE PHASE PROBLEM IN SAD/MAD



Anomalous differences are smaller than for HA.

However, the great advantage of anomalous phasing is that we can use a single crystal (no need for a native data set).

Seleno-methionine has been the silver bullet for the last two decades

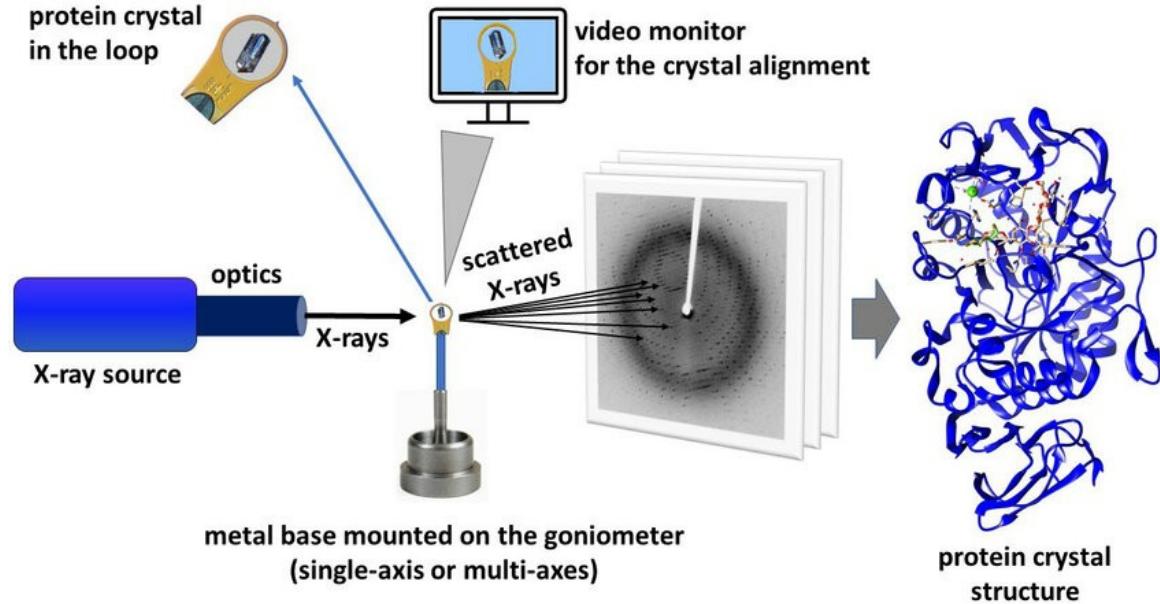
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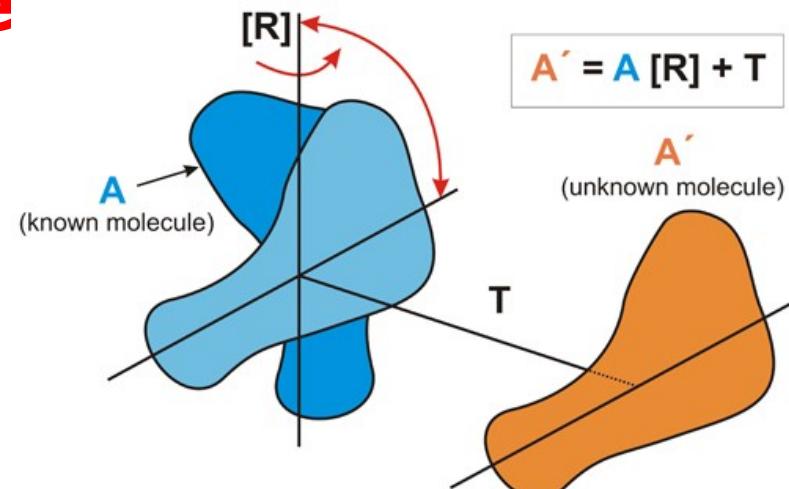
SIR, MIR

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Isomorphous Replacement

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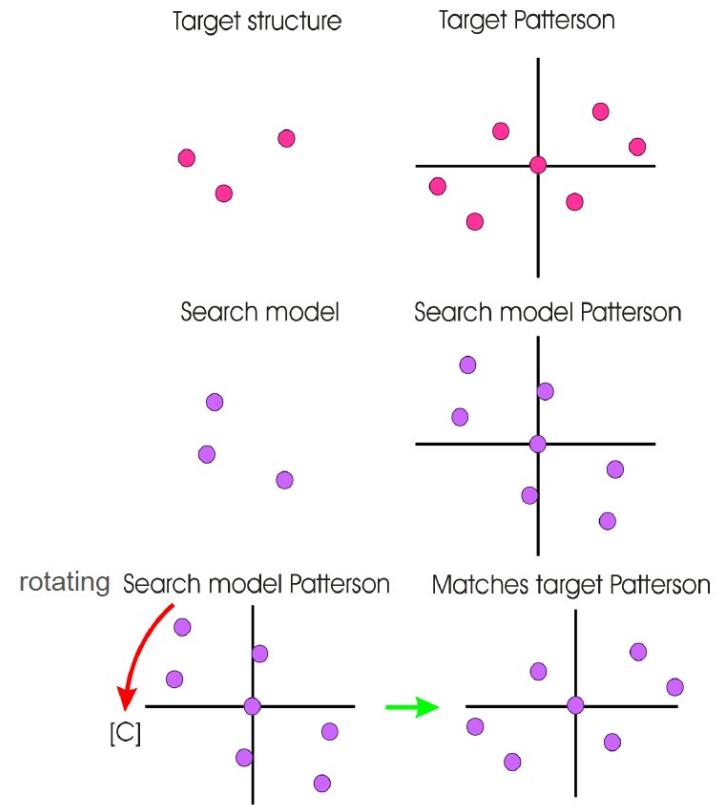


THE ROTATION-TRANSLATION FUNCTION

The Patterson function
(phase zero inverse Fourier):

P

R-factor for the translation function:



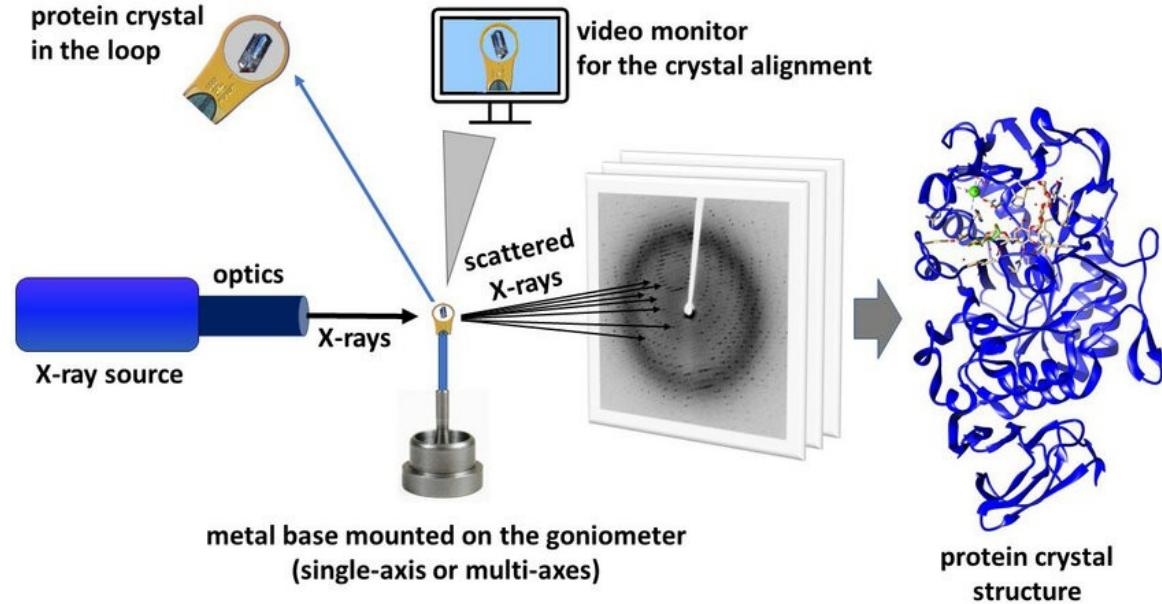
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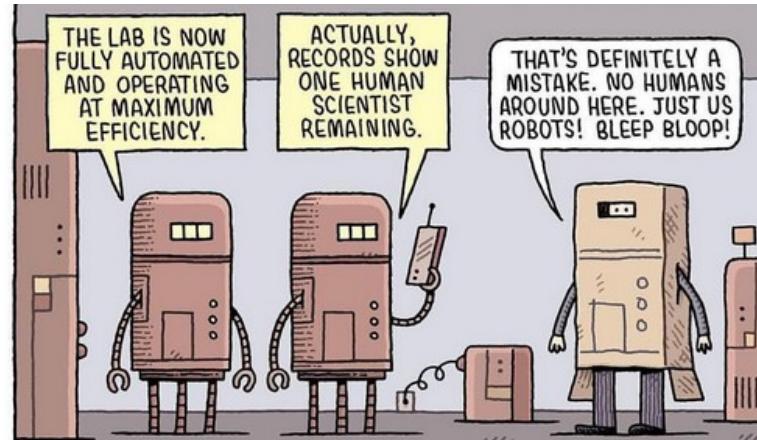
1. *Crystallogenesis*
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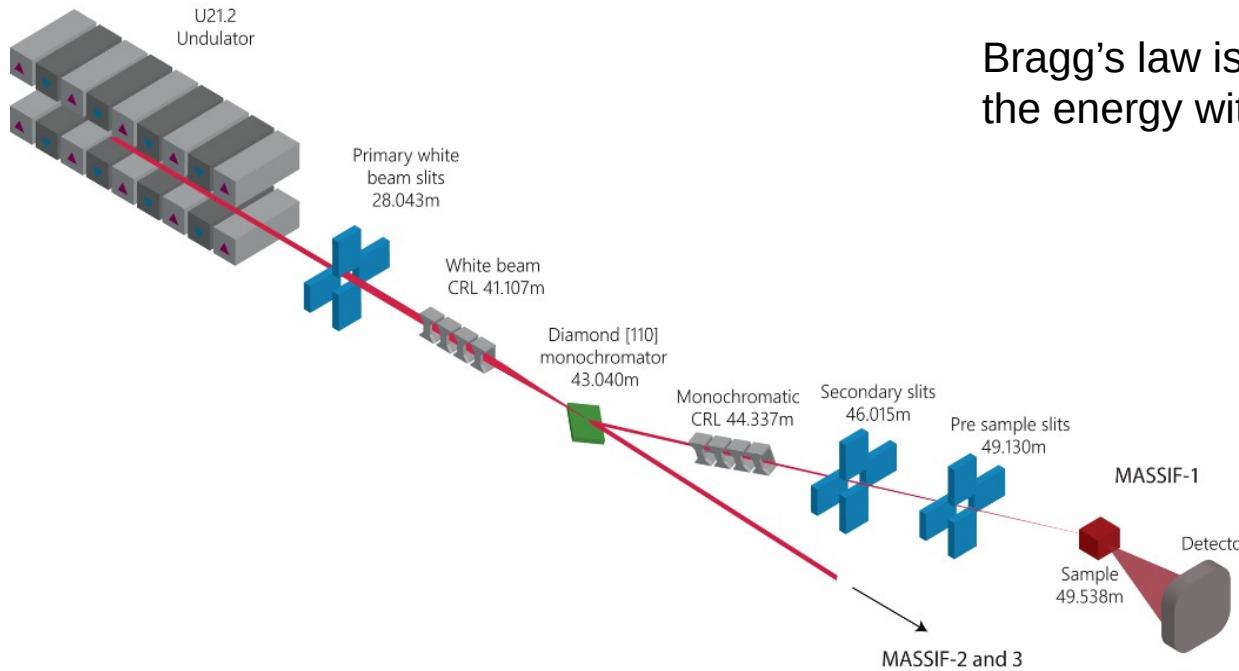
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Automated synchrotron STRUCTURAL BIOLOGY at MASSIF-1



MASSIF-1 LAYOUT

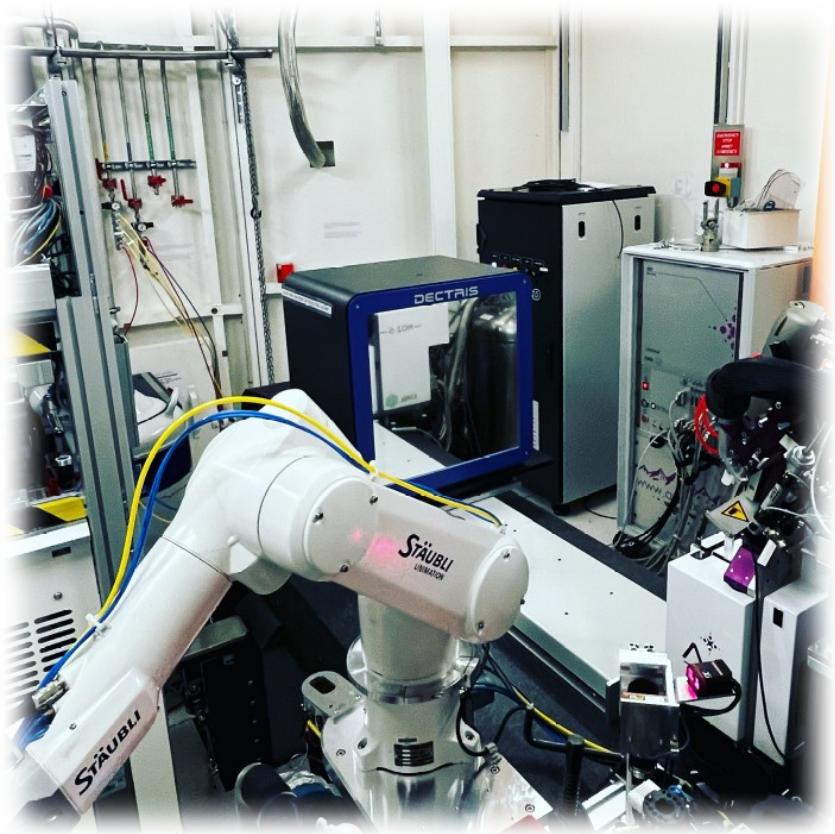


Bragg's law is used also for defining the energy with the monochromator:

$$\lambda$$

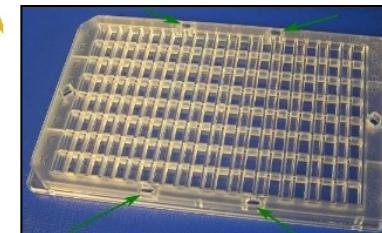
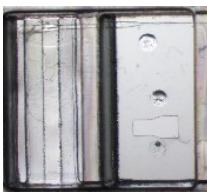
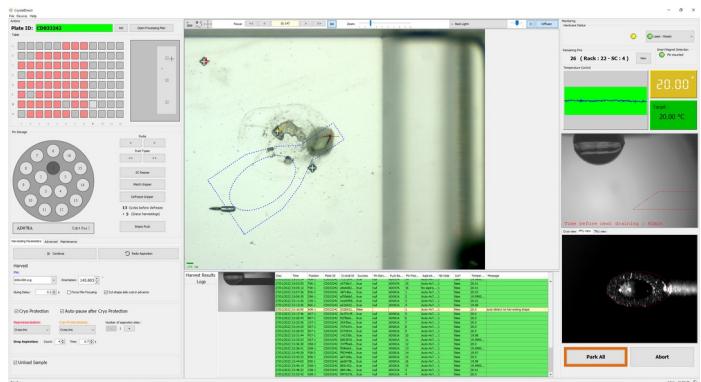
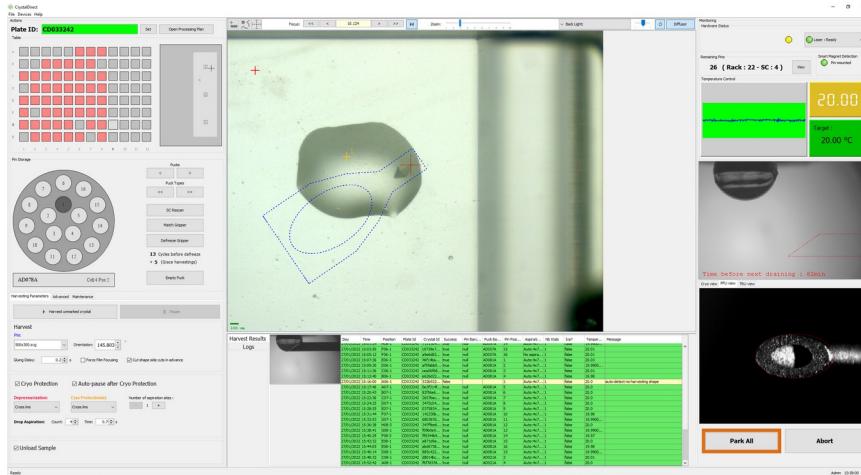
Bowler, MW, Nurizzo, D et al. JSR, Volume 22 | Part 6 | November 2015 | Pages 1540–1547 |

EXPERIMENTAL HUTCH



- Fully autonomous beamline
 - no user control
 - data collection optimized for every sample
- Flexible booking, queuing system
- Fully automated data collection from any sample either room or cryogenic temperatures with complex strategies and optimized parameters for each sample
- **Flex HCD Sample changer – 396 samples capacity**
- **Pilatus3 6M**
- **Arinax MD2S diffractometer with mini-Kappa**
- **CrystalDirect Harvester**

AUTOMATED CRYSTAL HARVESTING



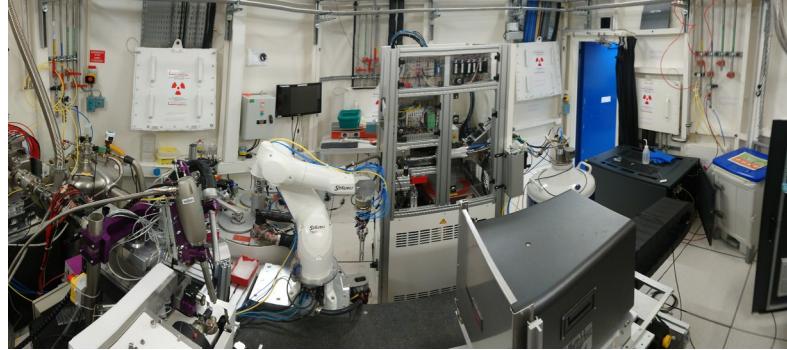
Crystal Direct technology

The European Synchrotron

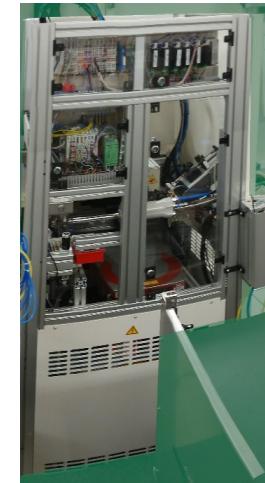
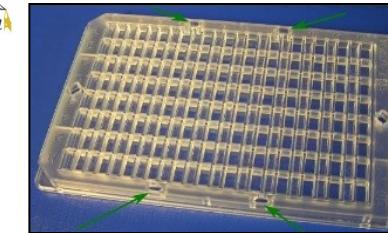
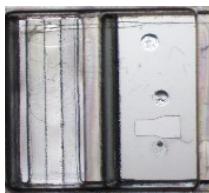


AUTOMATED CRYSTAL HARVESTING

The screenshot shows the CrystalDirect software interface. On the left, there's a grid of small wells and a larger circular well plate diagram. In the center, a crystal image is displayed with a blue dashed line indicating the harvesting area. To the right, a control panel shows 'Harvesting Status' with a progress bar at 26%, a temperature of 20.00 °C, and a target of 20.00 °C. Below these are two smaller images: one of a crystal being harvested and another of a harvested crystal. At the bottom, a 'Harvest Results Log' table lists numerous harvested entries with columns for Date, Time, Position, Plate ID, Crystal ID, Success, PdL No., PdL Plate, Amino N, pH, Salt, and Message.



This screenshot is similar to the one above, showing the CrystalDirect software interface. It includes a well plate diagram, a crystal image with a harvesting area outlined, and a control panel with a progress bar at 26%. The 'Harvest Results Log' table at the bottom contains many harvested entries.



Crystal Direct technology

The European Synchrotron



AUTOMATED CRYSTAL HARVESTING

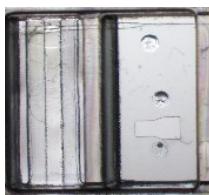
Harvest Results Log

Time	Date	Position	Plate ID	Crystal ID	Status	Pick No.	Pick Date	Aperture	Y0	Z0	Temp	Processor
2024-07-10 10:45:00	2024-07-10	B6	00000000	401	Success	1	2024-07-10 10:45:00	20.00	-0.00	-0.00	20.00	Siemens
2024-07-10 10:45:00	2024-07-10	B6	00000000	402	Success	2	2024-07-10 10:45:00	20.00	-0.00	-0.00	20.00	Siemens
2024-07-10 10:45:00	2024-07-10	B6	00000000	403	Success	3	2024-07-10 10:45:00	20.00	-0.00	-0.00	20.00	Siemens
2024-07-10 10:45:00	2024-07-10	B6	00000000	404	Success	4	2024-07-10 10:45:00	20.00	-0.00	-0.00	20.00	Siemens
2024-07-10 10:45:00	2024-07-10	B6	00000000	405	Success	5	2024-07-10 10:45:00	20.00	-0.00	-0.00	20.00	Siemens
2024-07-10 10:45:00	2024-07-10	B6	00000000	406	Success	6	2024-07-10 10:45:00	20.00	-0.00	-0.00	20.00	Siemens
2024-07-10 10:45:00	2024-07-10	B6	00000000	407	Success	7	2024-07-10 10:45:00	20.00	-0.00	-0.00	20.00	Siemens
2024-07-10 10:45:00	2024-07-10	B6	00000000	408	Success	8	2024-07-10 10:45:00	20.00	-0.00	-0.00	20.00	Siemens
2024-07-10 10:45:00	2024-07-10	B6	00000000	409	Success	9	2024-07-10 10:45:00	20.00	-0.00	-0.00	20.00	Siemens
2024-07-10 10:45:00	2024-07-10	B6	00000000	410	Success	10	2024-07-10 10:45:00	20.00	-0.00	-0.00	20.00	Siemens
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Harvest Results Log

Time	Date	Position	Plate ID	Crystal ID	Status	Pick No.	Pick Date	Aperture	Y0	Z0	Temp	Processor
2024-07-10 10:45:00	2024-07-10	B6	00000000	401	Success	1	2024-07-10 10:45:00	20.00	-0.00	-0.00	20.00	Siemens
2024-07-10 10:45:00	2024-07-10	B6	00000000	402	Success	2	2024-07-10 10:45:00	20.00	-0.00	-0.00	20.00	Siemens
2024-07-10 10:45:00	2024-07-10	B6	00000000	403	Success	3	2024-07-10 10:45:00	20.00	-0.00	-0.00	20.00	Siemens
2024-07-10 10:45:00	2024-07-10	B6	00000000	404	Success	4	2024-07-10 10:45:00	20.00	-0.00	-0.00	20.00	Siemens
2024-07-10 10:45:00	2024-07-10	B6	00000000	405	Success	5	2024-07-10 10:45:00	20.00	-0.00	-0.00	20.00	Siemens
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2024-07-10 10:45:00	2024-07-10	B6	00000000	407	Success	7	2024-07-10 10:45:00	20.00	-0.00	-0.00	20.00	Siemens
2024-07-10 10:45:00	2024-07-10	B6	00000000	408	Success	8	2024-07-10 10:45:00	20.00	-0.00	-0.00	20.00	Siemens
2024-07-10 10:45:00	2024-07-10	B6	00000000	409	Success	9	2024-07-10 10:45:00	20.00	-0.00	-0.00	20.00	Siemens
2024-07-10 10:45:00	2024-07-10	B6	00000000	410	Success	10	2024-07-10 10:45:00	20.00	-0.00	-0.00	20.00	Siemens



MiTegen



Crystal Direct technology

The European Synchrotron



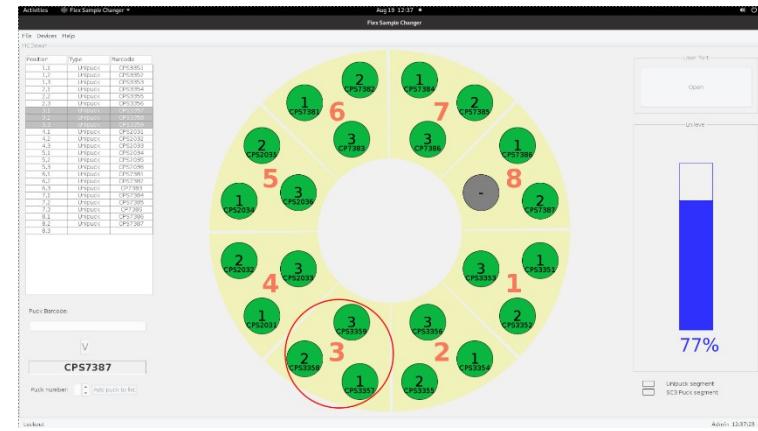
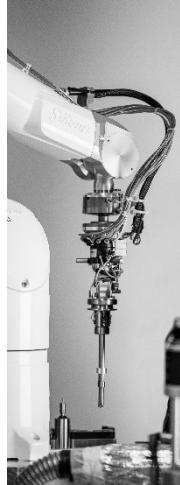
COURIER DELIVERY

Dry shippers are delivered daily at the beamline as part of our queuing system

Delivery is free of charge for Academic Users



CRYSTAL TRANSFER



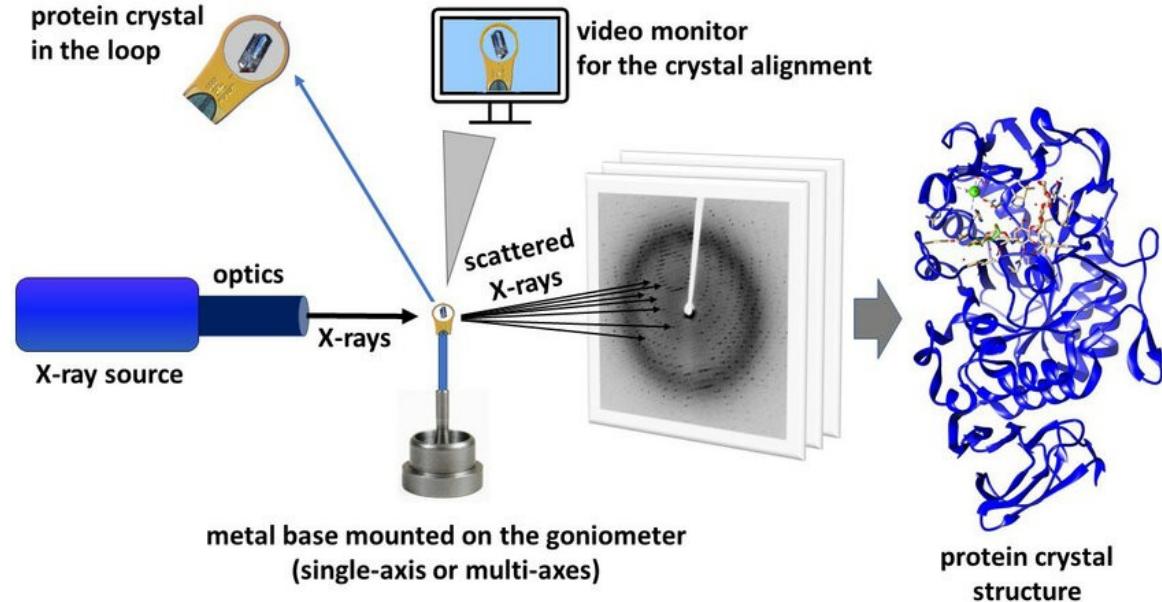
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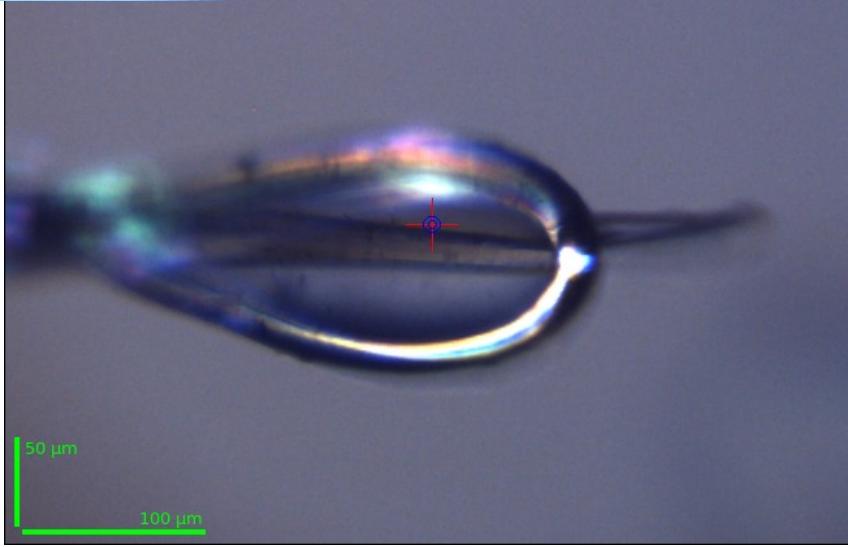
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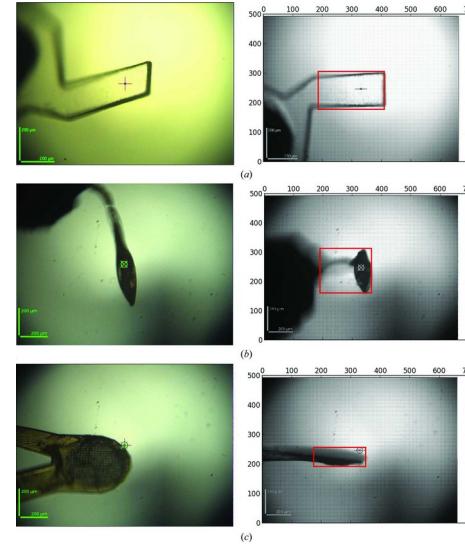
6. *Crystal harvesting*
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OPTICAL LOOP ALIGNMENT



No restrictions on
the mounting
system

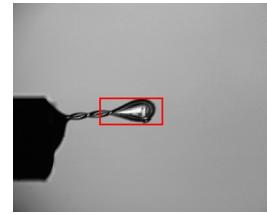
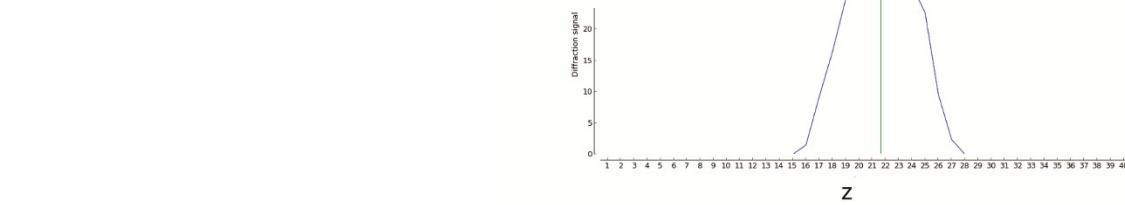
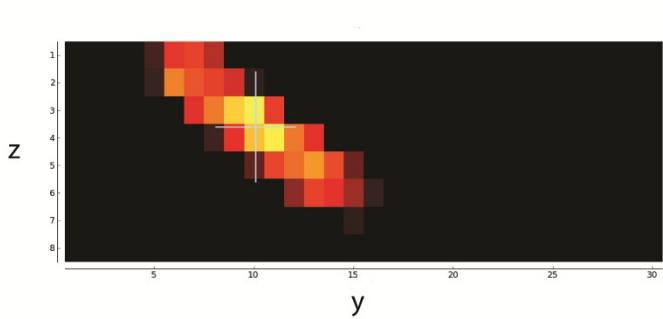
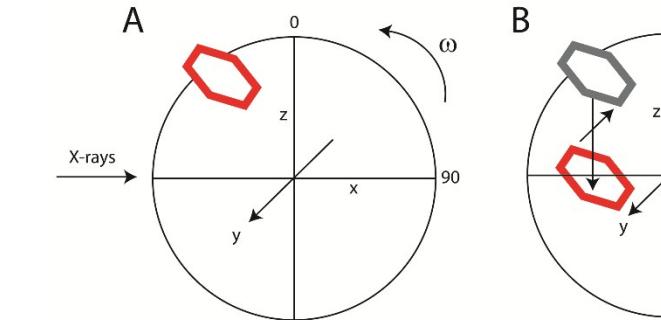


Optical defects
might be
disastrous



Svensson, O., Malbet-Monaco, S., Popov, A., Nurizzo, D. & Bowler, M. W. (2015). Acta Cryst. D71, 1757-1767.

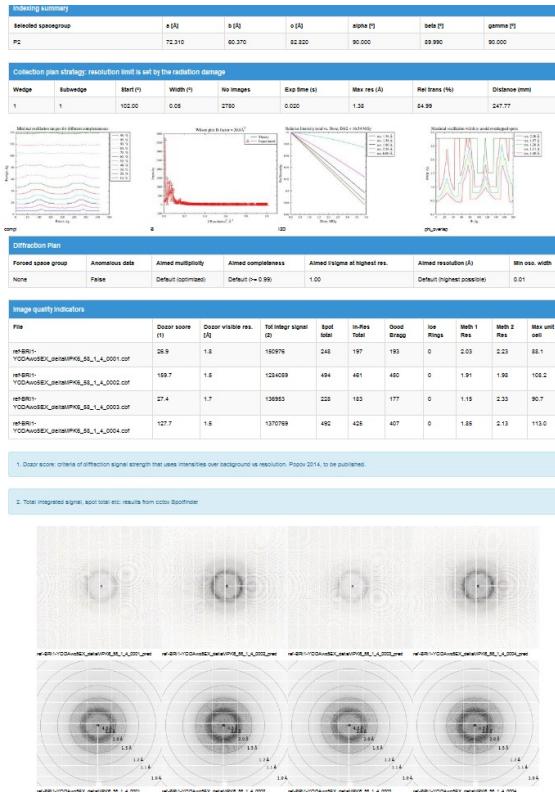
X-RAY ALIGNMENT



The centering table fitted on the ω axis brings the sample at the center of the camera and in the X-ray beam

Characteristics such as beam size and flux as well as crystal volume lead to highly optimised data collection

CHARACTERIZATION



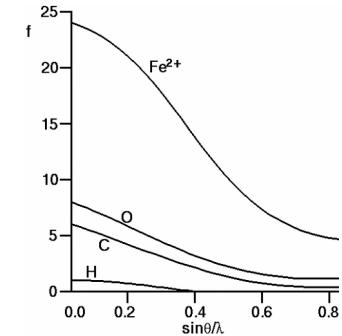
Cell parameters $a, b, c, \alpha, \beta, \gamma$

Point group (Bravais type)

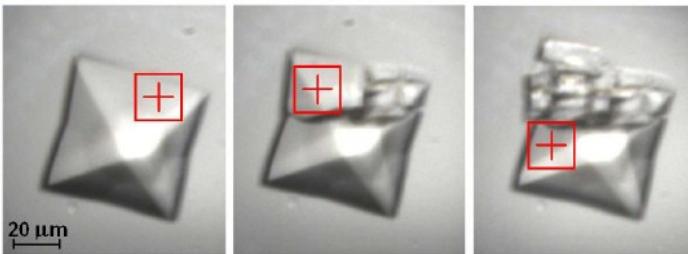
The total rotation angle to collect the entire reciprocal space

The expected resolution according to the crystal size and beam size

Check the quality of X-ray centering (feedback loop)



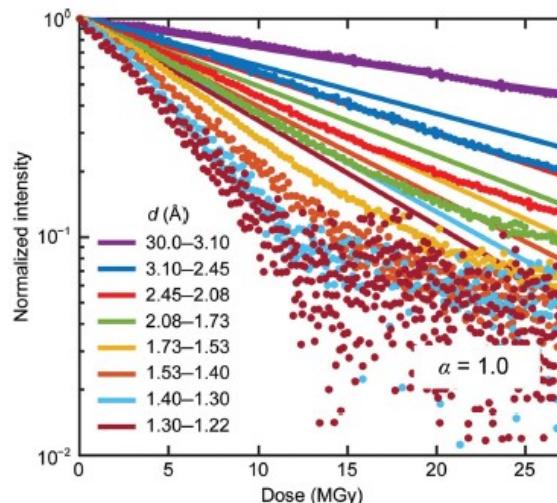
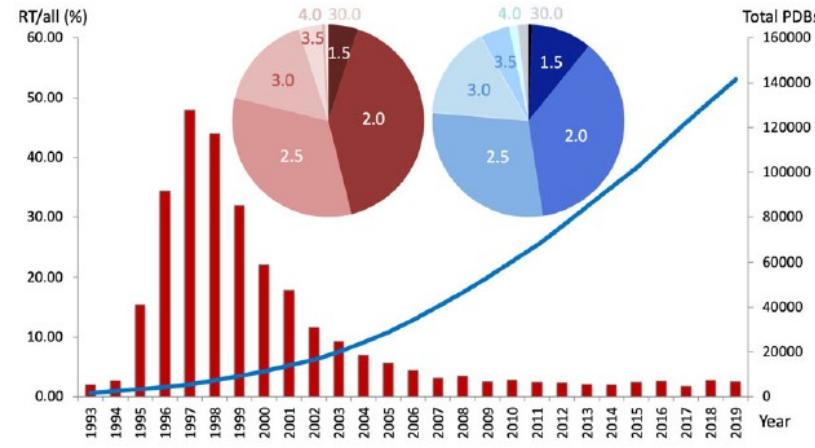
DC STRATEGY – RADIATION DAMAGE



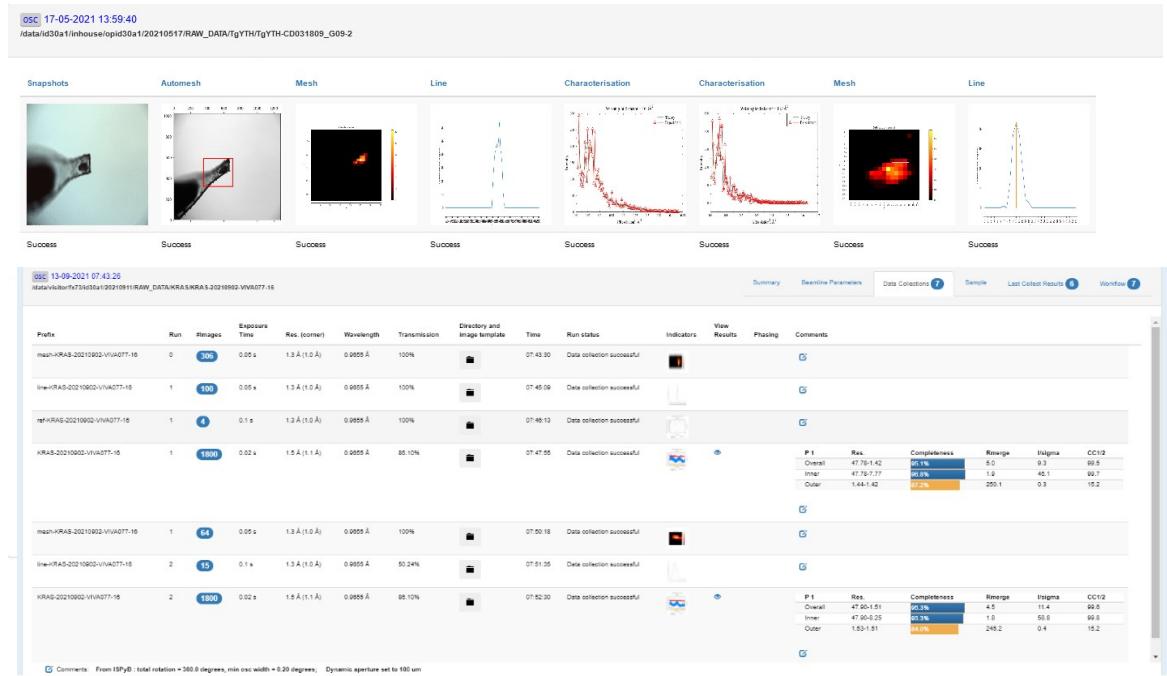
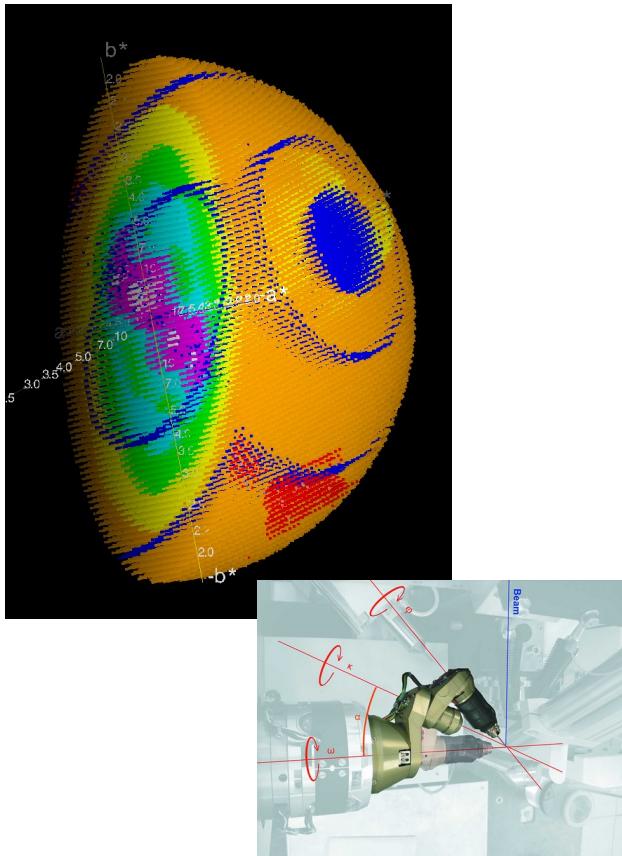
DC is mainly done (>90%) at cryo-temperature

RD is visible even at cryo-temperature

Exposure time / transmission is adjusted to collect a **complete** data set without **theoretical RD** (Henderson limit = 20MGy)



CUSP IN P1



In triclinic and monoclinic SG some volume of reciprocal space is not accessible with a rotation around a single axis (mini- κ)

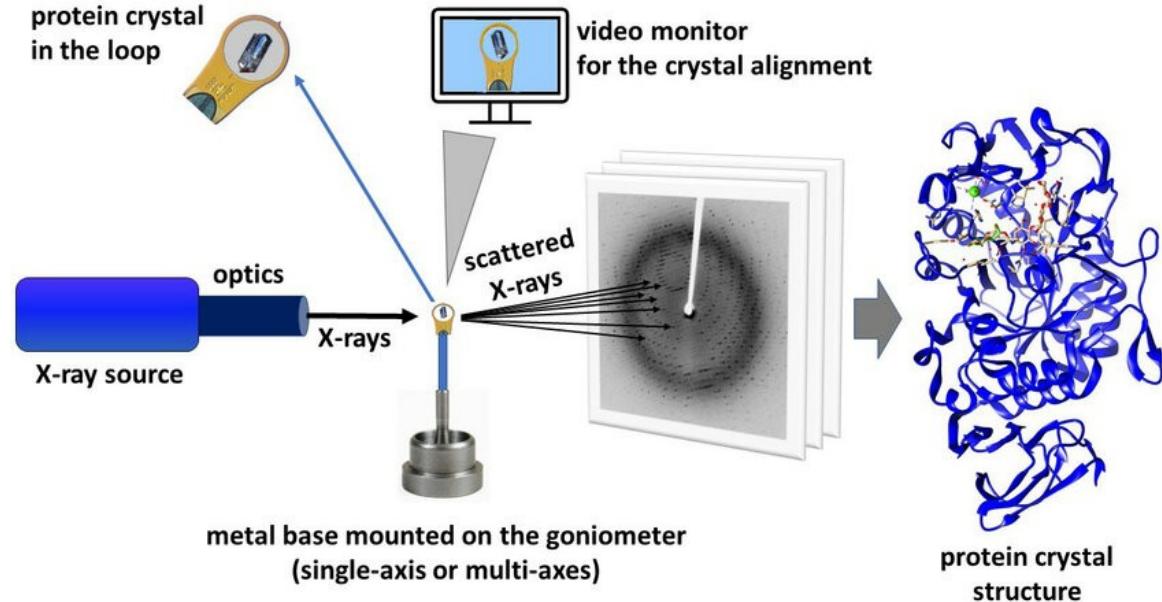
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Theory

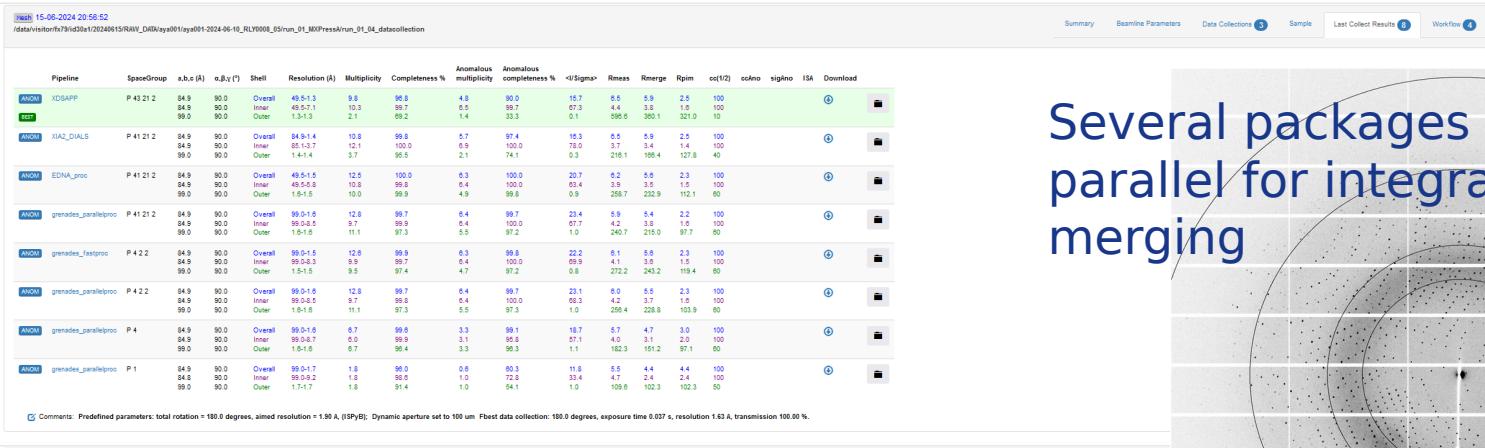
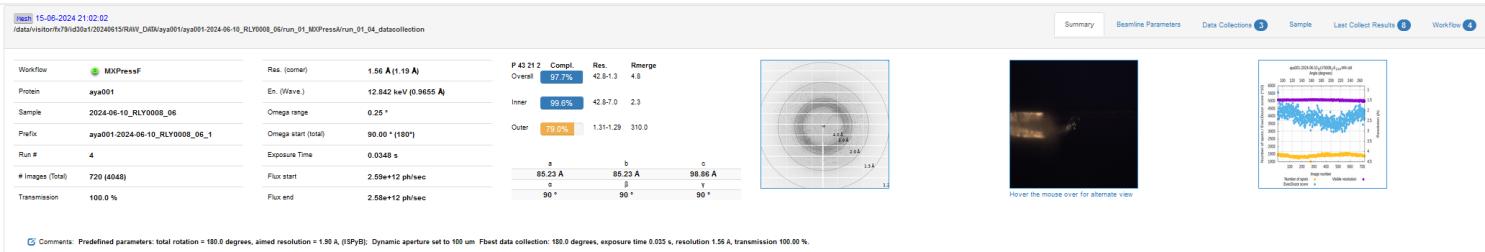
1. *Crystallogenesis*
2. Crystal symmetries
3. *X-rays*
4. *Diffraction*
5. *Phase problem*

Practice

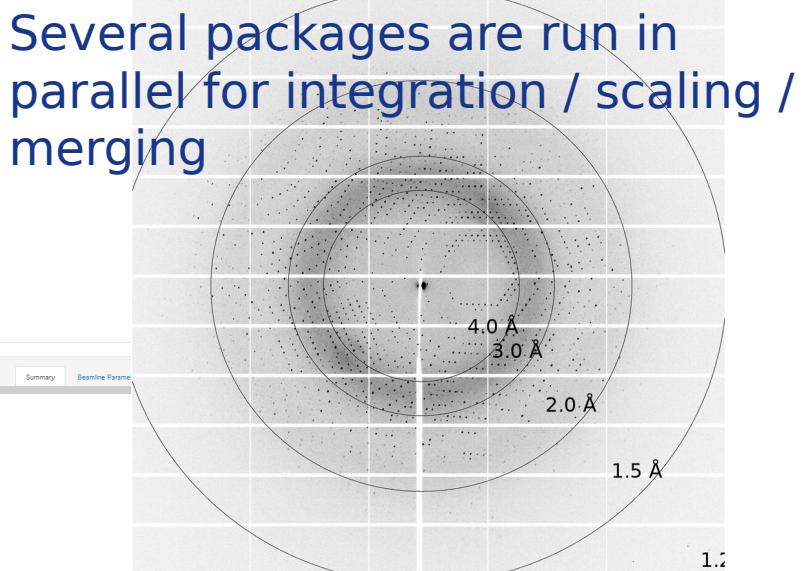
6. *Crystal harvesting*
7. *Data collection*
8. *Data processing*
9. *Examples*



DATA PROCESSING



Recd: 15-06-2024 20:51:45
 /data/visitor/rf79/d301/20240615/Raw_Diff/aya001/aya001-2024-06-10_RLY0008_04/run_01_MXPress/run_01_04_datacollection



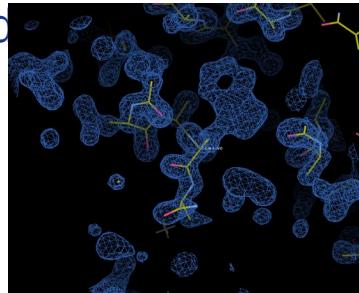
SOLVING THE PHASE PROBLEM

SAD

look for anomalous signal
comparing $F(hkl)$ and $F(-h-k-l)$ in
XDS

Find the heavy atom site(s) with
SHELXD

Run density modification (NCS,
solvent flattening, histogram
matching) in both hands

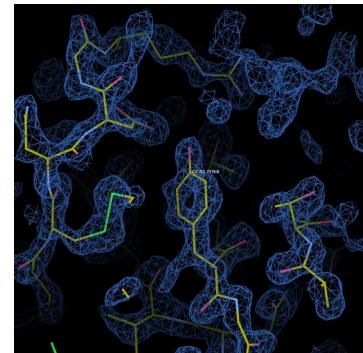


MR

look for a model in the PDB with
same cell or use the model
provided by the user

Run the molecular replacement
(Rotation and translation function)

Refine the MR model



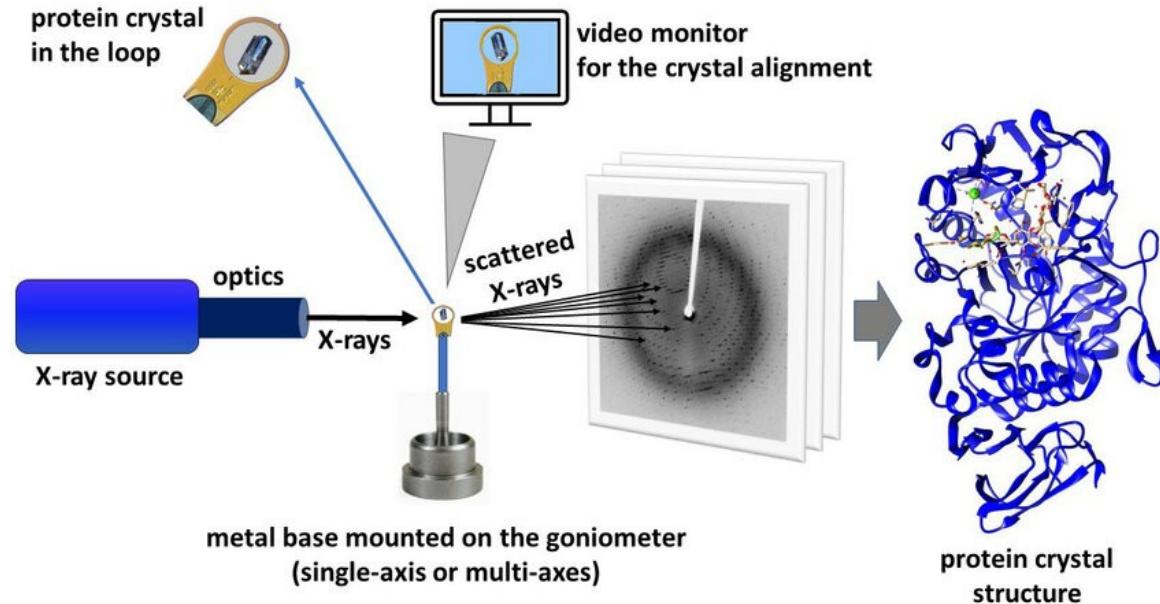
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Theory

1. *Crystallogenesis*
2. Crystal symmetries
3. *X-rays*
4. *Diffraction*
5. *Phase problem*

Practice

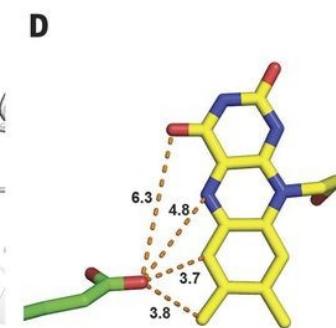
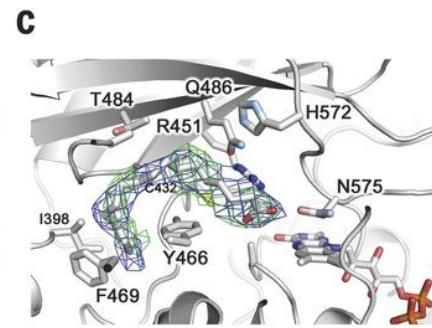
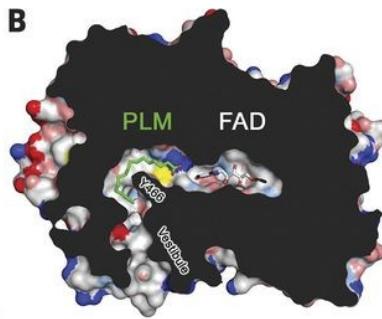
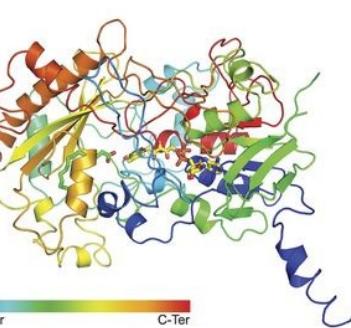
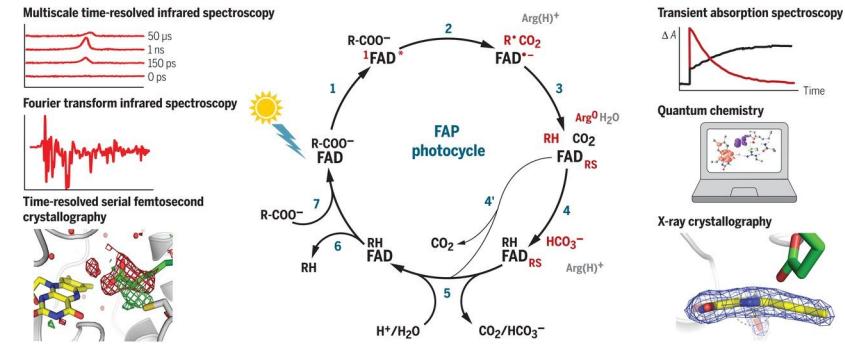
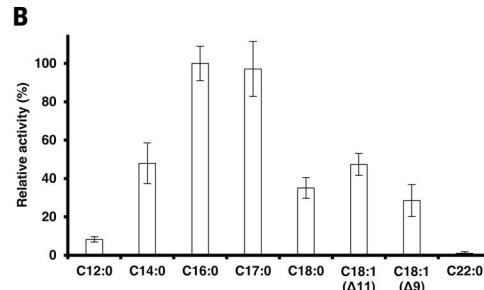
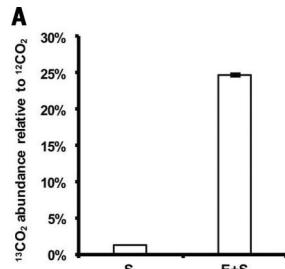
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9. *Examples*



DESIGN OF MEMBRANE PROTEINS ANALOGUES

Computational design of soluble and functional membrane protein analogues. Casper et al. Nature DOI: 10.1038/s41586-024-07601-y

FATTY ACID PHOTODECARBOXYLASE



An algal photoenzyme converts fatty acids to hydrocarbons. Sorrigué et al. Science. DOI: 10.1126/science.aan6349

During a protein crystallography experiments, most of the X-ray photons that interact with the sample...

- a. damage the sample, and only a small part contributes to the diffraction pattern
- b. contribute to the diffraction pattern, and only a small part damages the sample
- c. cause fluorescence in the sample

How can synchrotron radiation be advantageous for protein crystallography studies?

- a. Because of its high level of automation
- b. Because of its high intensity
- c. Because of its high stability

Why do we collect diffraction data at 100K?

- a. Crystal quality is higher at 100K than at room temperature
- b. To reduce the size of the cell
- c. To reduce radiation damage
- d. Crystals are easier to carry at 100K

Why proteins crystalize only in 65 space groups out of the 230?

- a. Because of the chirality of the amino-acid C α
- b. Because their molecular weight being too high
- c. Because of the water molecules surrounding the protein in the mother liquor

What is mathematical relation between the electron density and the amplitudes?

- a. A linear regression
- b. A Fourier transform
- c. The square root