

Linked List Data Structures

Data Structures for Computer Professionals

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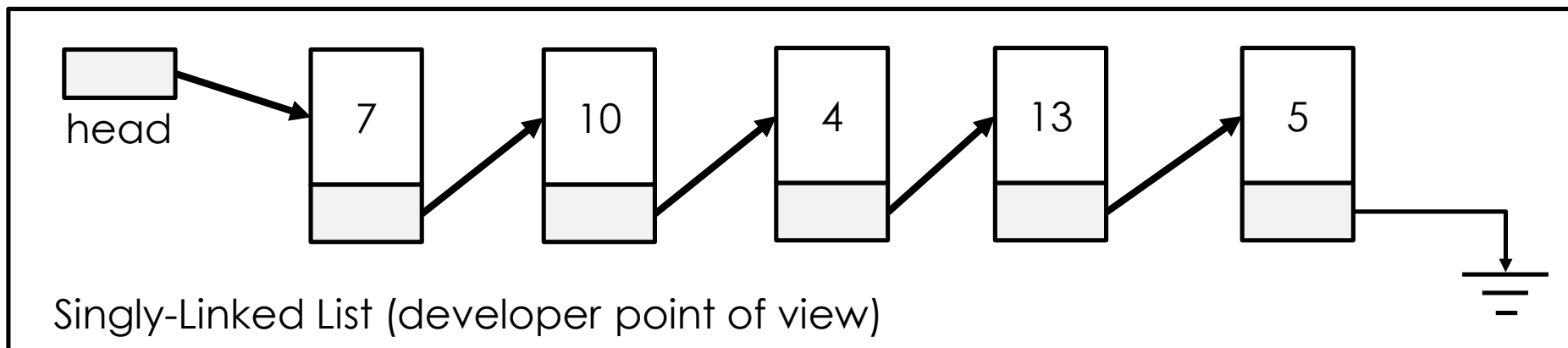
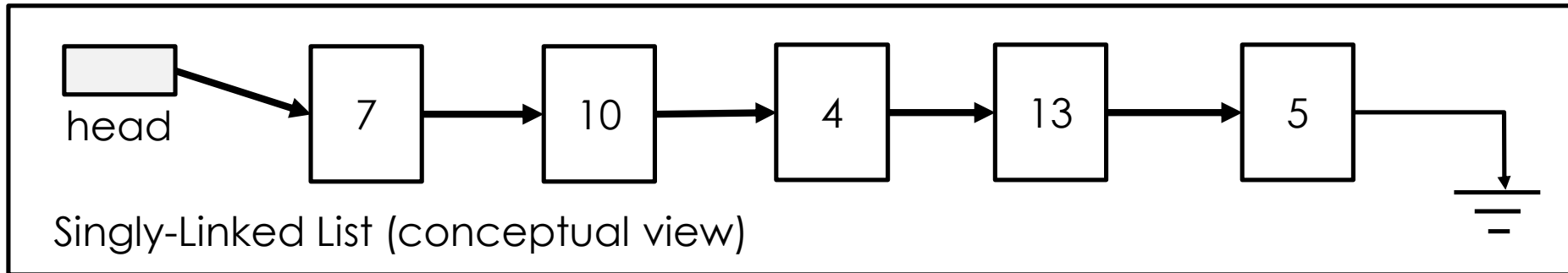
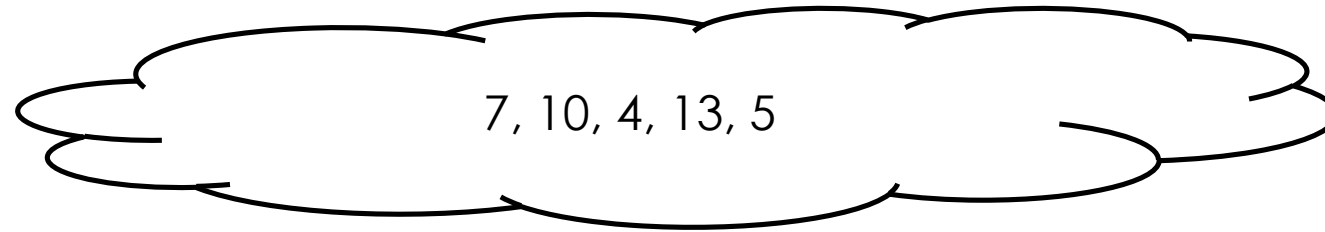
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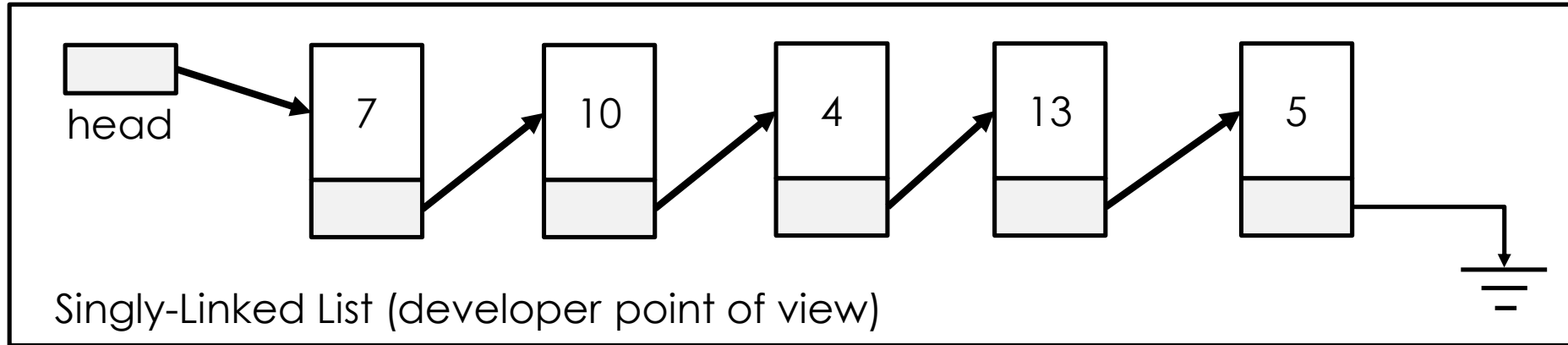
Problem with Arrays

- You need to allocate free space in memory for storing data
- In the static array, “IndexOutOfRangeException” Exception will raise when the data size exceeds the capacity
- Dynamic array allows you to add new data indefinitely as long as there is free space in memory BUT
 - You need to waste space twice the size of the data structure just only for storing one new object
 - Reallocation cost you $O(n)$
- Question is “Is there any other data structure that guarantee $O(1)$ every time for adding a new object?”
- How about “Linked List” data structure

Linked List Data Structures

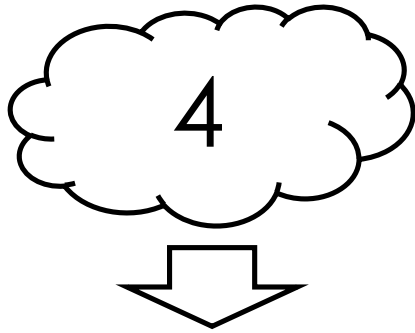


(Singly) Linked List Data Structures

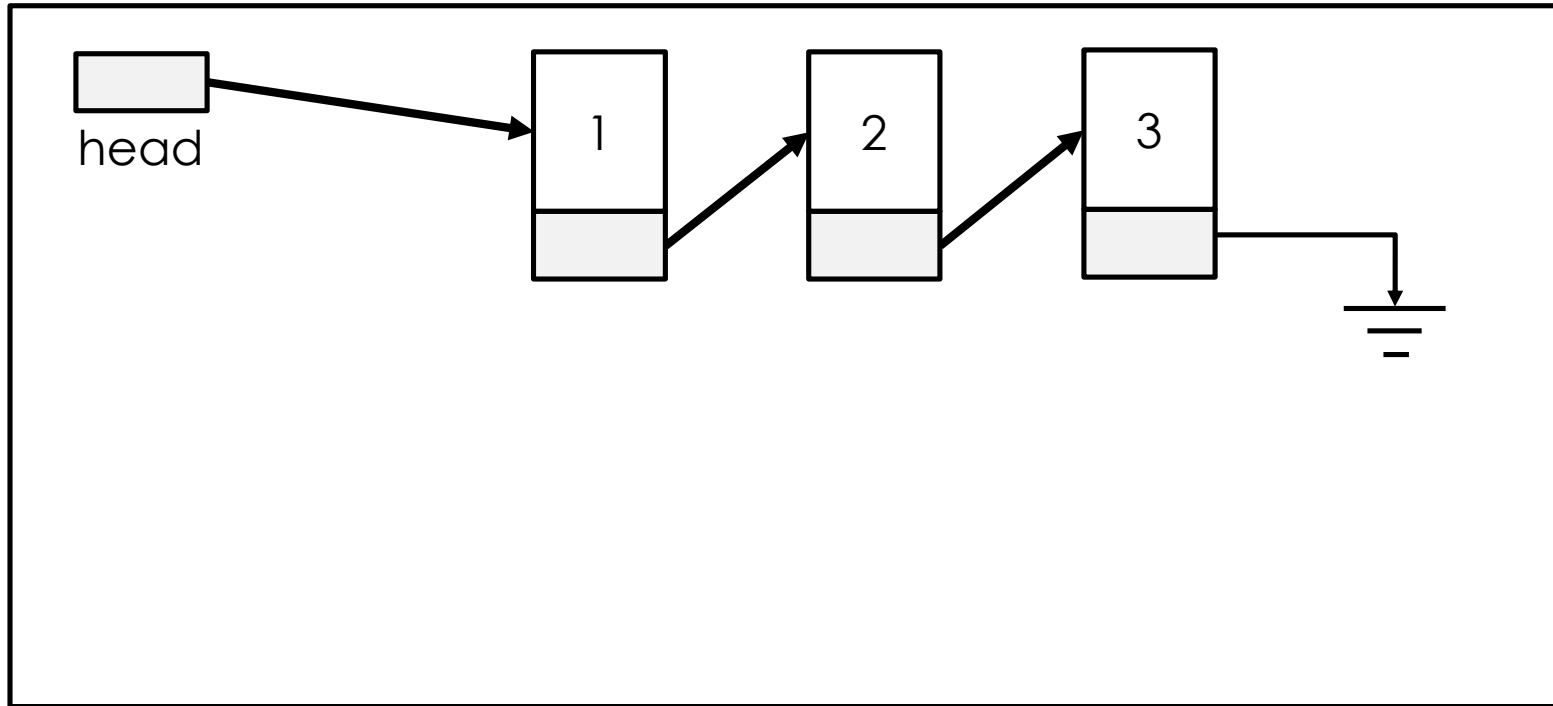


- Linked list consists of the **head** and list of **nodes**
- The **head** is a pointer/reference to the first node
- If Linked List is empty, the head will point to *null*
- Each individual **key** contained within a node
- A node consists of a key and the **next** pointer
- The **next** pointer of a node will point to the next node or *null*

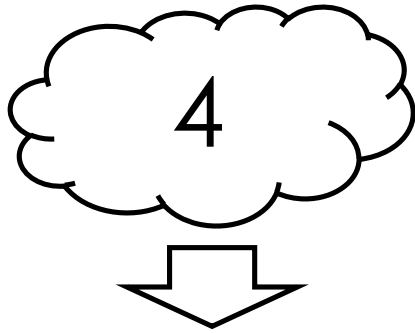
PushFront operation



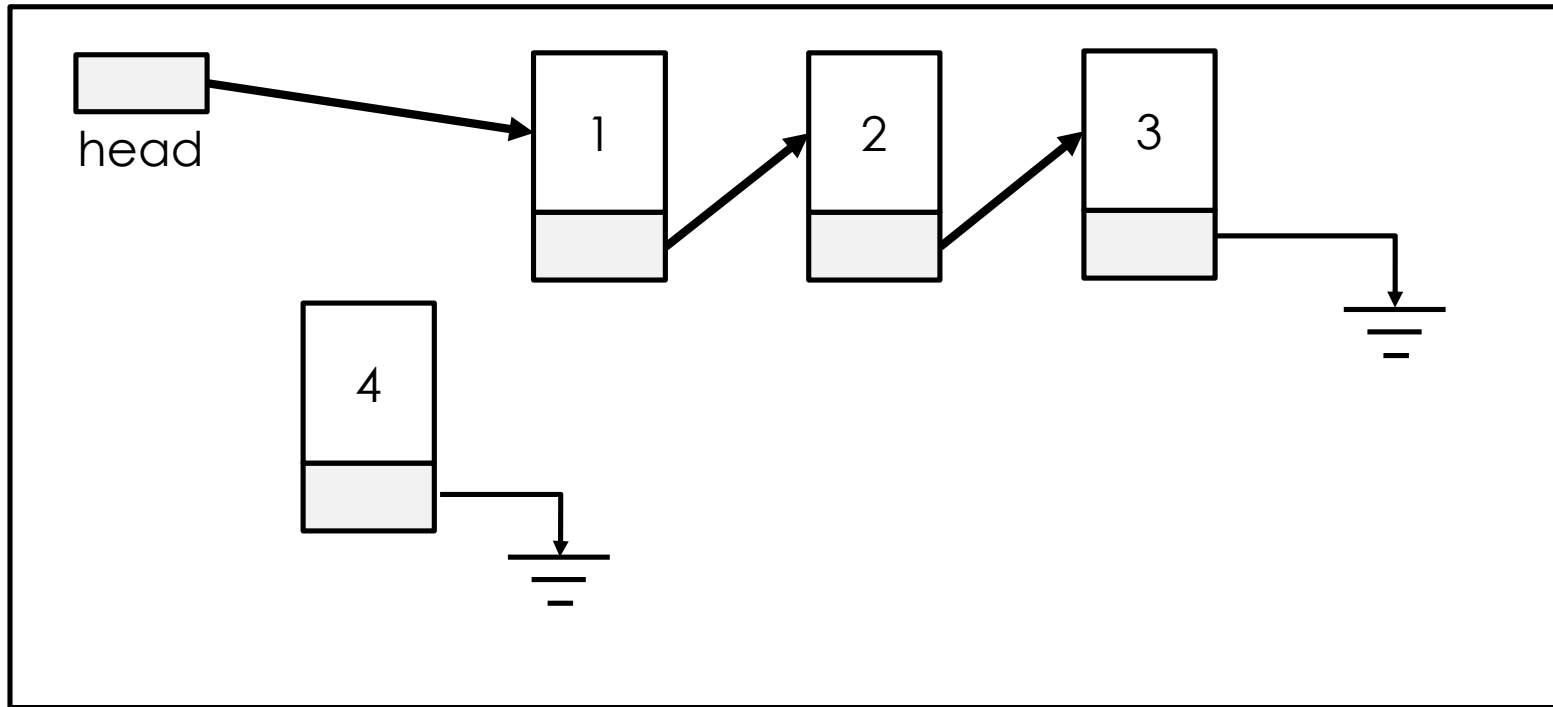
Problem: You want to add new key 4 to the front of the list



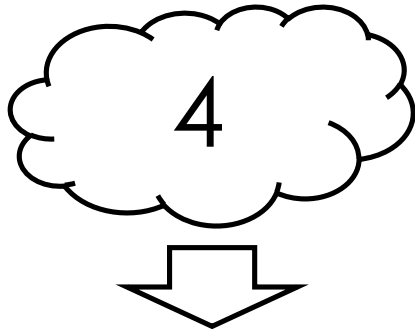
PushFront operation



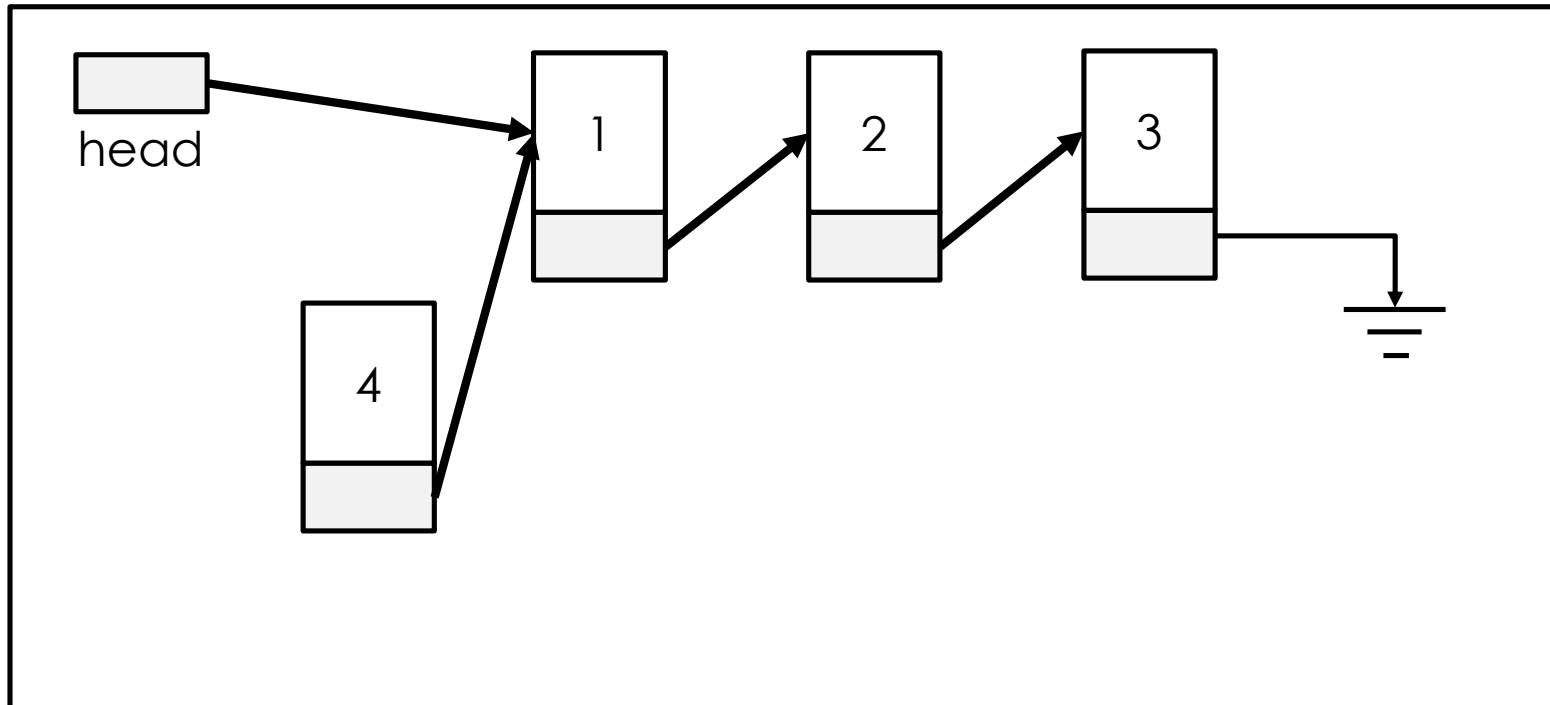
Step 1: Create a node that contains "4"



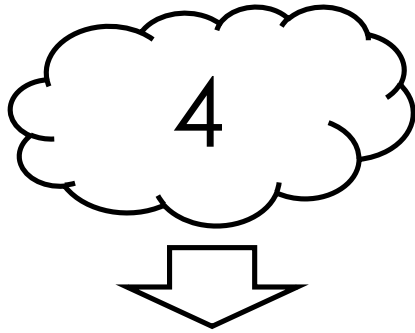
PushFront operation



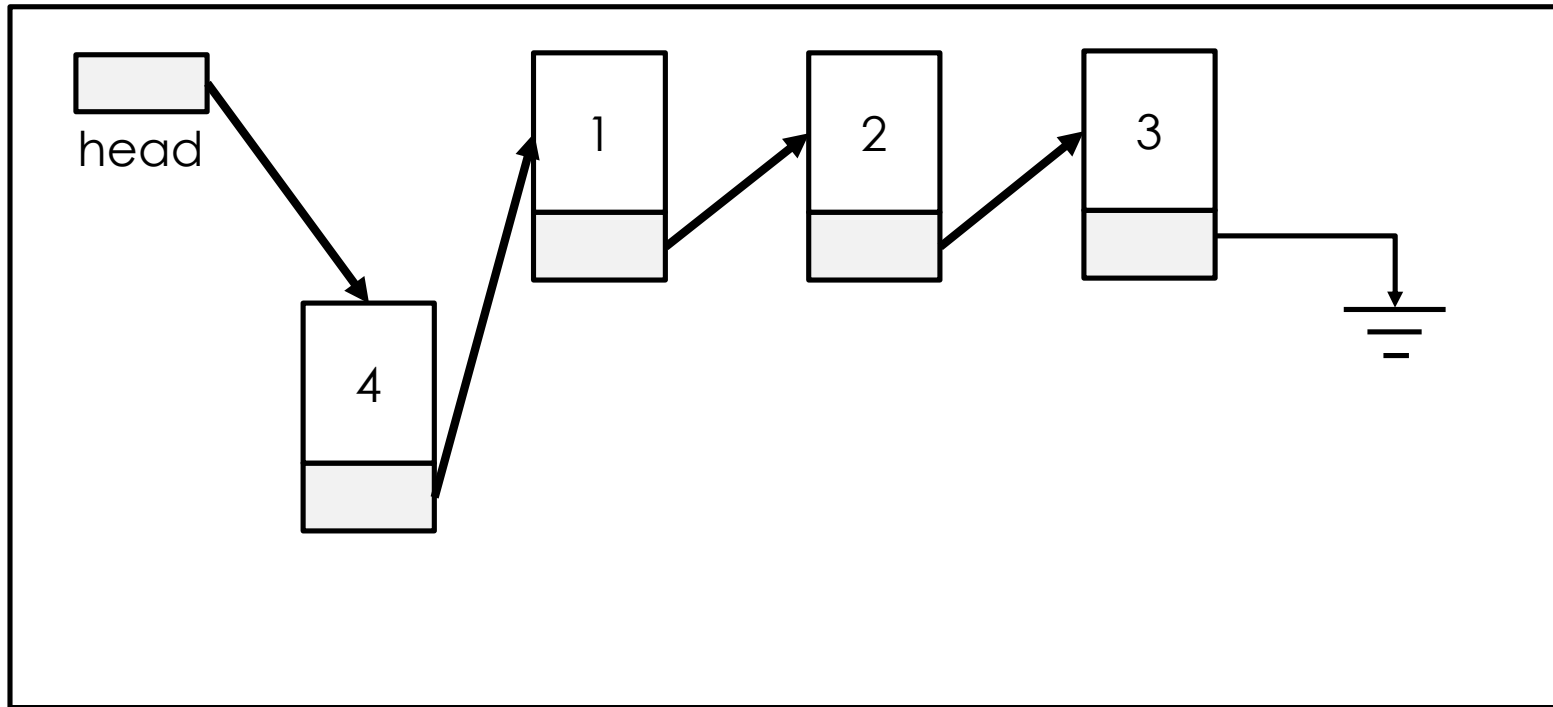
Step 2: Set next pointer of the new node to point to the node that the head points to (or the first node)



PushFront operation

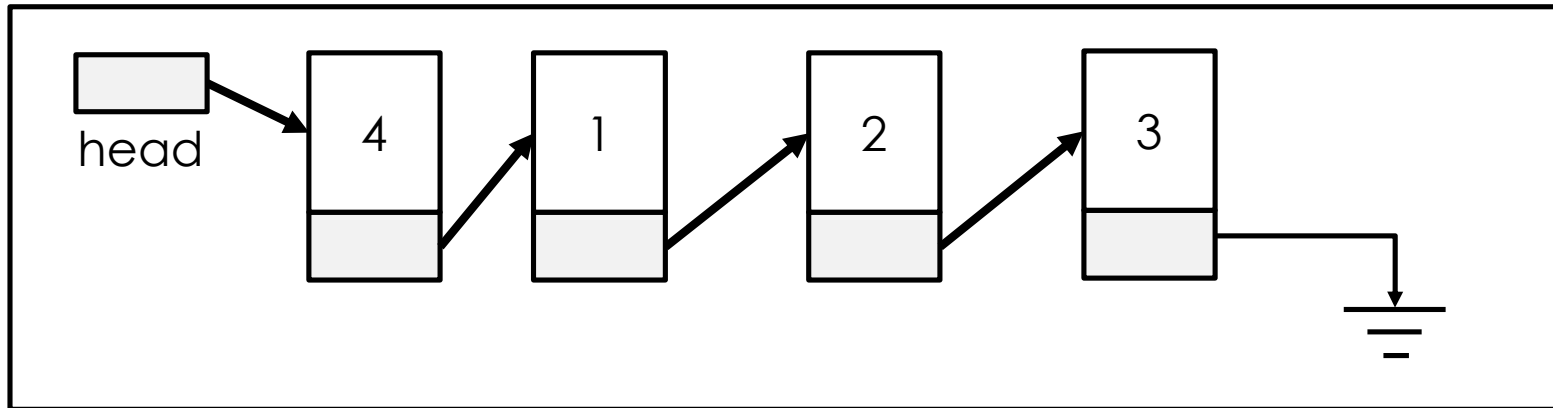


Step 3: Set the *head* to point to the new node



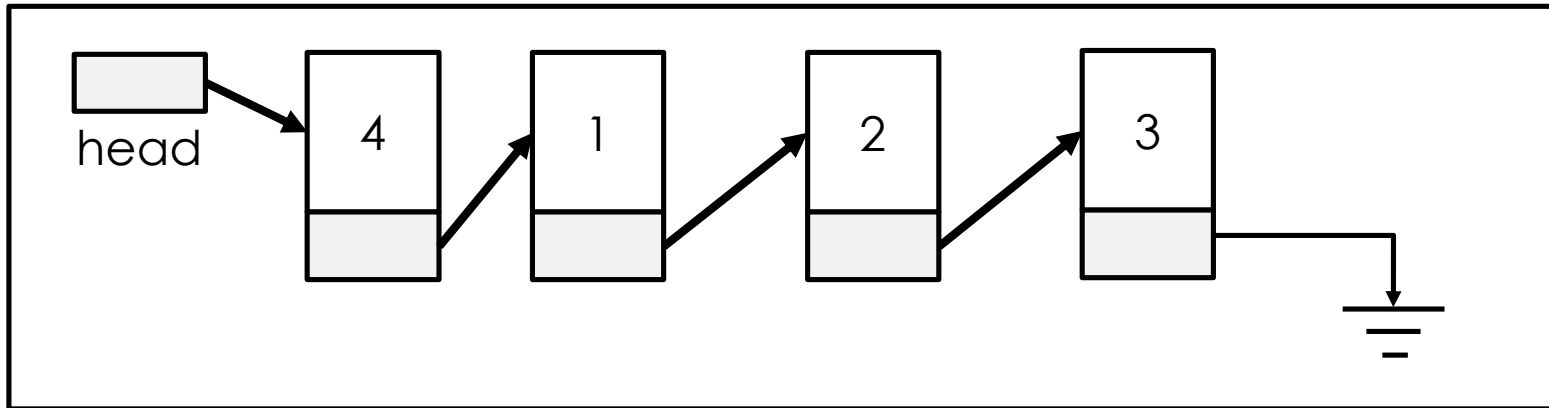
PushFront operation

What is the Big O?
 $O(1)$



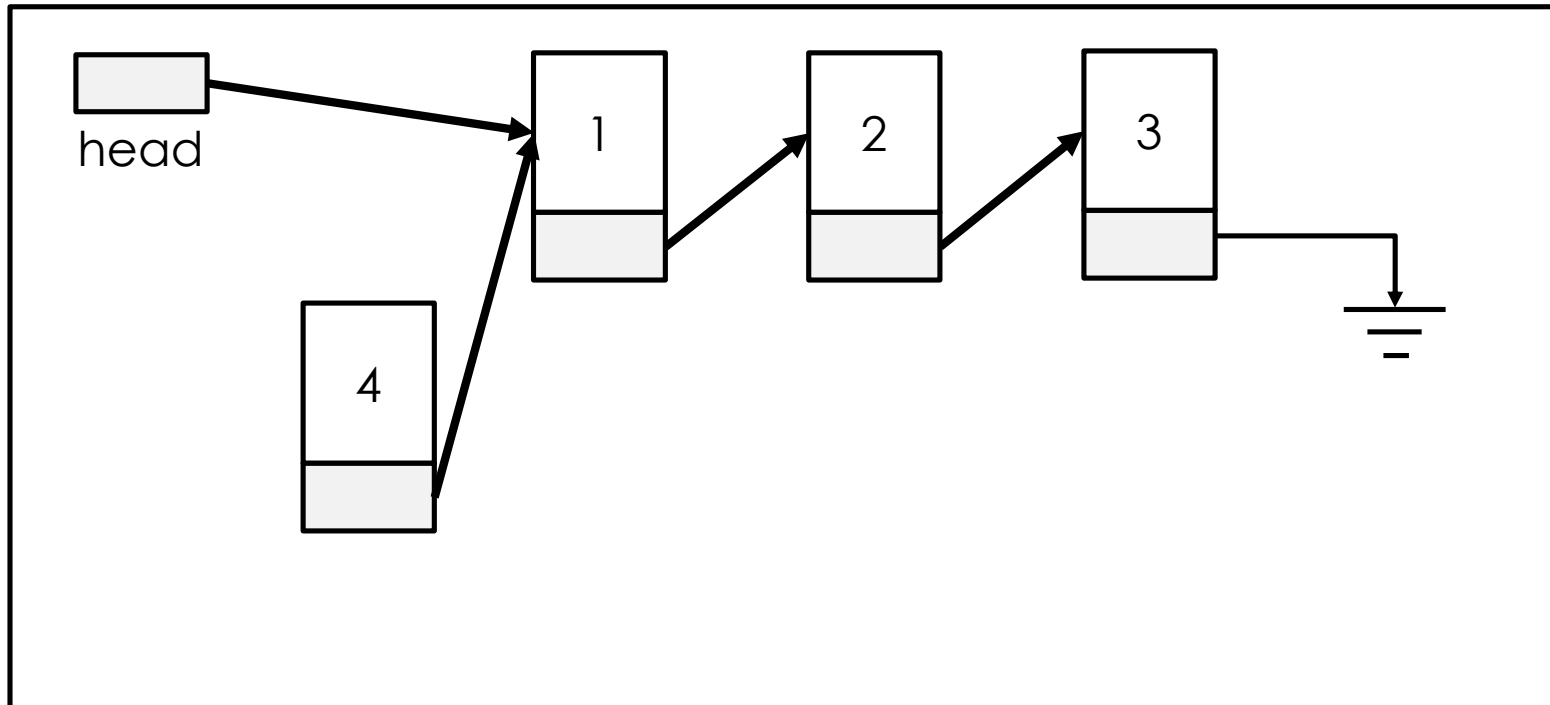
How about remove the front!

The operation is called “PopFront”



PopFront operation

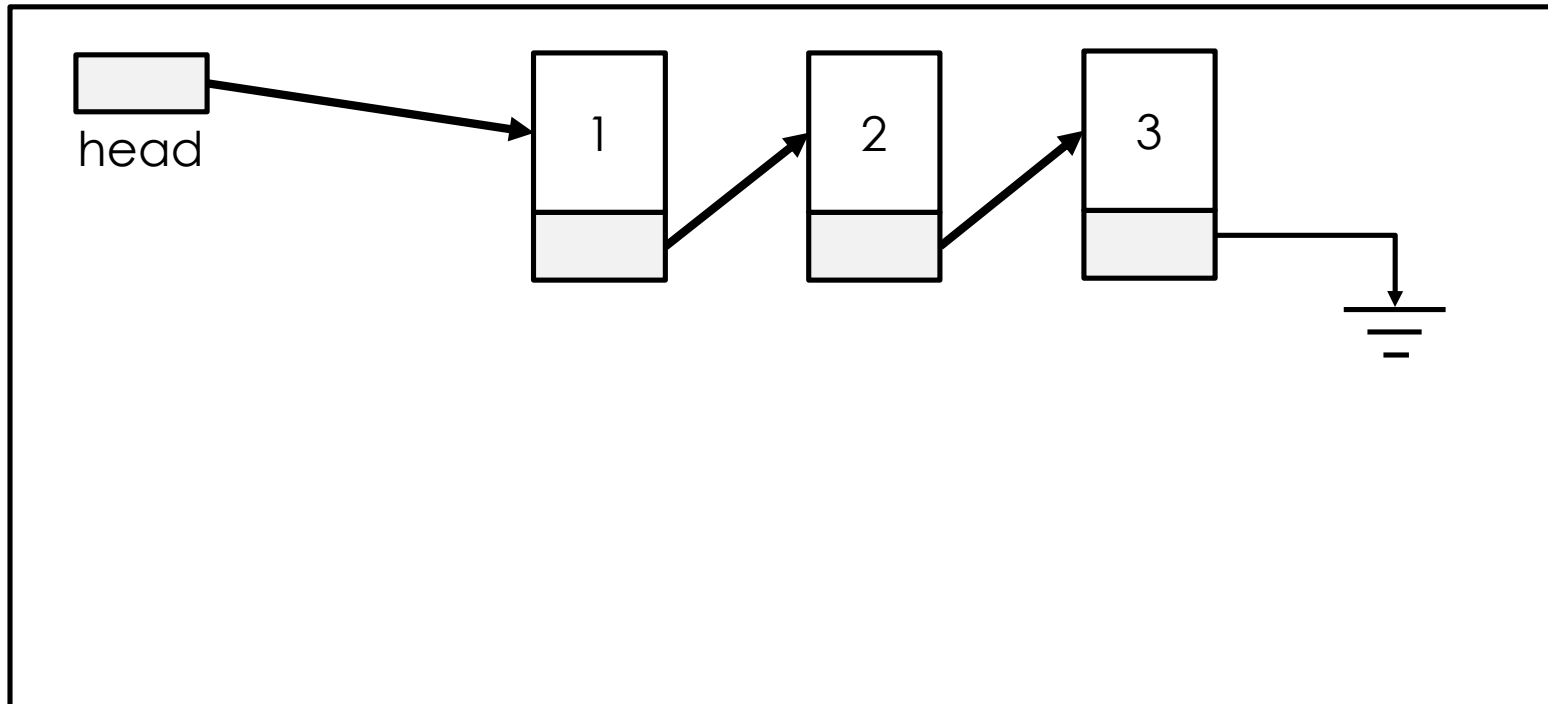
Step 1: Set **head** to point to “the node that the first node points to” or “the second node”



PopFront operation

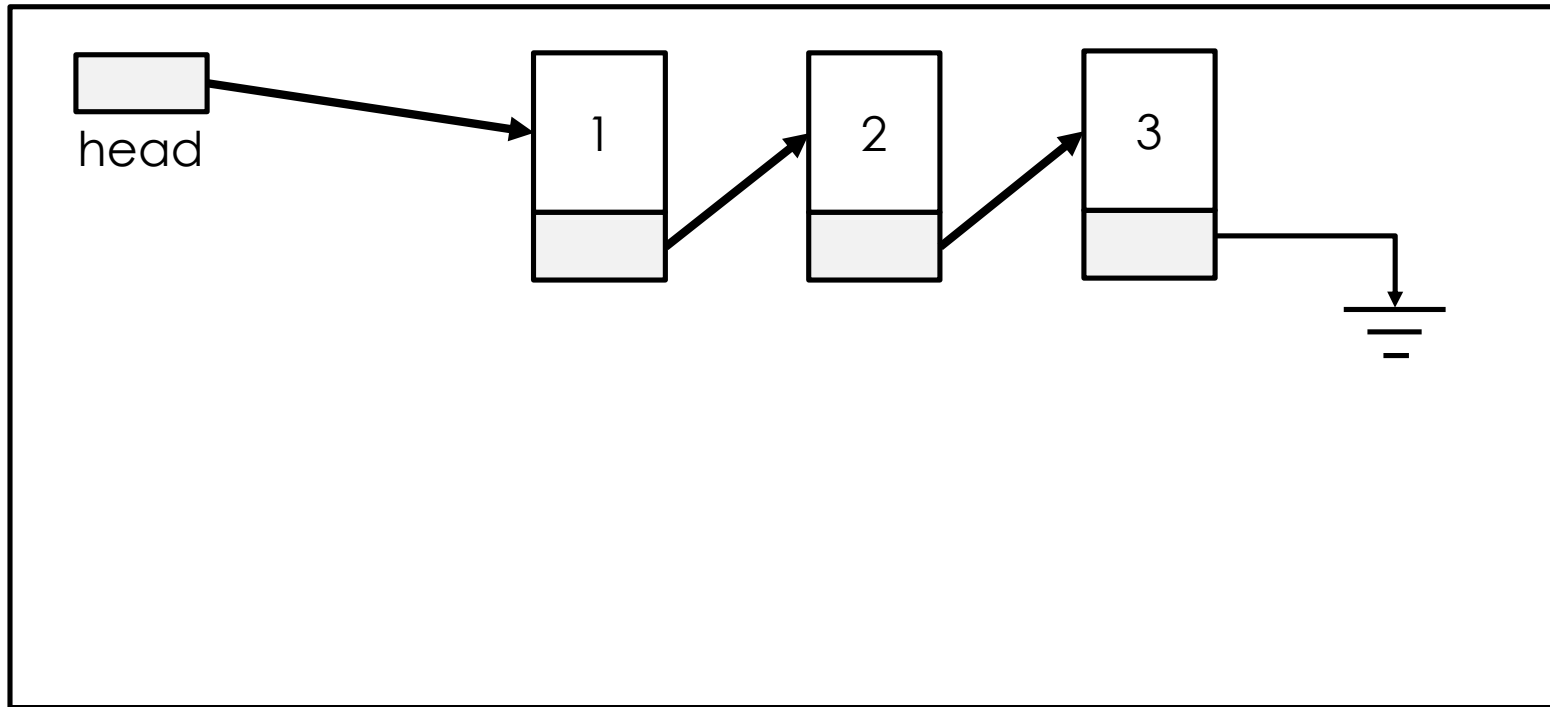
Step 2: Delete the first node

- In C#, the *Garbage Collection Module* will automatically mark and delete any objects that are not referenced
- In C++, you need to manually delete the object using *delete* keyword otherwise there will be “memory leaks”

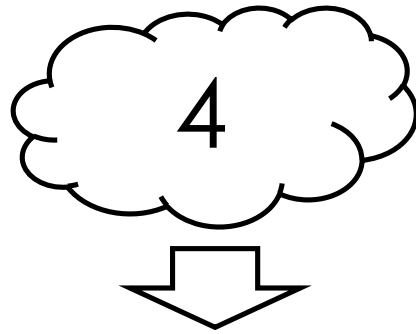


PopFront operation

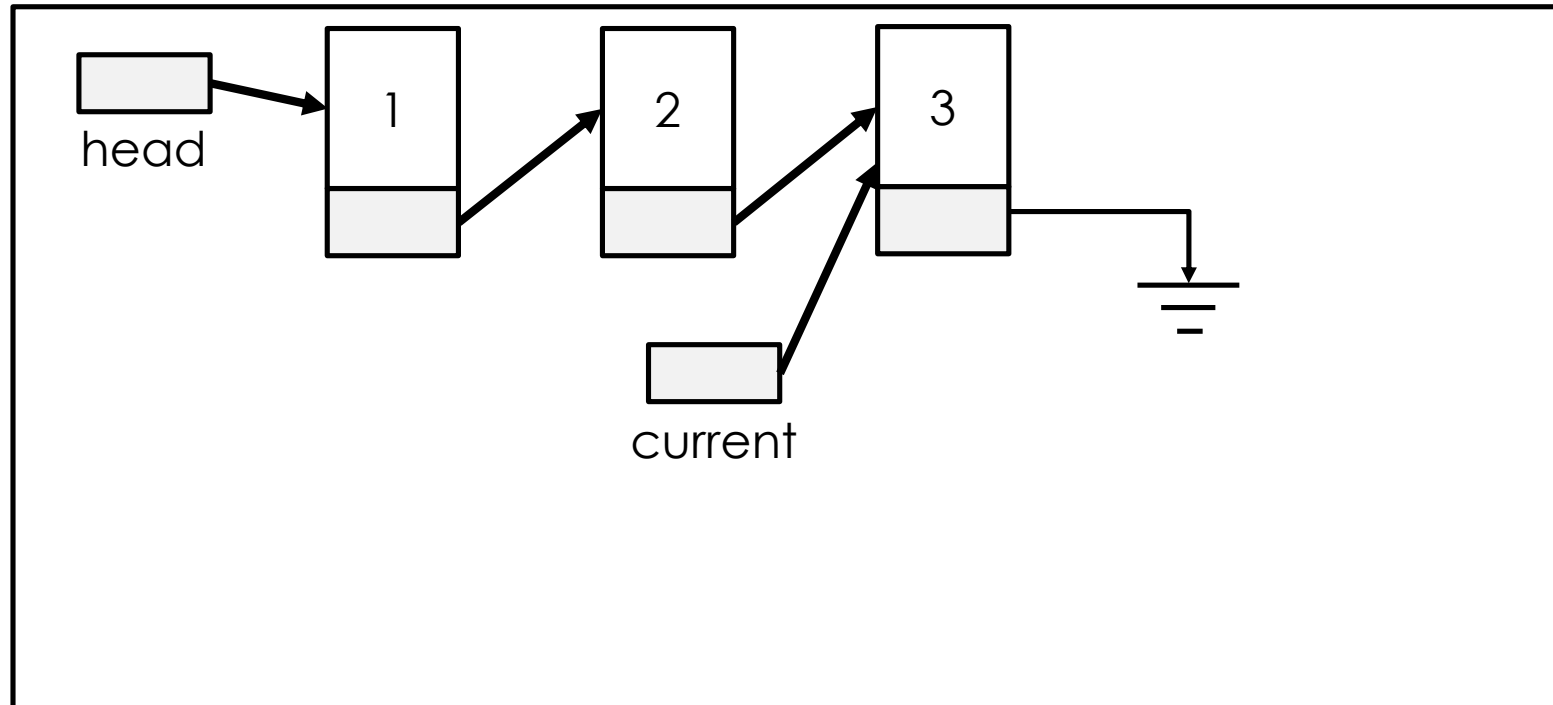
What is the Big O?
 $O(1)$



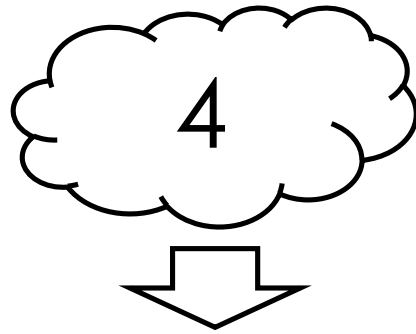
PushBack Operation



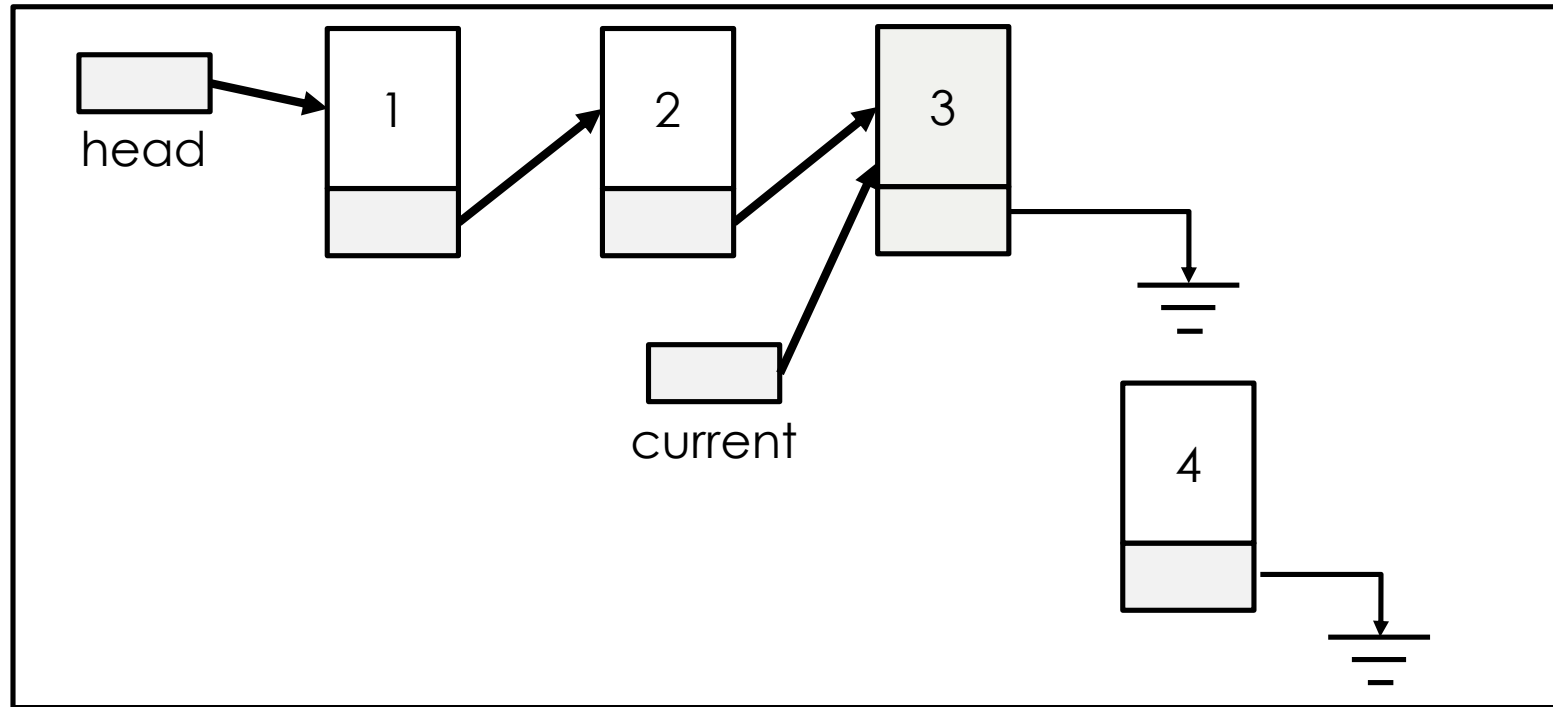
Step 1: Find the last node; start from **head**



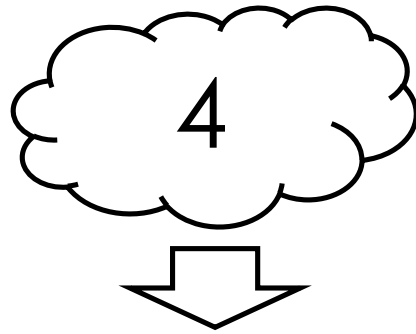
PushBack Operation



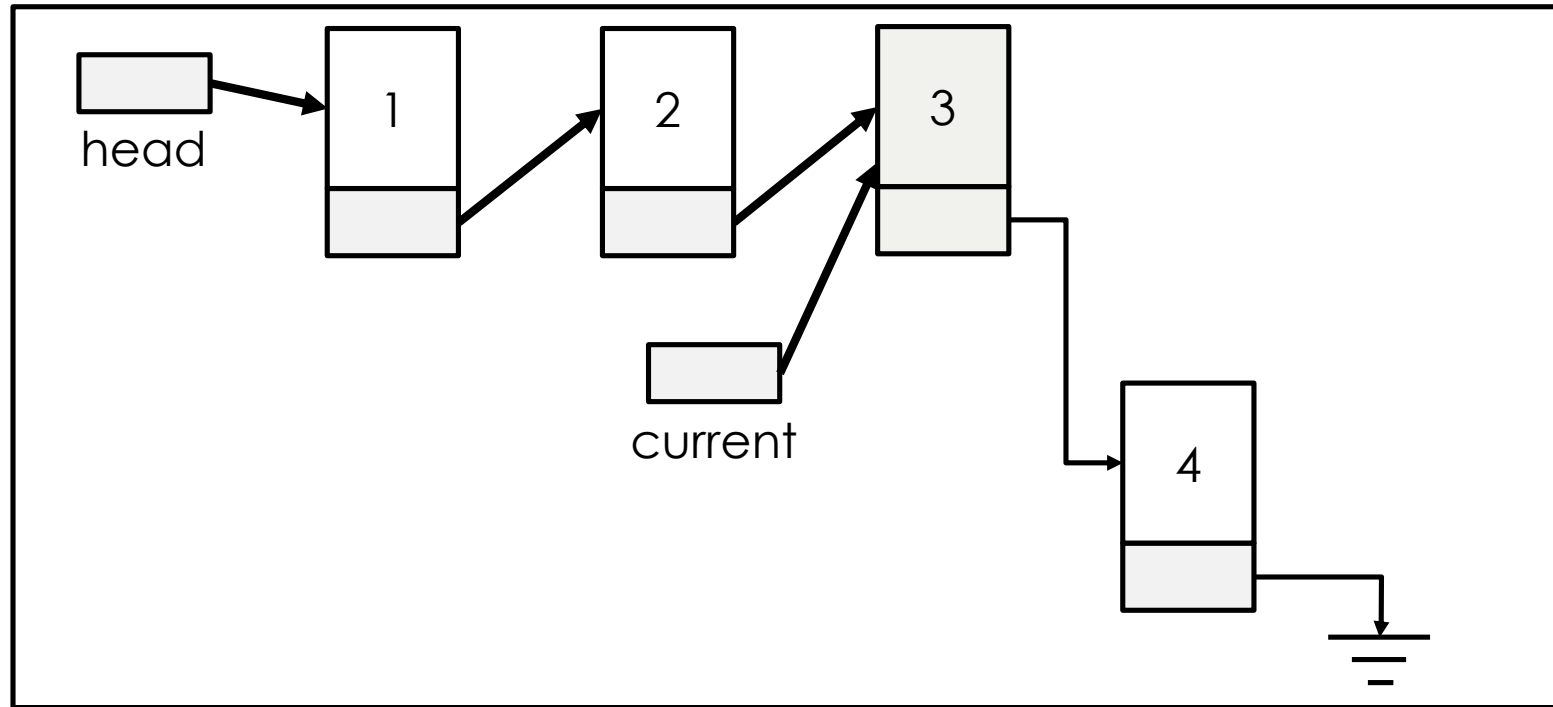
Step 2: Create a node that contains “4”



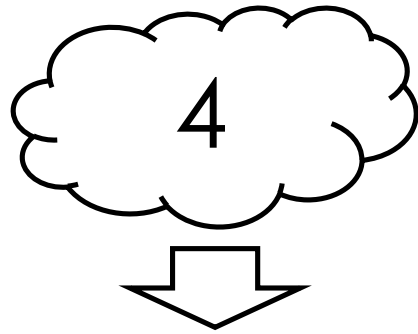
PushBack Operation



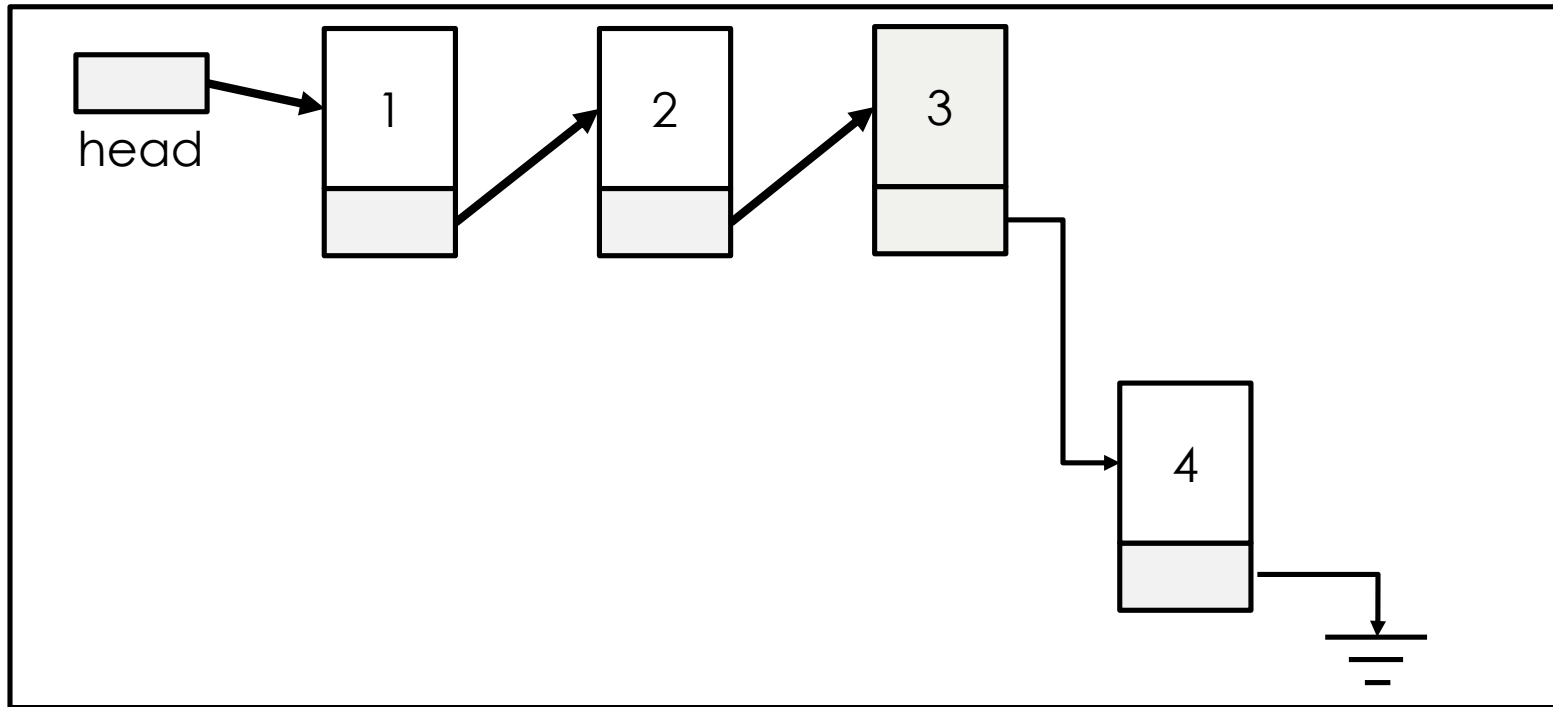
Step 3: Set next pointer of the last node to point to the new node



PushBack Operation

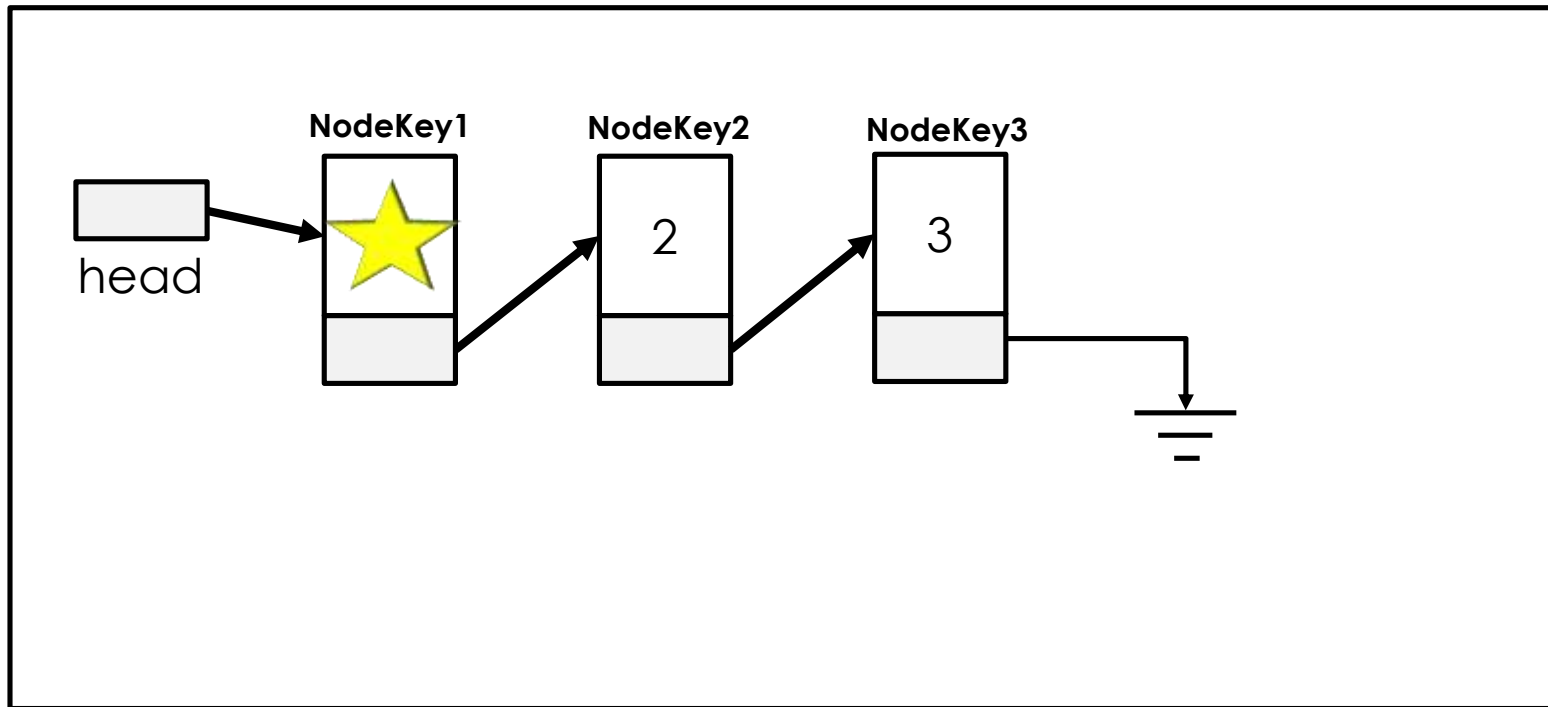


What is the Big O?
 $O(n)$



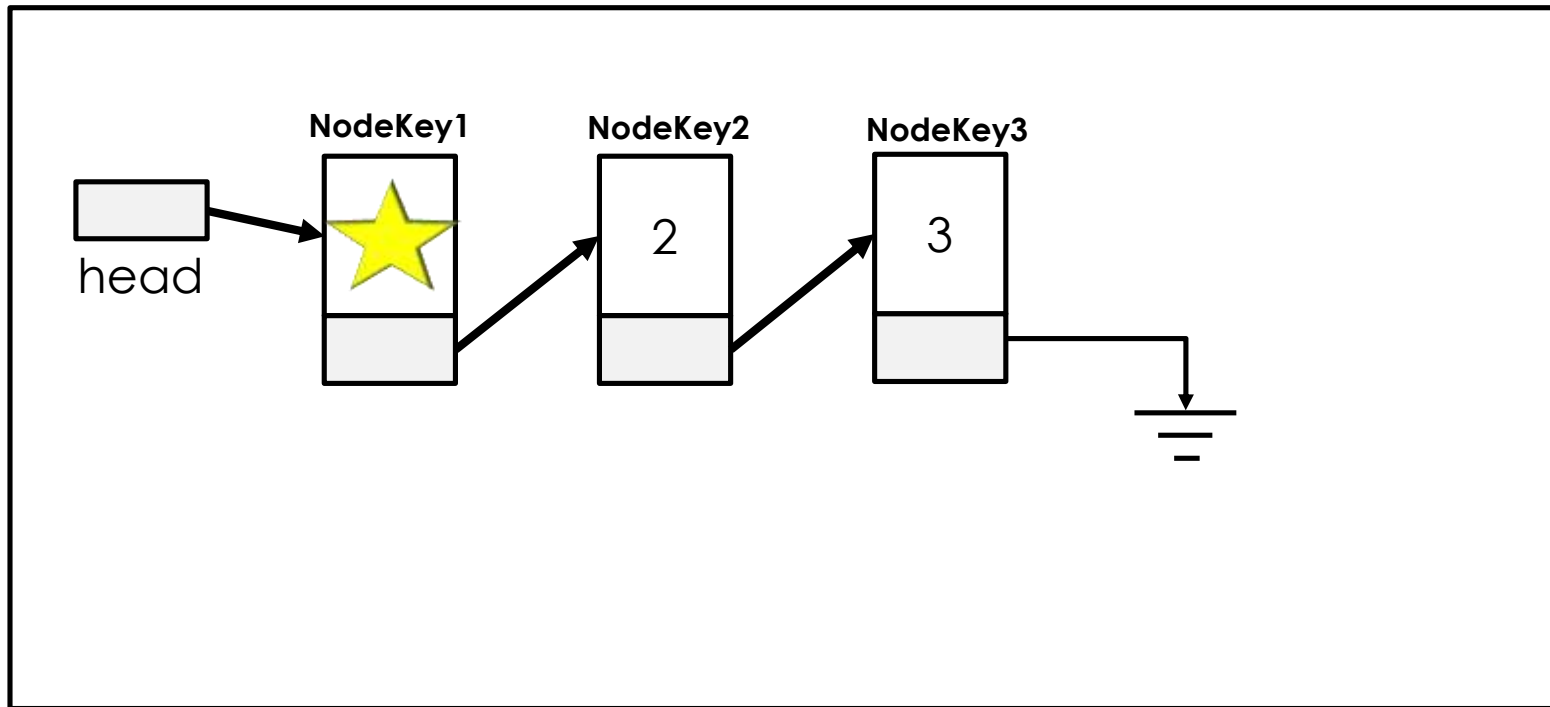
PopBack Operation

Step 1: Start from **head**, check if the next node (NodeKey1) points to *null* or not



PopBack Operation

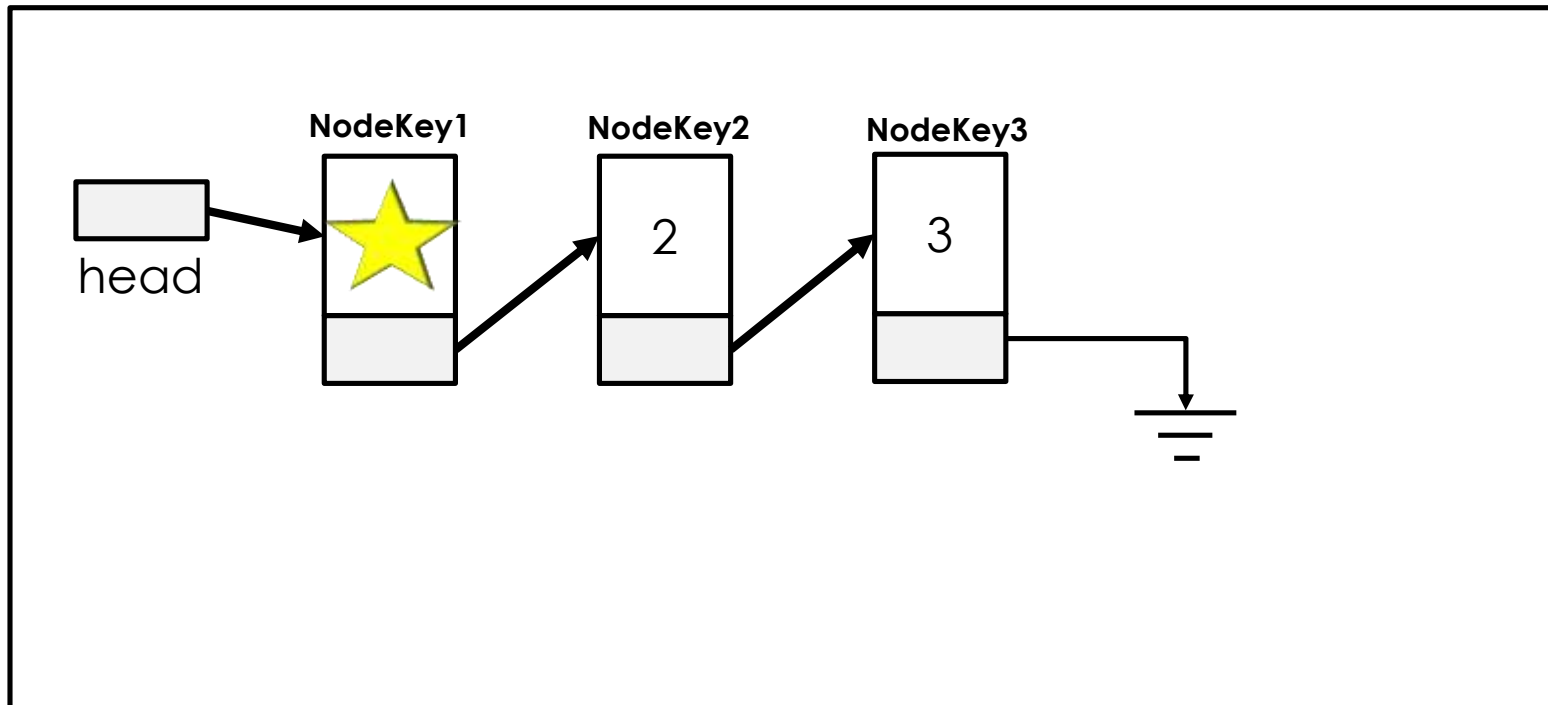
Step 2: If not, move to the next node (NodeKey1).



PopBack Operation

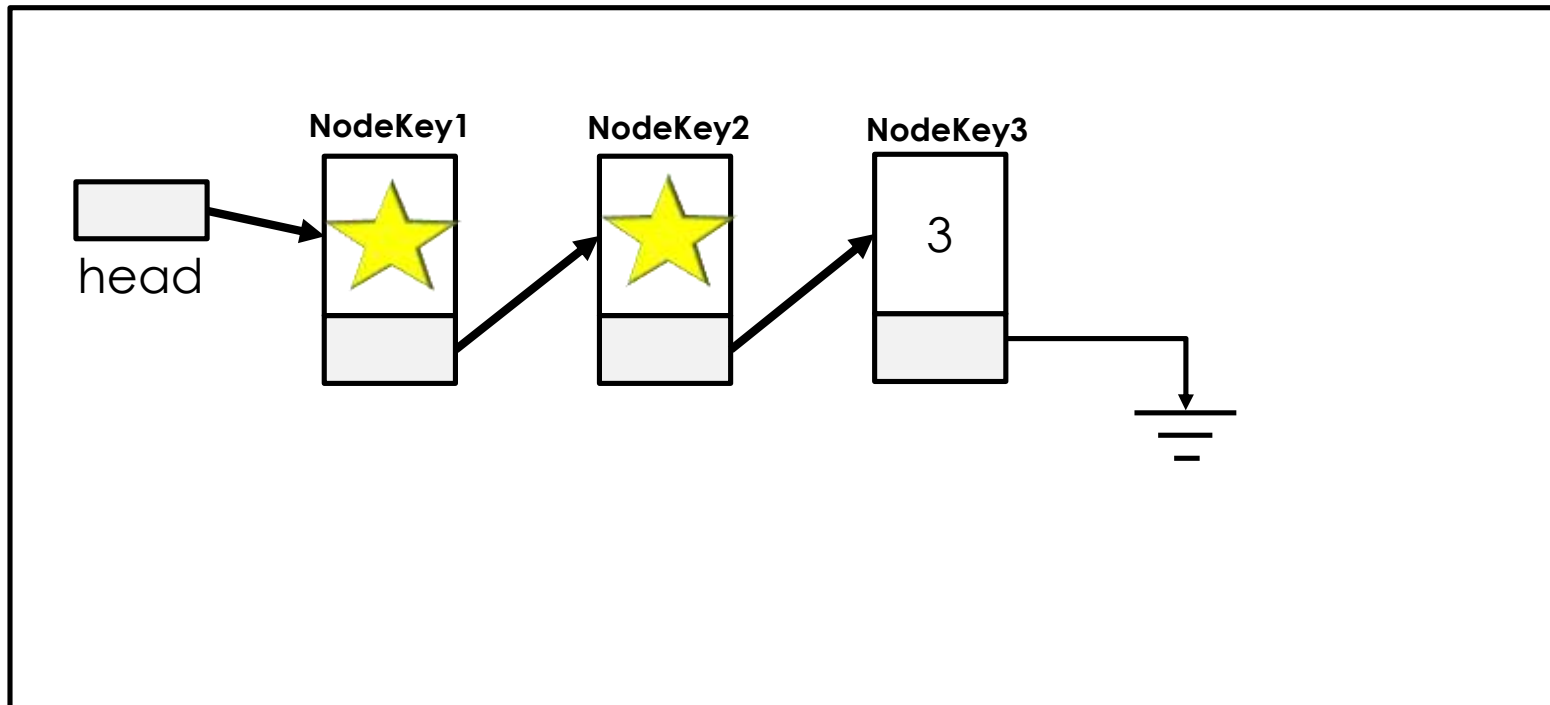
Step 2: Repeat the process.

Check if the next node (NodeKey2) points to *null* or not?



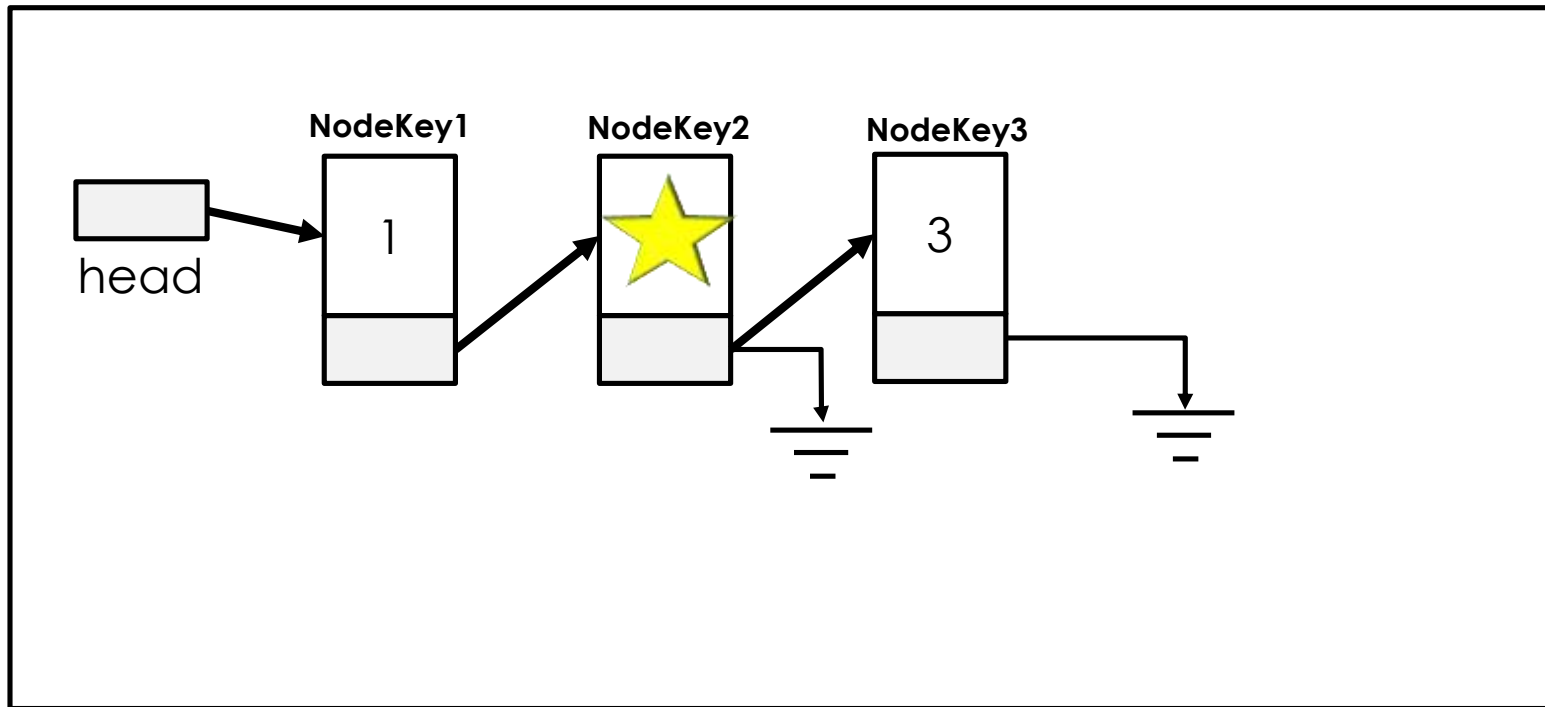
PopBack Operation

Step 2: If not, repeat the process.
Move and then check if the next node (NodeKey3)
points to *null* or not?



PopBack Operation

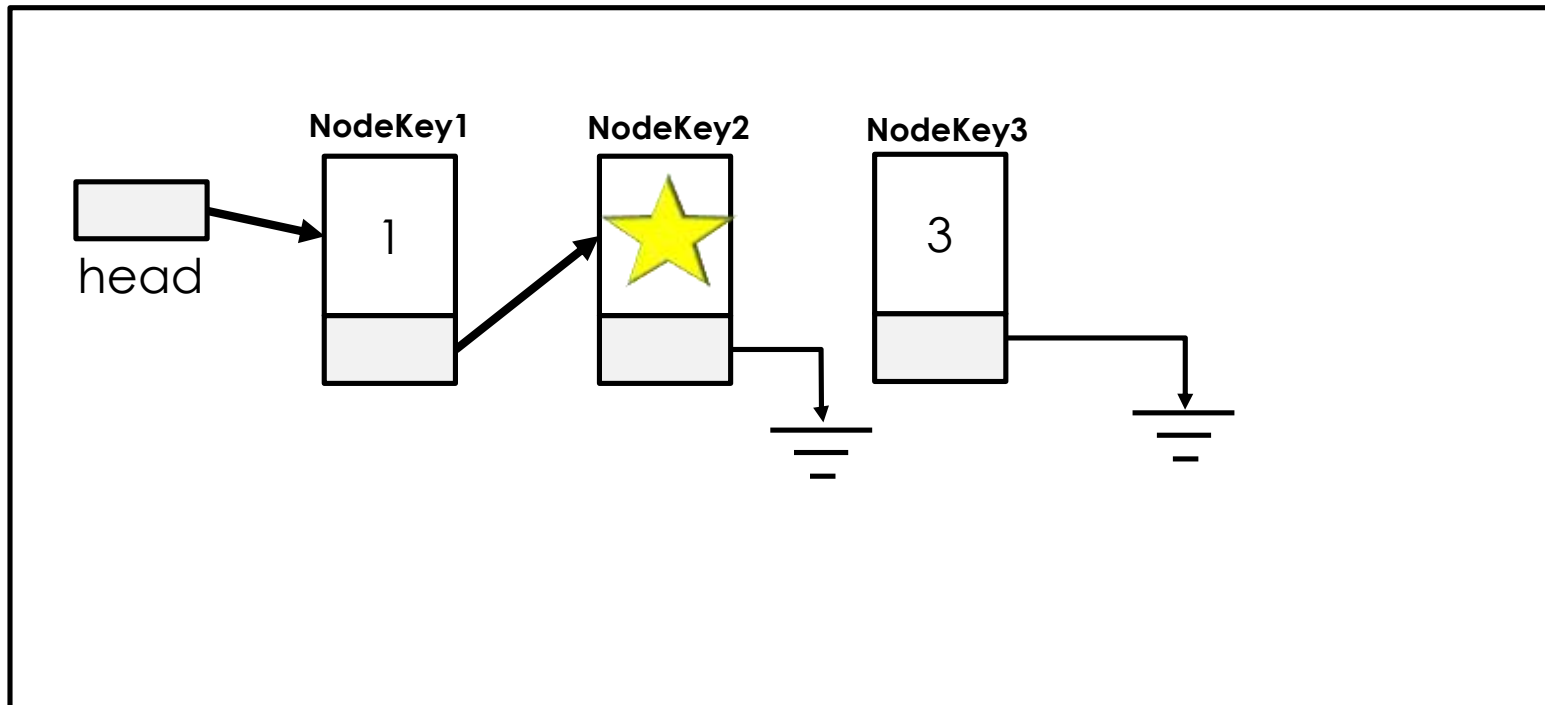
Step 2: If the next node (NodeKey3) points to *null*, set the current next pointer to *null*



PopBack Operation

Step 2: Free NodeKey3

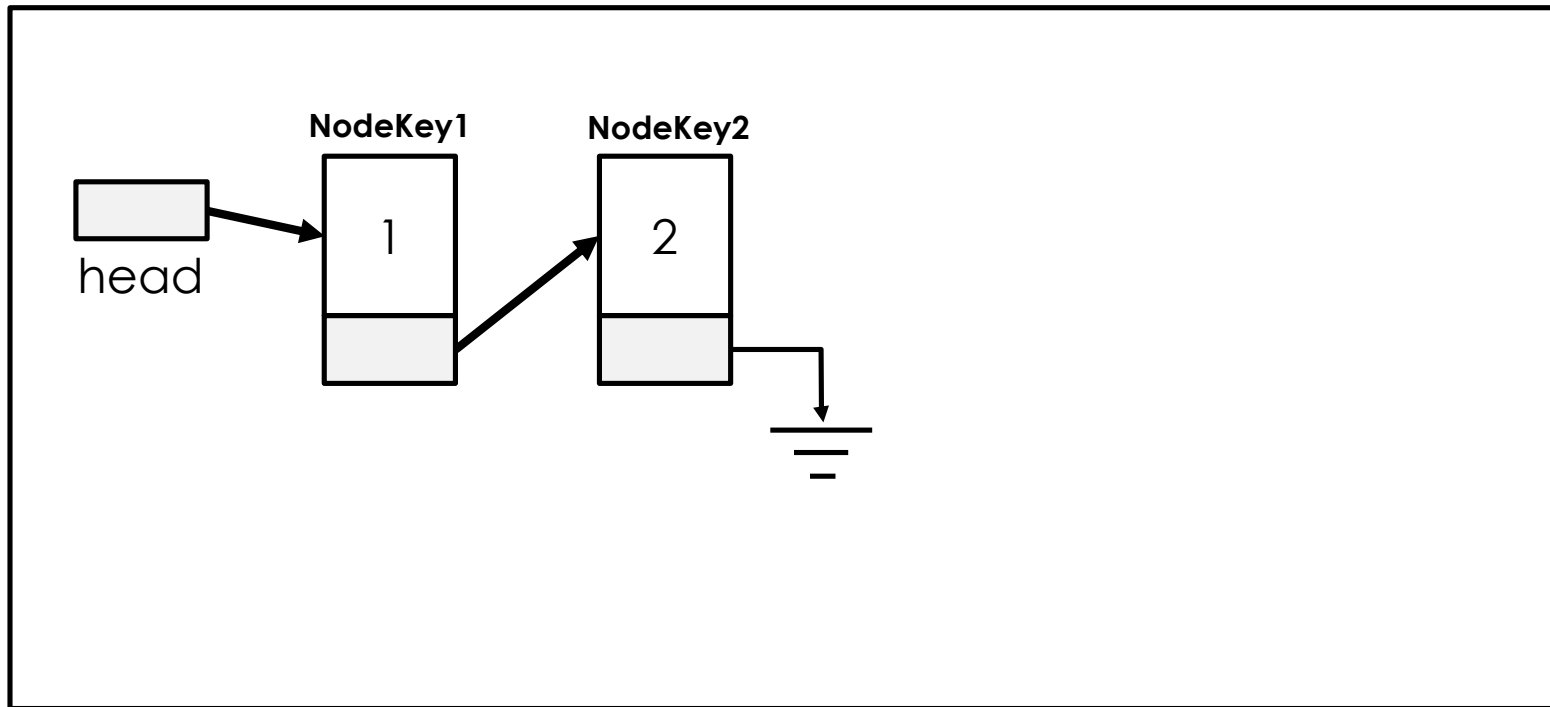
In C#, it will be automatically cleared by the .NET Garbage Collection, because it is not referenced by any variables
In C++, you need to clear memory by using *delete* keyword



PopBack Operation

What is the Big O?

$O(n)$

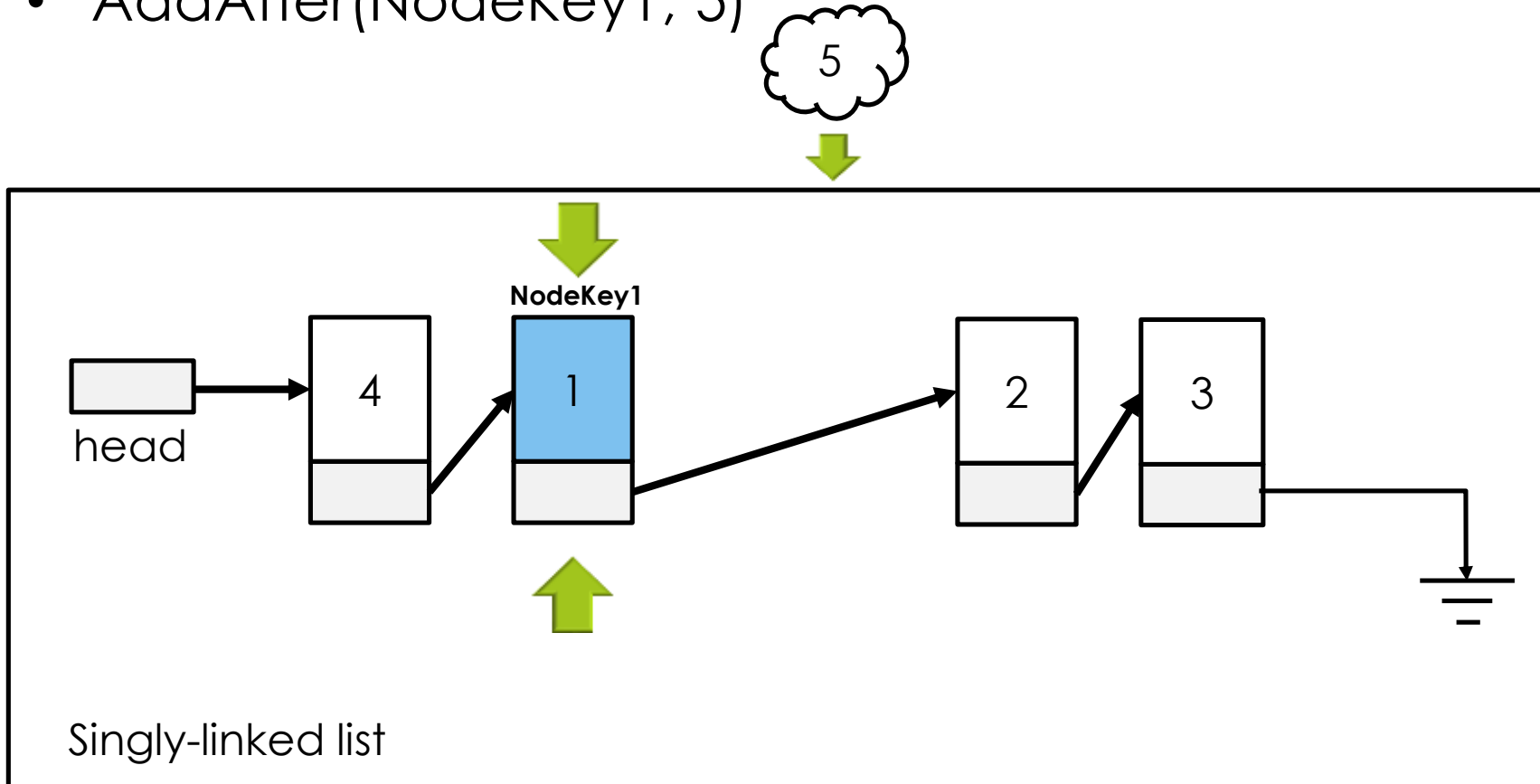


List Application Programming Interface

■ PushFront(Key)	add to front
■ PushBack(Key)	add to back
■ Key PopFront()	remove front item
■ Key PopBack()	remove back item
■ Key TopFront()	return front item
■ Key TopBack()	return back item
■ Boolean Find(Key)	is key in list?
■ Erase(Key)	remove key front list
■ Empty()	empty list?
■ AddBefore(Node, Key)	Add key before node
■ AddAfter(Node, Key)	Add key after node

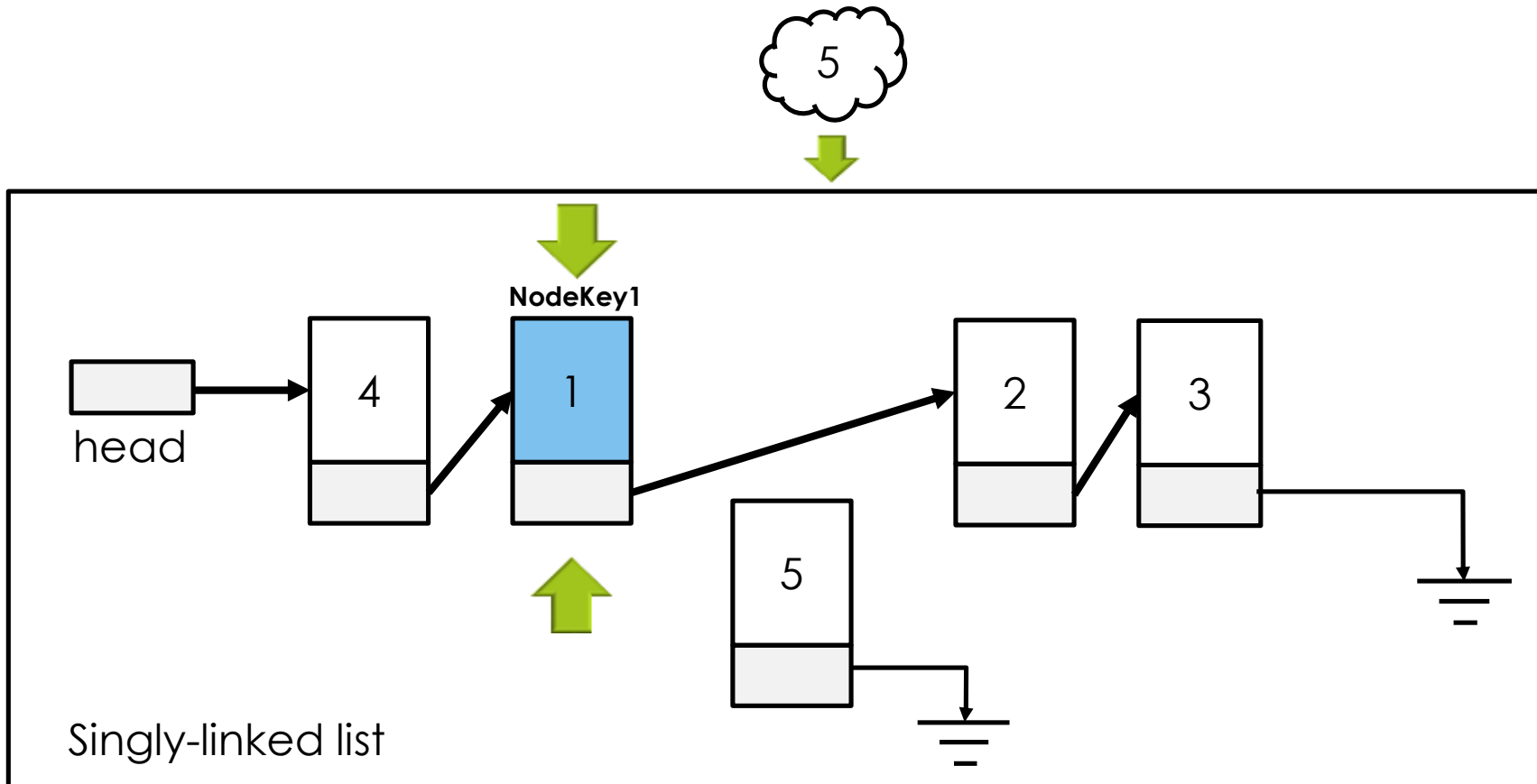
AddAfter(Node, Key) operation

- Given a node and a key, add another with the key after that node
- AddAfter(NodeKey1, 5)



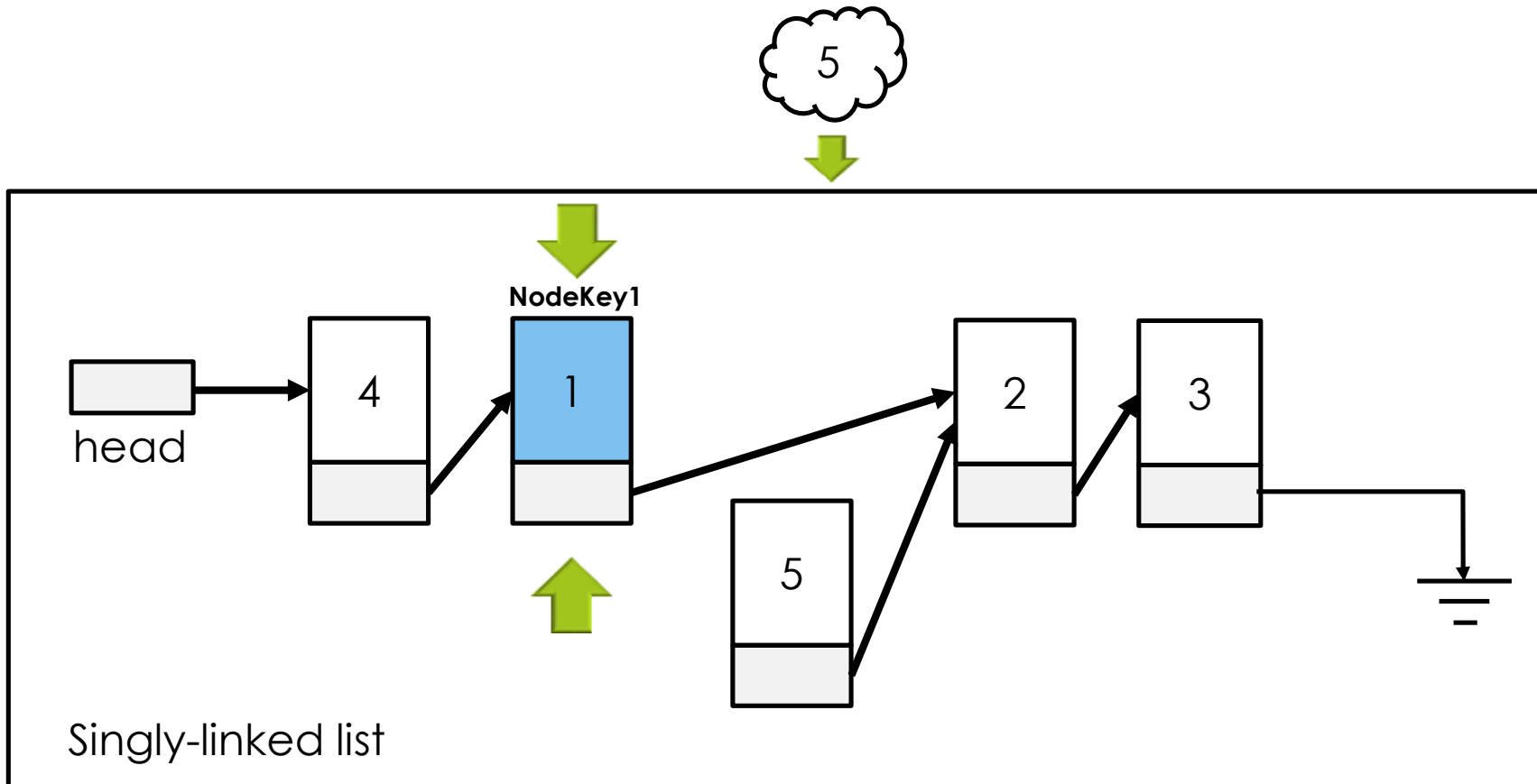
AddAfter(Node, Key) operation

- Step 1: Create a node that contains Key "5"



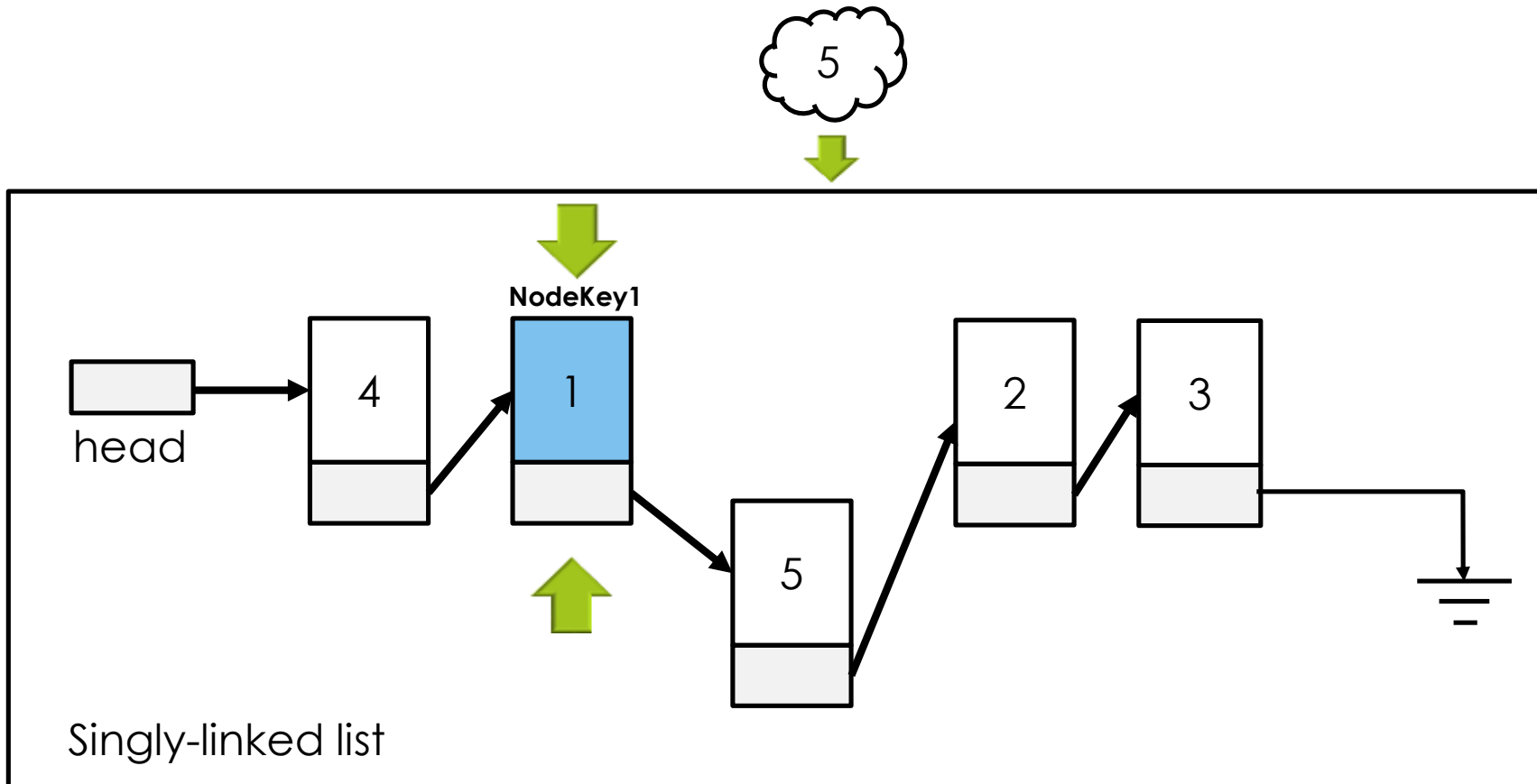
AddAfter(Node, Key) operation

- Step 2: Set pointer of the new node (NodeKey5) to the node pointed by the NodeKey1



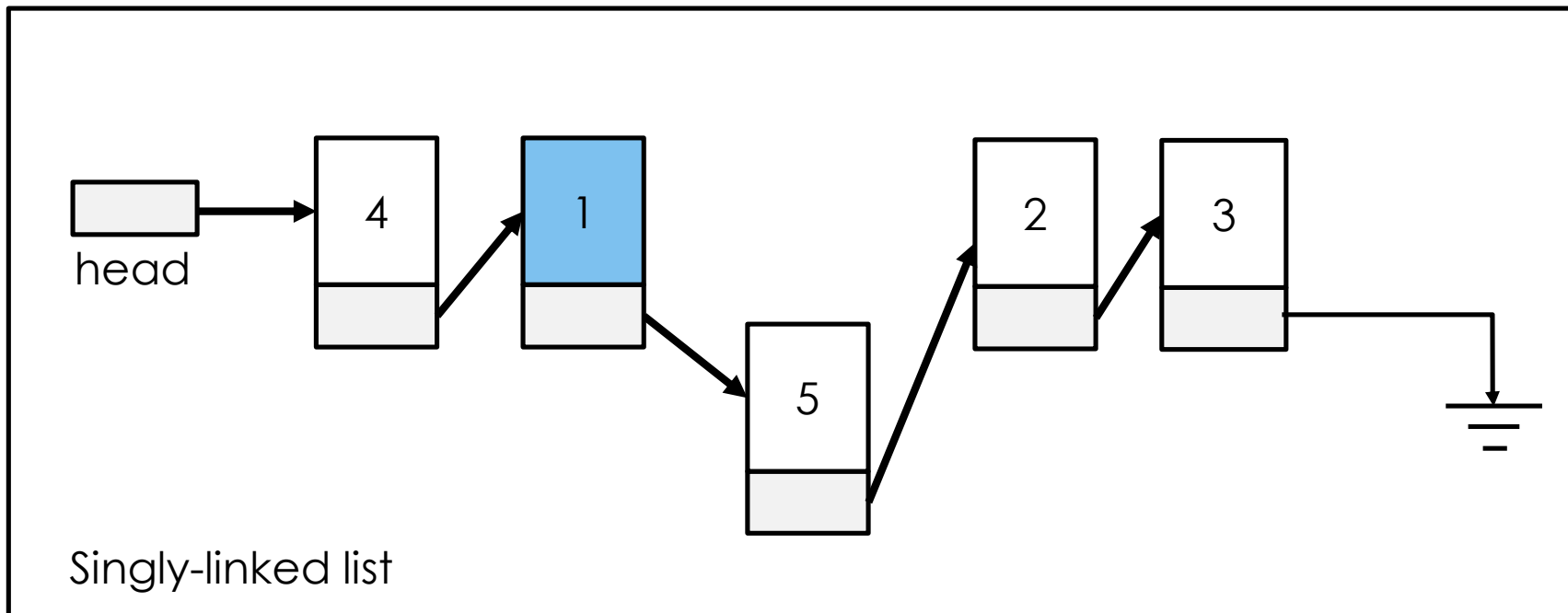
AddAfter(Node, Key) operation

- Step 3: Set pointer of the NodeKey1 to the new node (NodeKey5)



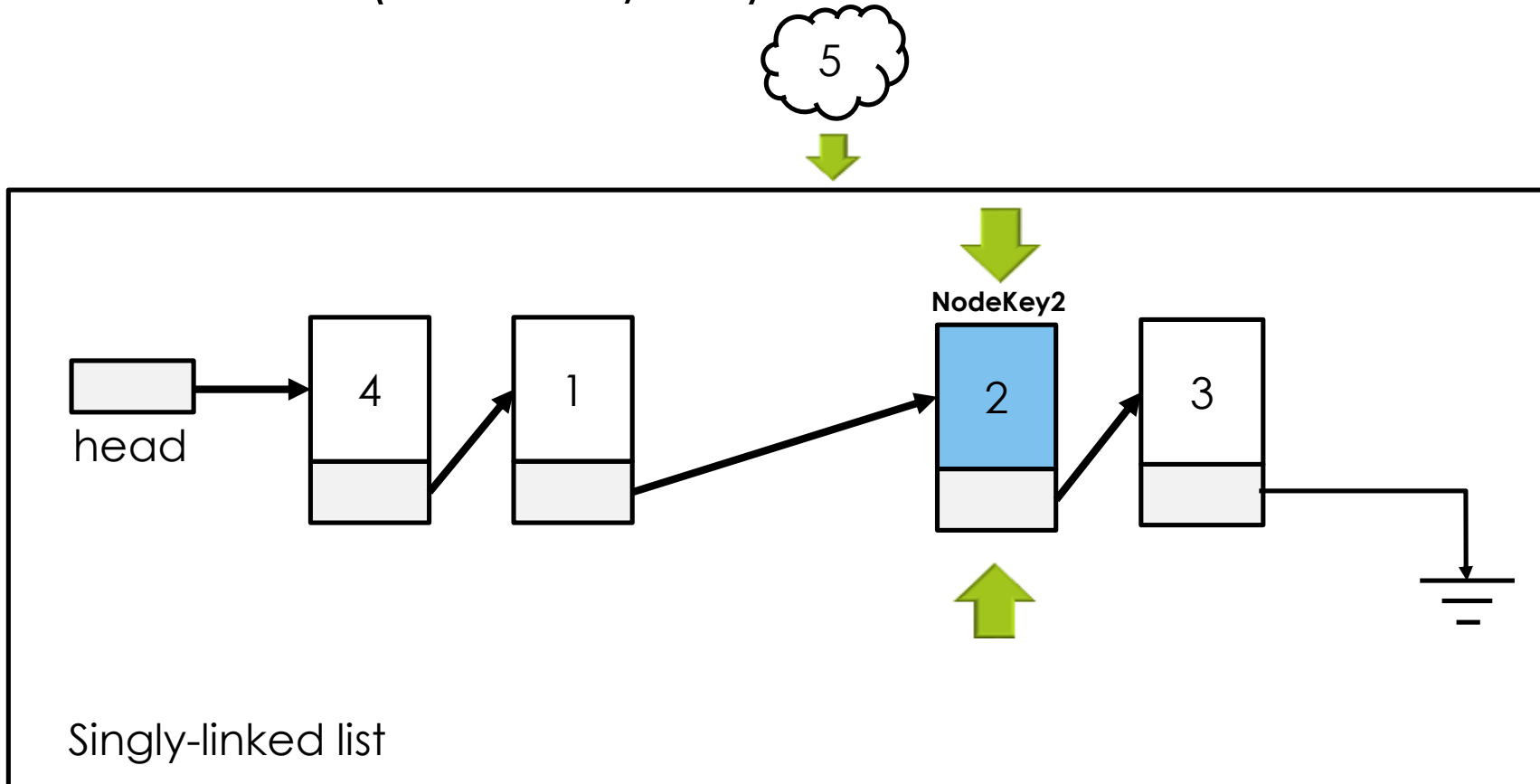
AddAfter(Node, Key) operation

- What is the Big O?
- Ans: $O(1)$
- or $O(n)$ in what case?



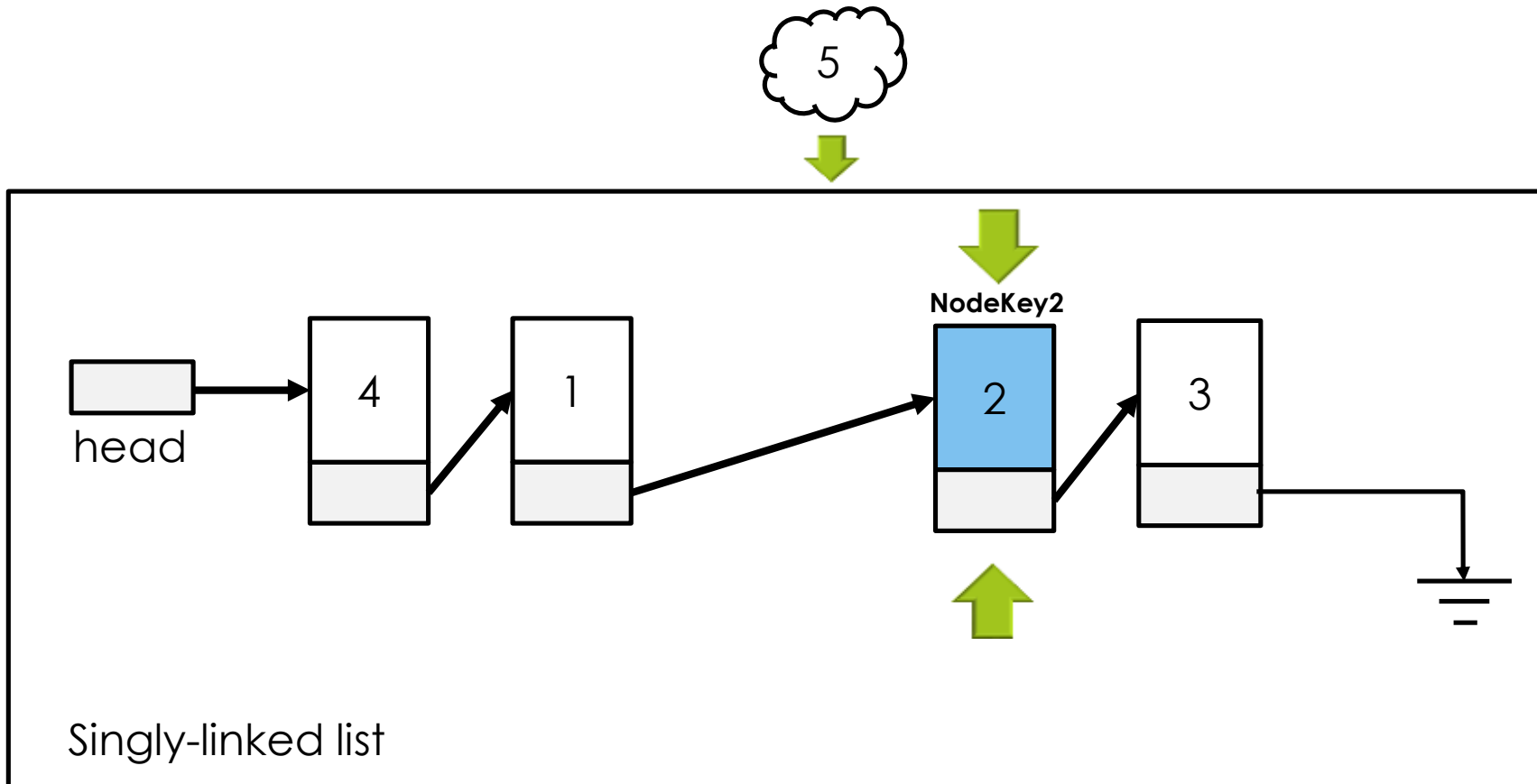
AddBefore(Node, Key) operation

- Given a node and a key, add another with the key before that node
- AddBefore(NodeKey2, 5)



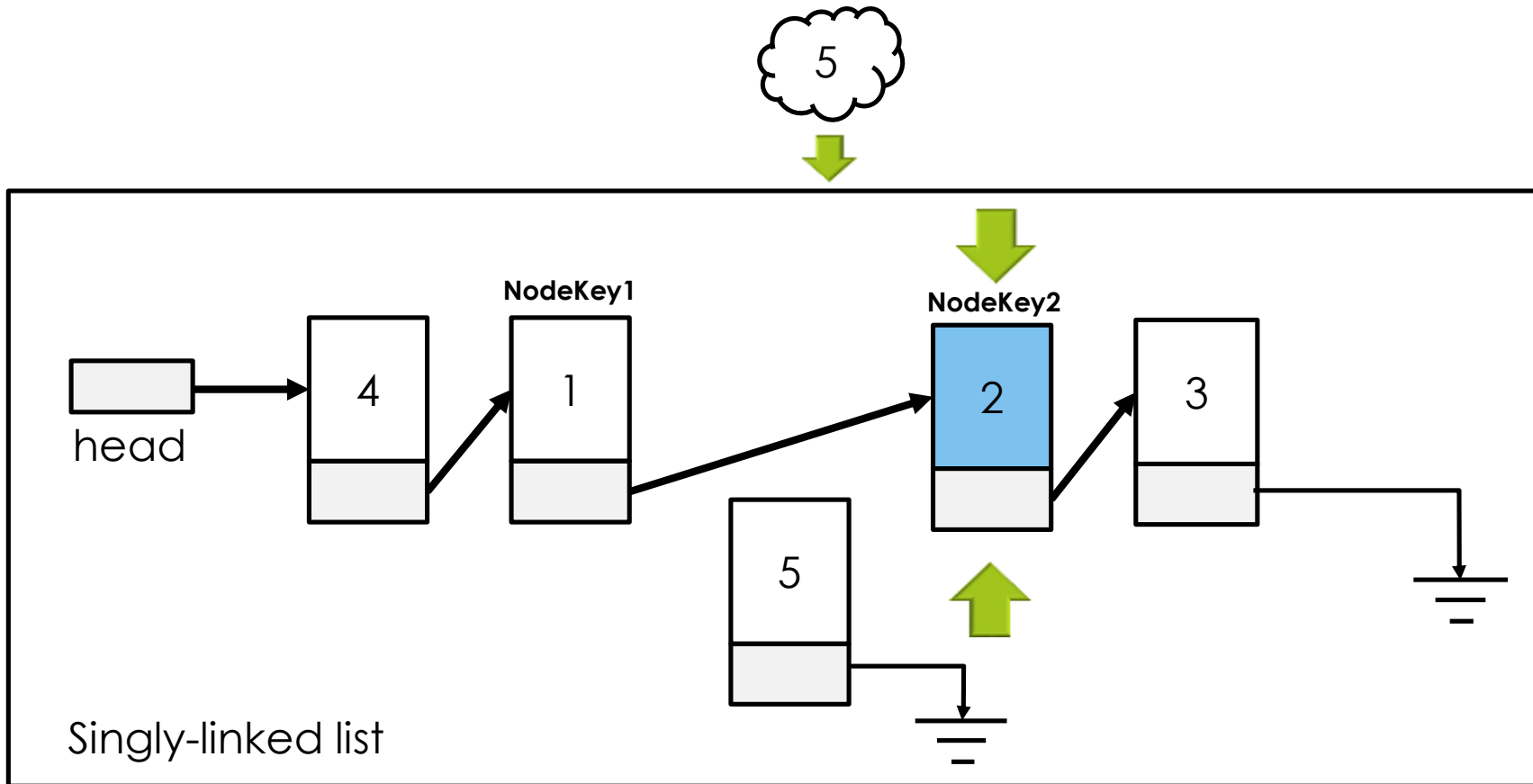
AddBefore(NodeKey2, 5) operation

- Step 1: Start from the head; Go node by node until you find the Node that points NodeKey2



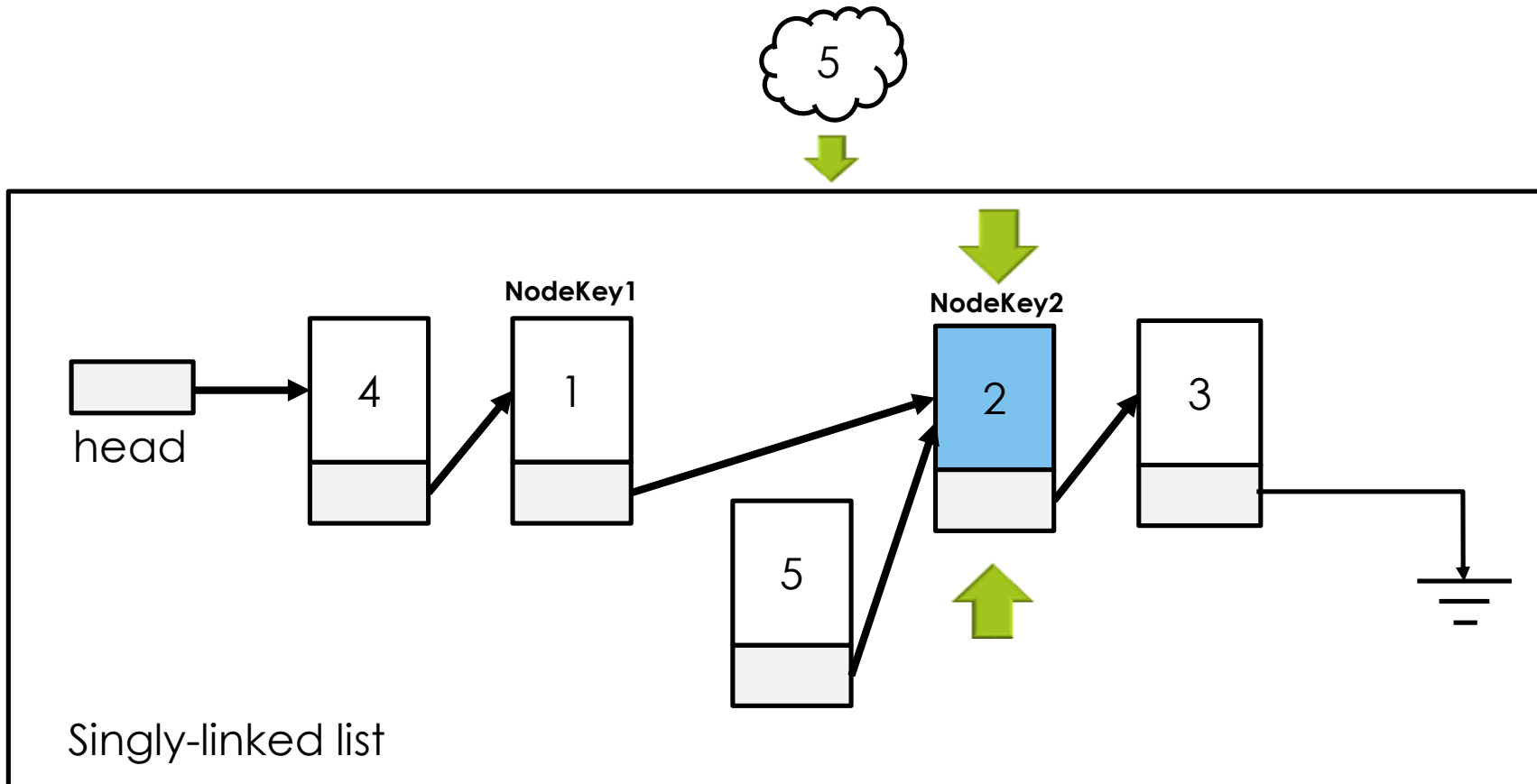
AddBefore(NodeKey2, 5) operation

- Step 2: Create a node that contains Key "5"



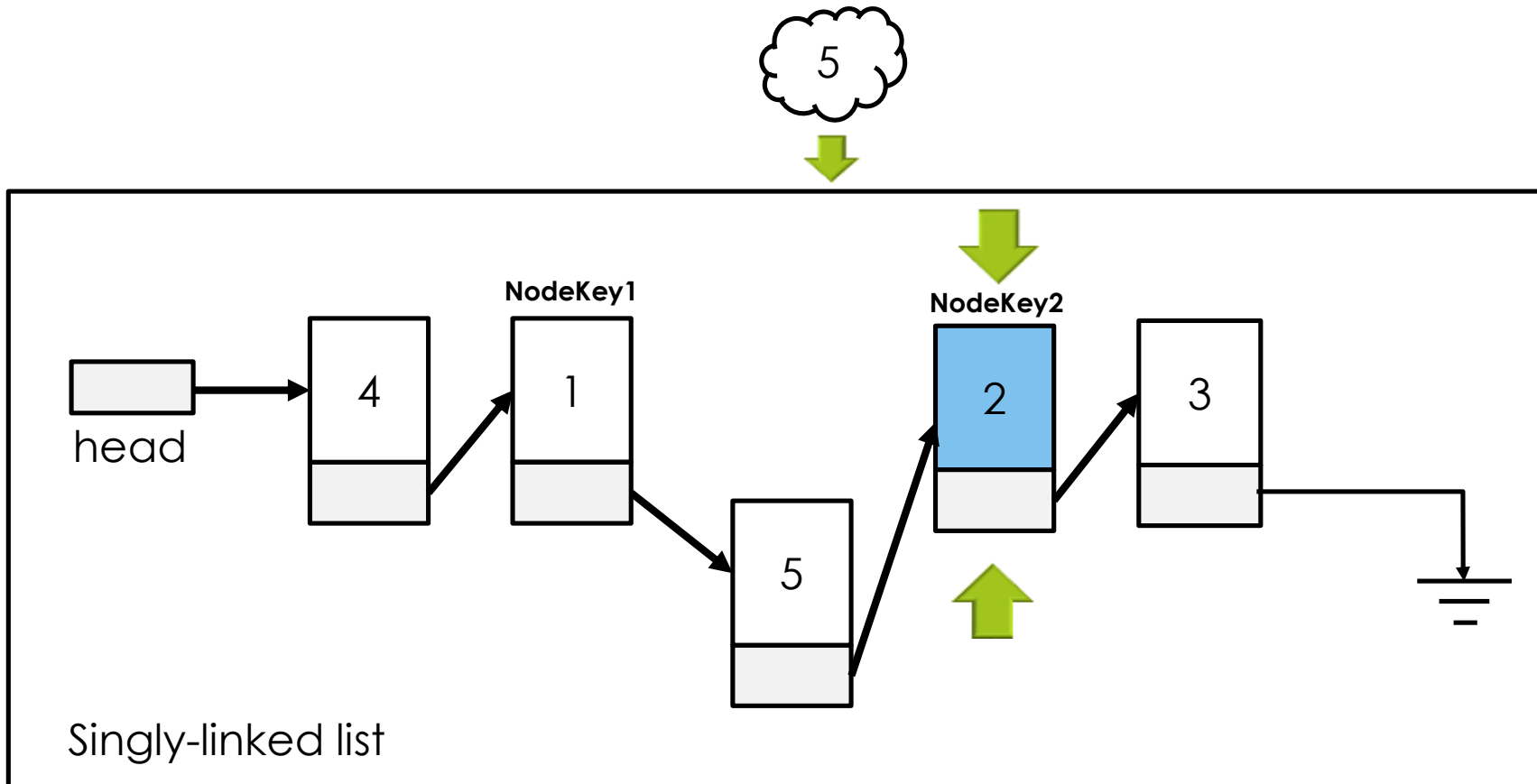
AddBefore(NodeKey2, 5) operation

- Step 3: Set pointer of the new node (NodeKey5) to point to the NodeKey2



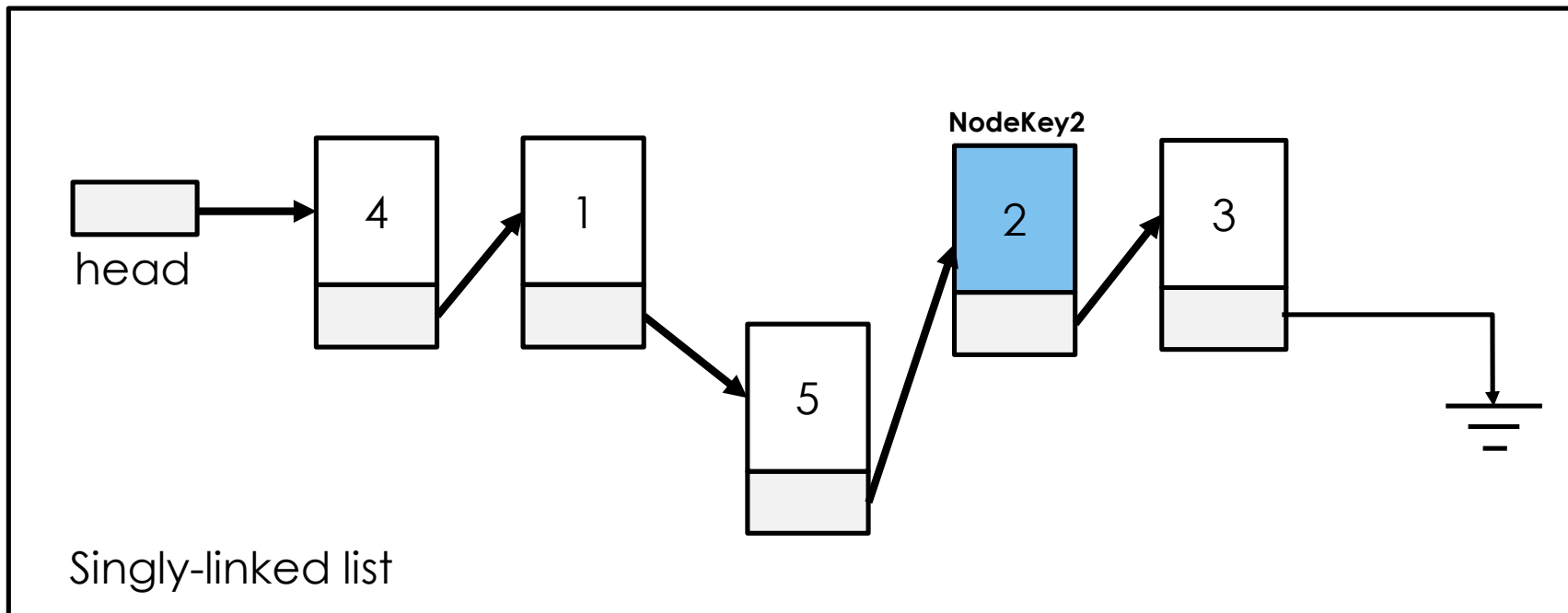
AddBefore(NodeKey2, 5) operation

- Step 4: Set pointer of the NodeKey1 to point to the new node (NodeKey5)



AddBefore(NodeKey2, 5) operation

- What is the Big O?
- Ans: $O(n)$



Running Time

Singly-linked list operations

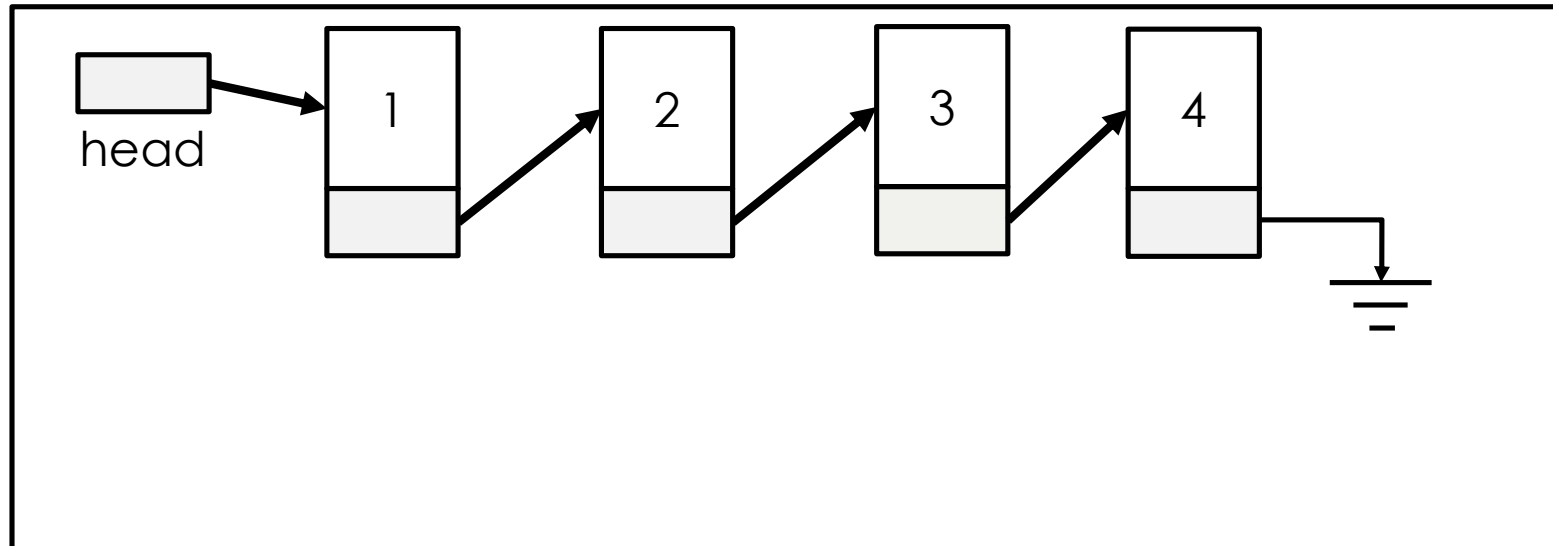
Running time

PushFront (Key)	$O(1)$	What if you are allowed to modify the linked-list in order to improve the performance, what will you do?
TopFront()	$O(1)$	
PopFront()	$O(1)$	
PushBack(Key)	$O(n)$	
TopBack()	$O(n)$	
PopBack()	$O(n)$	
Find(Key)	$O(n)$	
Erase(Key)	$O(n)$	
Empty()	$O(1)$	
AddBefore(Node, Key)	$O(n)$	
AddAfter(Node, Key)	$O(1)$	

How to improve PushBack, TopBack, and PopBack operations?

The current complexity is $O(n)$

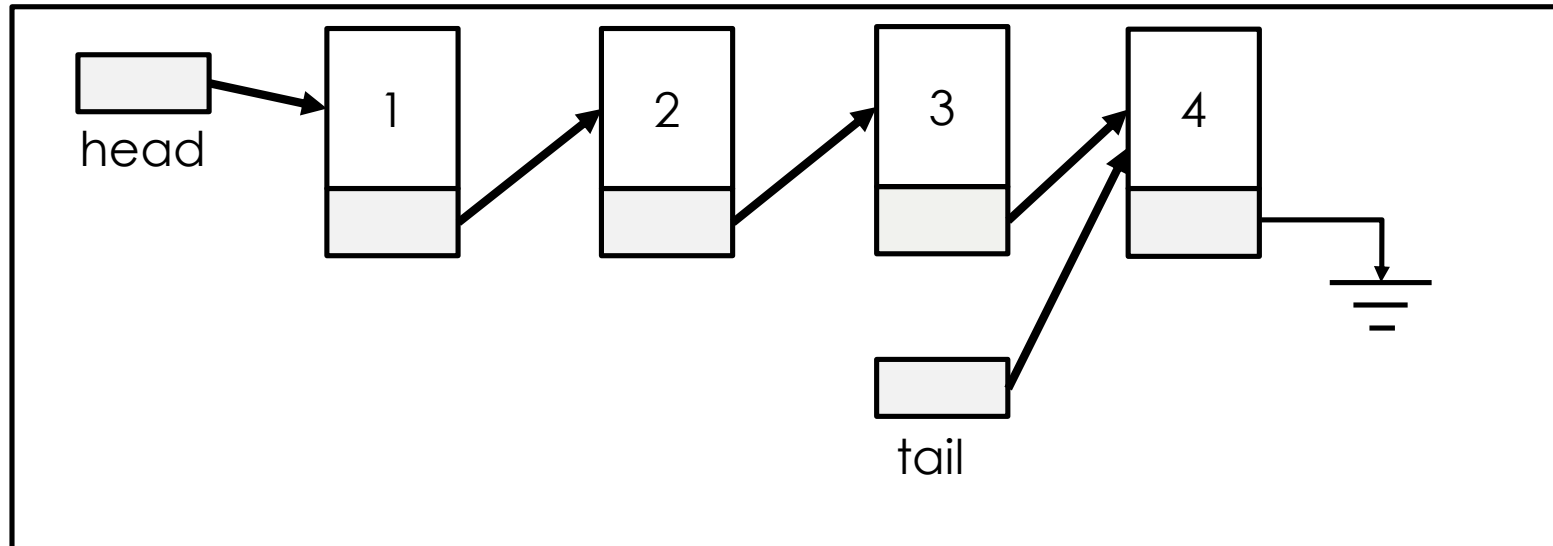
Assume you can add another variable to the structure



How to improve PushBack, TopBack, and PopBack operations?

The current complexity is $O(n)$

Assume you can add another variable to the structure

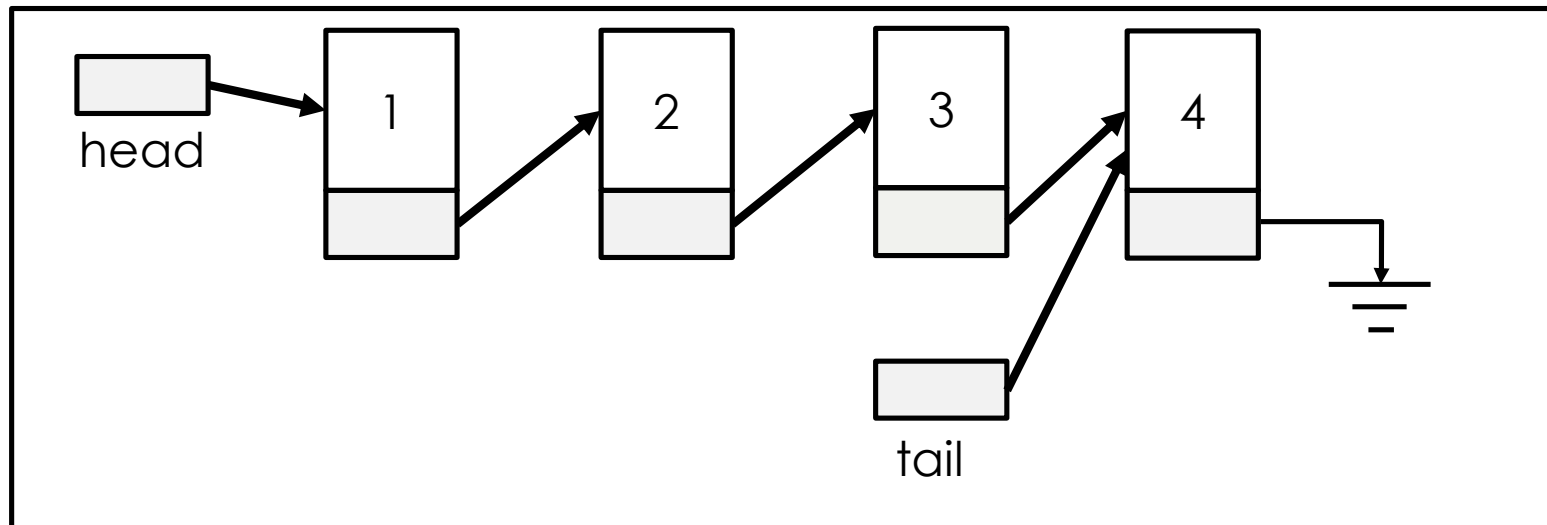


How to improve PushBack, TopBack, and PopBack operations?

PushBack(Key); Key TopBack(); PopBack();
Show Steps how these function works with **tail** variable?

What is the complexity of those operations after adding **tail** variable?

Ans: $O(1)$



Running Time with Tail variable

Singly-linked list operations	No tail	With tail
PushFront (Key)	$O(1)$	
TopFront()	$O(1)$	
PopFront()	$O(1)$	
PushBack(Key)	$O(n)$	$O(1)$
TopBack()	$O(n)$	$O(1)$
PopBack()	$O(n)$	$O(n)$
Find(Key)	$O(n)$	
Erase(Key)	$O(n)$	
Empty()	$O(1)$	
AddBefore(Node, Key)	$O(n)$?
AddAfter(Node, Key)	$O(1)$	

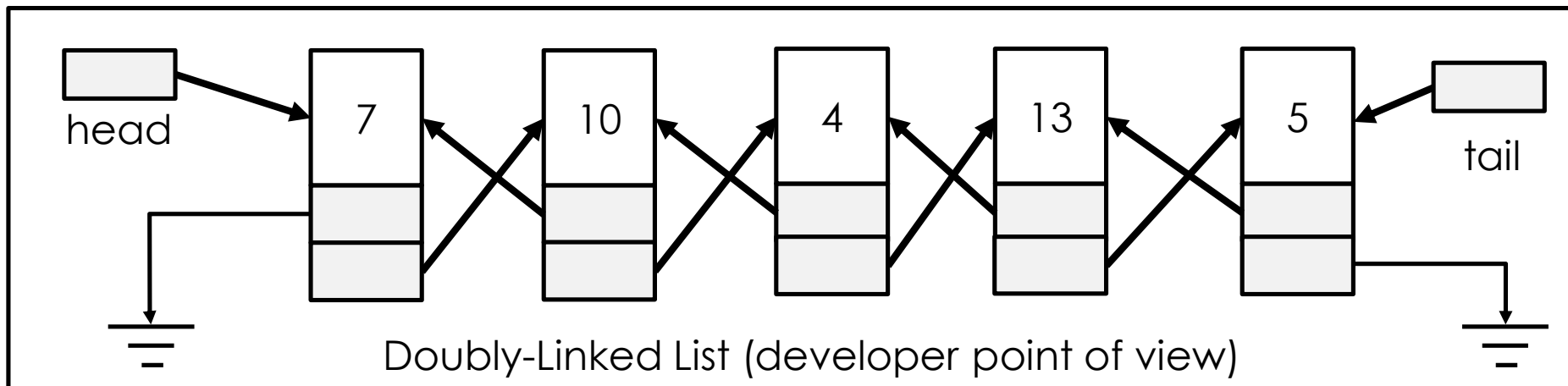
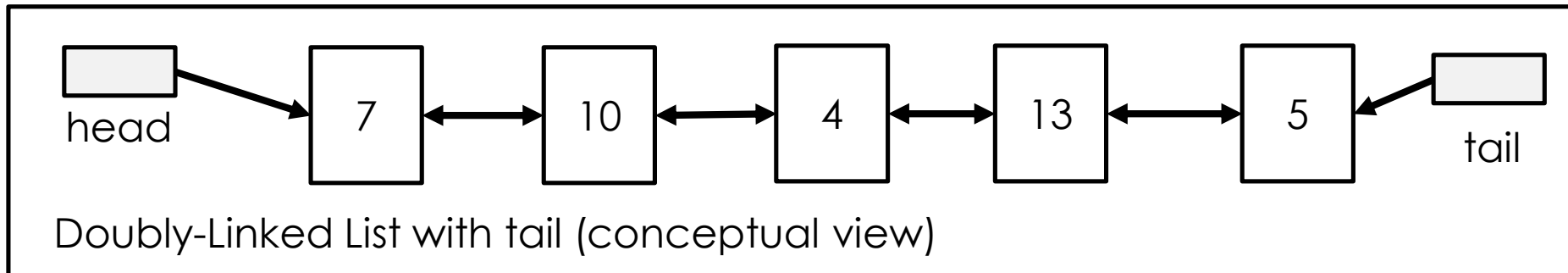
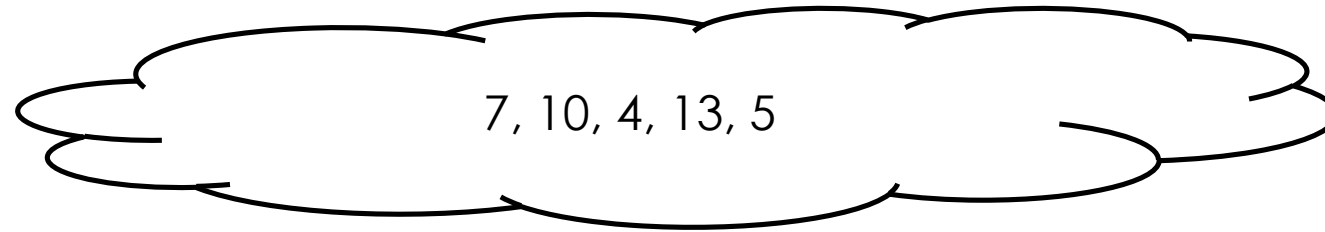


?

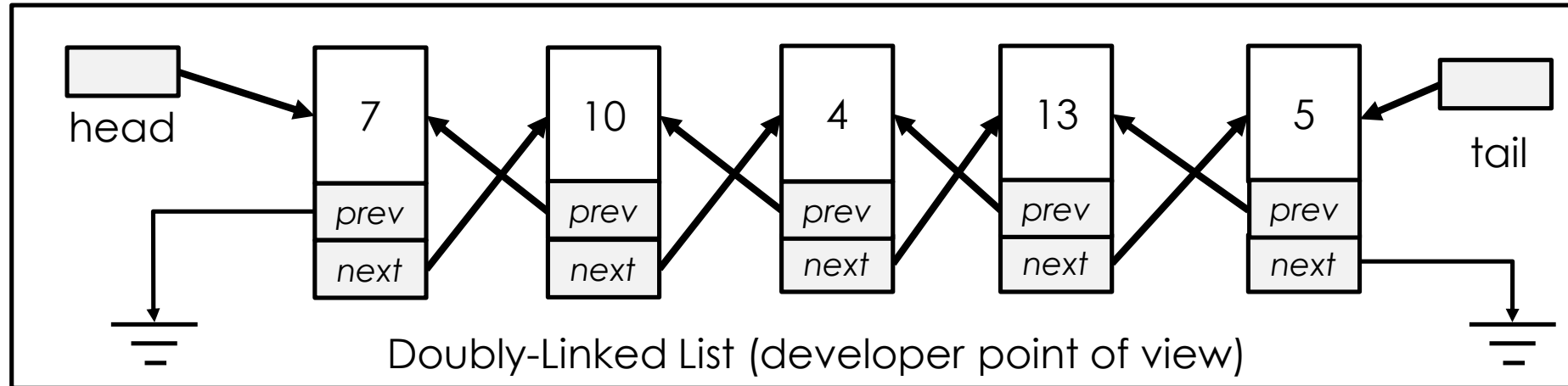
Problem with Singly-linked list

- One-way traveling
 - Go right only
 - Given a node, we always know who is on the right
 - So AddAfter is super fast
 - But AddBefore is much slower because we do not know who is on the left (we must start from the beginning)
- Solution?
- Doubly-linked list

Doubly-linked List with Tail



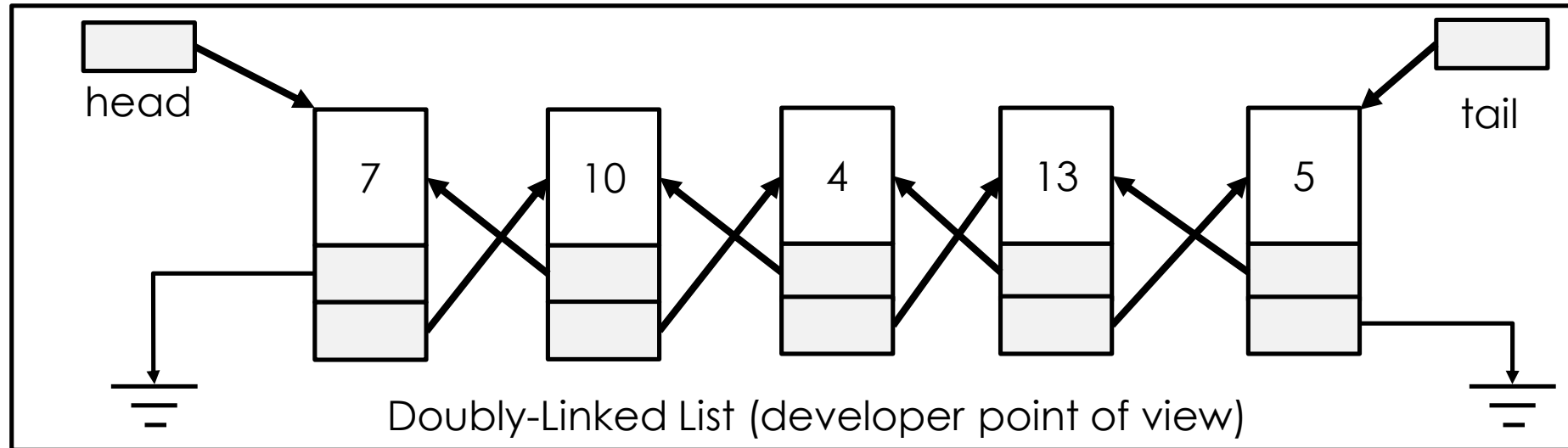
Doubly-linked List with Tail



Node contains

- **key**
- **next** pointer
- **prev** pointer

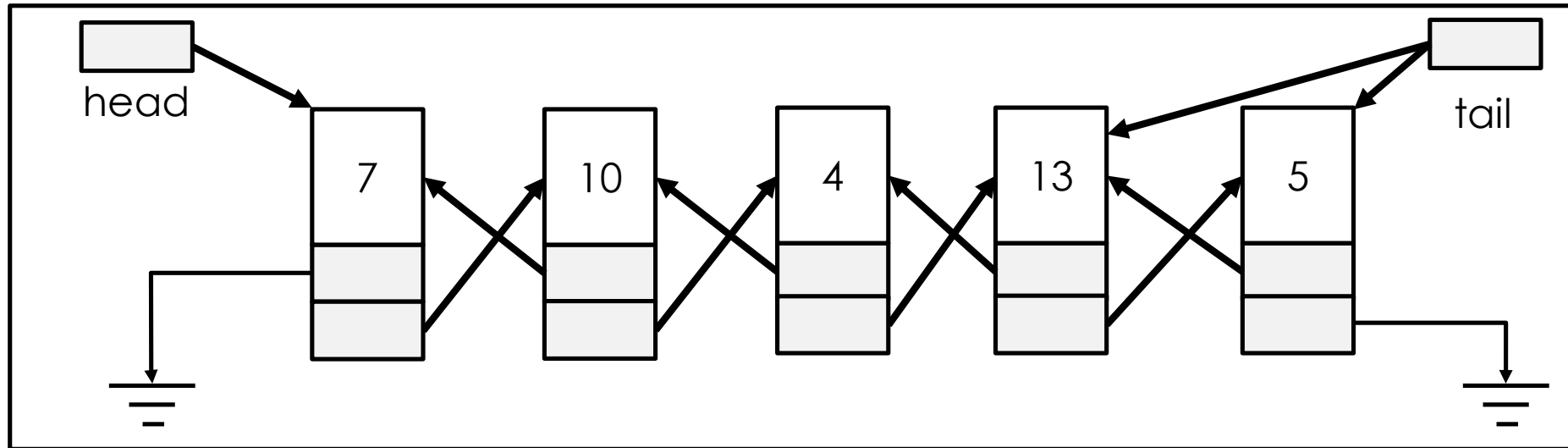
PopBack() in Doubly-linked List with Tail



PopBack() removes the last node

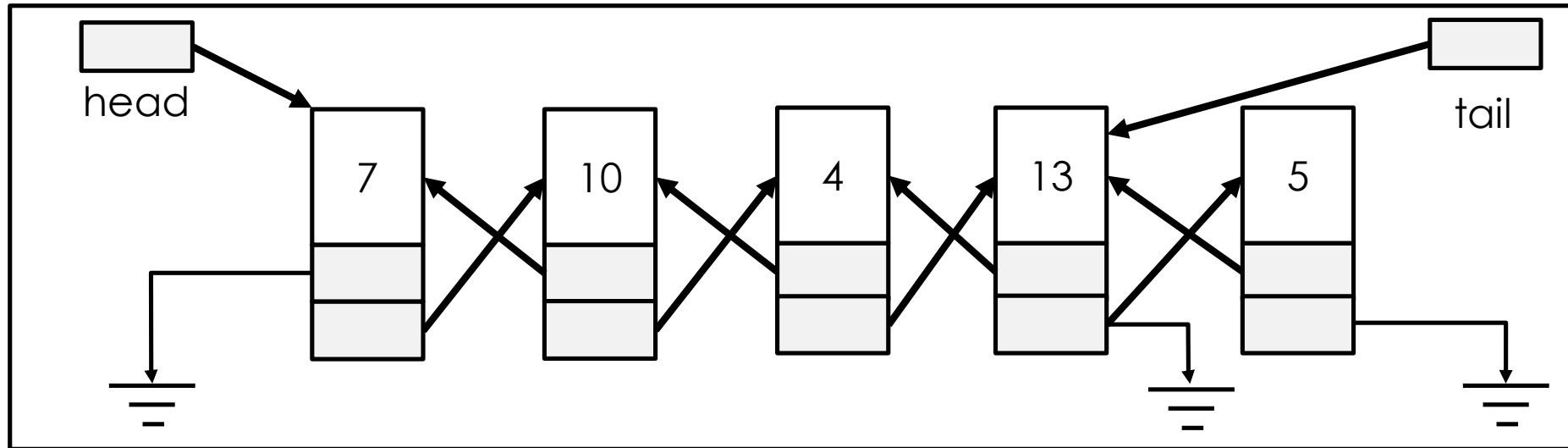
In the singly-linked list, the operation cost $O(n)$
How about the doubly-linked list?

PopBack() in Doubly-linked List with Tail



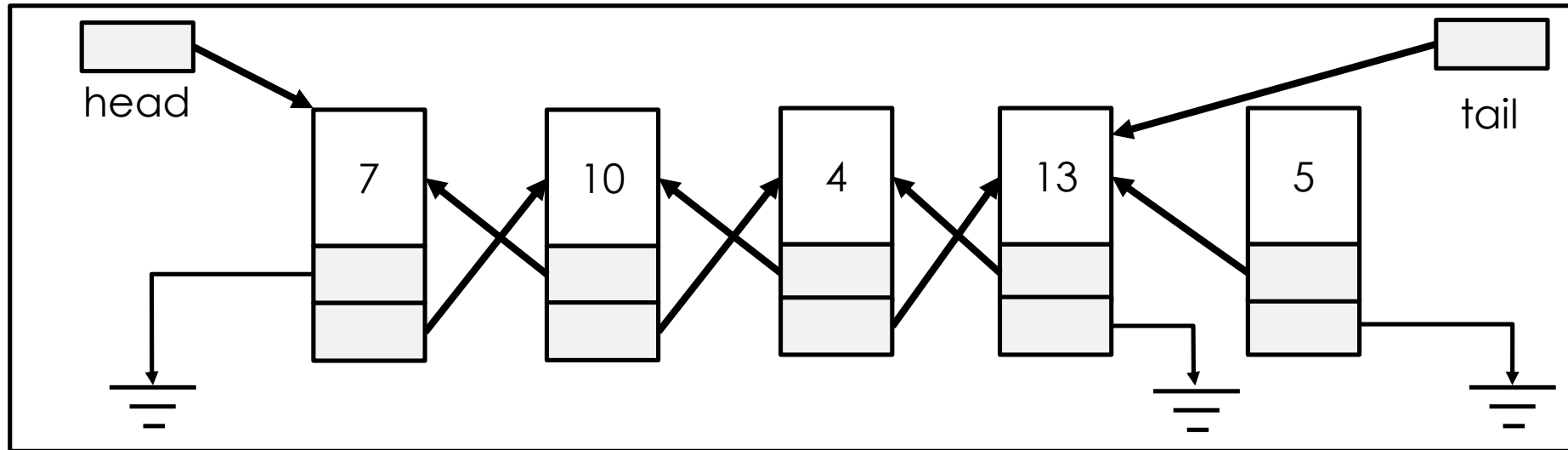
Step 1: Set **tail** to the node that the *prev* pointer of the last node points to

PopBack() in Doubly-linked List with Tail



Step 2: Set *prev* pointer of the node pointed by the **tail** to null

PopBack() in Doubly-linked List with Tail



Step 3: Delete the last node

This process is automatically done in C#

For other languages such as C++, you may create temp pointer to point to the last node in the step 2, then you can use "delete temp" command

What can be improved if you use doubly-linked lists instead

Singly-linked list operations	No tail	With tail
PushFront (Key)	$O(1)$	
TopFront()	$O(1)$	
PopFront()	$O(1)$	
PushBack(Key)	$O(n)$	$O(1)$
TopBack()	$O(n)$	$O(1)$
PopBack()	$O(n)$	$O(n)$
Find(Key)	$O(n)$	
Erase(Key)	$O(n)$	
Empty()	$O(1)$	
AddBefore(Node, Key)	$O(n)$	
AddAfter(Node, Key)	$O(1)$	



What can be improved if you use doubly-linked lists instead

Doubly-linked list operations	No tail	With tail
PushFront (Key)	$O(1)$	
TopFront()	$O(1)$	
PopFront()	$O(1)$	
PushBack(Key)	$O(n)$	$O(1)$
TopBack()	$O(n)$	$O(1)$
PopBack()	$O(n)$	$O(1)$
Find(Key)	$O(n)$	
Erase(Key)	$O(n)$	
Empty()	$O(1)$	
AddBefore(Node, Key)	$O(1)$	
AddAfter(Node, Key)	$O(1)$	



Summary

- ▣ Constant time to insert at or remove from the front.
- ▣ With tail and doubly-linked, constant time to insert at or remove from the back.
- ▣ $O(n)$ time to find arbitrary element.
- ▣ List elements need not be contiguous.
- ▣ With doubly-linked list, constant time to insert between nodes or remove a node.

Demo

- ▣ Singly-linked list, `pushFront(X)`, `printHead2Tail()`
- ▣ Your job is to do the rest for singly-linked list and doubly-linked list

Demo

- ▣ Array of Objects (Demo X1)
- ▣ List of Objects (Demo X2)
- ▣ Object consists of student_ID, GPA, name
- ▣ Find the top GPA student; Show student_ID and Name

Student_ID (string)	Name (string)	GPA (double)
5906001	Matthew	3.50
5906002	Mark	2.75
5906003	Luke	3.00
5906004	John	3.75
5906005	James	3.25