## NONLINEAR TIME-SERIES ANALYSIS FOR HUMAN-ROBOT MOVEMENT VARIABILITY TO HUMAN-ROBOT INTERACTION

by

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