

Experimental Design and Analysis for Tree Improvement











$\begin{array}{c} \textbf{Experimental Design and Analysis for} \\ \textbf{tree Improvement using } \textbf{R} \end{array}$

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This book contains R codes and tutorials from R package eda4treeR on Experimental Design and Analysis for tree Improvement by E.R. Williams, C.E. Harwood and A.C. Matheson.

The development version of R package eda4treeR can be installed from github as follows:

```
if (!require("remotes")) install.packages("remotes")
remotes::install_github("myaseen208/eda4treeR")
```

The stable version of R package eda4treeR can be installed from CRAN as follows:

```
install.packages("eda4treeR")
```

1Introduction





2Experimental Planning and Layout

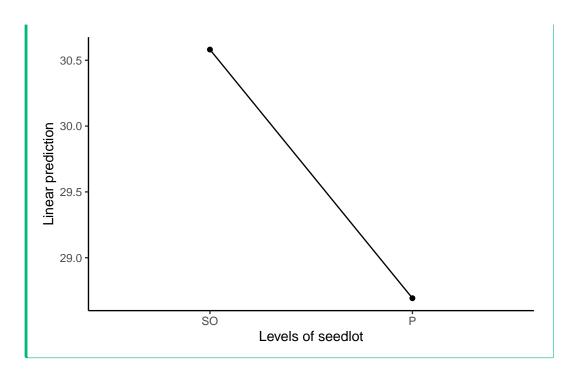
2.1 Example 2.1 (Pg. 24)

? Example 2.1 (Pg. 24)

A field trial was planted to compare a seedlot derived from a seed orchard (SO) with one collected from a routine plantation (P). There were eight plots of each seedlot, thinned at seven years of age. Tree diameters at breast height (dbh) were measured at 15 years and plot means calculated.

```
library(car)
library(dae)
library(dplyr)
library(emmeans)
library(ggplot2)
library(lmerTest)
library(magrittr)
library(predictmeans)
data(DataExam2.1)
# Pg. 22
fmtab2.3
          <- lm(formula = dbh ~ seedlot, data = DataExam2.1)
# Pg. 23
anova(fmtab2.3)
Analysis of Variance Table
Response: dbh
         Df Sum Sq Mean Sq F value Pr(>F)
         1 14.27 14.2695
                            3.2531 0.09284 .
Residuals 14 61.41 4.3864
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
# Pg. 23
emmeans(object = fmtab2.3, specs = ~ seedlot)
seedlot emmean SE df lower.CL upper.CL
          30.6 0.74 14
                          29.0
                                    32.2
          28.7 0.74 14
                           27.1
                                    30.3
Confidence level used: 0.95
emmip(object = fmtab2.3, formula = ~ seedlot) +
  theme_classic()
```





2.2 Example 2.2 (Pg. 26)

```
? Example 2.2 (Pg. 26)
library(car)
library(dae)
library(dplyr)
library(emmeans)
library(ggplot2)
library(lmerTest)
library(magrittr)
library(predictmeans)
data(DataExam2.2)
# Pg. 24
fmtab2.5 <-
           lm (
              formula = dbh ~ block + seedlot
            , data = DataExam2.2
# Pg. 26
anova(fmtab2.5)
Analysis of Variance Table
Response: dbh
```



```
Df Sum Sq Mean Sq F value Pr(>F)
          7 48.867 6.9810 3.8959 0.04671 *
block
          1 14.270 14.2695 7.9635 0.02570 *
seedlot
Residuals 7 12.543 1.7919
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
# Pg. 26
emmeans(object = fmtab2.5, specs = ~ seedlot)
                SE df lower.CL upper.CL
seedlot emmean
           30.6 0.473 7
28.7 0.473 7
                            29.5
                                   31.7
                             27.6
                                       29.8
Results are averaged over the levels of: block
Confidence level used: 0.95
emmip(object = fmtab2.5, formula = ~ seedlot) +
  theme_classic()
  30.5
Linear prediction
  29.0
                     so
                            Levels of seedlot
```



3Data Collection and Pre-Processing

3.1 Example 3.1 (Pg. 30)

? Example 3.1 (Pg. 30)

We illustrate the recommended layout for data sheets with one of the trials conducted by the Australian Centre for International Agricultural Research (ACIAR) in Queensland, Australia (Experiment 309). This was a species trial planted in 1985; survival was poor. For our example we will examine only part of the data from this experiment. Five of the species with good survival have been extracted at random, namely *Acacia*, *Angophora*, *Casuarina*, *Melaleuca* and *Petalostigma*.

```
library(car)
library(dae)
library(dplyr)
library(emmeans)
library(ggplot2)
library(lmerTest)
library(magrittr)
library(predictmeans)
library(supernova)
data(DataExam3.1)
# Pg. 28
fmtab3.3 <-
              formula = ht ~ repl*seedlot
              data = DataExam3.1
fmtab3.3ANOVA1 <-
  anova(fmtab3.3) %>%
  mutate(
  "F value" =
           anova(fmtab3.3)[1:2, 3]/anova(fmtab3.3)[3, 3]
         , anova(fmtab3.3)[3, 4]
         , NA
         )
          )
 # Pg. 33 (Table 3.3)
fmtab3.3ANOVA1 %>%
  mutate(
```



```
"Pr(>F)" =
       c (
         NA
        , pf(
            q = fmtab3.3ANOVA1[2, 4]
          , df1 = fmtab3.3ANOVA1[2, 1]
          , df2 = fmtab3.3ANOVA1[3, 1], lower.tail = FALSE
       , NA
       , NA
       )
            Df Sum Sq Mean Sq F value Pr(>F)
            1 20.30 20.301 3.4197
repl
seedlot
            4 505.87 126.467 21.3035 0.005851 **
repl:seedlot 4 23.75 5.936 2.3663
           70 175.61
Residuals
                        2.509
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
 # Pg. 33 (Table 3.3)
 emmeans(object = fmtab3.3, specs = ~ seedlot)
seedlot
                      SE df lower.CL upper.CL
             emmean
             10.29 0.396 70
Acacia
                                9.50
                                       11.08
              7.10 0.396 70
                                 6.31
                                         7.89
Angophora
               5.51 0.396 70
Casuarina
                                 4.72
                                          6.30
Melaleuca
               4.94 0.396 70
                                 4.15
                                          5.73
Petalostigma 2.73 0.396 70
                                 1.94
                                          3.52
Results are averaged over the levels of: repl
Confidence level used: 0.95
 # Pg. 34 (Figure 3.2)
 ggplot(
    mapping = aes(
                  x = fitted.values(fmtab3.3)
                 , y = residuals(fmtab3.3)
                ) +
 geom_point(size = 2) +
 labs(
    x = "Fitted Values"
   , y = "Residual"
   ) +
  theme_classic()
```



```
# Pg. 33 (Table 3.4)
DataExam3.1m <- DataExam3.1</pre>
DataExam3.1m[c(28, 51, 76), 5] <- NA
DataExam3.1m[c(28, 51, 76), 6] \leftarrow NA
fmtab3.4 <-
          lm (
              formula = ht ~ repl*seedlot
            , data
                       = DataExam3.1m
fmtab3.4ANOVA1 <-</pre>
  anova(fmtab3.4) %>%
  mutate(
      "F value" =
            c (
                anova(fmtab3.4)[1:2, 3]/anova(fmtab3.4)[3, 3]
              , anova(fmtab3.4)[3, 4]
             , NA
             )
             )
# Pg. 33 (Table 3.4)
fmtab3.4ANOVA1 %>%
  mutate(
  "Pr(>F)" =
       c (
         NA
       , pf(
            q = fmtab3.4ANOVA1[2, 4]
          , df1 = fmtab3.4ANOVA1[2, 1]
          , df2 = fmtab3.4ANOVA1[3, 1], lower.tail = FALSE
       , NA
       , NA
```



```
Df Sum Sq Mean Sq F value
            1 18.88 18.877 10.4201
repl
            4 588.68 147.169 81.2367 0.00044 ***
seedlot
repl:seedlot 4 7.25
                     1.812 2.4163
Residuals
          67 50.23
                       0.750
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
 # Pg. 33 (Table 3.4)
 emmeans(object = fmtab3.4, specs = ~ seedlot)
seedlot
          emmean SE df lower.CL upper.CL
            10.87 0.224 67
                             10.42
Acacia
                                      11.31
             7.76 0.231 67
                              7.30
                                       8.22
Angophora
Casuarina
             5.51 0.216 67
                              5.08
                                       5.94
Melaleuca
             4.94 0.216 67
                              4.51
                                       5.38
             2.73 0.216 67
                                2.30
                                       3.16
Petalostigma
Results are averaged over the levels of: repl
Confidence level used: 0.95
```

3.2 Example 3.1 (continued) (Pg. 34)

```
Example 3.1 (continued) (Pg. 34)
The analysis of variance table for ht is given below:
library(car)
library(dae)
library(dplyr)
library(emmeans)
library(ggplot2)
library(lmerTest)
library(magrittr)
library(predictmeans)
data(DataExam3.1.1)
# Pg. 36
fm3.8 <-
          formula = ht ~ repl + seedlot
        , data = DataExam3.1.1
# Pg. 40
 anova (fm3.8)
```



```
Analysis of Variance Table
Response: ht
         Df Sum Sq Mean Sq F value Pr(>F)
          1 2.538 2.5376 3.4197 0.138108
repl
          4 63.234 15.8084 21.3035 0.005851 **
seedlot
Residuals 4 2.968 0.7421
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
# Pg. 40
emmeans(object = fm3.8, specs = ~seedlot)
seedlot emmean SE df lower.CL upper.CL
             10.29 0.609 4 8.60
                                      11.98
Acacia
Angophora
              7.10 0.609 4
                                 5.41
                                         8.79
Casuarina
              5.51 0.609 4
                                3.82
                                         7.20
Melaleuca
               4.94 0.609 4
                                 3.25
                                         6.63
              2.73 0.609 4
                                 1.04
                                         4.42
Petalostigma
Results are averaged over the levels of: repl
Confidence level used: 0.95
emmip(object = fm3.8, formula = ~seedlot) +
 theme_classic()
  10 -
   8
Linear prediction
   4
                             Casuarina
                                        Melaleuca
         Acacia
                  Angophora
                                                  Petalostigma
                          Levels of seedlot
```



4Experimental Design

4.1 Example 4.3 (Pg. 53)

? Example 4.3 (Pg. 53)

Major seed distributors such as the Australian Tree Seed Centre (ATSC) routinely conduct seed viability tests so that, when seed is dispatched, the purchaser has an indication of the germination percentage of the seed. As part of the ATSC research program, a series of experiments was conducted in 1992 by Debbie Solomon on provenances of *Acacia mangium* to investigate methods of pre-treatment and loss of viability of stored seed. Each experiment involved six seedlots of *Acacia mangium* and four seed pre-treatments in a factorial design with three replicates.

```
library(car)
library(dae)
library(dplyr)
library(emmeans)
library(ggplot2)
library(lmerTest)
library(magrittr)
library(predictmeans)
data(DataExam4.3)
 # Pg. 50
 fm4.2
   aov(
       formula =
       percent ~ repl + contcomp + seedlot +
                 treat/contcomp + contcomp/seedlot +
                 treat/contcomp/seedlot
        data
             = DataExam4.3
 # Pg. 54
 anova (fm4.2)
Analysis of Variance Table
Response: percent
                      Df Sum Sq Mean Sq F value
                                                                Pr(>F)
                             35
repl
                       2
                                     18
                                         0.1804
                                                             0.8355379
                      1 58542
                                  58542 601.5217 < 0.000000000000000022
contcomp
seedlot
                      5 2894
                                  579 5.9481
                                                             0.0002538 ***
treat
                      2 5300
                                   2650 27.2295
                                                         0.00000001576 ***
contcomp:seedlot
                      5 1347
                                   269 2.7682
                                                             0.0287571 *
```



```
0.4674993
contcomp:seedlot:treat 10 961
                                  96 0.9876
                     46 4477
                                  97
Residuals
___
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
 # Pg. 54
 model.tables(x = fm4.2, type = "means")
Tables of means
Grand mean
51.38889
repl
            2
       1
   52.33 50.67 51.17
rep 24.00 24.00 24.00
contcomp
   Treated control
     67.85 2
               18
rep
   54.00
seedlot
   18211 18212 18217 18248 18249 18265
      58 52.33 49 40.67 48.67 59.67
      12 12.00
                 12 12.00 12.00 12.00
rep
treat
    nick bw&s control bw1min
   40.43 49.31 51.39 64.43
rep 18.00 18.00 18.00 18.00
contcomp:seedlot
        seedlot
contcomp 18211 18212 18217 18248 18249 18265
 Treated 77.33 69.33 63.11 53.33 64.89 79.11
 rep 9.00 9.00 9.00 9.00 9.00 9.00
 control 0.00 1.33 6.67 2.67 0.00 1.33
 rep
         3.00 3.00 3.00 3.00 3.00 3.00
contcomp:seedlot:treat
, , treat = nick
        seedlot
contcomp 18211 18212 18217 18248 18249 18265
 Treated 65.33 54.67 57.33 40.00 49.33 74.67
         3.00 3.00 3.00 3.00 3.00 3.00
 rep
 control
        0.00 0.00 0.00 0.00 0.00 0.00
 rep
, , treat = bw\&s
        seedlot
contcomp 18211 18212 18217 18248 18249 18265
 Treated 78.67 68.00 54.67 52.00 61.33 80.00
         3.00 3.00 3.00 3.00 3.00 3.00
 control
          0.00 0.00 0.00 0.00 0.00 0.00
 rep
```

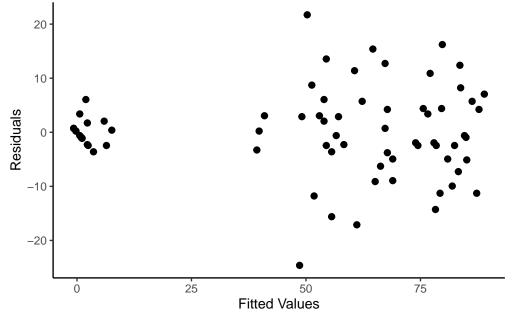


```
, , treat = control
        seedlot
contcomp 18211 18212 18217 18248 18249 18265
 Treated
          0.00 0.00 0.00 0.00 0.00 0.00
 control 0.00 1.33 6.67 2.67 0.00 1.33
         3.00 3.00 3.00 3.00 3.00 3.00
 rep
, , treat = bw1min
        seedlot
contcomp 18211 18212 18217 18248 18249 18265
 Treated 88.00 85.33 77.33 68.00 84.00 82.67
         3.00 3.00 3.00 3.00 3.00 3.00
 control
         0.00 0.00 0.00 0.00 0.00 0.00
 rep
 emmeans(object = fm4.2, specs = ~ contcomp)
contcomp emmean SE df lower.CL upper.CL
Treated
        67.9 1.34 46 65.15 70.55
           2.0 2.33 46
                         -2.68
                                  6.68
control
Results are averaged over the levels of: repl, seedlot, treat
Confidence level used: 0.95
 emmeans(object = fm4.2, specs = ~ seedlot)
seedlot emmean SE df lower.CL upper.CL
                               45.3
18211
        38.7 3.29 46 32.0
        35.3 3.29 46
18212
                        28.7
                                 42.0
18217
        34.9 3.29 46
                        28.3
                                 41.5
        28.0 3.29 46
                        21.4
18248
                                 34.6
        32.4 3.29 46
                        25.8
18249
                                 39.1
                        33.6
18265
        40.2 3.29 46
Results are averaged over the levels of: repl, treat, contcomp
Confidence level used: 0.95
 emmeans(object = fm4.2, specs = ~ contcomp + treat)
      contcomp emmean SE df lower.CL upper.CL
        Treated
                56.9 2.33 46
                               52.21
bw&s
        Treated
                  65.8 2.33 46
                                 61.10
                                         70.46
bw1min Treated 80.9 2.33 46 76.21
                                        85.57
                  2.0 2.33 46
control control
                                 -2.68
                                         6.68
Results are averaged over the levels of: repl, seedlot
Confidence level used: 0.95
 emmeans(object = fm4.2, specs = ~ contcomp + seedlot)
contcomp seedlot emmean SE df lower.CL upper.CL
Treated 18211 77.33 3.29 46 70.7
control 18211
                 0.00 5.70 46
                                 -11.5
Treated 18212 69.33 3.29 46
                                 62.7
control 18212
                 1.33 5.70 46
                                 -10.1
               63.11 3.29 46
6.67 5.70 46
Treated 18217
                                56.5
                                         69.7
control 18217
                                 -4.8
                 6.67 5.70 46
                                          18.1
Treated 18248 53.33 3.29 46
                              46.7
-8.8
                                 46.7 60.0
-8.8 14.1
control 18248 2.67 5.70 46
```



```
Treated 18249
               64.89 3.29 46
                                 58.3
                                          71.5
                                        11.5
                 0.00 5.70 46
 control 18249
                                 -11.5
 Treated 18265
                 79.11 3.29 46
                                72.5
                                         85.7
control 18265
                1.33 5.70 46
                                 -10.1
                                          12.8
Results are averaged over the levels of: repl, treat
Confidence level used: 0.95
 emmeans(object = fm4.2, specs = ~ contcomp + treat + seedlot)
      contcomp seedlot emmean SE df lower.CL upper.CL
treat
                        65.33 5.7 46
nick
        Treated 18211
                                      53.9
                                                76.8
        Treated 18211
bw&s
                        78.67 5.7 46
                                        67.2
                                                90.1
bw1min Treated 18211 88.00 5.7 46
                                        76.5
                                                99.5
                        0.00 5.7 46
control control 18211
                                      -11.5
                                                11.5
                                      43.2
       Treated 18212 54.67 5.7 46
                                               66.1
       Treated 18212 68.00 5.7 46
bw&s
                                       56.5
                                               79.5
bw1min Treated 18212 85.33 5.7 46
                                       73.9
                                               96.8
control control 18212
                        1.33 5.7 46
                                      -10.1
                                                12.8
        Treated 18217
                      57.33 5.7 46
                                      45.9
nick
                                                68.8
                      54.67 5.7 46
77.33 5.7 46
6.67 5.7 46
bw&s
        Treated 18217
                                        43.2
                                                66.1
                                       65.9
bw1min Treated 18217
                                                88.8
control control 18217
                                       -4.8
                                                18.1
       Treated 18248
                      40.00 5.7 46
                                       28.5
                                                51.5
nick
        Treated 18248 52.00 5.7 46
bw&s
                                       40.5
                                                63.5
bw1min Treated 18248 68.00 5.7 46
                                       56.5
                                                79.5
                      2.67 5.7 46
49.33 5.7 46
control control 18248
                                        -8.8
                                                14.1
        Treated 18249
nick
                                        37.9
                                                60.8
        Treated 18249 61.33 5.7 46
                                        49.9
                                                72.8
hw∦s
                                                95.5
bw1min Treated 18249 84.00 5.7 46
                                       72.5
                        0.00 5.7 46
control control 18249
                                      -11.5
                                                11.5
       Treated 18265 74.67 5.7 46
                                       63.2
nick
                                                86.1
bw&s
       Treated 18265 80.00 5.7 46
                                       68.5
                                                91.5
bw1min Treated 18265
                       82.67 5.7 46
                                       71.2
                                                94.1
control control 18265
                        1.33 5.7 46
                                       -10.1
                                                12.8
Results are averaged over the levels of: repl
Confidence level used: 0.95
 DataExam4.3 %>%
   dplyr::group_by(treat, contcomp, seedlot) %>%
   dplyr::summarize(Mean = mean(percent))
# A tibble: 24 x 4
# Groups: treat, contcomp [4]
  treat contcomp seedlot Mean
  <fct> <fct>
               <fct> <dbl>
1 nick Treated 18211 65.3
2 nick Treated 18212 54.7
3 nick Treated 18217
                       57.3
4 nick Treated 18248
                        40
5 nick Treated 18249
                        49.3
6 nick Treated 18265
                        74.7
7 bw&s Treated 18211
                        78.7
8 bw&s Treated 18212 68
9 bw&s Treated 18217
                       54.7
10 bw&s Treated 18248
                      52
# i 14 more rows
   RESFIT <-
          data.frame(
```





? Tip

Here the control pre-treatment was deleted.

```
library(car)
library(dae)
library(dplyr)
library(emmeans)
library(ggplot2)
library(lmerTest)
library(magrittr)
library(predictmeans)
data(DataExam4.3)
# Pg. 57
```



```
fm4.4
        <-
  aov(
      formula = percent ~ repl + treat*seedlot
     , data = DataExam4.3 %>%
                 filter(treat != "control")
     )
 # Pg. 57
 anova(fm4.4)
Analysis of Variance Table
Response: percent
             Df Sum Sq Mean Sq F value
                                          Pr(>F)
                  64.6 32.30 0.2511 0.7793606
repl
treat
              2 5300.1 2650.07 20.6055 0.000001375 ***
             5 4148.1 829.63 6.4507 0.0002578 ***
seedlot
treat:seedlot 10 961.2 96.12 0.7474
                                        0.6759614
Residuals 34 4372.7 128.61
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
 model.tables(x = fm4.4, type = "means", se = TRUE)
Tables of means
Grand mean
67.85185
repl
repl
         2
69.11 66.44 68.00
treat
treat
       bw&s bw1min
 nick
56.89 65.78 80.89
seedlot
seedlot
18211 18212 18217 18248 18249 18265
77.33 69.33 63.11 53.33 64.89 79.11
treat:seedlot
      seedlot
       18211 18212 18217 18248 18249 18265
        65.33 54.67 57.33 40.00 49.33 74.67
 bw&s 78.67 68.00 54.67 52.00 61.33 80.00
 bw1min 88.00 85.33 77.33 68.00 84.00 82.67
Standard errors for differences of means
        repl treat seedlot treat:seedlot
       3.780 3.780 5.346 9.260
replic.
         18
               18
                        9
 emmeans(object = fm4.4, specs = ~ treat)
treat emmean SE df lower.CL upper.CL
        56.9 2.67 34
nick
                      51.5 62.3
bw&s 65.8 2.67 34 60.3
bw1min 80.9 2.67 34 75.5
                                  71.2
                                  86.3
```



```
Results are averaged over the levels of: repl, seedlot
Confidence level used: 0.95
  emmeans(object = fm4.4, specs = ~ seedlot)
                  SE df lower.CL upper.CL
 seedlot emmean
 18211
           77.3 3.78 34
                             69.7
                                      85.0
 18212
           69.3 3.78 34
                             61.7
                                      77.0
           63.1 3.78 34
                             55.4
                                      70.8
 18217
 18248
           53.3 3.78 34
                             45.7
                                      61.0
 18249
           64.9 3.78 34
                             57.2
                                      72.6
 18265
           79.1 3.78 34
                             71.4
                                      86.8
Results are averaged over the levels of: repl, treat
Confidence level used: 0.95
 emmeans(object = fm4.4, specs = ~ treat * seedlot)
        seedlot emmean
                          SE df lower.CL upper.CL
                                              78.6
                  65.3 6.55 34
nick
        18211
                                    52.0
bw&s
        18211
                  78.7 6.55 34
                                    65.4
                                             92.0
                  88.0 6.55 34
bw1min 18211
                                    74.7
                                             101.3
nick
        18212
                  54.7 6.55 34
                                    41.4
                                             68.0
                                    54.7
bw&s
        18212
                  68.0 6.55 34
                                             81.3
                                             98.6
bw1min 18212
                  85.3 6.55 34
                                    72.0
                  57.3 6.55 34
                                    44.0
                                             70.6
nick
        18217
bw&s
        18217
                  54.7 6.55 34
                                    41.4
                                              68.0
bw1min 18217
                  77.3 6.55 34
                                    64.0
                                              90.6
nick
      18248
                  40.0 6.55 34
                                    26.7
                                             53.3
                                    38.7
        18248
                  52.0 6.55 34
bw&s
                                             65.3
bw1min 18248
                  68.0 6.55 34
                                    54.7
                                             81.3
nick
      18249
                  49.3 6.55 34
                                    36.0
                                             62.6
bw∦s
       18249
                  61.3 6.55 34
                                    48.0
                                             74.6
bw1min 18249
                                             97.3
                  84.0 6.55 34
                                    70.7
        18265
                  74.7 6.55 34
                                    61.4
                                             88.0
nick
bw&s
        18265
                  80.0 6.55 34
                                    66.7
                                             93.3
bw1min 18265
                  82.7 6.55 34
                                    69.4
                                             96.0
Results are averaged over the levels of: repl
Confidence level used: 0.95
```

4.2 Example 4.4 (Pg. 61)

? Example 4.4 (Pg. 61)

An experiment supported by the Shell Company was planted at Toolara Forest Reserve near Gympie, Queensland, in February 1987 to study the effects of irrigation and fertiliser on four seedlots of *Eucalyptus grandis*. Because of the difficulty in applying the irrigation and fertiliser treatments individually to each 7×6 plot of trees, the experiment was designed as a split-plot, with main-plot treatments, *irrig* and *fert*. There were two replicates of four main-plots each with four sub-plots.

```
library(car)
```



```
library(dae)
library(dplyr)
library(emmeans)
library(ggplot2)
library(lmerTest)
library(magrittr)
library(predictmeans)
data(DataExam4.4)
# Pg. 58
       <-
fm4.6
  aov(
      formula = height ~ repl + irrig*fert*seedlot +
                        Error(repl/irrig:fert)
    , data = DataExam4.4
# Pg. 61
 summary(fm4.6)
Error: repl
    Df Sum Sq Mean Sq
repl 1 0.7564 0.7564
Error: repl:irrig:fert
         Df Sum Sq Mean Sq F value Pr(>F)
          1 0.1 0.1 0.154 0.721
          1 590.6
                   590.6 841.110 0.00009 ***
fert
irrig:fert 1 0.0 0.0 0.010 0.926
Residuals 3 2.1
                      0.7
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Error: Within
                 Df Sum Sq Mean Sq F value
                                           Pr(>F)
                  3 39.65 13.218 19.680 0.000063 ***
seedlot
                 3 1.11 0.370 0.551 0.6572
irrig:seedlot
                 3 9.95 3.317
                                   4.938
fert:seedlot
                                           0.0185 *
irrig:fert:seedlot 3 1.74 0.579
                                    0.862 0.4874
Residuals
                 12 8.06
                            0.672
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
model.tables(x = fm4.6, type = "means")
Tables of means
Grand mean
10.00437
repl
repl
```



```
1 2
10.158 9.851
irrig
irrig
none plus
9.946 10.062
fert
fert
 none plus
5.708 14.301
seedlot
seedlot
Bulahdelah Coffs SO Pomona pltn Atherton 10.178 11.404 10.149 8.287
irrig:fert
    fert
irrig none plus
none 5.635 14.257
 plus 5.781 14.344
irrig:seedlot
    seedlot
irrig Bulahdelah Coffs SO Pomona pltn Atherton
none 10.060 11.647 10.055 8.022
               11.160 10.242 8.552
 plus 10.295
fert:seedlot
    seedlot
fert Bulahdelah Coffs SO Pomona pltn Atherton
 none 5.687 6.790 5.410 4.945
 plus 14.667
                                   11.630
               16.017
                       14.887
irrig:fert:seedlot
, , seedlot = Bulahdelah
    fert
irrig none plus
 none 5.275 14.845
 plus 6.100 14.490
, , seedlot = Coffs SO
    fert
irrig none plus
 none 7.125 16.170
 plus 6.455 15.865
, , seedlot = Pomona pltn
    fert
irrig none plus
none 5.625 14.485
 plus 5.195 15.290
, , seedlot = Atherton
```



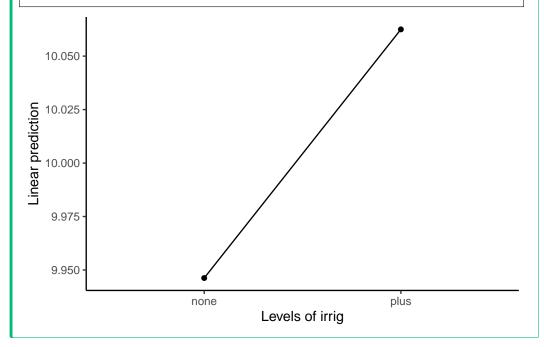
```
fert
irrig none plus
none 4.515 11.530
plus 5.375 11.730
```

Pg. 61

```
emmeans(object = fm4.6, specs = ~ irrig)
irrig emmean SE df asymp.LCL asymp.UCL
none 9.95 NaN NaN NaN NaN
plus 10.06 NaN NaN NaN NaN
```

Results are averaged over the levels of: repl, fert, seedlot Warning: EMMs are biased unless design is perfectly balanced Confidence level used: 0.95

```
emmip(object = fm4.6, formula = ~ irrig) +
    theme_classic()
```





5Analysis Across Sites

5.1 Example 5.1 (Pg. 68)

? Example 5.1 (Pg. 68)

In 1985 species/provenance trials were laid out at six sites in Thailand as part of an ACIAR project extending over several years to investigate Australian multi-purpose tree species. The experimental design in each case was an RCB design with three replicates and the number of seedlots ranged from 30 to 42. Plots consisted of 5×5 trees with a $2m \times 2m$ spacing. Plot summary files were constructed for the 24-month measurement according to the methods described in Chapter 3. Analyses were performed on the plot mean data at each site.

```
library(car)
library(dae)
library(dplyr)
library(emmeans)
library(ggplot2)
library(lmerTest)
library(magrittr)
library(predictmeans)
data(DataExam5.1)
# Pg.68
fm5.4 <-
           formula = ht ~ site*seedlot
           data = DataExam5.1
# Pg. 73
anova (fm5.4)
Analysis of Variance Table
Response: ht
             Df Sum Sq Mean Sq F value Pr(>F)
             3 919585 306528
                                 NaN
site
seedlot
            26 3176289
                        122165
                                    {\tt NaN}
                                            NaN
site:seedlot 78 707957
                          9076
                                    {\tt NaN}
                                            NaN
Residuals
            0
                    0
                            {\tt NaN}
# Pg. 73
emmeans(object = fm5.4, specs = ~ site)
            emmean SE df lower.CL upper.CL
Ratchaburi
            462 NaN
                       0
Sai Thong
               628 NaN
                       0
                               NaN
                                         NaN
```



```
Si Sa Ket
                 494 NaN 0
                                   {\tt NaN}
                                             NaN
                 370 NaN 0
 Sakaerat
                                   {\tt NaN}
                                             NaN
Results are averaged over the levels of: seedlot
Confidence level used: 0.95
emmeans(object = fm5.4, specs = ~ seedlot)
 seedlot emmean SE df lower.CL upper.CL
 13877
            365 NaN
                       0
                              {\tt NaN}
                                          NaN
 13866
             353 NaN
                       0
                               {\tt NaN}
                                          NaN
13689
             559 NaN
                       0
                                {\tt NaN}
                                          NaN
 13688
             546 NaN
                       0
                               {\tt NaN}
                                          {\tt NaN}
             627 NaN
                      0
                              {\tt NaN}
                                          \tt NaN
 13861
             628 NaN 0
                              {\tt NaN}
                                          \tt NaN
13854
13684
             660 NaN 0
                              {\tt NaN}
                                          \tt NaN
13864
            422 NaN 0
                              {\tt NaN}
                                          NaN
            586 NaN 0
                              {\tt NaN}
13863
                                          NaN
                              {\tt NaN}
             770 NaN
13683
                       0
                                          {\tt NaN}
 13681
             695 NaN
                       0
                               {\tt NaN}
                                          NaN
14175
             438 NaN
                       0
                               {\tt NaN}
                                          {\tt NaN}
14660
             521 NaN
                       0
                              {\tt NaN}
                                          NaN
13653
            592 NaN
                       0
                              {\tt NaN}
                                          {\tt NaN}
            440 NaN
                              {\tt NaN}
                                          NaN
13846
            384 NaN
                              NaN
                                          {\tt NaN}
13621
                       0
             272 NaN
                              {\tt NaN}
                                          NaN
 13871
                       0
 13519
             422 NaN
                       0
                                {\tt NaN}
                                          NaN
 13514
             369 NaN
                       0
                               {\tt NaN}
                                          NaN
                             {\tt NaN}
             273 NaN
 13148
                       Ω
                                          NaN
             282 NaN
 13990
                       0
                              {\tt NaN}
                                          NaN
14537
             780 NaN 0
                              {\tt NaN}
                                          {\tt NaN}
             772 NaN 0
14106
                              {\tt NaN}
                                          {\tt NaN}
12013
             616 NaN 0
                              {\tt NaN}
                                          NaN
             422 NaN
14130
                       0
                                {\tt NaN}
                                          NaN
 14485
             123 NaN
                        0
                                {\tt NaN}
                                          NaN
             273 NaN 0
                                {\tt NaN}
                                          NaN
11935
Results are averaged over the levels of: site
Confidence level used: 0.95
ANOVAfm5.4 <- anova(fm5.4)
ANOVAfm5.4[4, 1:3] \leftarrow c(208, 208*1040, 1040)
ANOVAfm5.4[3, 4] <- ANOVAfm5.4[3, 3]/ANOVAfm5.4[4, 3]
ANOVAfm5.4[3, 5]
             pf(
                          = ANOVAfm5.4[3, 4]
            , df1
                          = ANOVAfm5.4[3, 1]
            , df2
                      = ANOVAfm5.4[4, 1]
            , lower.tail = FALSE
# Pg. 73
ANOVAfm5.4
Analysis of Variance Table
Response: ht
               Df Sum Sq Mean Sq F value
                                                                Pr(>F)
```

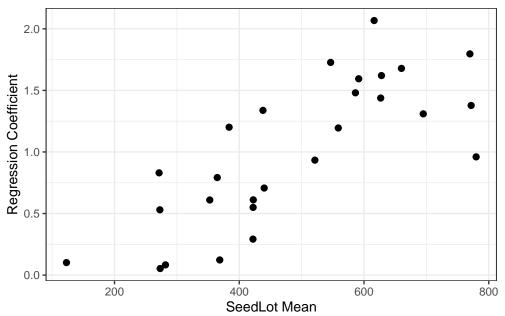


```
{\tt NaN}
site
              3 919585 306528
                                                             {\tt NaN}
seedlot
             26 3176289 122165
                                     {\tt NaN}
                                                             {\tt NaN}
site:seedlot 78 707957
                             9076 8.7273 < 0.00000000000000022
Residuals
            208 216320
                             1040
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
# Pg. 80
DataExam5.1 %>%
   filter(seedlot %in% c("13653", "13871")) %>%
   ggplot(
    data = .
   , mapping = aes(
                   х
                         = sitemean
                        = ht
                 , у
                  , color = seedlot
                   shape = seedlot
   ) +
   geom_point() +
   geom_smooth(
     method
               = lm
               = FALSE
    , fullrange = TRUE
    ) +
   theme_classic() +
   labs(
      x = "SiteMean"
     , y = "SeedLot Mean"
  800
SeedLot Mean
                                                        seedlot
                                                         13653
                                                         13871
  200
            400
                    450
                            500
                                     550
                                             600
                          SiteMean
 Tab5.10 <-
   DataExam5.1 %>%
   summarise(Mean = mean(ht), .by = seedlot) %>%
   left_join(
     DataExam5.1 %>%
      nest_by(seedlot) %>%
      mutate(fm1 = list(lm(ht ~ sitemean, data = data))) %>%
```



```
summarise(Slope = coef(fm1)[2])
   , by = "seedlot"
# Pg. 81
Tab5.10
   seedlot
             Mean
                       Slope
     11935 272.75 0.53017435
     14485 123.00 0.10170020
2
3
     14130 422.25 0.54976906
4
     12013 616.25 2.06723798
5
     14106 771.75 1.37751724
     14537 779.75 0.96012145
6
7
    13990 281.75 0.08298796
     13148 273.25 0.05333546
    13514 368.75 0.12307233
    13519 422.00 0.29211648
10
     13871 271.50 0.83048203
11
12
     13621 383.75 1.20085607
13
     13846 440.00 0.70691001
     13653 591.50 1.59434380
14
15
    14660 521.25 0.93353990
16
     14175 438.00 1.33770745
17
     13681 695.00 1.30937837
     13683 769.75 1.79629735
18
     13863 586.25 1.48034730
19
20
     13864 422.50 0.61113857
21
     13684 660.00 1.67860570
22
    13854 628.00 1.62026853
23
    13861 626.75 1.43784662
24
    13688 546.50 1.72717652
25
    13689 558.75 1.19475332
26
     13866 352.75 0.61009734
     13877 364.75 0.79221858
27
ggplot(data = Tab5.10, mapping = aes(x = Mean, y = Slope)) +
 geom_point(size = 2) +
 theme_bw() +
 labs(
     x = "SeedLot Mean"
    , y = "Regression Coefficient"
```





```
DevSS1 <-
  DataExam5.1 %>%
  nest_by(seedlot) %>%
  mutate(fm1 = list(lm(ht ~ sitemean, data = data))) %>%
  summarise(SSE = anova(fm1)[2, 2]) %>%
  ungroup() %>%
  summarise(Dev = sum(SSE)) %>%
  as.numeric()
ANOVAfm5.4[2, 2]
[1] 3176289
length(levels(DataExam5.1$SeedLot))
[1] 0
ANOVAfm5.4.1 <-
  rbind(
   ANOVAfm5.4[1:3, ]
   , c(
       ANOVAfm5.4[2, 1]
     , ANOVAfm5.4[3, 2] - DevSS1
     , (ANOVAfm5.4[3, 2] - DevSS1)/ANOVAfm5.4[2, 1]
     , NA
     , NA
   , c(
       ANOVAfm5.4[3, 1]-ANOVAfm5.4[2, 1]
     , DevSS1/(ANOVAfm5.4[3, 1]-ANOVAfm5.4[2, 1])
     , DevSS1/(ANOVAfm5.4[3, 1]-ANOVAfm5.4[2, 1])/ANOVAfm5.4[4, 3]
     , pf(
             q = DevSS1/(ANOVAfm5.4[3, 1]-ANOVAfm5.4[2, 1])/ANOVAfm5.4[4, 3]
         , df1 = ANOVAfm5.4[3, 1] - ANOVAfm5.4[2, 1]
         , df2 = ANOVAfm5.4[4, 1]
          lower.tail = FALSE
   , ANOVAfm5.4[4, ]
```



```
)
rownames(ANOVAfm5.4.1) <-</pre>
  c (
    "Site"
  , "seedlot"
  , "site:seedlot"
  , " regressions"
    " deviations"
    "Residuals"
# Pg. 82
ANOVAfm5.4.1
Analysis of Variance Table
Response: ht
              Df Sum Sq Mean Sq F value
                                                        Pr(>F)
              3 919585 306528
Site
                                                           NaN
             26 3176289 122165
seedlot
                                     {\tt NaN}
                                                           NaN
site:seedlot 78 707957
                         9076 8.7273 < 0.00000000000000022
 regressions 26 308503
                         11866
 deviations 52 399454
                           7682 7.3863 < 0.000000000000000022 ***
Residuals
            208 216320
                           1040
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
```

5.2 Example 5.2 (Pg. 72)

```
Example 5.2 (Pg. 72)

library(car)
library(dae)
library(dplyr)
library(ggplot2)
library(lmerTest)
library(magrittr)
library(predictmeans)
data(DataExam5.2)

# Pg. 75
fm5.7 <-
lm(
    formula = ht ~ site*seedlot
    , data = DataExam5.2</pre>
```



```
)
# Pg. 77
anova(fm5.7)
Analysis of Variance Table
Response: ht
              Df Sum Sq Mean Sq F value Pr(>F)
               5 4157543 831509
                                    {\tt NaN}
site
                                             NaN
              36 4425296 122925
seedlot
                                      {\tt NaN}
                                             NaN
site:seedlot 150 1351054
                           9007
                                      {\tt NaN}
                                             {\tt NaN}
Residuals
              0
                             {\tt NaN}
fm5.9 <-
 lm (
     formula = ht ~ site*seedlot
     data = DataExam5.2
# Pg. 77
anova(fm5.9)
Analysis of Variance Table
Response: ht
              Df Sum Sq Mean Sq F value Pr(>F)
              5 4157543 831509
                                  NaN
site
                                             NaN
seedlot
              36 4425296 122925
                                      {\tt NaN}
                                             NaN
                          9007
site:seedlot 150 1351054
                                      {\tt NaN}
                                             NaN
                     0
                             {\tt NaN}
Residuals
             0
ANOVAfm5.9 \leftarrow anova(fm5.9)
ANOVAfm5.9[4, 1:3] \leftarrow c(384, 384*964, 964)
ANOVAfm5.9[3, 4] <- ANOVAfm5.9[3, 3]/ANOVAfm5.9[4, 3]
ANOVAfm5.9[3, 5] <-
    pf(
         q = ANOVAfm5.9[3, 4]
     , df1 = ANOVAfm5.9[3, 1]
     , df2 = ANOVAfm5.9[4, 1]
     , lower.tail = FALSE
# Pg. 77
ANOVAfm5.9
Analysis of Variance Table
Response: ht
              Df Sum Sq Mean Sq F value
                                                          Pr(>F)
              5 4157543 831509 NaN
                                                             NaN
site
                                     {\tt NaN}
                                                             {\tt NaN}
seedlot
              36 4425296 122925
site:seedlot 150 1351054 9007 9.3434 < 0.00000000000000002 | **
Residuals 384 370176
                             964
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
Tab5.14 <-
   DataExam5.2 %>%
```



```
summarise(
        Mean = round(mean(ht, na.rm = TRUE), 0)
      , .by = seedlot
      ) %>%
    left_join(
       DataExam5.2 %>%
       nest_by(seedlot) %>%
       mutate(fm2 = list(lm(ht ~ sitemean, data = data))) %>%
       summarise(Slope = round(coef(fm2)[2], 2))
     , by = "seedlot"
     ) %>%
   as.data.frame()
# Pg. 81
Tab5.14
   seedlot Mean Slope
     13877
            291
                0.80
2
     13866
            302 0.56
3
     13689
            463
                1.07
4
     13688
            458
                1.20
5
     13861
            538 1.08
6
     13854
            536 1.16
7
     13686
           726 1.77
8
     13684
           549 1.34
            371 0.79
9
     13864
10
     13863
           586
                1.19
11
     13683
           673
                1.78
12
                1.33
     13681
           610
13
     13680
           645 2.08
14
     14623
           652 0.49
     14175
           378 1.22
15
16
     14660
           445 0.88
17
     13691
            511
                1.61
18
     13653
            477 1.35
     13846
            381 0.93
19
            304 0.98
20
     13621
21
     14176
           177 0.22
22
     13871
            220 0.64
23
           355
     14622
                1.65
            240 0.77
24
     13876
25
     13519
            342 0.71
26
     13514
            290
                0.66
27
     13148
           230 0.35
28
           260 0.29
     13990
29
     14537
            671
                1.15
30
     14106
            673 1.18
31
     12013
            529 1.30
            390 0.45
32
     14130
            108 0.16
33
     14485
34
     14166
            210 0.61
35
     11935
            211 0.61
36
     14170
            244 0.59
37
     14152 150 0.63
DevSS2 <-
  DataExam5.2 %>%
  nest_by(seedlot) %>%
  mutate(fm2 = list(lm(ht ~ sitemean, data = data))) %>%
   summarise(SSE = anova(fm2)[2, 2]) %>%
```



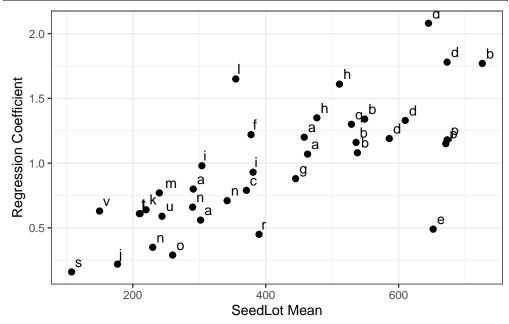
```
ungroup() %>%
   summarise(Dev = sum(SSE)) %>%
   as.numeric()
 ANOVAfm5.9.1 <-
   rbind(
      ANOVAfm5.9[1:3, ]
    , c(
         ANOVAfm5.9[2, 1]
       , ANOVAfm5.9[3, 2] - DevSS2
       , (ANOVAfm5.9[3, 2] - DevSS2)/ANOVAfm5.9[2, 1]
       , NA
      )
    , c(
         ANOVAfm5.9[3, 1]-ANOVAfm5.9[2, 1]
       , DevSS2
       , DevSS2/(ANOVAfm5.9[3, 1]-ANOVAfm5.9[2, 1])
       , DevSS2/(ANOVAfm5.9[3, 1]-ANOVAfm5.9[2, 1])/ANOVAfm5.9[4, 3]
       , pf(
               q = DevSS2/(ANOVAfm5.9[3, 1]-ANOVAfm5.9[2, 1])/ANOVAfm5.9[4, 3]
           , df1 = ANOVAfm5.9[3, 1] - ANOVAfm5.9[2, 1]
           , df2 = ANOVAfm5.9[4, 1]
           , lower.tail = FALSE
    , ANOVAfm5.9[4, ]
rownames (ANOVAfm5.9.1) <-
  c (
      "site"
     "seedlot"
     "site:seedlot"
     " regressions"
     " deviations"
     "Residuals"
# Pg. 82
ANOVAfm5.9.1
Analysis of Variance Table
Response: ht
               Df Sum Sq Mean Sq F value
                                                          Pr(>F)
site
               5 4157543 831509
                                     NaN
                                                             NaN
              36 4425296 122925
                                      NaN
seedlot
                                                             NaN
site:seedlot 150 1351054
                            9007 9.3434 < 0.000000000000000022
 regressions 36 703203
                           19533
 deviations 114 647851
                          5683 5.8951 < 0.00000000000000022 ***
Residuals
              384 370176
                             964
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Code <-
 c (
    "a", "a", "a", "a", "b", "b", "b", "b"
   "c","d","d","d","e","f","g"
  , "h", "h", "i", "i", "j", "k", "l", "m"
```



```
,"n","n","n","o","p","p","q","r"
, "s","t","t","u","v"
)

Tab5.14$Code <- Code

ggplot(
    data = Tab5.14
, mapping = aes(x = Mean, y = Slope)
) +
    geom_point(size = 2) +
    geom_text(
        mapping = aes(label = Code)
, hjust = -0.5
, vjust = -0.5
) +
    theme_bw() +
    labs(
        x = "SeedLot Mean"
, y = "Regression Coefficient"
)</pre>
```





6Variance Components and Genetics Concepts

6.1 Example 6.2 (Pg. 90)

? Example 6.2 (Pg. 90)

A progeny trial of Acacia mangium was planted at Segaluid, Sabah, by the Sabah Forest Research Centre in 1994. The trial was designed to test 48 open-pollinated families collected from natural provenances in Papua New Guinea (PNG, 41 families) and far north Queensland (five families) and two families of the land race that had developed in Sabah after introduction of A. mangium in the 1960s. Based on the results of many previous trials (Harwood & Williams 1992), it was expected that the Sabah and Queensland families would perform more poorly than those from PNG. The trial was set out as an RCB design with four replicates each containing 48 five-tree plots. Spacing was $3m \times 3m$ between trees, and an external perimeter row surrounded the trial. Diameter at breast height (dbh) and height (ht) measurements were taken in 1997, 36 months after planting.

```
library(car)
library(dae)
library(dplyr)
library(emmeans)
library(ggplot2)
library(lmerTest)
library(magrittr)
library(predictmeans)
data(DataExam6.2)
DataExam6.2.1 <-
    DataExam6.2 %>%
    filter(Province == "PNG")
# Pg. 94
fm6.3 <-
     lm (
          formula = Dbh.mean ~ Replication + Family
                  = DataExam6.2.1
     <- anova(fm6.3)
b
        <- function(x){length(x)/sum(1/x)}
```



```
<- HM(DataExam6.2.1$Dbh.count)
S2
         <- b[["Mean Sq"]][length(b[["Mean Sq"]])]</pre>
Sigma2t <- mean(DataExam6.2.1$Dbh.variance)</pre>
sigma2m <- S2-(Sigma2t/w)
fm6.3.1 <-
  lmer(
      formula = Dbh.mean ~ 1 + Replication + (1|Family)
     , data = DataExam6.2.1
     , REML
            = TRUE
    )
# Pg. 104
# summary(fm6.3.1)
varcomp(fm6.3.1)
                     vcov SE 2.5 % 97.5 %
Family.(Intercept) 0.2584 0.1286 0.0538 0.5767
residual
                   1.1667 0.1506 0.8954 1.4774
sigma2f <- 0.2584
h2 \leftarrow (sigma2f/(0.3))/(Sigma2t + sigma2m + sigma2f)
cbind(hmean = w, Sigma2t, sigma2m, sigma2f, h2)
       hmean Sigma2t sigma2m sigma2f
[1,] 4.408602 3.920732 0.2773606 0.2584 0.1932761
fm6.4 <-
  1 m (
      formula = Dbh.mean ~ Replication+Family
      , data = DataExam6.2
    <- anova(fm6.4)
b
        <- function(x){length(x)/sum(1/x)}
        <- HM(DataExam6.2$Dbh.count)
S2
        <- b[["Mean Sq"]][length(b[["Mean Sq"]])]</pre>
Sigma2t <- mean(DataExam6.2$Dbh.variance)</pre>
sigma2m <- S2-(Sigma2t/w)</pre>
fm6.4.1 <-
 lmer(
   formula = Dbh.mean ~ 1 + Replication + Province + (1|Family)
  , data = DataExam6.2
  , REML
           = TRUE
    )
# Pg. 107
varcomp(fm6.4.1)
                             SE 2.5 % 97.5 %
                     vcov
Family.(Intercept) 0.3514 0.1358 0.1203 0.6361
```



```
residual
            1.0951 0.1304 0.8584 1.3634
sigma2f <- 0.3514
h2 <- (sigma2f/(0.3))/(Sigma2t+sigma2m+sigma2f)
cbind(hmean = w, Sigma2t, sigma2m, sigma2f, h2)
       hmean Sigma2t sigma2m sigma2f
[1,] 4.451314 3.860156 0.227873 0.3514 0.2638477
fm6.7.1 <-
 lmer(
   formula = Dbh.mean ~ 1+Replication+(1|Family)
 , data = DataExam6.2.1
  , REML = TRUE
 )
# Pg. 116
varcomp(fm6.7.1)
                    vcov SE 2.5 % 97.5 %
Family.(Intercept) 0.2584 0.1286 0.0538 0.5767
residual
                 1.1667 0.1506 0.8954 1.4774
sigma2f[1] <- 0.2584
fm6.7.2<-
 lmer(
   formula = Ht.mean ~ 1 + Replication + (1|Family)
 , data = DataExam6.2.1
 , REML
          = TRUE
   )
# Pg. 116
varcomp(fm6.7.2)
                    vcov SE 2.5 % 97.5 %
Family.(Intercept) 0.2711 0.1243 0.0743 0.5794
residual
                  1.0549 0.1362 0.8097 1.3359
sigma2f[2] <- 0.2711
fm6.7.3 <-
   formula = Sum.means ~ 1 + Replication + (1|Family)
  , data = DataExam6.2.1
 , REML
          = TRUE
  , control = lmerControl()
 )
# Pg. 116
varcomp(fm6.7.3)
                    vcov SE 2.5 % 97.5 %
Family.(Intercept) 0.8729 0.3907 0.2553 1.8421
residual
                 3.2428 0.4186 2.4888 4.1063
sigma2f[3] <- 0.873
sigma2xy <- 0.5*(sigma2f[3]-sigma2f[1]-sigma2f[2])
GenCorr <- sigma2xy/sqrt(sigma2f[1]*sigma2f[2])</pre>
```





7Incomplete Block Designs



8Analysis of Generalized Lattice Designs

8.1 Example 8.1 (Pg. 139)

? Example 8.1 (Pg. 139)

In the early 1990s Khongsak Pinyopusarerk of CSIRO Forestry and Forest Products initiated a far-reaching study of Casuarina equisetifolia. This is a nitrogen-fixing tree of considerable social, economic and environmental importance in tropical/subtropical littoral zones of Asia, the Pacific and Africa. Provenance collections were obtained from 18 countries and, with this material, more than 40 trials were laid out in 20 countries. The number of seedlots included in each trial varied, depending on the suitability and size of the planting sites for the available material. One of the trials, in Weipa, northern Queensland, contained all the available seedlots and is the example used here.

```
library(car)
library(dae)
library(dplyr)
library(emmeans)
 library(ggplot2)
library(lmerTest)
library(magrittr)
library(predictmeans)
 data(DataExam8.1)
 # Pg. 141
 fm8.4 <-
     formula = dbh ~ inoc + Error(repl/inoc) +
                     inoc*country*prov
            = DataExam8.1
    data
      )
# Pg. 150
 summary(fm8.4)
Error: repl
          Df Sum Sq Mean Sq F value Pr(>F)
                     11.542
           1 11.542
                              11.46 0.0773 .
inoc
Residuals 2
            2.014
                      1.007
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
Error: Within
              Df Sum Sq Mean Sq F value
                                              Pr(>F)
```



```
country
            17 54.62
                       3.213
                               5.305 0.000000159 ***
            41 18.61
                     0.454
                              0.749
prov
                                           0.854
            17
                10.07
                       0.592
                               0.978
                                           0.487
inoc:country
                21.46
            41
                       0.523
                               0.864
                                           0.698
inoc:prov
           116
                70.26
                       0.606
Residuals
Signif. codes: 0 '*** 0.001 '** 0.01 '*' 0.05 '.' 0.1 ' ' 1
# Pg. 150
model.tables(x = fm8.4, type = "means")
Tables of means
Grand mean
3.40411
inoc
   7 weeks 1 week
     3.625
           3.183
rep 118.000 118.000
country
    India Vietnam Egypt Kenya Fiji Thailand Malaysia Philippines Australia
           3.276 2.498 3.491 2.612
                                      3.841 4.031
                                                         3.612
rep 24.000 20.000 12.000 32.000 12.000
                                      16.000
                                              36.000
                                                         12.000
                                                                  16.000
    PNG Solomon Is. Mauritius Sri Lanka Guam China Puerto Rico Vanuatu Benin
                   3.122 3.243 2.342 3.686
                                                 3.345
   3.65
          3.699
                                                            2.762 3.342
rep 4.00
             8.000
                      4.000
                              12.000 4.000 12.000
                                                      4.000
                                                              4.000 4.000
prov
                 3
                     4
                           5
                                6
                                      7
                                           8
                                                10
                                                     11
                                                         12
   2.623 4.013 3.71 3.27 3.404 3.093 3.701 3.541 3.371 3.301 $.18 3.37 3.404
rep 4.000 4.000 4.00 4.00 4.000 4.000 4.000 4.000 4.000 4.000 4.00 4.00 4.00 4.000
              17
                   18 19
                               20
                                     21
                                        22
                                              23 24
                                                         25 26
                                                                  27
      15
         16
   3.595 3.43 3.275 3.085 3.66 3.382 3.235 3.46 3.08 3.555 3.918 3.648 3.43
rep 4.000 4.00 4.000 4.000 4.000 4.000 4.000 4.00 4.00 4.000 4.000 4.000 4.000
                                                          38 39 40
                30
                    31 32 33
                                       34
                                            35
                                                       37
           29
                                                  36
   2.905 3.708 3.196 3.761 3.416 3.178 2.958 3.636 3.376 3.404 $.252 3.15 3.81
rep 4.000 4.000 4.000 4.000 4.000 4.000 4.000 4.000 4.000 4.000 4.000 4.000 4.00 4.00
                    46
                        47
                               48
                                      50
                                           51
                                                52
                                                           54 55
           42
                 45
                                                     53
   3.195 3.613 3.518 2.76 3.733 3.605 3.404 3.685 3.235 3.755 3 605 2.74 3.662
58 59 60 61 62 63
   3.408 3.404 3.404 3.528 3.178 3.506 3.418
rep 4.000 4.000 4.000 4.000 4.000 4.000 4.000
inoc:country
        country
         India Vietnam Egypt Kenya Fiji Thailand Malaysia Philippines
inoc
 7 weeks 3.672 3.443 2.747 3.609 2.955 3.611
                                                  4.502
                                                           3.558
                       6.000 16.000 6.000 8.000
         12.000 10.000
                                                  18.000
                                                           6.000
 rep
                      2.250 3.373 2.268 4.071
         3.477 3.110
                                                  3.559
                                                           3.665
 1 week
         12.000 10.000 6.000 16.000 6.000 8.000
                                                  18.000
                                                           6.000
        country
         Australia PNG
                      Solomon Is. Mauritius Sri Lanka Guam
inoc
                  3.850 4.200
                                   3.390
                                             3.695
 7 weeks 2.959
                                                      2.245 4.030
                   2.000 4.000
                                    2.000
                                             6.000
                                                      2.000
         8.000
                                                            6.000
 rep
                   3.450 3.197
                                   2.855
                                             2.792
                                                       2.440
 1 week
         2.304
                                                             3.342
         8.000
                   2.000 4.000
                                   2.000
                                             6.000
                                                       2.000
                                                             6.000
 rep
        country
```



```
inoc
         Puerto Rico Vanuatu Benin
 7 weeks 3.540
                       2.720
                               3.870
           2.000
                       2.000
                               2.000
 rep
                       2.805
 1 week
           3.150
                               2.815
           2.000
                      2.000
                               2.000
 rep
 inoc:prov
         prov
                                                    8
                          4
                                  5
                                        6
                                             7
                                                          10
                                                                11
inoc
         1
                      3
 7 weeks 2.427 4.682 3.757 3.637 3.625 3.540 4.100 3.774 3.559 3.544 3.135
          2.000 2.819 3.344 3.664 2.904 3.183 2.646 3.301 3.308 3.183 3.058
 1 week 2.819 3.344 3.664 2.904 3.183 2.646 3.301 3.308 3.183 3.058 3.225
         2.427 4.682 3.757 3.637 3.625 3.540 4.100 3.774 3.559 3.544 3.135
         prov
          13
                      15
                            16
                                  17
                                        18
                                              19
                                                    20
inoc
                14
 7 weeks 3.845 3.625 4.104 4.119 3.604 3.114 3.509 3.304 3.591 3.801 3.276
          3.225 2.895 3.183 3.085 2.740 2.945 3.055 3.810 3.460 2.880 3.120
  1 week 2.895 3.183 3.085 2.740 2.945 3.055 3.810 3.460 2.880 3.120 2.885
          3.845 3.625 4.104 4.119 3.604 3.114 3.509 3.304 3.591 3.801 3.276
 rep
         prov
inoc
          24
                25
                      26
                            27
                                  28
                                        29
                                              30
                                                    31
                                                          32
 7 weeks 3.021 3.976 4.286 4.186 2.866 3.663 2.988 3.793 4.358 3.343 3.468
          2.885 4.090 3.860 3.010 2.675 2.945 3.754 3.404 3.729 2.474 3.014
 1 week 4.090 3.860 3.010 2.675 2.945 3.754 3.404 3.729 2.474
                                                                3.014 2.449
          3.021 3.976 4.286 4.186 2.866 3.663 2.988 3.793 4.358 3.343 3.468
         prov
          35
                36
                      37
                            38
                                  39
                                        40
                                              41
                                                    42
                                                          45
                                                                46
inoc
 7 weeks 3.848 3.688 3.625 3.772 3.132 3.972 3.545 3.705 3.439 2.599 4.119
          2.449 3.424 3.064 3.183 2.733 3.168 3.648 2.845 3.520 3.597 2.922
 1 week 3.424 3.064 3.183 2.733 3.168 3.648 2.845 3.520 3.597 2.922 3.347
         3.848 \ 3.688 \ 3.625 \ 3.772 \ 3.132 \ 3.972 \ 3.545 \ 3.705 \ 3.439 \ 2.599 \ 4.119
 rep
         prov
                            52
                                  53
inoc
         48
               50
                     51
                                        54
                                              55
                                                    56
                                                          57
                                                                58
 7 weeks 4.344 3.625 4.137 4.152 4.047 3.167 2.622 3.895 3.478 3.625 3.625
          3.347 2.867 3.183 3.233 2.318 3.463 4.043 2.858 3.430 3.339 3.183
 1 week 2.867 3.183 3.233 2.318 3.463 4.043 2.858 3.430 3.339 3.183 3.183
        4.344 3.625 4.137 4.152 4.047 3.167 2.622 3.895 3.478 3.625 3.625
         prov
          60
                61
                     62
inoc
 7 weeks 3.685 3.630 3.560 3.235
          3.183 3.371 2.726 3.451
 1 week 3.371 2.726 3.451 3.601
 rep
         3.685 3.630 3.560 3.235
 RESFit <-
    data.frame(
      fittedvalue = fitted.aovlist(fm8.4)
      residualvalue = proj(fm8.4)$Within[,"Residuals"]
 ggplot(
          = RESFit
  data
  , mapping = aes(x = fittedvalue, y = residualvalue)
 geom_point(size = 2) +
 labs(
  x = "Residuals vs Fitted Values"
  , y = ""
  ) +
```



```
theme_bw()
0
-1
                                                    5
                    Residuals vs Fitted Values
# Pg. 153
fm8.6 <-
 aov(
   formula = terms(
                  dbh \sim inoc + repl + col +
                       repl:row + repl:col +
                        prov + inoc:prov
                    keep.order = TRUE
 , data
          = DataExam8.1
summary(fm8.6)
           Df Sum Sq Mean Sq F value
                                                 Pr(>F)
           1 11.54 11.542 48.054
                                         0.00000000327 ***
inoc
           2
              2.01
                     1.007 4.193
                                               0.019746 *
repl
           9 65.24
                     7.249 30.182 < 0.0000000000000000 ***
col
                     0.830 3.454
repl:row
           20 16.59
                                               0.000105 ***
repl:col
        27 16.41 0.608 2.530
                                               0.001443 **
                                         0.00000026687 ***
prov
          58 53.89 0.929 3.869
inoc:prov 58 8.47 0.146 0.608
                                               0.970544
Residuals 60 14.41 0.240
```

Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1



8.2 Example 8.1 (continued) (Pg. 147)

```
Example 8.1 (continued) (Pg. 147)
library(car)
library(dae)
library(dplyr)
library(emmeans)
library(ggplot2)
library(lmerTest)
library(magrittr)
library(predictmeans)
 data(DataExam8.1)
 # Pg. 155
fm8.8 <-
 lmerTest::lmer(
     formula = dbh ~ 1 + repl + col + prov +
                     (1|repl:row) + (1|repl:col)
   , data
            = DataExam8.1
     REML
            = TRUE
# Pg. 157
#\dontrun{
varcomp(fm8.8)
                              SE 2.5 % 97.5 %
                      VCOV
repl:col.(Intercept) 0.0459 0.0262 0.0000 0.0565
repl:row.(Intercept) 0.0640 0.0294 0.0210 0.1161
residual
                    0.1951 0.0253 0.1126 0.1782
#}
anova(fm8.8)
Type III Analysis of Variance Table with Satterthwaite's method
     Sum Sq Mean Sq NumDF DenDF F value
                                                    Pr(>F)
repl 2.581 0.86023 3 21.257 4.4082
                                                    0.01469
                      9 23.705 14.1627 0.00000015112494790
col 24.874 2.76378
prov 55.433 0.95574 58 136.623 4.8976 0.0000000000001306
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
anova(fm8.8, ddf = "Kenward-Roger")
Type III Analysis of Variance Table with Kenward-Roger's method
    Sum Sq Mean Sq NumDF DenDF F value
                                                   Pr(>F)
repl 2.580 0.86016 3 22.622 4.4078
                                                    0.0139 *
col 24.824 2.75827 9 22.947 14.1337 0.0000002097637857 **
prov 54.795 0.94473 58 133.852 4.8396 0.0000000000000283 **
```



```
predictmeans(model = fm8.8, modelterm = "repl")
$`Predicted Means`
repl
           2
                 3
3.7543 3.1269 3.2128 3.5023
$`Standard Error of Means`
All means have the same SE
                   0.13629
$`Standard Error of Differences`
 {\tt Max.SED}
          Min.SED Aveg.SED
0.1927495 0.1927423 0.1927472
$LSD
Max.LSD Min.LSD Aveg.LSD
0.39910 0.39909 0.39910
attr(,"Significant level")
[1] 0.05
attr(,"Degree of freedom")
[1] 22.62
$mean_table
                 SE Df LL(95%) UL(95%)
 repl Mean
   1 3.7543 0.13629 22.6214 3.4721 4.0365
    2 3.1269 0.13629 22.6214 2.8447 3.4091
   3 3.2128 0.13629 22.6214 2.9306 3.4950
   4 3.5023 0.13629 22.6214 3.2201 3.7845
predictmeans(model = fm8.8, modelterm = "col")
$`Predicted Means`
col
                        4
                                5
                                        6
                                               7
3.5053 3.4996 3.8509 3.8280 3.5947 3.7829 3.3059 3.5158 3.1776 1 9301
$`Standard Error of Means`
col
                                      5
0.15496 \ \ 0.15649 \ \ 0.15493 \ \ 0.15494 \ \ 0.15490 \ \ 0.15721 \ \ 0.15479 \ \ 0.15699 \ \ \phi.15485 \ \ 0.15648
$`Standard Error of Differences`
 Max.SED Min.SED Aveg.SED
0.2132295 0.2061223 0.2086161
$LSD
Max.LSD Min.LSD Aveg.LSD
0.43742 0.42284 0.42796
attr(,"Significant level")
[1] 0.05
attr(,"Degree of freedom")
[1] 27.12
$mean_table
  col Mean SE Df LL(95%) UL(95%)
```

Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1



```
3 3.8509 0.15493 27.11736 3.5330 4.1687
3
    4 3.8280 0.15494 27.11736 3.5101
4
                                  4.1458
5
    5 3.5947 0.15490 27.11736 3.2769
                                  3.9125
6
    6 3.7829 0.15721 27.11736 3.4604 4.1054
7
    7 3.3059 0.15479 27.11736 2.9883 3.6234
    8 3.5158 0.15699 27.11736 3.1938 3.8379
    9 3.1776 0.15485 27.11736 2.8599 3.4952
  10 1.9301 0.15648 27.11736 1.6091 2.2511
10
predictmeans(model = fm8.8, modelterm = "prov")
$`Predicted Means`
                               6
                           5
                                        7
                                                    10
2.4222 3.1425 2.8646 2.2599 3.7189 3.5445 3.9474 2.7469 2.6459 2.0497 2.7497
            15 16 17 18 19 20 21
                                                         22
  13 14
2.9833 2.6534 3.4459 3.9209 3.4294 3.3624 3.6540 3.3685 3.2210 3 3315 3.2453
      25
            26 27
                        28
                              29
                                    30
                                          31 32
                                                         33
3.6933 3.8460 3.5233 3.5271 3.1001 3.8997 3.5447 4.1294 4.2755 3 7429 3.8890
                                                         46 47
   35 36 37 38
                        39 40 41
                                          42 45
4.1179\ 3.8526\ 3.4538\ 3.0379\ 3.5306\ 3.7412\ 3.7422\ 3.8765\ 4.2126\ 3.4660\ 4.4688
       50 51 52
                        53 54
                                    55
                                           56 57
                                                         58 59
3.7503 2.5571 3.4571 3.3227 3.5926 3.5337 2.7157 2.7702 3.9805 2 9968 3.3978
  60 61 62 63
3.0115 3.2238 3.2814 3.5751
$`Standard Error of Means`
prov
                        4 5 6
                  3
0.25362 \ 0.25446 \ 0.25278 \ 0.25443 \ 0.25423 \ 0.25588 \ 0.25420 \ 0.25338 \ \phi.25417 \ 0.\overline{25259}
          13 14 15 16 17
                                         18 19
                                                         20
0.25306 \ 0.25436 \ 0.25259 \ 0.25232 \ 0.25502 \ 0.25319 \ 0.25340 \ 0.25309 \ \emptyset.25294 \ 0.25204
         23 24 25 26 27
                                          28 29
                                                         30
0.25350 0.25355 0.25358 0.25316 0.25289 0.25294 0.25291 0.25341
                                                       0.25254 0.25330
    32
        33
              34 35 36
                                   37
                                          38 39
                                                         40
0.25377 0.25387 0.25510 0.25347 0.25351 0.25352 0.25416 0.25393 0.25450 0.25416
               46 47
                                          51 52
          45
                            48
                                   50
                                                        53
0.25303 0.25257 0.25323 0.25316 0.25356 0.25354 0.25372 0.25361
                                                       0.25237 0.25321
   55 56 57 58 59 60
                                          61 62
                                                        63
0.25374 0.25639 0.25173 0.25319 0.25250 0.25303 0.25378 0.25266 0.25500
$`Standard Error of Differences`
Max.SED Min.SED Aveg.SED
0.3591712 0.3326719 0.3482665
$LSD
Max.LSD Min.LSD Aveg.LSD
0.70924 0.65691 0.68770
attr(, "Significant level")
[1] 0.05
attr(,"Degree of freedom")
[1] 162.73
$mean_table
             SE Df LL(95%) UL(95%)
  prov Mean
    1 2.4222 0.25362 162.7269 1.9214 2.9230
```

1

2

1 3.5053 0.15496 27.11736 3.1874 3.8232

2 3.4996 0.15649 27.11736 3.1786 3.8207



2	2	3.1425	0.25446	162.7269	2.6401	3.6450
3	3	2.8646	0.25278	162.7269	2.3655	3.3638
4	4	2.2599	0.25443	162.7269	1.7575	2.7623
5	5	3.7189	0.25423	162.7269	3.2169	4.2209
6	6	3.5445	0.25588	162.7269	3.0392	4.0498
7	7	3.9474	0.25420	162.7269	3.4454	4.4493
8	8	2.7469	0.25338	162.7269	2.2466	3.2473
9	10	2.6459	0.25417	162.7269	2.1440	3.1478
10		2.0497	0.25259	162.7269	1.5509	2.5485
1:		2.7497	0.25306	162.7269	2.2500	3.2494
12		2.9833	0.25436	162.7269	2.4810	3.4855
13	3 14	2.6534	0.25259	162.7269	2.1546	3.1522
14	4 15	3.4459	0.25232	162.7269	2.9476	3.9441
15	5 16	3.9209	0.25502	162.7269	3.4173	4.4245
16	3 17	3.4294	0.25319	162.7269	2.9294	3.9293
17	7 18	3.3624	0.25340	162.7269	2.8620	3.8628
18	3 19	3.6540	0.25309	162.7269	3.1543	4.1538
19		3.3685	0.25294	162.7269	2.8690	3.8680
20		3.2210	0.25204	162.7269	2.7234	3.7187
2:		3.3315	0.25350	162.7269	2.8310	3.8321
22		3.2453		162.7269	2.7447	3.7460
			0.25355			
23		3.6933	0.25358	162.7269	3.1926	4.1941
24		3.8460	0.25316	162.7269	3.3461	4.3459
25		3.5233	0.25289	162.7269	3.0239	4.0227
26		3.5271	0.25294	162.7269	3.0276	4.0265
27	7 28	3.1001	0.25291	162.7269	2.6007	3.5996
28	3 29	3.8997	0.25341	162.7269	3.3993	4.4001
29	9 30	3.5447	0.25254	162.7269	3.0460	4.0434
30	31	4.1294	0.25330	162.7269	3.6293	4.6296
3:	1 32	4.2755	0.25377	162.7269	3.7744	4.7766
32	2 33	3.7429	0.25387	162.7269	3.2416	4.2442
33	3 34	3.8890	0.25510	162.7269	3.3853	4.3928
34	4 35	4.1179	0.25347	162.7269	3.6174	4.6185
35	5 36	3.8526	0.25351	162.7269	3.3520	4.3532
36		3.4538	0.25352	162.7269	2.9532	3.9544
37		3.0379	0.25416	162.7269	2.5360	3.5398
38		3.5306	0.25393	162.7269	3.0291	4.0320
39			0.25450		3.2386	4.2437
40			0.25416		3.2403	4.2440
4:			0.25410			4.3761
				162.7269	3.3769 3.7139	4.7114
42			0.25257	162.7269		
43			0.25323	162.7269	2.9660	3.9661
44			0.25316	162.7269	3.9689	4.9687
45			0.25356	162.7269	3.2496	4.2510
46		2.5571	0.25354	162.7269	2.0564	3.0577
47		3.4571	0.25372	162.7269	2.9561	3.9582
48		3.3227	0.25361	162.7269	2.8219	3.8235
49			0.25237	162.7269	3.0943	4.0910
50				162.7269	3.0337	4.0337
5:	1 55	2.7157	0.25374	162.7269	2.2146	3.2167
52	2 56	2.7702	0.25639	162.7269	2.2640	3.2765
53	3 57	3.9805	0.25173	162.7269	3.4834	4.4776
54			0.25319	162.7269	2.4968	3.4968
55			0.25250	162.7269	2.8992	3.8963
56			0.25303	162.7269	2.5118	3.5112
57			0.25378	162.7269	2.7227	3.7250
58			0.25266	162.7269	2.7825	3.7803
59					3.0716	4.0787
	, 00	5.0701	3.20000	102.1200	0.0110	1.0101



```
# Pg. 161
  RCB1 <-
        aov(dbh ~ prov + repl, data = DataExam8.1)
  RCB <-
        emmeans(RCB1, specs = "prov") %>%
        as_tibble()
  Mixed <-
          emmeans(fm8.8, specs = "prov") %>%
          as_tibble()
  table8.9 <-
      left_join(
              = RCB
         x
               = Mixed
       , by = "prov"
       , suffix = c(".RCBD", ".Mixed")
  print(table8.9)
# A tibble: 59 x 11
  prov emmean.RCBD SE.RCBD df.RCBD lower.CL.RCBD upper.CL.RCBD emmean.Mixed
  <fct>
             <dbl>
                     <dbl> <dbl>
                                         <dbl>
                                                      <dbl>
                                                                   <dbl>
                                                        2.60
              1.85
                     0.382
                              174
                                           1.10
                                                                     2.42
                    0.382
              3.24
                              174
                                          2.49
                                                        3.99
                                                                    3.14
3 3
              2.94 0.382
                                                        3.69
                              174
                                          2.18
                                                                    2.86
                                                       3.25
4 4
              2.50 0.382
                              174
                                          1.74
                                                                    2.26
5 5
              3.34 0.382
                              174
                                         2.59
                                                        4.10
                                                                    3.72
              3.37 0.382
                                         2.62
                                                        4.13
                                                                    3.54
6 6
                              174
7 7
             3.98 0.382
                              174
                                          3.23
                                                        4.74
                                                                    3.95
             2.63
                                          1.88
                                                                    2.75
8 8
                     0.382
                              174
                                                        3.39
                                          1.71
                                                        3.22
9 10
              2.47
                     0.382
                               174
                                                                    2.65
       2.40
                     0.382
                              174
                                                        3.15
                                                                    2.05
10 11
                                          1.64
# i 49 more rows
# i 4 more variables: SE.Mixed <dbl>, df.Mixed <dbl>, lower.CL.Mixed <dbl>,
   upper.CL.Mixed <dbl>
```

8.3 Example 8.1 (continued) (Pg. 155)

```
Example 8.1 (continued) (Pg. 155)
library(car)
library(dae)
library(dplyr)
library(emmeans)
library(ggplot2)
library(lmerTest)
```



```
library(magrittr)
library(predictmeans)
 data(DataExam8.1)
# Pg. 167
fm8.11 <-
  aov(
       formula = dbh ~ country + country:prov
      , data
             = DataExam8.1
  b <- anova(fm8.11)
  Res <- length(b[["Sum Sq"]])</pre>
   df <- 119
  MSS <- 0.1951
   b[["Df"]][Res] <- df
  b[["Sum Sq"]][Res] <- MSS*df
  b[["Mean Sq"]][Res] <- b[["Sum Sq"]][Res]/b[["Df"]][Res]
  b[["F value"]][1:Res-1] <-
            b[["Mean Sq"]][1:Res-1]/b[["Mean Sq"]][Res]
  b[["Pr(>F)"]][Res-1] <-
     df(
       b[["F value"]][Res-1]
      , b[["Df"]][Res-1]
      , b[["Df"]][Res]
Analysis of Variance Table
Response: dbh
             Df Sum Sq Mean Sq F value
                                              Pr(>F)
             17 54.619 3.2129 16.468 0.00000001235 ***
country
country:prov 41 18.606 0.4538 2.326
                                            0.001502 **
Residuals
            119 23.217 0.1951
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
 emmeans(fm8.11, specs = "country")
            emmean SE df lower.CL upper.CL
country
                                       3.90
India
              3.57 0.165 177
                               3.25
Vietnam
              3.28 0.181 177
                                 2.92
                                         3.63
Egypt
              2.50 0.233 177
                                 2.04
                                         2.96
                                 3.21
              3.49 0.143 177
                                         3.77
Kenya
              2.61 0.233 177
                                 2.15
                                         3.07
Fiji
Thailand
              3.84 0.202 177
                                 3.44
                                          4.24
              4.03 0.135 177
                                 3.77
                                          4.30
Malaysia
Philippines 3.61 0.233 177
                                 3.15
                                          4.07
```



```
Australia
               2.63 0.202 177
                                   2.23
                                            3.03
 PNG
               3.65 0.404 177
                                            4.45
                                   2.85
                                            4.26
Solomon Is.
               3.70 0.285 177
                                   3.14
                                            3.92
Mauritius
               3.12 0.404 177
                                   2.33
                                   2.78
                                            3.70
Sri Lanka
               3.24 0.233 177
Guam
               2.34 0.404 177
                                   1.55
                                            3.14
China
               3.69 0.233 177
                                   3.23
                                            4.15
Puerto Rico
               3.35 0.404 177
                                   2.55
                                            4.14
               2.76 0.404 177
                                   1.97
                                            3.56
Vanuatu
Benin
               3.34 0.404 177
                                   2.55
                                            4.14
Results are averaged over the levels of: prov
Confidence level used: 0.95
```

8.4 Example 8.2 (Pg. 157)

? Example 8.2 (Pg. 157)

In Example 7.1 we discussed a Eucalyptus clone trial conducted in Vietnam and described the experimental layout. The trial tested 56 hybrid clones of the interspecific hybrid combination $E.\ urophylla \times E.\ pellita$ (UP). These candidates had been selected from progeny trials of control-pollinated hybrid families; here we ignore the parental origins of the different UP clones.

```
library(car)
library(dae)
library(dplyr)
library(emmeans)
library(ggplot2)
library(lmerTest)
library(magrittr)
library(predictmeans)
data(DataExam8.2)
# Pg.
fm8.2
      <-
  lmerTest::lmer(
    formula = dbh ~ repl + column +
                     contcompf + contcompf:standard +
                     (1|repl:row) + (1|repl:column) +
                     (1|contcompv:clone)
  , data
            = DataExam8.2
    )
#\dontrun{
varcomp(fm8.2)
```



```
vcov
                                       SE 2.5 % 97.5 %
\verb|contcompv:clone.(Intercept)| 0.4950 0.1126 0.3057 0.7422|
repl:row.(Intercept) 0.0802 0.0351 0.0173 0.1458 repl:column.(Intercept) 0.0529 0.0326 0.0000 0.0783
repl:column.(Intercept)
residual
                            0.3992 0.0435 0.3245 0.5024
#}
anova(fm8.2)
Type III Analysis of Variance Table with Satterthwaite's method
                    Sum Sq Mean Sq NumDF DenDF F value
                                                                  Pr(>F)
                                    4 26.467 2.0489
repl
                    3.2720 0.8180
                                                                0.1162606
                                    5 19.545 1.5539
column
                    3.1018 0.6204
                                                                0.2194719
                    5.3203 5.3203
                                                                0.0005845 ***
contcompf
                                      1 54.905 13.3265
contcompf:standard 20.6587 6.8862
                                      3 207.152 17.2488 0.0000000004896 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
 Anova(fm8.2, type = "II", test.statistic = "Chisq")
Analysis of Deviance Table (Type II Wald chisquare tests)
Response: dbh
                     Chisq Df Pr(>Chisq)
                    8.1957 4
repl
                                0.08467 .
                    7.7694 5
                                 0.16941
column
                    4.6841 1
                                0.03044 *
contcompf
contcompf:standard 51.7463 3 3.392e-11 ***
Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
predictmeans(model = fm8.2, modelterm = "repl")
$`Predicted Means`
repl
            2
                   3
7.8926 8.2070 8.3429 8.4604 8.5464
$`Standard Error of Means`
repl
             2
                      3
0.33123 0.33126 0.32992 0.32992 0.32992
$`Standard Error of Differences`
  Max.SED
          Min.SED Aveg.SED
0.2239675 0.2167320 0.2196681
$LSD
Max.LSD Min.LSD Aveg.LSD
0.44792 0.43345 0.43932
attr(,"Significant level")
[1] 0.05
attr(,"Degree of freedom")
[1] 60.56
$mean_table
                   SE
                          Df LL(95%) UL(95%)
 repl Mean
    1 7.8926 0.33123 60.55892 7.2302 8.5551
     2 8.2070 0.33126 60.55892 7.5445 8.8695
2
3
     3 8.3429 0.32992 60.55892 7.6831 9.0027
4
     4 8.4604 0.32992 60.55892 7.8006 9.1202
```



```
predictmeans(model = fm8.2, modelterm = "column")
$`Predicted Means`
column
          2
                3
                       4
                             5
8.2214 8.4708 8.3779 7.9721 7.8166 8.7141
$`Standard Error of Means`
column
                        4
0.31662 0.39168 0.39315 0.26648 0.26646 0.31653
$`Standard Error of Differences`
 Max.SED Min.SED Aveg.SED
0.2714760 0.2102583 0.2373610
$LSD
Max.LSD Min.LSD Aveg.LSD
0.54250 0.42017 0.47433
attr(,"Significant level")
[1] 0.05
attr(,"Degree of freedom")
[1] 62.99
$mean_table
 column Mean SE Df LL(95%) UL(95%)
      1 8.2214 0.31662 62.99437 7.5887 8.8542
      2 8.4708 0.39168 62.99437 7.6881 9.2535
     3 8.3779 0.39315 62.99437 7.5923 9.1636
     4 7.9721 0.26648 62.99437 7.4396 8.5047
     5 7.8166 0.26646 62.99437 7.2841 8.3491
      6 8.7141 0.31653 62.99437 8.0816 9.3467
emmeans(object = fm8.2, specs = ~contcompf|standard)
contcompf = 1, standard = 0:
emmean SE df lower.CL upper.CL
  8.91 0.117 65.9
                    8.67
contcompf = 0, standard = UG323:
emmean SE df lower.CL upper.CL
  8.97 0.770 55.6
                  7.43
contcompf = 0, standard = U6:
emmean SE df lower.CL upper.CL
  6.55 0.770 55.5
                    5.01
                           8.10
contcompf = 0, standard = PN14:
emmean SE df lower.CL upper.CL
  7.70 0.771 55.8 6.16 9.25
contcompf = 0, standard = SSOseed:
emmean SE df lower.CL upper.CL
                           7.63
  6.08 0.770 55.5 4.54
Results are averaged over the levels of: repl, column
```

5 8.5464 0.32992 60.55892 7.8866 9.2062



Degrees-of-freedom method: kenward-roger Confidence level used: 0.95



Experimental Design and Analysis for Tree Improvement







