# Imperative programming - tutorial week 2

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```
short a=350;
int b=3, c=10;
long d=1;
float x=391;
double y=0.71, z=0.35;
```

```
short a=350;
int b=3, c=10;
long d=1;
float x=391;
double y=0.71, z=0.35;
1. d = a * b;
```

```
short a=350;
int b=3, c=10;
long d=1;
float x=391;
double y=0.71, z=0.35;

1. d = a * b;
    short * int → int, fits in long
```

```
short a=350;
int b=3, c=10;
long d=1;
float x=391;
double y=0.71, z=0.35;

1. d = a * b;
    short * int → int, fits in long
    Result: d = 1050
```

```
short a=350;
int b=3, c=10;
long d=1;
float x=391;
double y=0.71, z=0.35;

1. d = a * b;
    short * int → int, fits in long
    Result: d = 1050
2. c = a / b;
```

```
short a=350;
int b=3, c=10;
long d=1;
float x=391;
double y=0.71, z=0.35;

1. d = a * b;
    short * int → int, fits in long
    Result: d = 1050

2. c = a / b;
    short / int → int, fits in int
```

```
short a=350;
int b=3, c=10;
long d=1;
float x=391;
double y=0.71, z=0.35;
  1. d = a * b;
     short * int \rightarrow int, fits in long
     Result: d = 1050
  2. c = a / b;
     short / int \rightarrow int, fits in int
     Result: c = 116 (integer division)
```

```
short a=350;
int b=3, c=10;
long d=1;
float x=391;
double y=0.71, z=0.35;
  1. d = a * b;
     short * int \rightarrow int, fits in long
     Result: d = 1050
  2. c = a / b;
     short / int \rightarrow int, fits in int
     Result: c = 116 (integer division)
  3. y = c / b;
```

```
short a=350;
int b=3, c=10;
long d=1;
float x=391;
double y=0.71, z=0.35;
  1. d = a * b;
     short * int \rightarrow int, fits in long
     Result: d = 1050
  2. c = a / b;
     short / int \rightarrow int, fits in int
     Result: c = 116 (integer division)
  3. y = c / b;
     int / int \rightarrow int, fits in double
```

```
short a=350;
int b=3, c=10;
long d=1;
float x=391;
double v=0.71, z=0.35;
  1. d = a * b;
     short * int \rightarrow int, fits in long
     Result: d = 1050
  2. c = a / b;
     short / int \rightarrow int, fits in int
     Result: c = 116 (integer division)
  3. y = c / b;
     int / int \rightarrow int, fits in double
     Result: v = 3.0
```

```
short a=350;
int b=3, c=10;
long d=1;
float x=391;
double v=0.71, z=0.35;
  1. d = a * b;
     short * int \rightarrow int, fits in long
     Result: d = 1050
  2. c = a / b;
     short / int \rightarrow int, fits in int
     Result: c = 116 (integer division)
  3. y = c / b;
     int / int \rightarrow int, fits in double
     Result: v = 3.0
 4. y = b + x;
```

```
short a=350;
int b=3, c=10;
long d=1;
float x=391;
double v=0.71, z=0.35;
  1. d = a * b;
     short * int \rightarrow int, fits in long
     Result: d = 1050
  2. c = a / b;
     short / int \rightarrow int, fits in int
     Result: c = 116 (integer division)
  3. y = c / b;
     int / int \rightarrow int, fits in double
     Result: v = 3.0
  4. y = b + x;
     int + float \rightarrow float, fits in double
```

```
short a=350;
int b=3, c=10;
long d=1;
float x=391;
double y=0.71, z=0.35;
  1. d = a * b;
     short * int \rightarrow int, fits in long
     Result: d = 1050
  2. c = a / b;
     short / int \rightarrow int, fits in int
     Result: c = 116 (integer division)
  3. y = c / b;
     int / int \rightarrow int, fits in double
     Result: v = 3.0
  4. y = b + x;
     int + float \rightarrow float, fits in double
     Result: y = 394.0
```

```
short a=350;
int b=3, c=10;
long d=1;
float x=391;
double y=0.71, z=0.35;
```

```
short a=350;
int b=3, c=10;
long d=1;
float x=391;
double y=0.71, z=0.35;
5. a = a + 1;
```

```
short a=350;
int b=3, c=10;
long d=1;
float x=391;
double y=0.71, z=0.35;

5. a = a + 1;
    short + int → int, does not fit in short
```

```
short a=350;
int b=3, c=10;
long d=1;
float x=391;
double y=0.71, z=0.35;

5. a = a + 1;
    short + int → int, does not fit in short
    Solution: a = (short)(a + 1);
    Note: In practice, few programmers will cast this, although in some language (like Java) you have to.
    Result: a = 351
```

```
short a=350:
int b=3, c=10;
long d=1;
float x=391;
double y=0.71, z=0.35;
 5. a = a + 1;
     short + int \rightarrow int, does not fit in short
     Solution: a = (short)(a + 1);
     Note: In practice, few programmers will cast this, although in some
     language (like Java) you have to.
     Result: a = 351
 6. a++;
```

Given are the following declarations:

```
short a=350:
int b=3, c=10;
long d=1;
float x=391;
double y=0.71, z=0.35;
 5. a = a + 1:
     short + int \rightarrow int, does not fit in short
     Solution: a = (short)(a + 1);
     Note: In practice, few programmers will cast this, although in some
     language (like Java) you have to.
     Result: a = 351
 6. a++:
```

The '++' operation on a short yields a short. So, this is ok.

Given are the following declarations:

```
short a=350:
int b=3, c=10;
long d=1;
float x=391;
double y=0.71, z=0.35;
 5. a = a + 1:
     short + int \rightarrow int, does not fit in short
     Solution: a = (short)(a + 1);
     Note: In practice, few programmers will cast this, although in some
     language (like Java) you have to.
     Result: a = 351
```

a++;
 The '++' operation on a short yields a short. So, this is ok.
 Result: a = 351:

```
short a=350:
int b=3, c=10;
long d=1;
float x=391;
double y=0.71, z=0.35;
  5. a = a + 1:
     short + int \rightarrow int, does not fit in short
     Solution: a = (short)(a + 1);
     Note: In practice, few programmers will cast this, although in some
     language (like Java) you have to.
     Result: a = 351
  6. a++:
     The '++' operation on a short yields a short. So, this is ok.
     Result: a = 351:
  7. b = a + 1
```

```
short a=350:
int b=3, c=10;
long d=1;
float x=391;
double y=0.71, z=0.35;
  5. a = a + 1:
     short + int \rightarrow int, does not fit in short
     Solution: a = (short)(a + 1);
     Note: In practice, few programmers will cast this, although in some
     language (like Java) you have to.
     Result: a = 351
  6. a++;
     The '++' operation on a short yields a short. So, this is ok.
     Result: a = 351:
  7. b = a + 1
     short + int \rightarrow int, fits in int
```

```
short a=350:
int b=3, c=10;
long d=1;
float x=391;
double y=0.71, z=0.35;
  5. a = a + 1:
     short + int \rightarrow int, does not fit in short
     Solution: a = (short)(a + 1);
     Note: In practice, few programmers will cast this, although in some
     language (like Java) you have to.
     Result: a = 351
  6. a++;
     The '++' operation on a short yields a short. So, this is ok.
     Result: a = 351:
  7. b = a + 1
     short + int \rightarrow int, fits in int
     Result: b = 351
```

```
short a=350;
int b=3, c=10;
long d=1;
float x=391;
double y=0.71, z=0.35;
8. d = 100 * (x - y);
```

```
short a=350; int b=3, c=10; long d=1; float x=391; double y=0.71, z=0.35;  
8. d = 100 * (x - y); int * (float - double) \rightarrow int * double \rightarrow double, does not fit in long
```

```
short a=350;
int b=3, c=10;
long d=1;
float x=391;
double y=0.71, z=0.35;

8. d = 100 * (x - y);
    int * (float - double) → int * double → double, does not fit in long
    Solution 1: d = (long)(100 * (x-y)); Result: d = 39029
    Solution 2: d = 100 * (long)(x-y); Result: d = 39000
```

```
short a=350;
int b=3, c=10;
long d=1;
float x=391;
double y=0.71, z=0.35;

8. d = 100 * (x - y);
   int * (float - double) → int * double → double, does not fit in long
   Solution 1: d = (long)(100 * (x-y)); Result: d = 39029
   Solution 2: d = 100 * (long)(x-y); Result: d = 39000

9. x = (float)(a / b);
```

```
short a=350;
int b=3, c=10;
long d=1;
float x=391;
double y=0.71, z=0.35;

8. d = 100 * (x - y);
    int * (float - double) → int * double → double, does not fit in long
    Solution 1: d = (long)(100 * (x-y)); Result: d = 39029
    Solution 2: d = 100 * (long)(x-y); Result: d = 39000

9. x = (float)(a / b);
    (float)(short / int) → (float)(int) → float, fits in float
```

```
short a=350:
int b=3, c=10;
long d=1;
float x=391:
double y=0.71, z=0.35;
 8. d = 100 * (x - y);
     int * (float - double) \rightarrow int * double \rightarrow double, does not fit in long
     Solution 1: d = (long)(100 * (x-y)); Result: d = 39029
     Solution 2: d = 100 * (long)(x-y); Result: d = 39000
  9. x = (float)(a / b);
     (float)(short / int) \rightarrow (float)(int) \rightarrow float, fits in float
     Result: x = 116.0
```

```
short a=350:
int b=3, c=10;
long d=1;
float x=391:
double y=0.71, z=0.35;
 8. d = 100 * (x - y);
     int * (float - double) \rightarrow int * double \rightarrow double, does not fit in long
     Solution 1: d = (long)(100 * (x-y)); Result: d = 39029
     Solution 2: d = 100 * (long)(x-y); Result: d = 39000
  9. x = (float)(a / b);
     (float)(short / int) \rightarrow (float)(int) \rightarrow float, fits in float
     Result: x = 116.0
 10. z = (float)a / c:
```

```
short a=350:
int b=3, c=10;
long d=1;
float x=391:
double v=0.71, z=0.35;
 8. d = 100 * (x - y);
     int * (float - double) \rightarrow int * double \rightarrow double, does not fit in long
     Solution 1: d = (long)(100 * (x-y)); Result: d = 39029
     Solution 2: d = 100 * (long)(x-y); Result: d = 39000
  9. x = (float)(a / b);
     (float)(short / int) \rightarrow (float)(int) \rightarrow float, fits in float
     Result: x = 116.0
 10. z = (float)a / c;
     (float)short / int \rightarrow float / int \rightarrow float, fits in double
```

```
short a=350:
int b=3, c=10;
long d=1;
float x=391:
double y=0.71, z=0.35;
 8. d = 100 * (x - y);
     int * (float - double) \rightarrow int * double \rightarrow double, does not fit in long
     Solution 1: d = (long)(100 * (x-y)); Result: d = 39029
     Solution 2: d = 100 * (long)(x-y); Result: d = 39000
  9. x = (float)(a / b);
     (float)(short / int) \rightarrow (float)(int) \rightarrow float, fits in float
     Result: x = 116.0
 10. z = (float)a / c;
     (float)short / int \rightarrow float / int \rightarrow float, fits in double
     Result: z = 35.0;
```

```
short a=350:
int b=3, c=10;
long d=1;
float x=391:
double v=0.71, z=0.35;
 8. d = 100 * (x - y);
     int * (float - double) \rightarrow int * double \rightarrow double, does not fit in long
     Solution 1: d = (long)(100 * (x-y)); Result: d = 39029
     Solution 2: d = 100 * (long)(x-y); Result: d = 39000
  9. x = (float)(a / b);
     (float)(short / int) \rightarrow (float)(int) \rightarrow float, fits in float
     Result: x = 116.0
 10. z = (float)a / c:
     (float)short / int \rightarrow float / int \rightarrow float, fits in double
     Result: z = 35.0:
 11. a = (int)y + x;
```

```
short a=350:
int b=3, c=10;
long d=1;
float x=391;
double v=0.71, z=0.35;
 8. d = 100 * (x - y);
     int * (float - double) \rightarrow int * double \rightarrow double, does not fit in long
     Solution 1: d = (long)(100 * (x-y)); Result: d = 39029
     Solution 2: d = 100 * (long)(x-y); Result: d = 39000
  9. x = (float)(a / b);
     (float)(short / int) \rightarrow (float)(int) \rightarrow float, fits in float
     Result: x = 116.0
 10. z = (float)a / c;
     (float)short / int \rightarrow float / int \rightarrow float, fits in double
     Result: z = 35.0;
 11. a = (int)y + x;
     (int)double + float \rightarrow int + float \rightarrow float, does not fit in short
```

```
short a=350:
int b=3, c=10;
long d=1;
float x=391;
double v=0.71, z=0.35;
 8. d = 100 * (x - y);
     int * (float - double) \rightarrow int * double \rightarrow double, does not fit in long
     Solution 1: d = (long)(100 * (x-y)); Result: d = 39029
     Solution 2: d = 100 * (long)(x-y); Result: d = 39000
  9. x = (float)(a / b);
     (float)(short / int) \rightarrow (float)(int) \rightarrow float, fits in float
     Result: x = 116.0
 10. z = (float)a / c;
     (float)short / int \rightarrow float / int \rightarrow float, fits in double
     Result: z = 35.0:
 11. a = (int)y + x;
     (int)double + float \rightarrow int + float \rightarrow float, does not fit in short
     Solution: a = (short)(y + x); Result: a = 391
```

```
short a=350;
int b=3, c=10;
long d=1;
float x=391;
double y=0.71, z=0.35;
12. a = (int)(y + x);
```

```
short a=350;
int b=3, c=10;
long d=1;
float x=391;
double y=0.71, z=0.35;

12. a = (int)(y + x);
    (int)(double + float) → (int)double → int, does not fit in short
```

```
short a=350;
int b=3, c=10;
long d=1;
float x=391;
double y=0.71, z=0.35;

12. a = (int)(y + x);
   (int)(double + float) → (int)double → int, does not fit in short
   Solution: a = (short)(y + x);
   Result: a = 391
```

```
short a=350;
int b=3, c=10;
long d=1;
float x=391;
double y=0.71, z=0.35;

12. a = (int)(y + x);
    (int)(double + float) → (int)double → int, does not fit in short
    Solution: a = (short)(y + x);
    Result: a = 391

13. a = (short)(y + x);
```

```
short a=350;
int b=3, c=10;
long d=1;
float x=391;
double y=0.71, z=0.35;
12. a = (int)(y + x);
     (int)(double + float) \rightarrow (int)double \rightarrow int, does not fit in short
     Solution: a = (short)(y + x);
     Result: a = 391
13. a = (short)(y + x);
     (short)(double + float) \rightarrow (short)(double \rightarrow short, fits in short)
```

```
short a=350;
int b=3, c=10;
long d=1;
float x=391;
double y=0.71, z=0.35;
12. a = (int)(y + x);
     (int)(double + float) \rightarrow (int)double \rightarrow int, does not fit in short
     Solution: a = (short)(y + x);
     Result: a = 391
 13. a = (short)(y + x);
     (short)(double + float) \rightarrow (short)(double \rightarrow short, fits in short)
     Result: a = 391
```

```
short a=350;
int b=3, c=10;
long d=1;
float x=391;
double y=0.71, z=0.35;
12. a = (int)(y + x);
     (int)(double + float) \rightarrow (int)double \rightarrow int, does not fit in short
     Solution: a = (short)(y + x);
     Result: a = 391
 13. a = (short)(y + x);
     (short)(double + float) \rightarrow (short)(double \rightarrow short, fits in short)
     Result: a = 391
14. c = (int)a / z:
```

```
short a=350:
int b=3, c=10;
long d=1;
float x=391:
double y=0.71, z=0.35;
 12. a = (int)(y + x);
     (int)(double + float) \rightarrow (int)double \rightarrow int, does not fit in short
     Solution: a = (short)(y + x);
     Result: a = 391
 13. a = (short)(y + x);
     (short)(double + float) \rightarrow (short)double \rightarrow short, fits in short
     Result: a = 391
 14. c = (int)a / z;
     (int)short / double \rightarrow int / double \rightarrow double, does not fit in int
```

```
short a=350;
int b=3, c=10;
long d=1;
float x=391:
double y=0.71, z=0.35;
 12. a = (int)(y + x);
     (int)(double + float) \rightarrow (int)double \rightarrow int, does not fit in short
     Solution: a = (short)(y + x);
     Result: a = 391
 13. a = (short)(y + x);
     (short)(double + float) \rightarrow (short)double \rightarrow short, fits in short
     Result: a = 391
 14. c = (int)a / z;
     (int)short / double \rightarrow int / double \rightarrow double, does not fit in int
     Solution: c = (int)(a/z);
     Result: c = 1000
```

```
short a=350;
int b=3, c=10;
long d=1;
float x=391;
double y=0.71, z=0.35;
15. c = a / (int)z;
```

```
short a=350; int b=3, c=10; long d=1; float x=391; double y=0.71, z=0.35; 15. \ c = a \ / \ (int)z; \\ short \ / \ (int)double \rightarrow short \ / \ int \rightarrow int, \ fits in \ int
```

```
short a=350;
int b=3, c=10;
long d=1;
float x=391;
double y=0.71, z=0.35;

15. c = a / (int)z;
    short / (int)double → short / int → int, fits in int
    Crashes with "Floating point exception". We divide by zero, since
    (int)0.35 == 0.
```

```
short a=350;
int b=3, c=10;
long d=1;
float x=391;
double y=0.71, z=0.35;

15. c = a / (int)z;
    short / (int)double → short / int → int, fits in int
    Crashes with "Floating point exception". We divide by zero, since
    (int)0.35 == 0.
    Solution: c = (int)(a / z);
    Result: c = 1000
```

```
short a=350:
int b=3, c=10;
long d=1;
float x=391;
double y=0.71, z=0.35;
15. c = a / (int)z;
     short / (int)double \rightarrow short / int \rightarrow int, fits in int
     Crashes with "Floating point exception". We divide by zero, since
     (int)0.35 == 0.
     Solution: c = (int)(a / z);
     Result: c = 1000
16. c = (int)(a / z):
```

```
short a=350:
int b=3, c=10:
long d=1;
float x=391;
double y=0.71, z=0.35;
15. c = a / (int)z;
     short / (int)double \rightarrow short / int \rightarrow int, fits in int
     Crashes with "Floating point exception". We divide by zero, since
     (int)0.35 == 0.
     Solution: c = (int)(a / z);
     Result: c = 1000
 16. c = (int)(a / z);
     (int) (short / double) \rightarrow (int) double \rightarrow int, fits in int
```

```
short a=350:
int b=3, c=10:
long d=1;
float x=391;
double y=0.71, z=0.35;
15. c = a / (int)z;
     short / (int)double \rightarrow short / int \rightarrow int, fits in int
     Crashes with "Floating point exception". We divide by zero, since
     (int)0.35 == 0.
     Solution: c = (int)(a / z);
     Result: c = 1000
 16. c = (int)(a / z);
     (int) (short / double) \rightarrow (int) double \rightarrow int, fits in int
     Result: c = 1000;
```

#### 3.3.2.1 Divisors

```
#include <stdio.h>
#include <stdlib.h>
int main() {
  int number, divisor;
  printf("Please type a positive integer: ");
  scanf("%d", &number);
  printf("The divisors of %d are:", number);
  for (divisor = 1; divisor <= number/2; divisor++) {</pre>
    if (number % divisor == 0) {
      printf(" %d", divisor);
  }
  /* each number divides itself */
  printf(" %d\n", number);
  return 0;
```

#### 3.3.2.2 Exponentiation

```
#include <stdio.h>
#include <stdlib.h>
int main() {
  int g, m, power;
  printf("g (>=0): ");
  scanf("%d", &g);
  printf("m (>=0): ");
  scanf("%d", &m);
  power = 1;
  while (m > 0) {
    /* loop invariant: power*exponentiation(q,m) == X */
    power = power*g;
    m --:
  printf("exponentiation(g,m) = %d\n", power);
  return 0;
```

### 3.3.2.3 Integer logarithm

```
#include <stdio.h>
#include <stdlib.h>
int main() {
  int g, x, power, exponent;
  printf("base g(>=2): ");
  scanf("%d", &g);
  printf("integer x(>=1): ");
  scanf("%d", &x);
  power = 1;
  exponent = 0; /* invariant: power == exponentiation
     (q, m) */
  while (power*g <= x) {
    power = power*g;
    exponent++;
  printf("intlog(%d) = %d\n", x, exponent);
  return 0:
```

#### 3.3.2.4 The inverse of the factorial function

```
#include <stdio.h>
#include <stdlib.h>
int main() {
  int n, count, fac;
  scanf("%d", &n);
  count = 1;
  fac = 1;
  while (fac*(count+1) <= n) {
    /* loop invariant: fac == count! */
    count++;
    fac = fac*count;
  }
  printf("caf(%d) == %d\n", n, count);
  return 0;
```