



# A Nonlinear Dynamics Approach to Human Activity Recognition Using Inertial Sensors

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Internal Research Conference Presentation  
EECE School  
10th March 2015

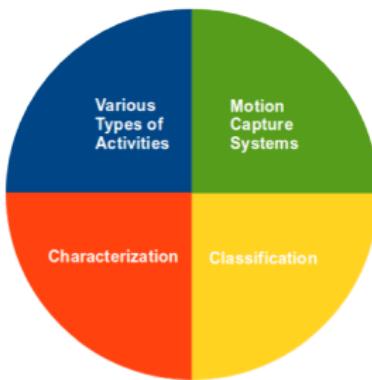


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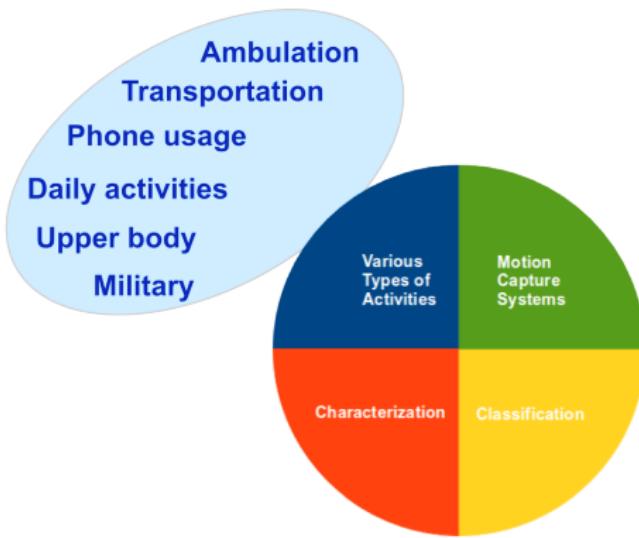


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BIRMINGHAM

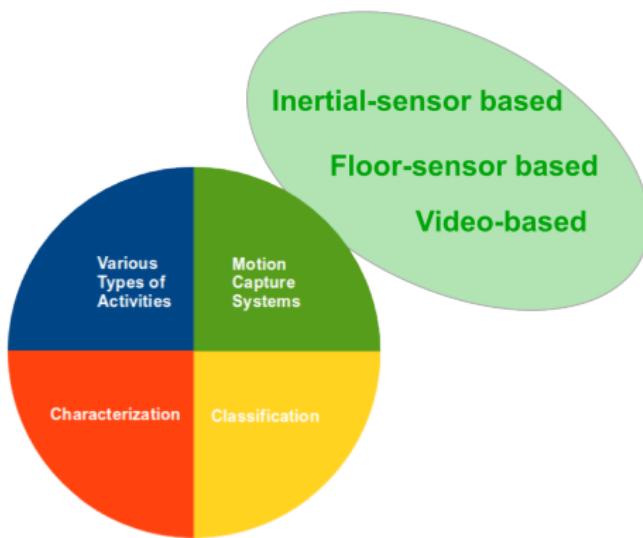
# Why is HAR a challenging task?



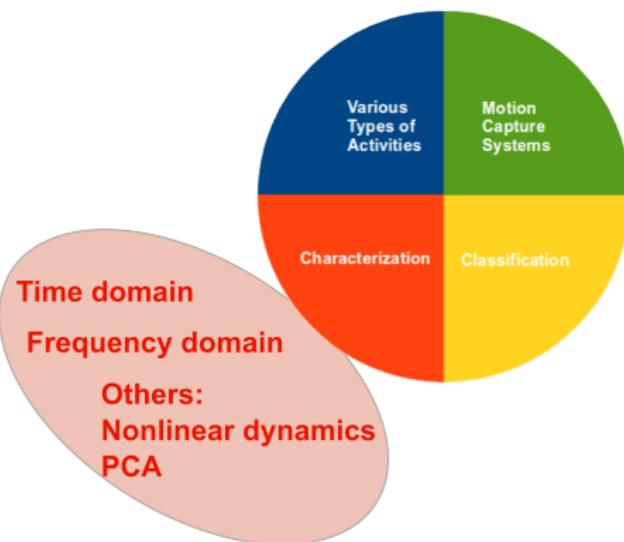
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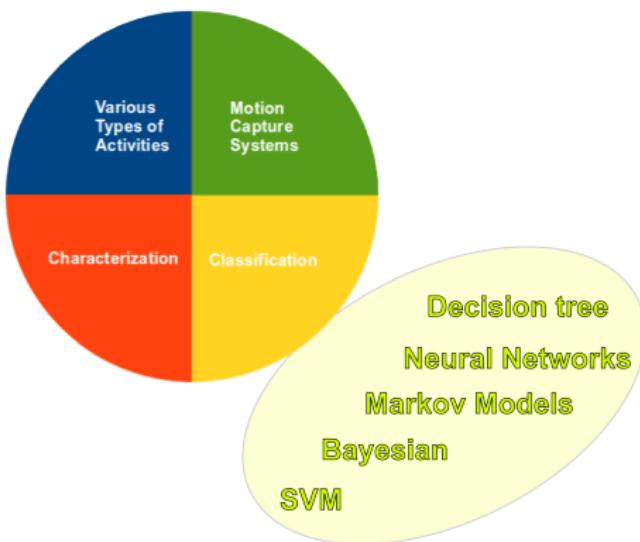
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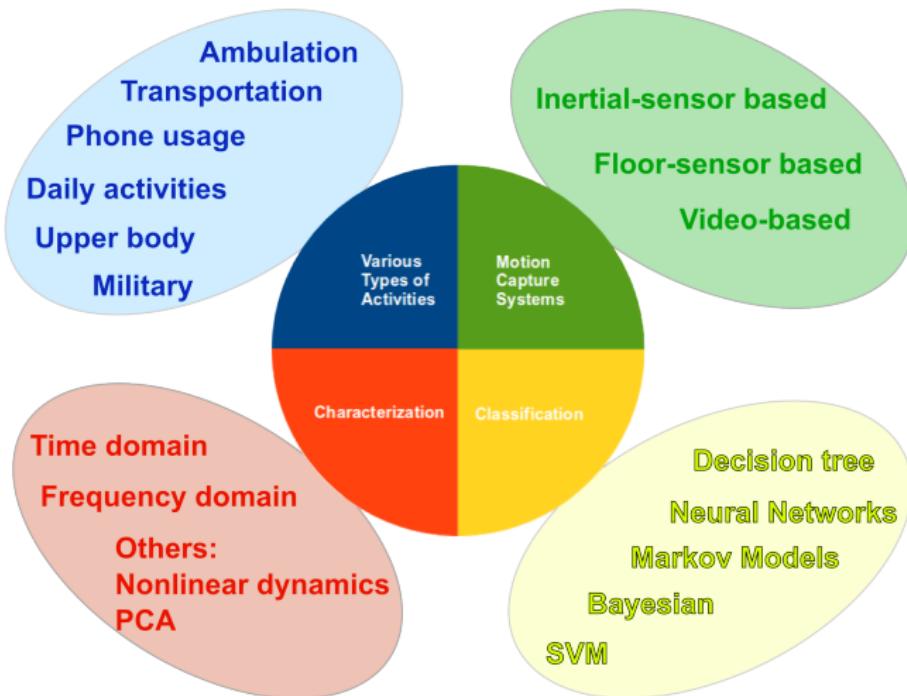
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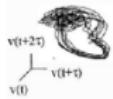
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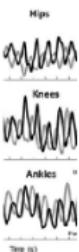
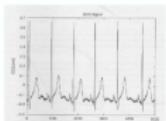
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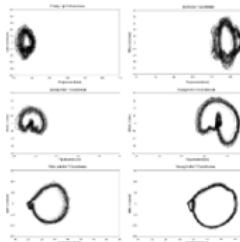
# Study of electrophysiological time series



Korn et al (2003)

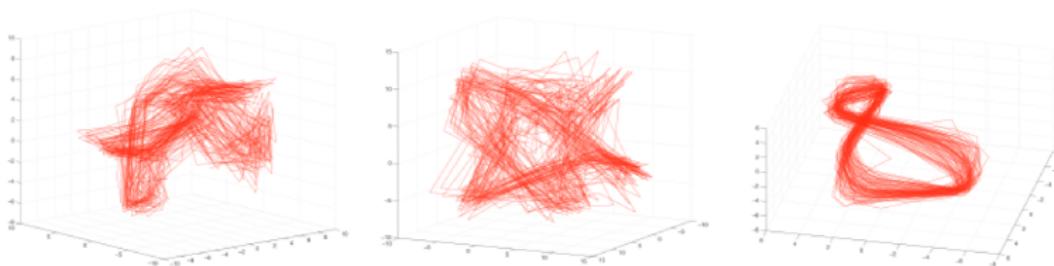


Fojt et al (1998)



Buzzi et al (2013)

# Time Series Classification

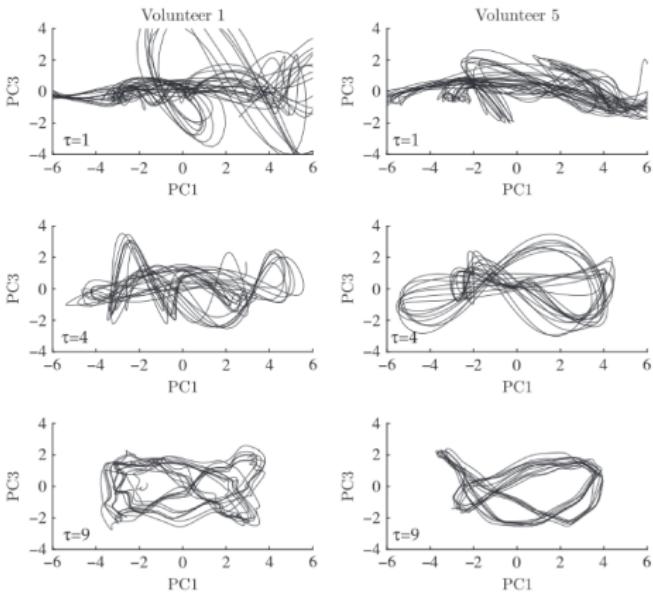


**Jordan et al (2013)**

Reconstructed state spaces for walking (left), running (middle), and biking (right) from noisy accelerometer data.



# Gait Identification



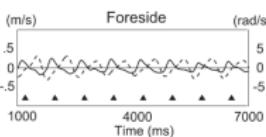
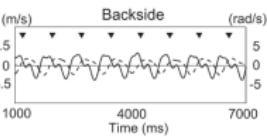
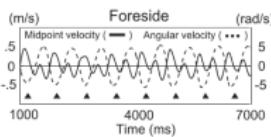
**Sama et al (2013)**

Reconstruction of the trajectory of the first and third PC for two individuals.

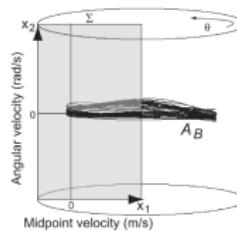
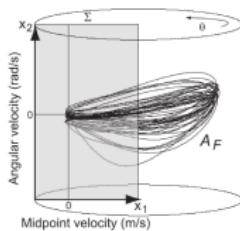
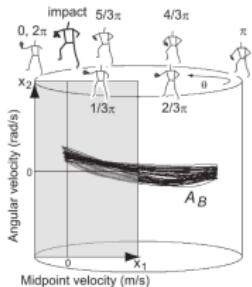
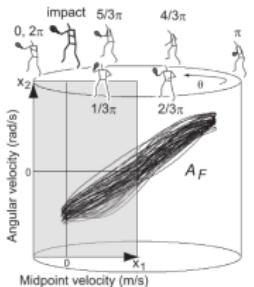
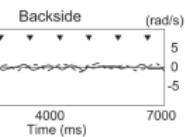


# Dexterity of Tennis Players

Expert #5



Novice #4



**Suzuki et al (2013)**

Time series and hyper-cylindrical phase space from Expert #5 and Novice #4.

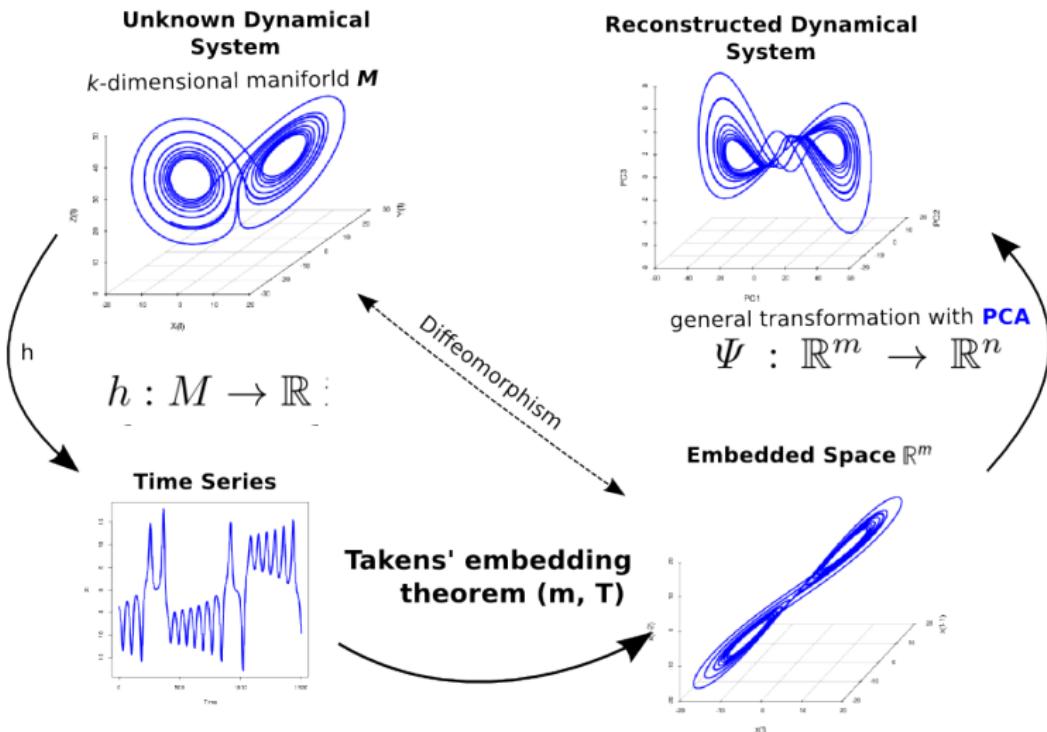


# Research Questions

- How the reconstructed state space can quantify the dexterity of human body activities?
- Is the Takens's Theorem the best tool to quantify Human Activities in terms of the reconstruct the state space?
- Which concepts from nonlinear dynamics can be used to characterize human body activities?



# The Reconstructed State Space



# Takens' Theorem (1981)

According to Takens' Theorem, the reconstructed state space in  $m$  **embedding dimension** with  $\tau$  **embedding delay** of the original system is given by

$$\overline{x(t)} = (x(t), x(t - \tau), x(t - 2\tau), \dots, x(t - (m - 1)\tau)).$$

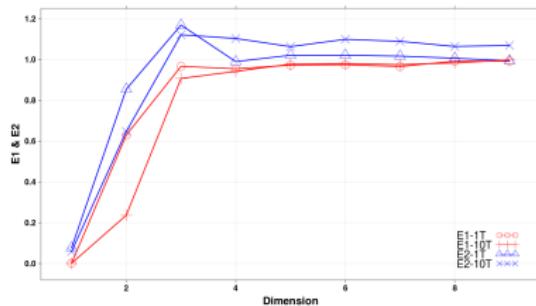
Takens' Theorem, also known as time-delay embeddings method, states that for a large enough  $m$  to unfold the attractor and  $\tau > 0$  chosen to maximize the information content of  $x(t)$ , this method provides a one-to-one reconstruction of the true dimension  $k$  system ( $\mathbb{R}^k$ ).



# Minimum embedding parameters

**Cao (1997)** proposed a method based on the false neighbor method to determine the minimum embedding dimension from time-series based on Taken's theorem.

**Fraser et al (1985)** used the mutual information method for the choice of the delay embedding.

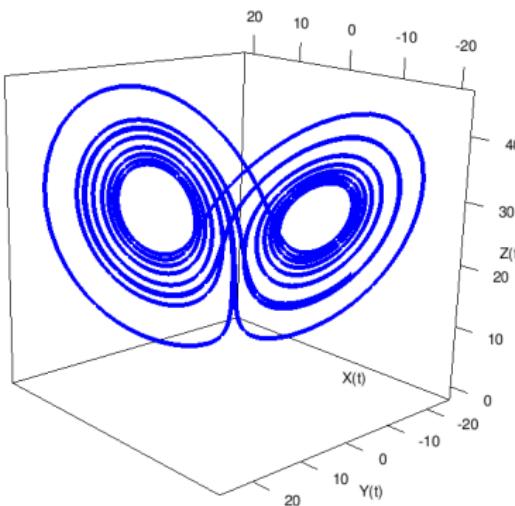


The values E1 and E2 from Lorenz attractor **Cao (1997)**

# Time-Delay Embedding Example

Lorenz System

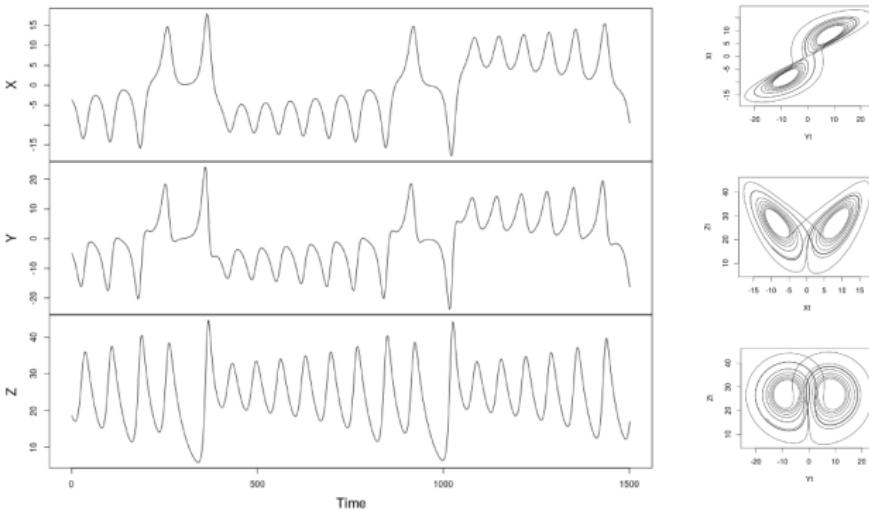
$$\begin{aligned}\frac{dx}{dt} &= \sigma(x - y), \\ \frac{dy}{dt} &= x(\rho - z) - y, \\ \frac{dz}{dt} &= xy - \beta z.\end{aligned}$$



**Figure:**  $\sigma = 10$ ,  $\rho = 28$  and  $\beta = 3/8$



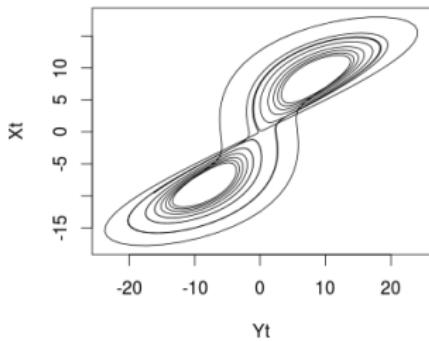
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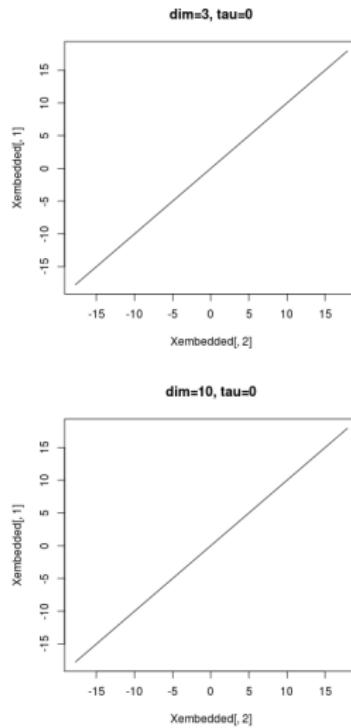
**Figure:** Time series of the Lorenz System and 2D manifolds



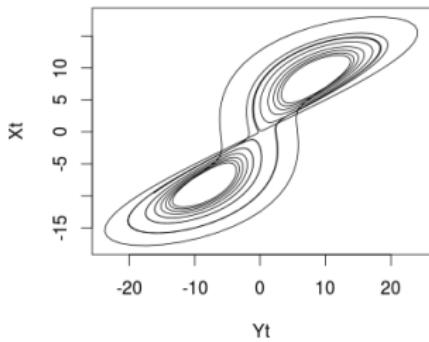
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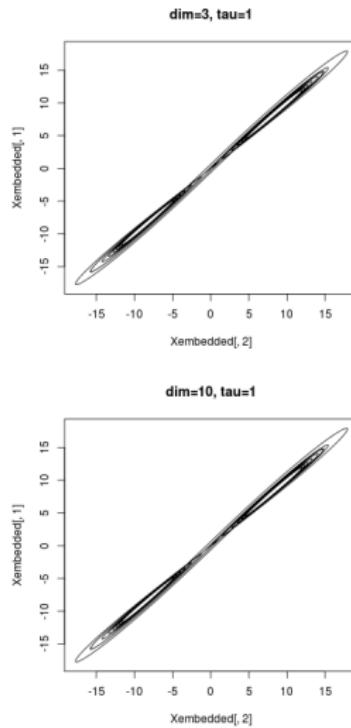
**Figure:** Original Manifold



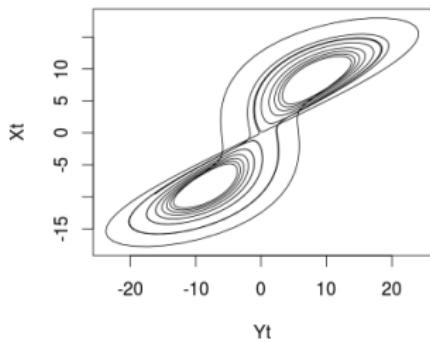
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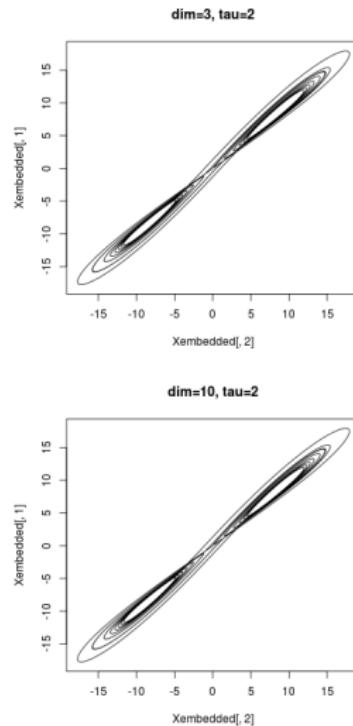
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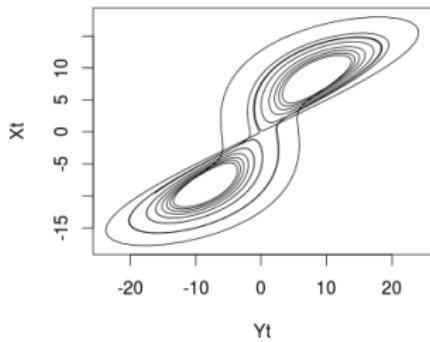
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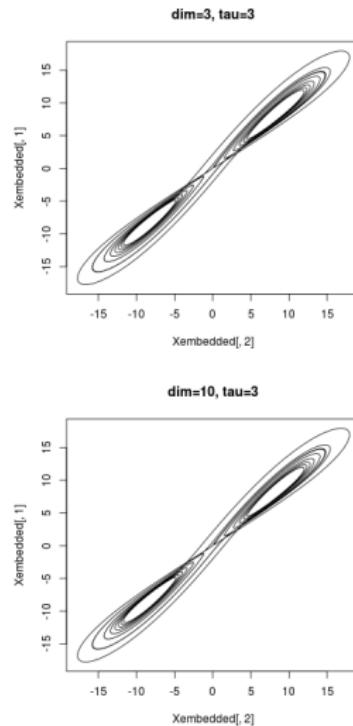
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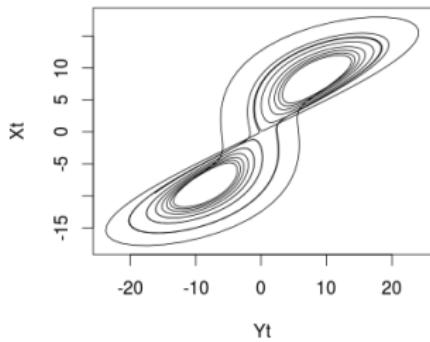
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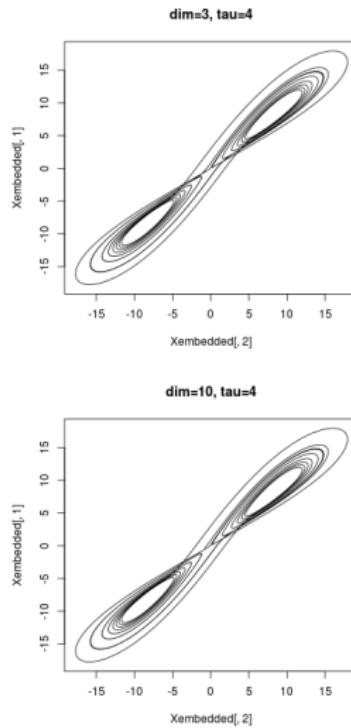
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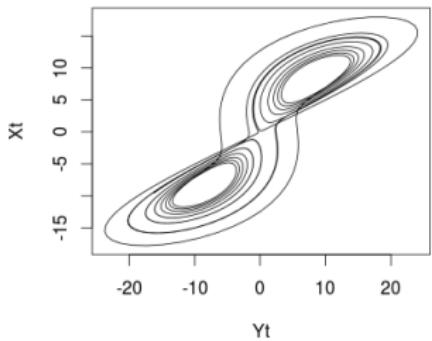
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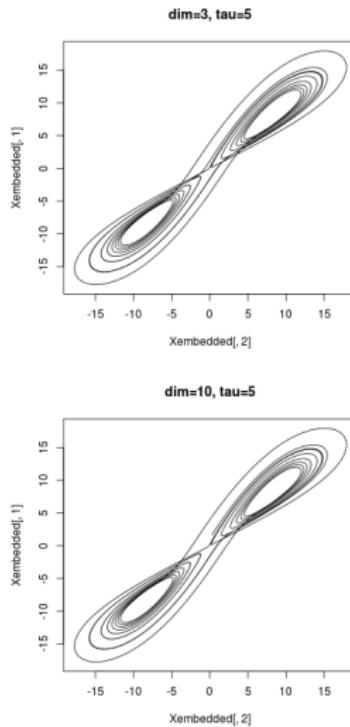
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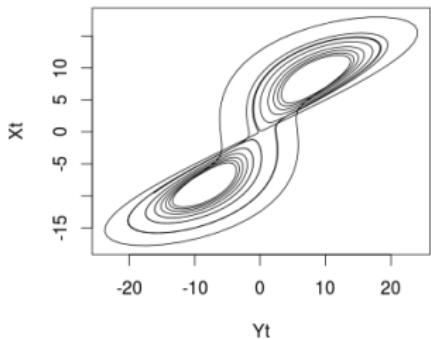
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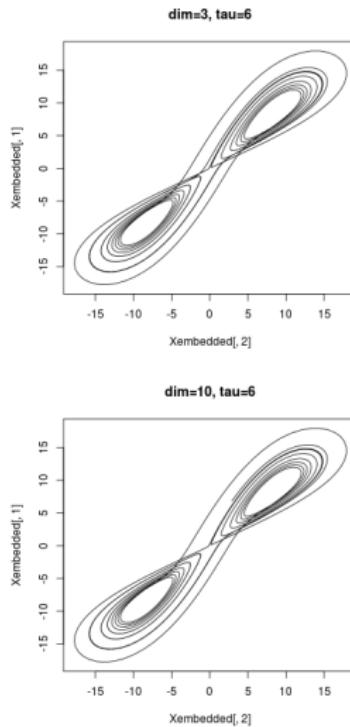
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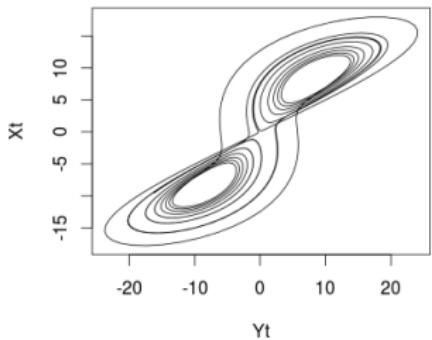
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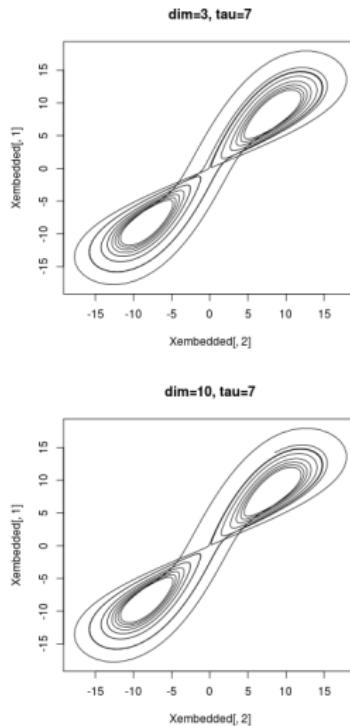
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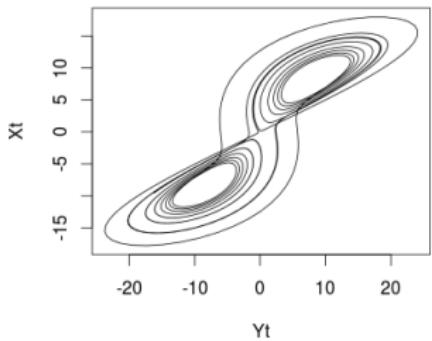
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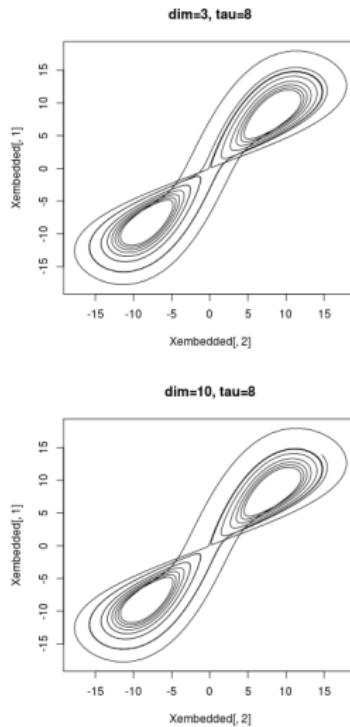
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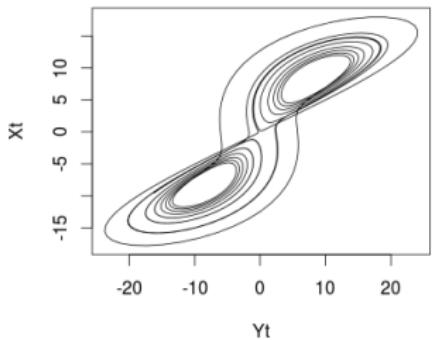
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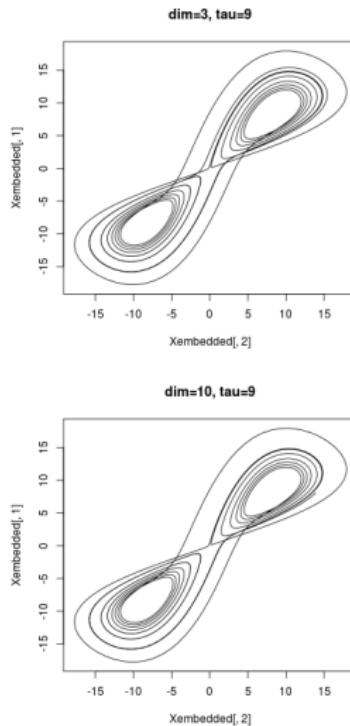
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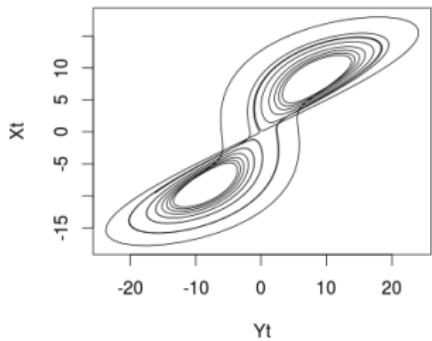
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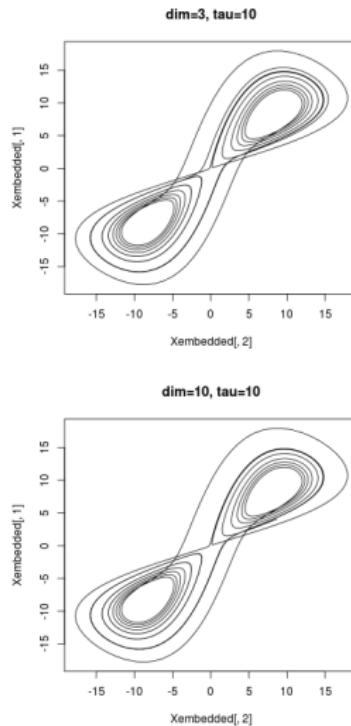
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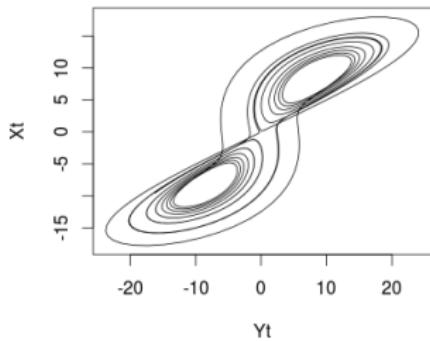
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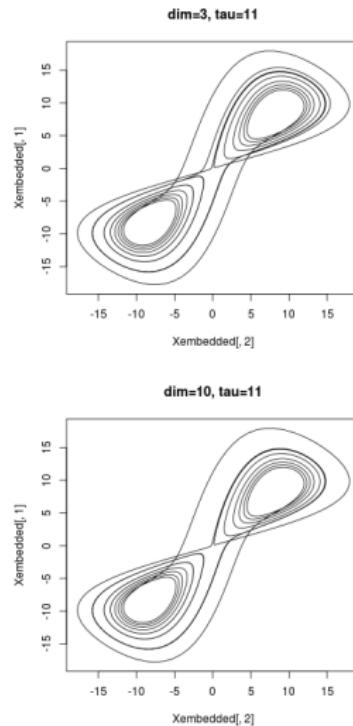
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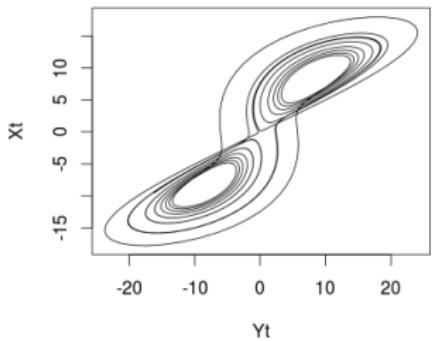
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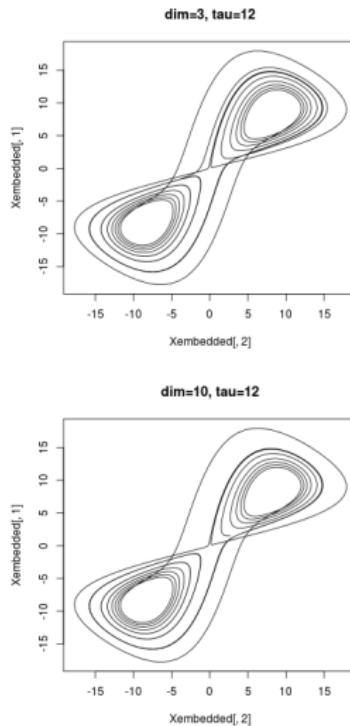
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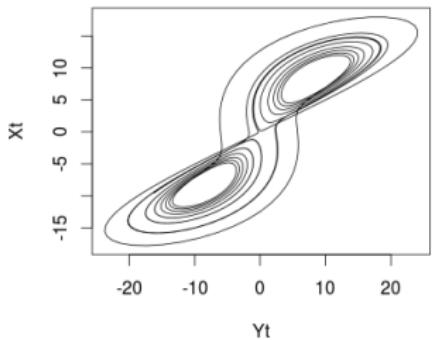
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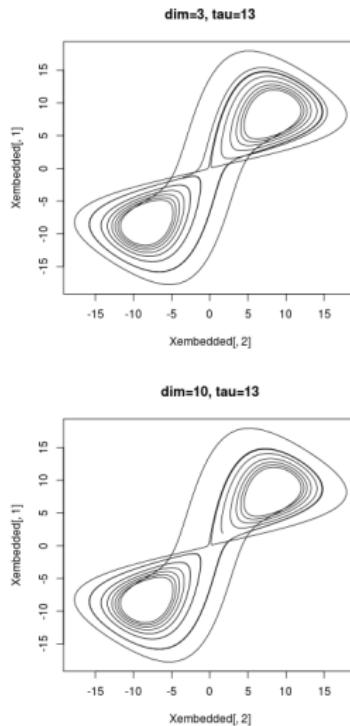
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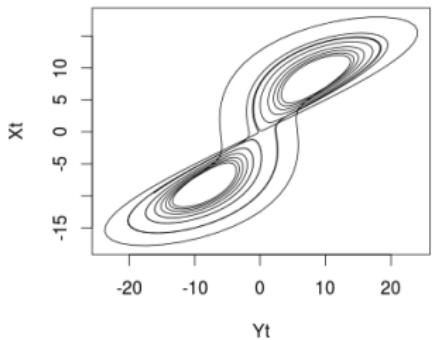
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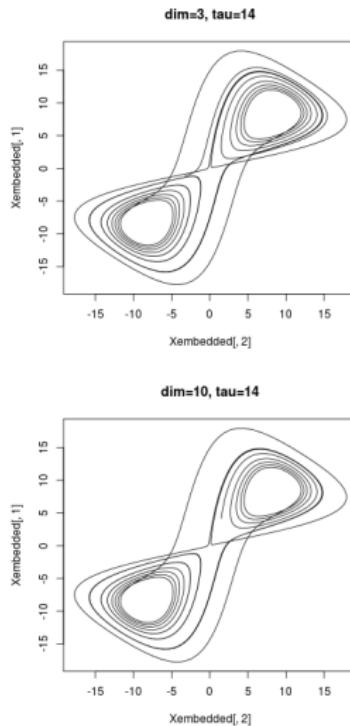
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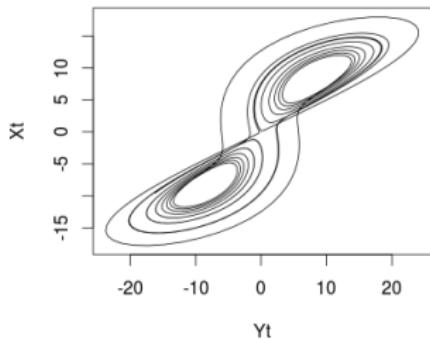
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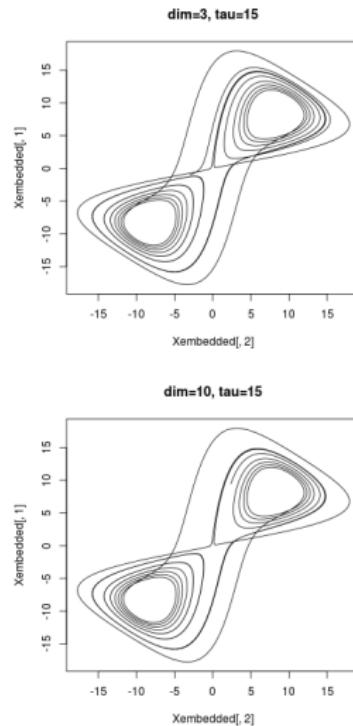
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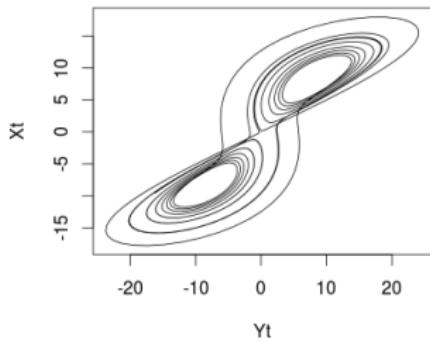
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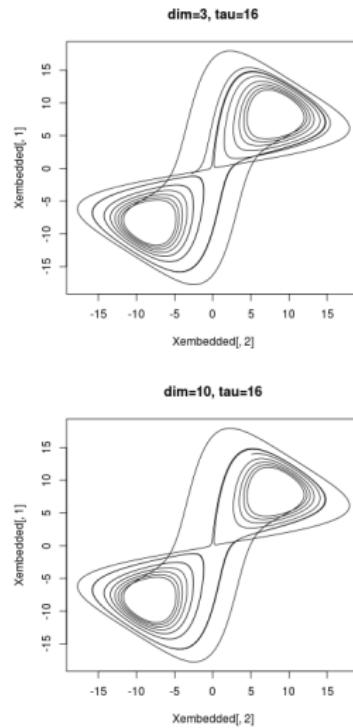
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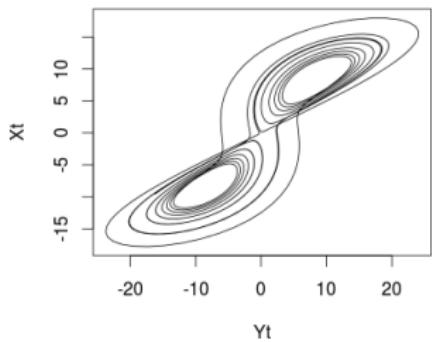
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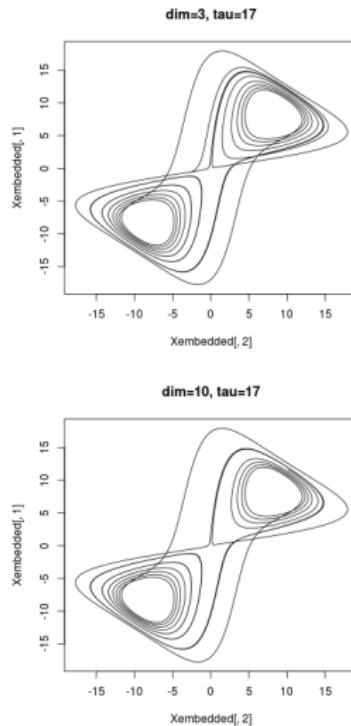
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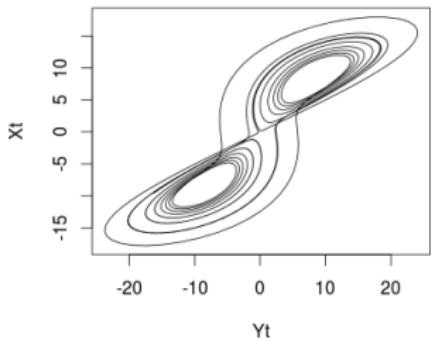
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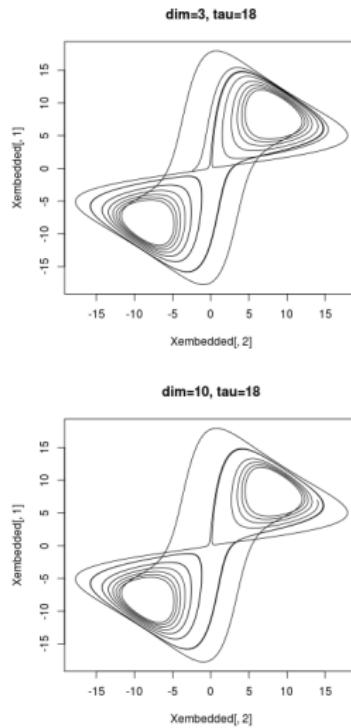
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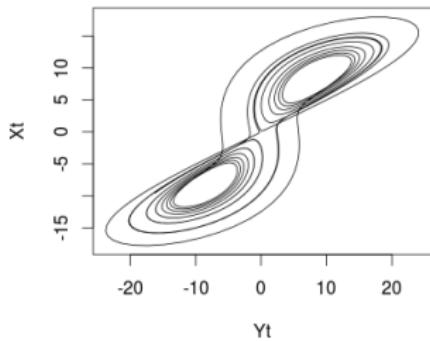
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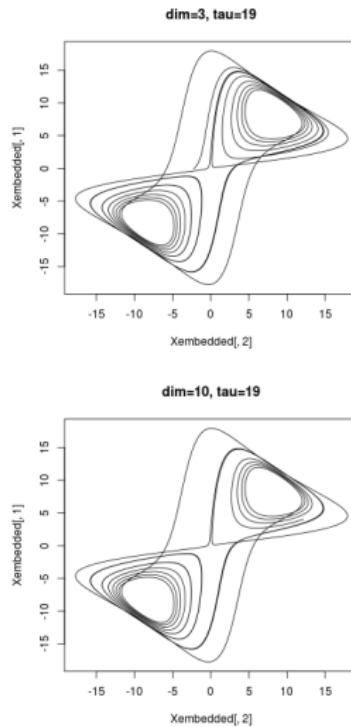
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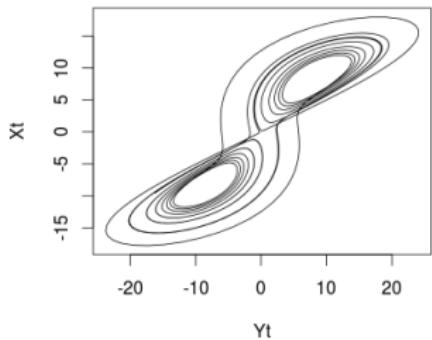
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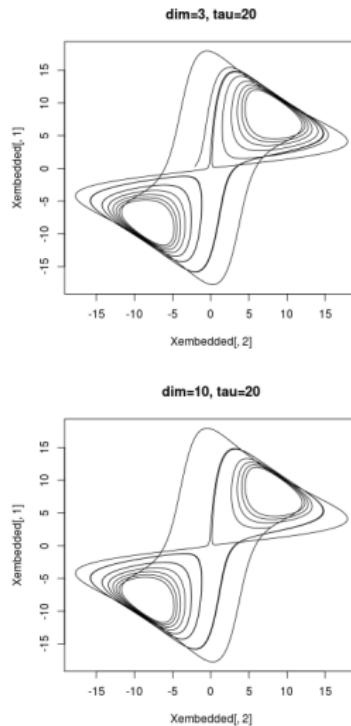
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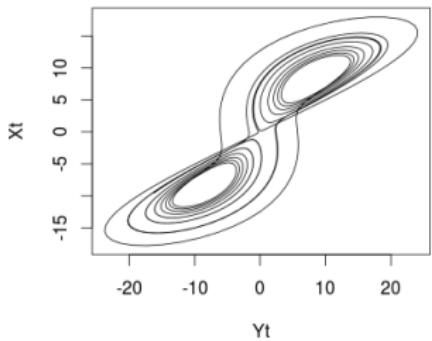
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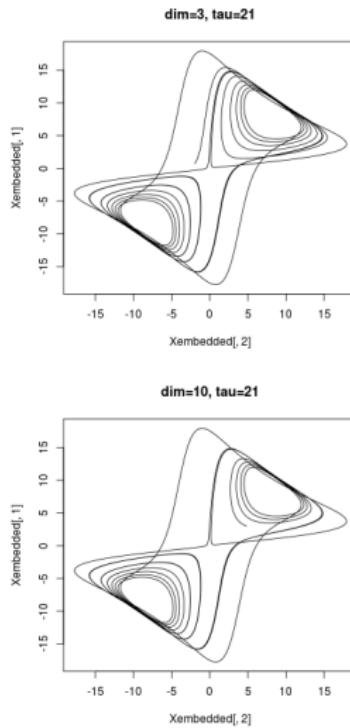
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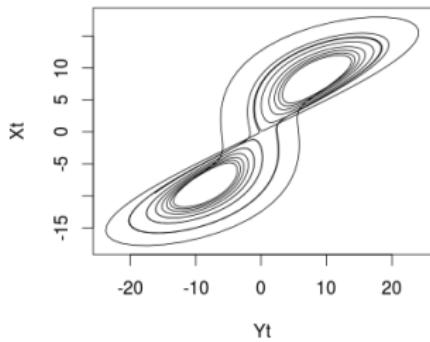
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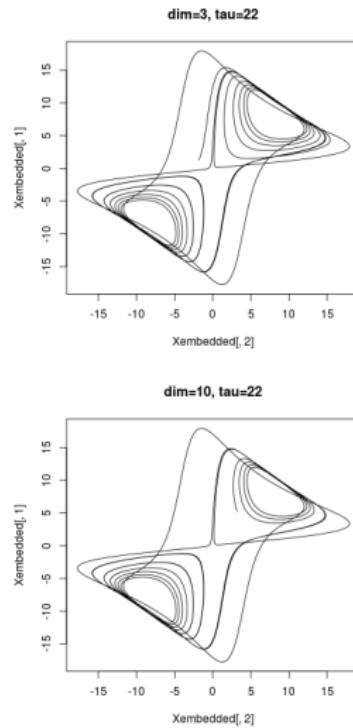
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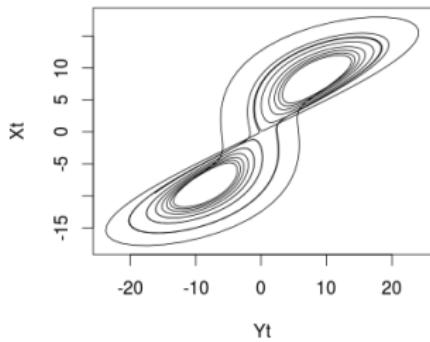
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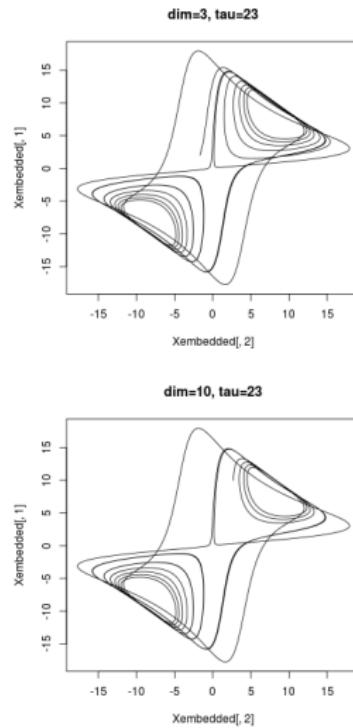
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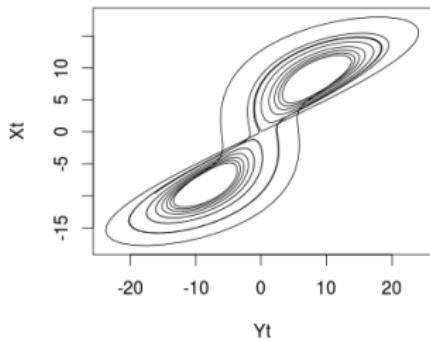
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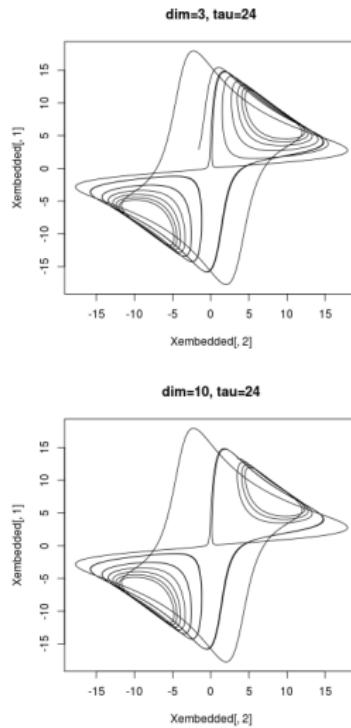
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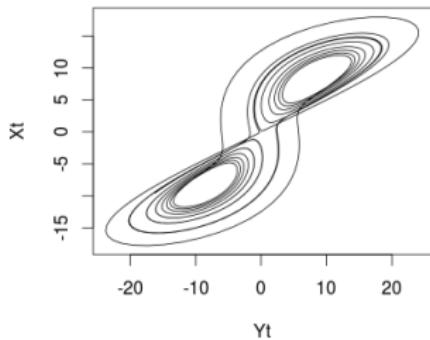
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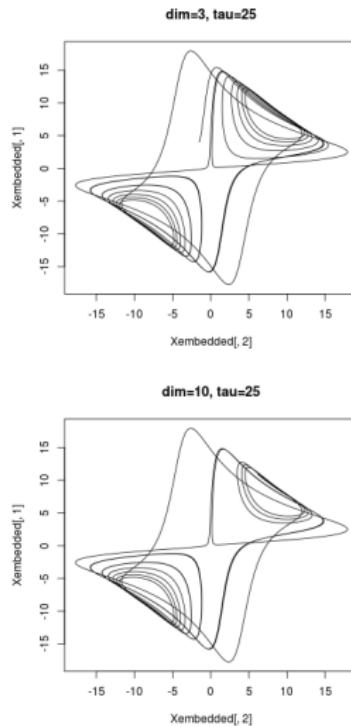
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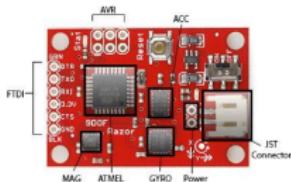
# My goals this month

- Determine the technique(s) to quantify the dexterity of Salsa Dancers based on the analysis of the reconstructed state space.
- Submit a paper in The International Symposium on Wearable Computers (ISWC). Deadline: April 10th, 2015.



# DECIMUS Class in C++

## 9DOF Razor IMU



Accelerometer  
X  
Y  
Z  
[m]

Magnetometer  
X  
Y  
Z  
[m]

Gyroscope  
X  
Y  
Z  
[m]

Yaw  
Pitch  
Roll



## DECIMUS Class in C++

*time-Delay Embedding theorem for  
ReConstructing state spaces  
Using Inertial Measurement Units*

### Time-Delay Embedding Parameters

```
DataAnalysis.Set_SpaceReconstructionParameters(50,10,5); // (lengthwindowframe, dim, tau)
```

```
Decimus DataAnalysis
Kind: Variable definition
Defd: main.cpp:96 Show uses
DataAnalysis Object
```

### Principal Component Analysis

```
mat A;
A= EmbeddedMatrix.t() * EmbeddedMatrix; // generate a symmetric matrix --- mat B = A.t() * A;

vec eigval_original, eigval;
mat eigvec_original, eigvec, transformedData;
eig_sym(eigval_original, eigvec, transformedData);
eig_sym(eigval_original, eigvec_original, A.t(), "dc"); // divide-and-conquer

eigval = flipud(eigval_original);
eigvec = fliplr(eigvec_original);
transformedData = fliplr(eigvec_original).t() * EmbeddedMatrix.t();

cout << "DIY:eigenvalues \n" << eigval << endl;
cout << "DIY:eigenvectors \n" << eigvec << endl;
cout << "DIY:transformedData \n" << transformedData << endl;
```

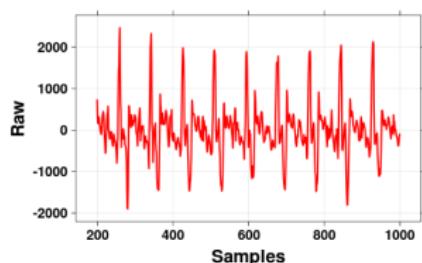
## IMU, Axes and C++ Class

# Seven Beginner Salsa Feet Patterns



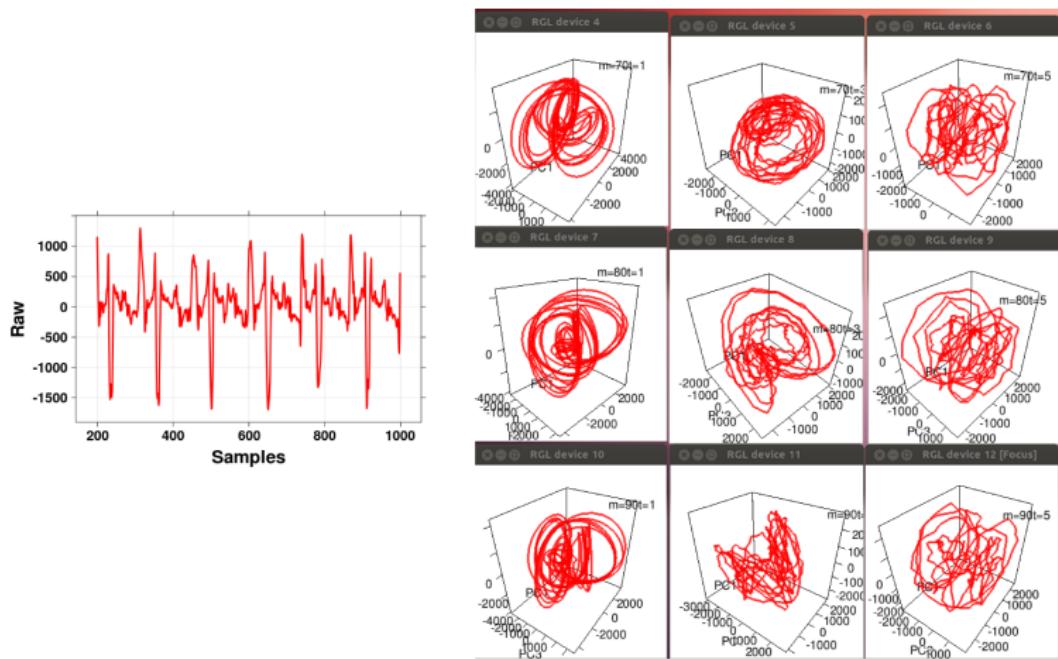
# RSS for Feet Pattern 2

## Participan 0 (Woman)- IMU1 GYR Z



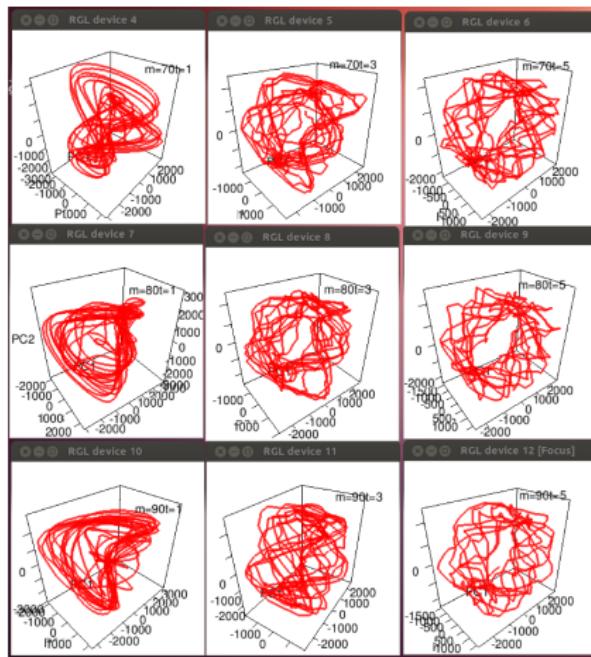
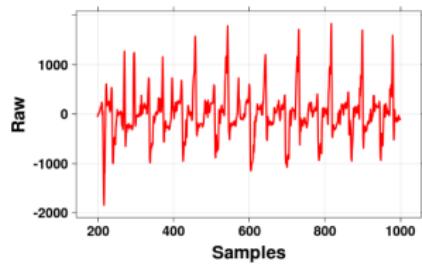
# RSS for Feet Pattern 2

## Participan 1 (Woman) - IMU1 GYR Z



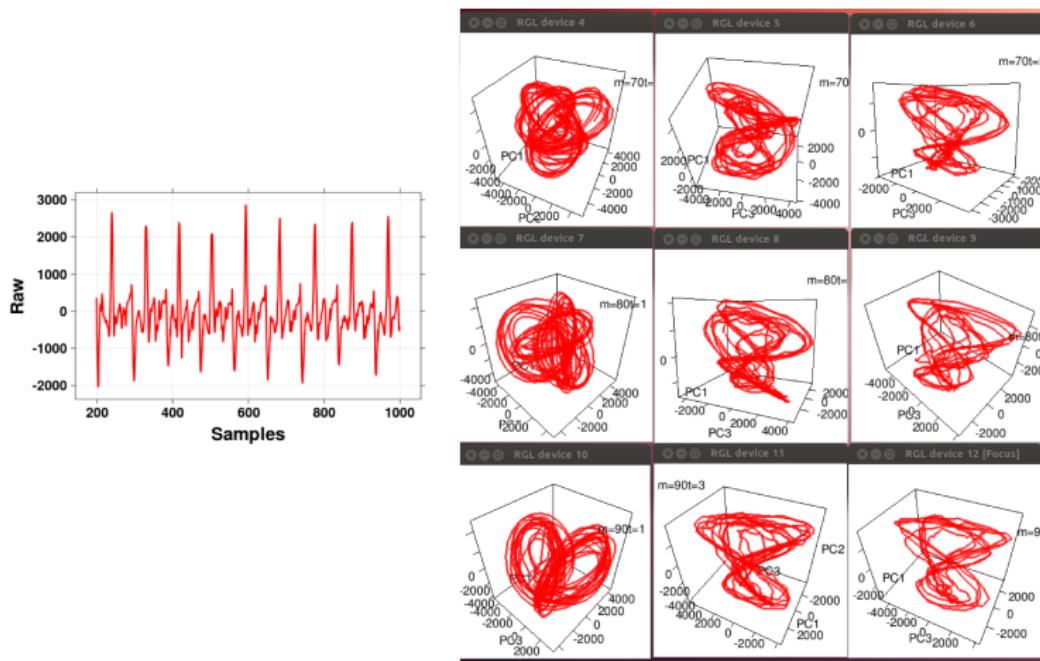
# RSS for Feet Pattern 2

## Participan 2 (Man) - IMU1 GYR Z



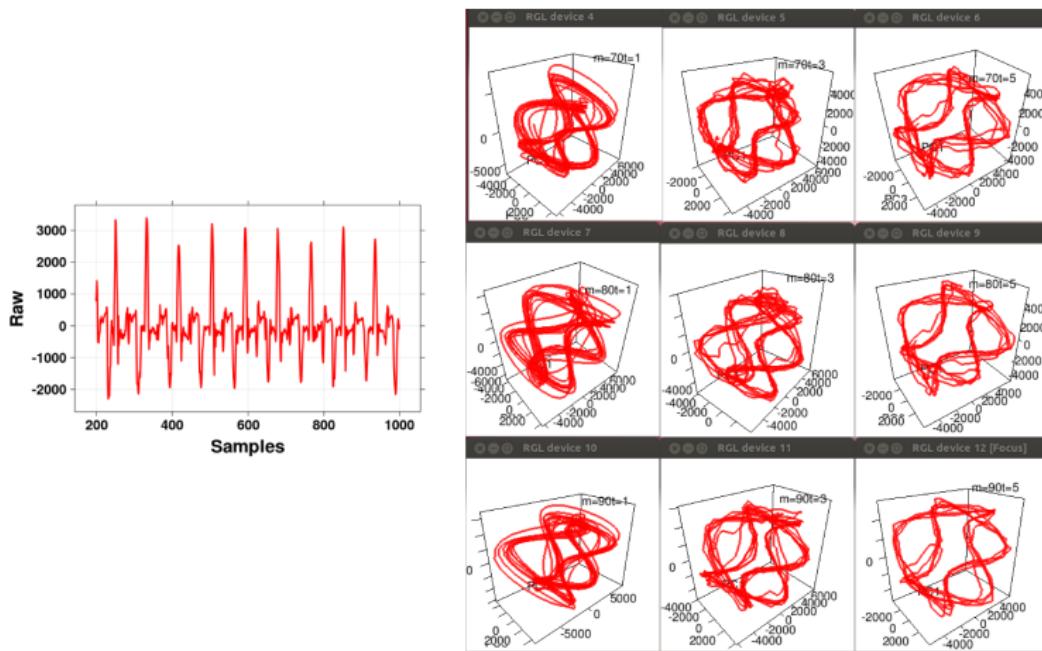
# RSS for Feet Pattern 2

## Participan 3 (Man) - IMU1 GYR Z

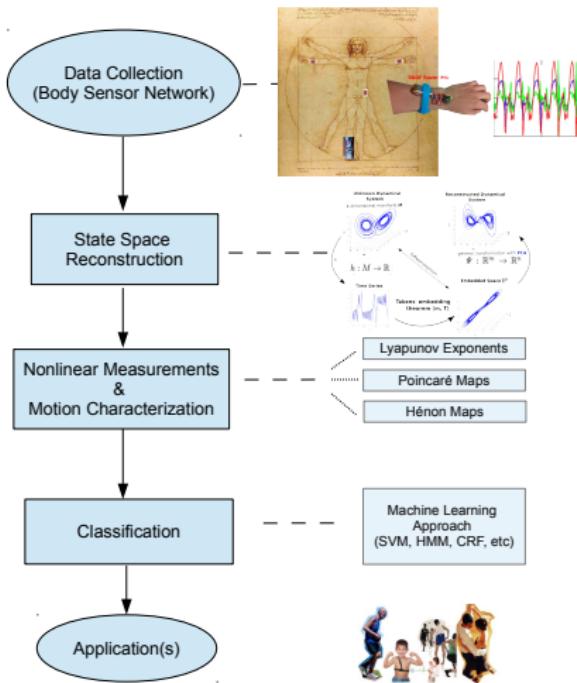


# RSS for Pattern 2

## Participan 4 (Man) - IMU1 GYR Z



# PhD Framework

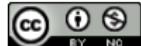


# QUESTIONS?

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# A Nonlinear Dynamics Approach to Human Activity Recognition Using Inertial Sensors

Pérez-Xochicale Miguel Angel

Internal Research Conference Presentation  
EECE School  
10th March 2015

