

GSOE9210 Engineering Decisions

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Victor Jauregui Engineering Decisions

Introduction

- 1 Introduction
 - Motivation
 - Decision problems: examples
 - Course overview
- 2 Decision problems: representation
 - Decision problem elements
 - Uncertainty
 - Decision trees
 - Decision tables

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Outline

1 Introduction

- Motivation
- Decision problems: examples
- Course overview

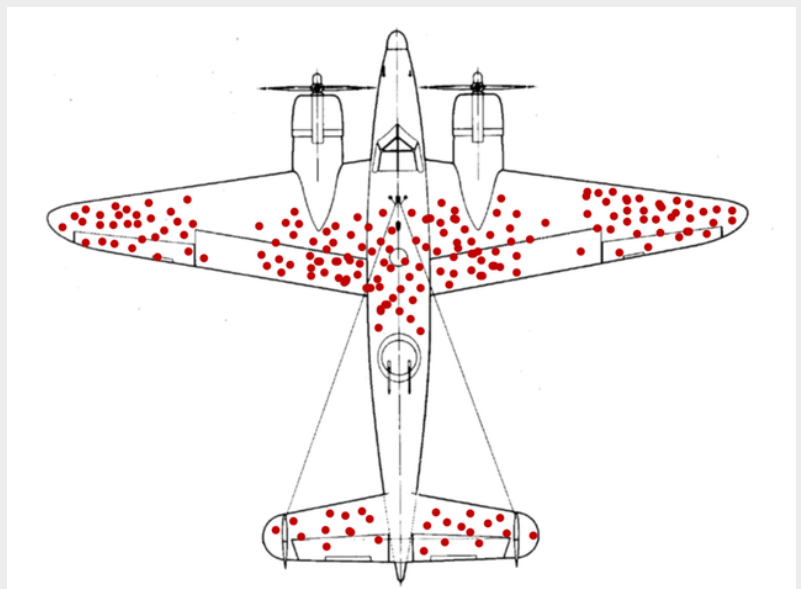
2 Decision problems: representation

- Decision problem elements
- Uncertainty
- Decision trees
- Decision tables

The tale of the missing bullets

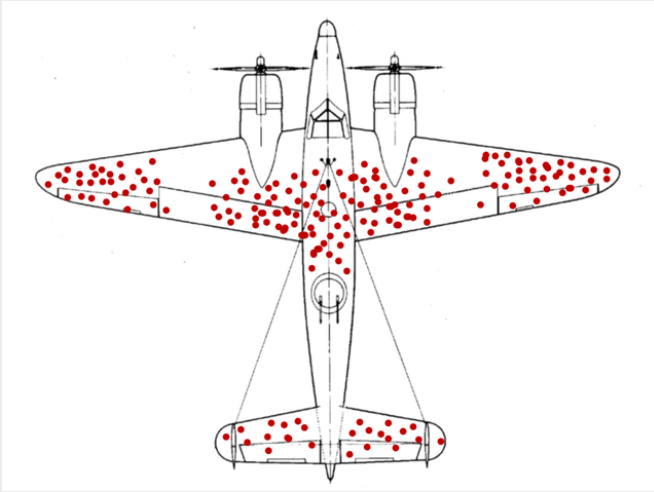


Abraham Wald (1902–1950)



By McGeddon—Own work, CC BY-SA 4.0,
<https://commons.wikimedia.org/w/index.php?curid=53081927>

The tale of the missing bullets . . .



Airforce General:

Professor Wald, how much armour should we put on our aircraft?

<http://paristampablog.com/2014/09/25/abraham-wald-and-the-missing-bullet-holes/>

Decision problems



Example (Oil exploration)

You're the chief petroleum engineer of an oil company which owns a drilling option on an area of sea. Should you drill before the option expires?

Considerations:

- likelihood of finding oil, amount and quality, projected oil demand
- size and location of drilling
- cost of drilling and raising the oil, etc.

Decision problems



Example (Drug development)

You're the chief chemical engineer in a pharmaceuticals company which is considering whether to mass produce a new cancer treatment drug. Initial findings are inconclusive as to the drug's effectiveness. Should you go into development and/or production?

Considerations:

- likelihood of drug's effectiveness
- level of investment, timing, competition, *etc.*
- cost to the company of synthesis and trials value of human life, *etc.*

Decision problems



Example (Manufacturing processes)

You're the head process engineer of Acme Inc., a company which manufactures mechanical components for the automobile industry. A new technology could mean increased demand for Acme's components in the near future. The managing director has requested a report on existing plant capacity and possible production options. What is your recommendation?

Considerations:

- likelihood and degree of increased demand
- options for increasing plant production
- cost-benefit analysis of capital investment, *etc.*

Decision problems



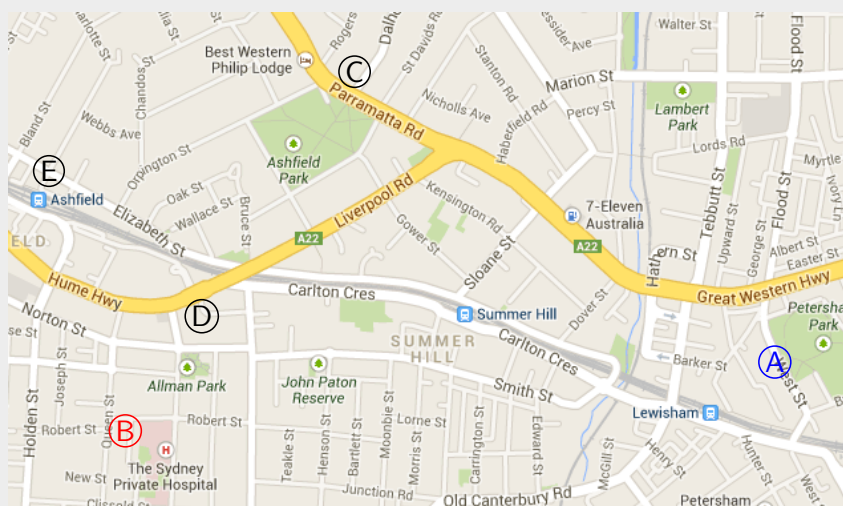
Considerations:

- value of necklace
- cost of insurance
- likelihood of theft

Example (To insure or not)

You own a necklace which you intend to sell at the end of the year. Should you insure it against theft?

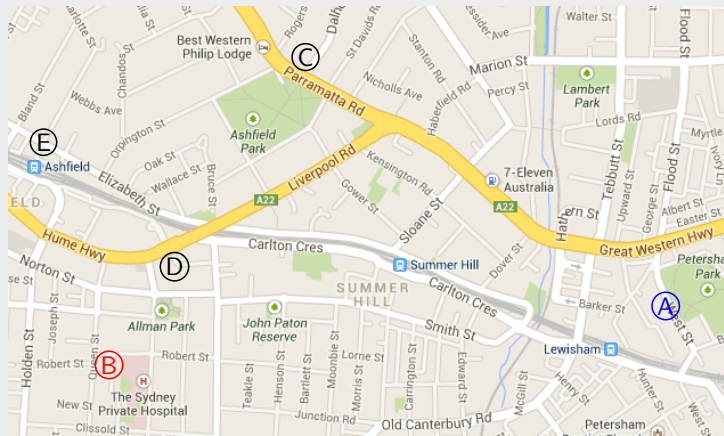
Decision problems



Example (Getting from A to B)

You have to get from Petersham Park (A) to the Hospital (B) by either train or bus. The train goes to Ashfield Station (E). You don't know the bus route: either via Parramatta Rd (C) or Liverpool Rd (D).

Decision problems: discussion



Suppose you:

- are an ER surgeon
- are a tourist
- *have an injured foot . . .*

Quantitative problems

Example (Inventory)

Your football club needs to provide playing uniforms for each of its members. The initial order needs to be placed before registrations are complete; *i.e.*, before the final number of members has been determined. The initial (early) order incurs a fee of \$500 plus \$20 per uniform. Late orders incur an additional \$300 fee plus the usual \$20 per uniform. Uniforms are sold for \$40 each.



How many uniforms should you order initially?

Group decisions

Example (Song contest)

Seven judges vote for four songs: A, B, C, D.

	J1	J2	J3	J4	J5	J6	J7	Tot.
A	4	1	2	4	1	2	4	18
B	3	4	1	3	4	1	3	19
C	2	3	4	2	3	4	2	20
D	1	2	3	1	2	3	1	13

What if song D is disqualified?

	J1	J2	J3	J4	J5	J6	J7	Tot.
A	3	1	2	3	1	2	3	15
B	2	3	1	2	3	1	2	14
C	1	2	3	1	2	3	1	13

Group decisions

Example

Three people (P1, P2, P3) vote for three candidates A, B, C in a poll. The preferences are:

	P1	P2	P3
1st	B	C	A
2nd	C	A	B
3rd	A	B	C

What should be the group preference?

- Most preferred, second preference, ...
- Majority: two voters prefer B to C, two C to A, ...

Motivation



“If . . . decision-theoretic structures do not in the future occupy a large part of the education of engineers, then the engineering profession will find that its traditional role of managing scientific and economic resources for the benefit of man has been forfeited to another profession.”

—Ron Howard (1966)
Professor of Management Science and
Engineering
Stanford University

Course overview

Course aims:

To equip engineering graduates with analytical decision-making skills and techniques.

Course structure:

- Single-agent decisions
- Multi-agent decisions: games

Teaching methodology:

- Mix of theoretical and applied
- Universal principles rather than domain specific knowledge

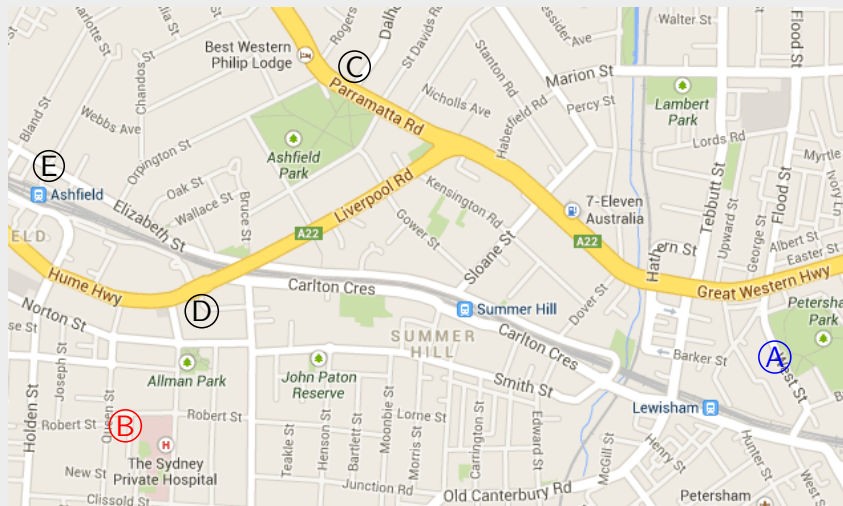
Single-agent decisions: overview

- ① Decision problems
- ② Decision problem representations: trees and tables
- ③ Decisions under uncertainty (ignorance and risk)
- ④ Measuring uncertainty: probability
- ⑤ Preference and utility
- ⑥ Information and its value

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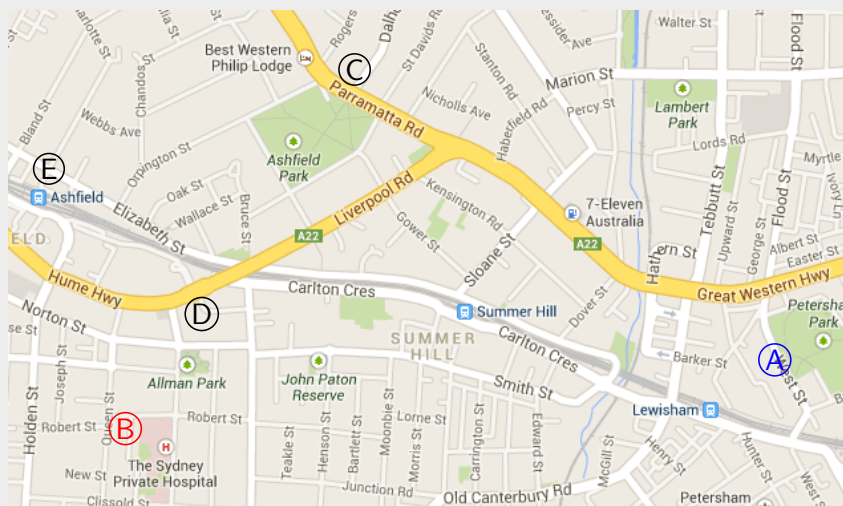
Decision problems



Example (Getting from A to B)

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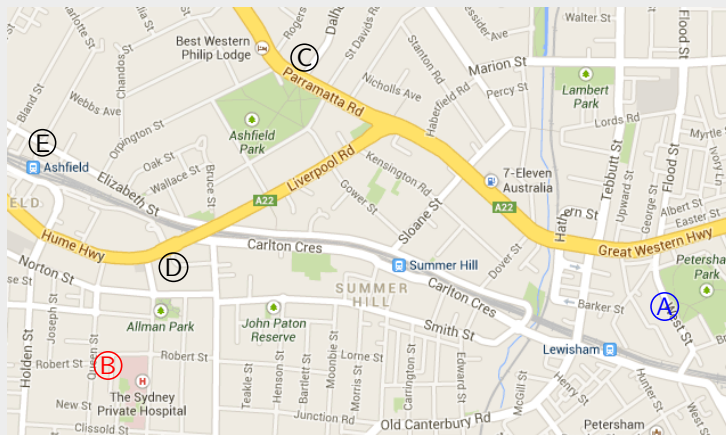
Decision problems: elements



The basic elements common to *decision problems* are:

- *actions* (alternatives, strategies) (\mathcal{A}): Tr, Bu
- *possible states* (events, cases, circumstances, contexts) (\mathcal{S}): e.g., Liverpool Rd bus (b_L) or Parramatta Rd bus (b_P)
- *outcomes* (consequences) (Ω): arrive at C, D, or E

Decision problems: elements



- $\mathcal{A} = \{\text{Tr}, \text{Bu}\}$, $\Omega = \{C, D, E\}$, $\mathcal{S} = \{b_L, b_P\}$
- each action is associated with a set of possible outcomes:
e.g., Tr: $\{E\}$, Bu: $\{C, D\}$

Decision problems



Example (To insure or not)

You own a necklace which you intend to sell at the end of the year.
Should you insure it against theft?

- *actions* (\mathcal{A}): Insure, don't insure
- *events* (\mathcal{S}): necklace stolen, necklace not stolen
- *outcomes* (Ω): uninsured necklace sold (not stolen), insured necklace sold, necklace stolen and not insured, necklace stolen but insured

Quantitative problems

Example (Inventory)

Your football club needs to provide playing uniforms for each of its members. The initial order needs to be placed before registrations are complete; *i.e.*, before the final number of members has been determined. The initial (early) order incurs a fee of \$500 plus \$20 per uniform. Late orders incur an additional \$300 fee plus the usual \$20 per uniform. Uniforms are sold for \$40 each.



- *actions* (\mathcal{A}): Order quantity (q): $O_0, O_1, O_2, \dots, O_q, \dots$
- *events* (\mathcal{S}): Membership (m): $r_0, r_1, r_2, \dots, r_m, \dots$
- *outcomes* (Ω): Profit is some binary function of q and m , $f(q, m) \dots$

Oil exploration; uncertainty

Example (Oil exploration)

You're the chief petroleum engineer of an oil company which owns a drilling option on an area of sea. Should you drill before the option expires?

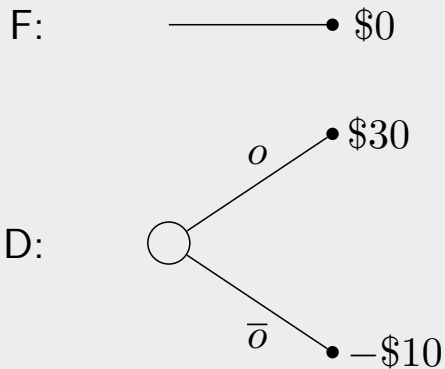
- *actions* (\mathcal{A}): Drill (D), Forfeit rights (F) (don't drill (\bar{D}))
- *states* (\mathcal{S}): Oil present (o), no oil (\bar{o})
- *outcomes* (Ω): Profit (\$30), loss ($-\10), status quo (\$0)

Uncertainty

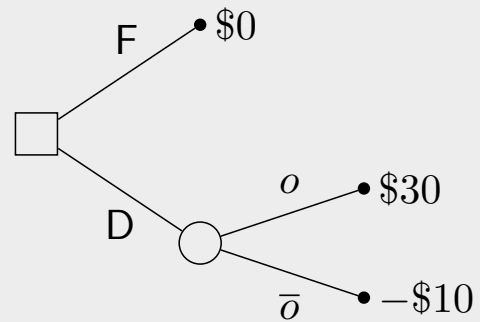
There is *uncertainty* due to incomplete information about which of multiple possible states is *actual*.

Oil exploration analysis

- Decide between two options:

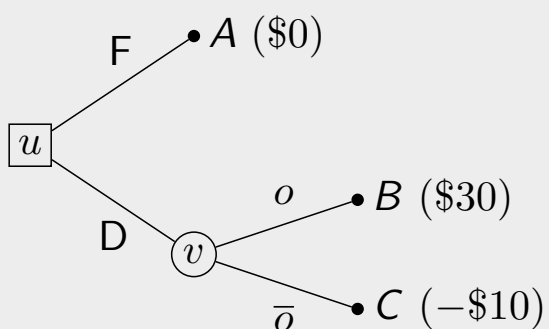


- Combined into a decision tree:



Choosing between uncertain situations is one of the fundamental problems of complex decision-making.

Decision trees



In a decision tree:

- each leaf node represents an outcome
- each branch represents either an action or an (chance) event
- internal nodes can be *decision nodes* (boxes) or *chance nodes* (circles)

Exercises

- What type of node is u ? v ? B?
- What does the branch labelled D represent?
- What does the branch labelled \bar{o} represent?

Problem representation

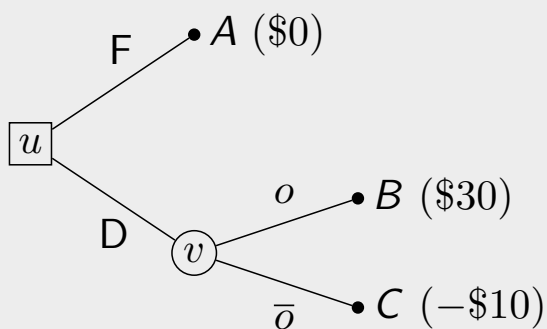
Exercises

Draw decision trees for the problems below:

- Alice's insurance problem
- Alice's football club inventory problem

How would you modify the representations above if Alice had two insurance policies to choose from?

Problem representation: decision tables



Represented as a table:

		\mathcal{S}	
		ω	\bar{o}
\mathcal{A}	F	A	A
	D	B	C

Decision tables:

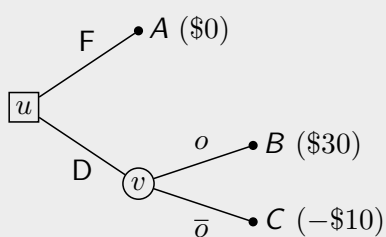
- Observation: Each combination of an **action and a state** uniquely determine an outcome
- Model as a binary function:
 $\omega : \mathcal{A} \times \mathcal{S} \rightarrow \Omega$
 - row = action
column = state
 - Interpretation: $B = \omega(D, o)$ means “B is the outcome of action D in state o”;

Decision tables

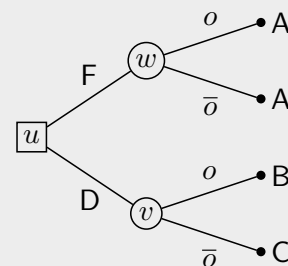
		\mathcal{S}					
		s_1	s_2	\dots	s_k	\dots	s_n
\mathcal{A}	A_1	ω_{11}	ω_{12}	\dots	ω_{1k}	\dots	ω_{1n}
	A_2	ω_{21}	ω_{22}	\dots			
	\vdots						
	A_j	ω_{j1}	ω_{j2}	\dots	ω_{jk}	\dots	
	\vdots						
	A_m	ω_{m1}	ω_{m2}	\dots	ω_{mk}	\dots	ω_{mn}

- A decision table represents the binary function $\omega : \mathcal{A} \times \mathcal{S} \rightarrow \Omega$, where $\mathcal{A} = \{A_1, \dots, A_m\}$ and $\mathcal{S} = \{s_1, \dots, s_n\}$, and the entry in the j -th row and k -th column is $\omega_{jk} = \omega(A_j, s_k)$
- Formally, a 4-tuple $T = (\mathcal{A}, \Omega, \mathcal{S}, \omega)$

Trees and tables



	o	\bar{o}
F	\$0	\$0
D	\$30	-\$10



- Multiple trees may correspond to the same table
- Going from tables (*normal form*) to trees (*extensive form*) is straight forward, but the converse can be tricky
- Which representation is better: trees or tables?
- Which representation facilitates decision analysis most?

Outcomes

1 Introduction

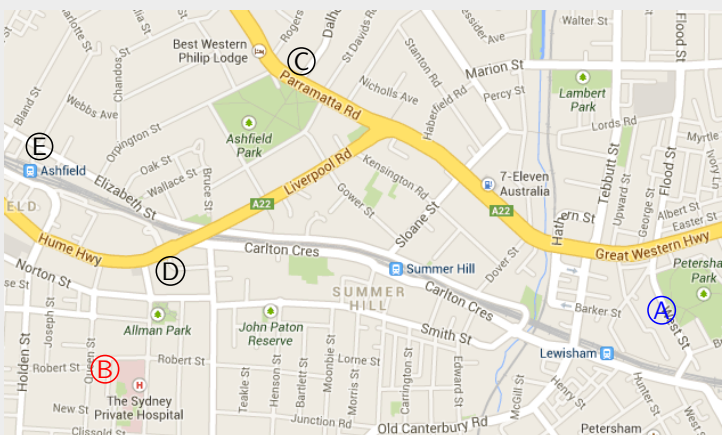
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Comparing outcomes: value/payoff functions

- Preferences over outcomes can be easily expressed if the outcomes can be quantified numerically

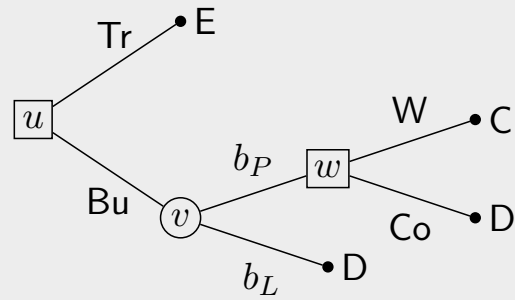
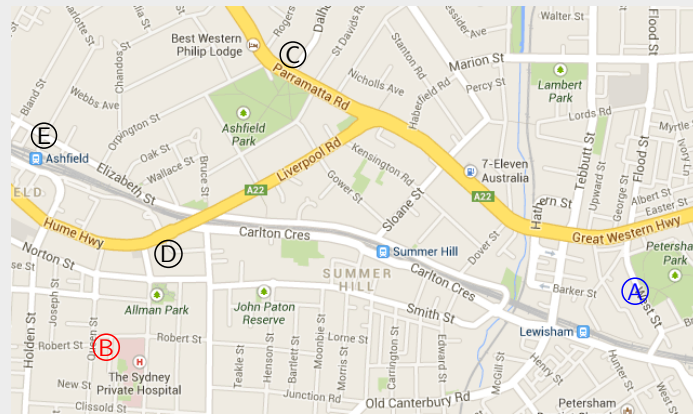


Distance to B:

ω	$d(\omega, B)$
B	0km
C	4km
D	1km
E	2km

- Prefer E to C because $d(E, B) < d(C, B)$

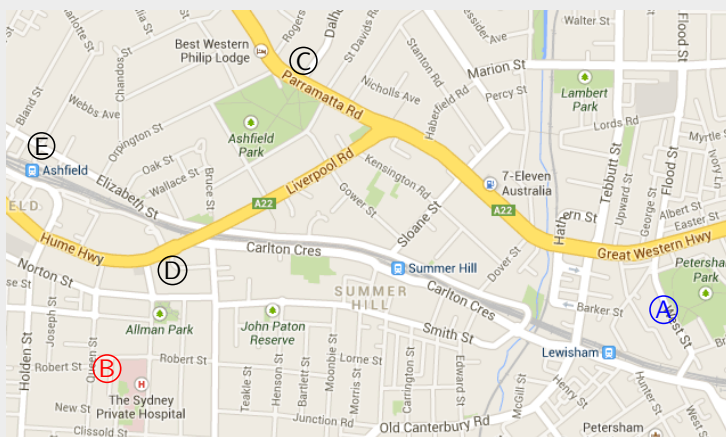
Outcomes and values



Question

Suppose that the route up Parramatta Rd loops around to D providing the new option to either walk from C or continue to D. Do the two D leaf nodes correspond to the same outcome if we evaluate them according to:
(a) distance; (b) total travel time?

Outcomes and values



Values of outcomes based on distance (km):

	b_L	b_P
Tr	2	2
Bu	1	4

- Walking distance? Straight line?
- Consider values based on travel times (mins):

	b_L	b_P
Tr	30	30
Bu	10	40

Decision and preference

- Agents have *subjective* (individual) *preferences* over outcomes
- Often assign each outcome a numerical *value*; e.g., money, distance, etc. i.e., each agent has its own *value function*: $v : \Omega \rightarrow \mathbb{R}$
- A value function is essentially a generalised *random variable*
- A decision problem is now: $P = (\mathcal{A}, \mathcal{S}, \Omega, \omega, v)$

Convention

Value assignments usually assign higher values to more preferred (more desirable) outcomes.

The epistemic state

An agent's decisions depends on:

- their preferences (e.g., values on outcomes)
- their *epistemic state* (e.g., information about the state at the world when the decision is made)

Definition (Epistemic state)

An agent's *epistemic state* is the knowledge (information) or belief it has about the actual state.

Decision problems and rules

Fundamental problem of decision theory

For any given decision problem, to come up with a *rational* choice from among the possible actions.

Definition (Decision rule)

A *decision rule* is a way of choosing, for each decision problem, an action or set of actions.

Questions:

- What constitutes a *rational* decision rule?
- How does an agent's epistemic state affect a decision rule?

Summary

- Decision problems
- Elements in a (any) decision: actions, states, outcomes
- Representing decision problems: trees and tables
- Uncertainty and information (epistemic state)
- Preference (value) over outcomes