Paper Title

Afg Cer, A. Bcd, P. Qwe, R. Bcgfee, and R.Y. Tedf School of XYZ and RST, University of ABCDEF, Qwergh-12345, XYZ

Abstract. We propose a deep learning approach for low light enhancement, leveraging Retinex [?] theory to decompose images into reflectance and illumination. Our extended U-Net[?] architecture integrates residual connections, attention mechanisms, and multi-scale fusion to enhance brightness while preserving details. A four-channel input, including a maximum intensity channel, enriches feature representation. Spectral normalization stabilizes training, while adversarial training with GANs [?] refines illumination and realism. To further improve enhancement quality, we employ a diverse set of loss functions to guide the model's optimization. Implemented with PyTorch and Kornia, our model outperforms benchmarks on SSIM and PSNR, ensuring superior brightness restoration, structural consistency, and color fidelity.

1 Introduction

Low-light image enhancement is challenging due to issues like noise, low contrast, and color distortion, but a deep learning approach inspired by Retinex theory can address these challenges while preserving image details[?][?][?][?]. The proposed method uses an extended U-Net architecture with residual learning, attention mechanisms, and multi-scale fusion to adaptively enhance images[?].

1.1 Attacks on MANETS[11]

In MANETS, there are two types of attacks- Passive and Active. Passive attacks capture valuable data in transit and active attacks cause huge damage to the network by disrupting the normal flow of the operations. Malicious nodes cause both active and passive attacks. A malicious node is the one, which does not authenticate itself to other honest nodes and misbehaves in the network. An honest node can also be compromised if it is under the control of the attacker. As the network comprises of layers of protocols, the attacks are specific to a layer and the security should also be implemented in the corresponding layer. Since the mobile nodes share a wireless medium, the messages transmitted can eavesdrop or fake messages may be injected at physical layer. Because of one-hop connectivity maintained among neighbors, the attacker can launch traffic analysis and traffic monitoring attacks. In network layer, the attacker exploits the routing algorithms to create routing hops and network congestion^[4]. The attacker uses a compromised node to perform SYN flooding and denial of service(DOS) attacks at transport layer. The majority of attacks in the application layer are worm attacks, mobile viruses and repudiation attacks. Some attacks like denial of service and man-in-the-middle can be launched from several layers. This paper proposes node authentication using BLS signature, so that many of the attacks can be avoided.

1.2 Distributed PKI

Public key cryptography(PKC)[12] provides many security services like confidentiality, integrity, authentication, non-repudiation, encryption and digital signatures. Public key infrastructure(PKI)[5] manages digital certificates which are important in the deployment of public key cryptography. In PKI environment, Certificate authority(CA) issues and

maintains the certificates of participating entities, the certificate contains the public key and the ID of the entity, the CA signs the certificate using the master secret key s and this certificate can be verified by the master public key PK. In MANETS we cannot adopt the same PKI, as the network is dynamic and infrastructure-less. So the role of the CA needs to be distributed to the nodes i.e., the master secret key s is to be shared among different nodes and the master secret key can only be generated if atleast the threshold number of shares of secret are pooled together.

1.3 Threshold Cryptography

As MANET is a decentralized network, the master secret key (s) of the PKI is distributed among the nodes using secret sharing schemes. One of the popular and most widely used secret sharing technique is the Shamir's secret sharing technique[8]. In this scheme, dealer distributes a secret s among n users. Each user receives it's share privately from the dealer. To reconstruct a secret, it uses (t, n) threshold access structure, where t out of n shares are required. Shamir's secret sharing scheme can be adopted in MANETS. Even the role of the dealer can be played by the nodes of MANET itself. This is achieved by using a bi-variate polynomial. This is discussed in section 3.1.

1.4 Related work

One common issue faced by MANET when applying cryptography is, how to distribute the role of CA or trusted authority, many proposals use secret sharing technique to distribute secret key s of CA or trusted authority to secure MANET. Zhou and Haas[6] were the first to propose distributed CA for MANETS. They used threshold cryptography to distribute the role of the Certification Authority (CA) in a PKI scenario among a set of selected servers. However, this proposal is not suitable for a purely ad-hoc environment as these selected nodes may not always be available. Kong et al.[13] adapted a similar idea to distribute trust among all the nodes. However, their specific RSA threshold scheme has been proved insecure [14][15]. Shamir secret sharing technique [8] is the most widely used secret sharing technique. We show that Shamir secret sharing technique along with the use of bi-variate polynomial helps to distribute the secret of CA among all nodes of MANET. In other works, bi-variate polynomials have already been used to dynamically allow new nodes joining the network without the need of any external trusted party. This technique is the result of inspiration from the original work of [16]. Anzai et al. [17] and Herranz et al.[18] constructed decentralized, flexible, dynamic group key distribution schemes by using polynomials in two variables. The goal is to generate common group secret keys. Saxena et al. [19] used similar technique to establish pairwise keys in a non-interactive way for a mobile ad-hoc scenario. Recently Daxing et al. [22] proposed aggregate signature algorithm for MANET using bilinear pairing and Hanaoka et al. [24] construct multi user setting signature with tight security based on BLS signature.

Our work is more related to the cryptographic techniques proposed for MANETs by Herranz et al. [18]. They proposed a fully self managed MANET and the ways to authenticate communication among the nodes. Our paper proposes the node authentication in their set up using BLS signature proposed by Boneh et al.[10]. Our proposal reduces the size of keys used as it uses the bilinear pairing. This scenario is much suitable for MANET because its nodes are mostly resource constraint devices and they can not afford the heavy computational overhead required by larger keys.

2 preliminaries

2.1 Self-Organized PKI and Secret Sharing Technique

In self-organized PKI for MANETS, the role of PKI is completely distributed among the nodes of MANET using secret sharing scheme[8]. Blakley [7] and Shamir [8] were the first to introduce secret sharing techniques. In general a secret sharing scheme contains a dealer and a set $U = \{u_1, u_2, \cdots, u_n\}$ of n users. The dealer has a secret S and wants to distribute the share s_i of the secret corresponding to the user u_i privately. A valid subset u (for : $u \subset U$) of atleast t number of users holding valid shares can reconstruct the secret S. The t is refereed as the threshold number and (t,n) is refereed to as the threshold access structure[8]. In our paper, we use Shamir's secret sharing technique that uses a (t,n) threshold access structure[8]. Shamir's secret sharing scheme uses (t,n) threshold access structures using polynomial interpolation. Let Z_q be a finite field with q > n and let $S \in Z_q$ be the secret. The dealer picks a polynomial P(x) of degree at most t-1, where the constant term of P(x) is S and all other coefficients are selected from Z_q uniformly and independently at random. That is,

$$P(x) = S + \sum_{i=1}^{t-1} a_i * x^i$$

Every user u_i is publicly associated to a field element a_i . Distinct parties are mapped to distinct field elements. The dealer privately sends to user u_i the value $[S]_i = P(a_i)$, for $i = 1, 2, \dots, n$. Without loss of generality, we can assume that the set of parties willing to recover the secret S is P_1, \dots, P_t . The secret S can obtained as $\sum_{i=1}^t l_i * [s]_i$ where $l_i = \prod_{j \neq i} \frac{a_j}{a_j - a_i}$ are the Lagrange coefficients. It is proven that any set of less than t parties obtain no information about S, that is, any secret is equally probable given their shares.

2.2 Bilinear Pairing and Related Assumptions[21]

Let G_1 be a cyclic additive group generated by some element P, whose order is a prime q, and G_2 be a cyclic multiplicative group of the same order q. Let a, b be elements of Z_q^* . We assume that the discrete logarithm problem (DLP) in both G_1 and G_2 are hard. A bilinear pairing is a map $e: G_1 \times G_1 \to G_2$ with the following properties:

- Bilinear: For all S, $T \in G_1$, $e(aS, bT) = e(S, T)^{ab}$.
- Non-degenerate: There exists S and $T \in G_1$ such that $e(S,T) \neq 1$.
- Computable: There is an efficient algorithm to compute e(S,T) for all $S,T \in G_1$.

We have the following assumptions:

- The Decisional Diffie-Hellman problem(DDHP) in G_1 should be easy.
- The DDHP in G_2 , the computational Diffie-Hellman problem (CDHP) and the discrete logarithm problem (DLP) in both G_1 and G_2 should be hard.
- The inversion of the bilinear pairing be hard, i.e., the bilinear pairing inversion problem(BPIP) is defined as:
 - BPIP : Given $S \in G_1$ and $e(S,T) \in G_2$, find $T \in G_1$.

2.3 BLS Signature[10]

This scheme was introduced by D. Boneh, B. Lynn, H. Schacham. It is based on Computational Diffie-Hellman assumption on certain elliptic curve. We discuss the Gap Diffie-Hellman Group where this signature scheme works.

Gap Diffie-Hellman Groups (GDH Groups) Consider a (multiplicative) cyclic group $G = \langle g \rangle$, with q = |G| a prime. There are three problems on G.

- Group Action: Given $u, v \in G$, find uv.
- Decision Diffie-Hellman : For a, b, c $\in \mathbb{Z}_q^*$, given (g, g^a, g^b, g^c) decide whether c = ab.
- Computational Diffie-Hellman : For a, b $\in \mathbb{Z}_q^*$, given (g,g^a,g^b) , compute g^{ab} .

The GDH group is defined as:

- G is a τ -decision group for Diffie-Hellman if the group action can be computed in one time unit, and Decision Diffie-Hellman can be computed on G in time at most τ .
- The advantage of an algorithm A in solving the Computational Diffie-Hellman problem in a group G is
 - $AdvCDH_A = Pr[A(g, g^a, g^b)] = g^{ab} : a, b \xleftarrow{R} Z_q^*$ Where the probability is over the choice of a and b, and the coin tosses of A. We say that an algorithm A (t, ϵ) -breaks Computational Diffie-Hellman in G if A runs in time at most t, and $AdvCDH_A \ge \epsilon$.
- A prime order group G is a (τ, t, ϵ) -GDH group if it is a τ -decision group for Diffie-Hellman and no algorithm (τ, ϵ) -breaks Computational Diffie-Hellman on it.

Signature Scheme

- Setup of protocol:

Public information: cryptographic hash function $H: \{0,1\}^* \to G_1$ and cryptographic bilinear map $e: G_1 \times G_1 \to G_2$

Signer's public key: generator $P \in G_1, P_{pub} = sP$, where s is the secret key and P_{pub} is the public key.

- Sign: For any message $M \in \{0,1\}^*$, signature is computed as sig = sH(M)
- Verify: Signature is only valid if the following equation holds.

$$e(P, sig) = e(P_{pub}, H(M))$$

- Proof: $e(P, sig) = e(P, sH(M)) = e(sP, H(m)) = e(P_{mib}, H(m))$

3 Our proposal

This section is divided into four major phases namely Setup, Key Generation, Signature Generation Protocol and Signature Verification Protocol.

3.1 Setup

In this phase every node n_i receives partial share s_i of the MANET secret s. This is achieved using the following protocol.

- Let n be the number of nodes in the MANET, t be the threshold and k be the founding number of nodes.
- The founding number of nodes are such $t \leq k \leq n$.
- Every founding node chooses a bi-variate polynomial $f_i(x, z)$, symmetric in x, z and the max degree.
- Every node n_i computes $f_{ij}(h(n_i), z)$ for all other founding nodes and itself, $1 \le i \le k$.
- Now every node secretly sends computed $f_{ij}(h(n), z)$ to corresponding node n_j . Furthermore, node n_i includes the value $y_i = f_i(0) * P$ in each of these messages.
- Finally every node has values received from other founding nodes and also it's own value $f_{ii}(h(n_i), z)$ with it.
 - Then every node n_i computes $f_i(z) = f(h(n_i), z) = \sum_{j \in k} f_{ji}(h(n_i), z)$.
- Now every node n_i has partial secret $s_i = f_i(0)$ and a secret equation $f(h(n_i), z)$.

The MANET secret function $f(x, z) = \Sigma_{i \in n} f_i(x, z)$ and MANET secret key is s = f(0, 0) are safe and hidden. This secret information can only be reconstructed if and only if there are at-least t nodes having partial share of MANET secret. For a new node n_w trying to join the network, it has to request at-least t nodes for the values $f_{iw}(h(n_i), h(n_w))$. When t nodes accept the node n_w request, then they send $f_{iw}(h(n_i), h(n_w))$ to node n_w . Now node n_w has t values and these values are used in Lagrange's interpolation to derive a secret polynomial corresponding to node n_w , Lagrange's interpolation is applied as follows:

$$f_w(z) = f(h(n_w), z) = \sum_{n_j \in n} \prod_{n_i \in n, n_i \neq n_j} \frac{(z - h(n_i))}{(h(n_j) - h(n_i))} * f(h(n_j), h(n_w))$$

- The partial secret of node n_w is $f_w(0)$ and secret polynomial of node n_w is $f_w(z)$ i.e., $f(h(n_w), z)$

3.2 Key Generation

After every node n_i has received a partial secret s_i , now the nodes run RSA key generation protocol. The protocol is responsible for generating a public (pk_i) and private (sk_i) key pair. The private key (sk_i) is kept secret with the node n_i and public key (pk_i) is made available to all other nodes. The public key pk_i is used to encrypt messages that are sent to node n_i , and the node n_i uses its private key sk_i to decrypt messages as well as to sign messages.

3.3 Signature Generation Protocol

Now every node n_i has two secret keys namely partial secret key of MANET s_i and individual secret key sk_i , partial secret key is used to partially sign a certificate and any to out of n nodes are required to sign a certificate to generate fully signed/valid certificate. When a node n_i wants to get a public key certificate, it asks its neighboring nodes to generate partial signature on the certificate linking $n_i||pk_i$. If the node n_i receives at-least (t-1) partial signs, then the node itself can generate a partial sign using it's own partial

share, now the node has t partially signed values, then it uses the following Lagrange's interpolation to generate a fully signed certificate.

- $-p_i = H(m) * s_i$ where s_i is the individual share of each user and H(m) is the hash of message m.
- The final signature (shm) is computed as $shm = \Sigma_{i \in t} p_i * L_i$, where L_i is Lagranges Coefficient. $L_i = \prod_{p_j \in t, j \neq i} \frac{(0-h(N_j))}{(h(N_i)-h(N_j))}$

Now that every node obtains its certificate in the above described manner. Next we discuss the protocol to verify the certificate.

3.4 Signature Verification Protocol

Any node n_j can verify the certificate of node n_i by running the following protocol. Node n_j has the following information regarding node n_i :

- the signed certificate of node n_i (shm).
- the public key of the MANET (PK) and value P.
- ID of node n_i and public key of node n_i $(N_i||pk_i)$.

The node n_i uses BLS signature to verify the certificate:

- Verify e(shm, P) = e(H(m), PK) If true certificate is valid, else invalid.

3.5 Example

- Setup
- Let the intial set of nodes $N_M = \{N_1, N_2, N_3, N_4\}$ No.of Nodes = 4
- Public Parmeters :

An additive group G of prime order q = 4019.

- The curve used is $E(F_{4019}): y^2 = x^3 + 1$
- The Generator is P = E(3198,578)
- Let t = 2 (degree of polynomials) and k = 67 (Field of Polynomials)
- An admissible bilinear pairing Weil Pairing
- Two explicit collision resistant hash functions HTP(Hash to Point) : $\{0,1\}^* \to G_2$ and HTR(Hash to Range) : $\{0,1\}^* \to G_1$ where HTP hashes the given message onto the elliptic curve group G_2 and HTR hashes the given value to the group G_1 .
- Each node chooses a random symmetric-bivariate polynomial in GF(67) $N1 = 3x^2z + 3z^2x + 8xz + 5z + 5x + 5$, $N2 = 5x^2z + 5z^2x + 3xz + 8z + 8x + 9$ $N3 = 8x^2z + 8z^2x + 5xz + 3z + 3x + 6$, $N4 = 2x^2z + 2z^2x + 4xz + 8z + 8x + 4$
- The implicit polynomial defined by all the nodes is $F(x,z) = N_1 + N_2 + N_3 + N_4$ $= 18x^2z + 18xz^2 + 20xz + 24x + 24z + 24$
- The secret s of the MANET is F(0,0) = 24.
- Each node secretly sends to each of the other founding nodes the univariate polynomial $F_{ij} = F_i(x, h(N_j))$.

- The hash values of the nodes are

$$h_{n1} = HTR('Node1', k) = 37, h_{n2} = HTR('Node2', k) = 54$$

 $h_{n3} = HTR('Node3', k) = 25, h_{n4} = HTR('Node4', k) = 17$

- Each node sends the following values to other Nodes:

- N1 also includes
$$Y_1 = 5 * P = (152,1437)$$

 $N_{11} = 44x^2 + 53x + 56, N_{12} = 28x^2 + 6x + 7$
 $N_{13} = 8x^2 + 3x + 63, N_{14} = 51x^2 + 3x + 23$

- N2 also includes
$$Y_2 = 9 * P = (409,2266)$$

 $N_{21} = 51x^2 + 63x + 37, N_{22} = 2x^2 + 10x + 39$
 $N_{23} = 58x^2 + 59x + 8, N_{24} = 18x^2 + 30x + 11$

- N3 also includes
$$Y_3 = 6 * P = (3063,3143)$$

 $N_{31} = 28x^2 + 18x + 50, N_{32} = 30x^2 + 17x + 34$
 $N_{33} = -x^2 + 36x + 14, N_{34} = 2x^2 + 55x + 57$

- N4 also includes
$$Y_4 = 4 * P = (3863,2497)$$

 $N_{41} = 7x^2 + 13x + 32, N_{42} = 41x^2 + 26x + 34$
 $N_{43} = 50x^2 + 18x + 3, N_{44} = 34x^2 + 51x + 6$

- Then all the nodes calculate their secret univariate polynomial from the recieved values.

$$-S_1(x) = 63x^2 + 13x + 41, S_2(x) = 34x^2 + 59x + 47$$

$$-S_3(x) = 48x^2 + 49x + 21, S_4(x) = 38x^2 + 5x + 30$$

- The public key, PK = s * P
=
$$24 * E(3198,578) = E(2651, 2267)$$

– PK should also equal to
$$Y_1 + Y_2 + Y_3 + Y_4$$

=E(152,1437)+E(409,2266)+E(3063,3143)+E(3863,2497) = E(2651, 2267)

- Each node calculates its share from $S_i(0)$. The shares of the nodes are - $S_1 = 41, S_2 = 47, S_3 = 21, S_4 = 30$
- These shares can be verified by substituting hash value of the nodes in the following polynomial f(z) = F(0,z) = 24 * z + 24
- If Node N_5 wants to join the MANET, It should identify it self to 3 other nodes and request for acceptance. $\{N_2, N_3, N_4\}$ $h_{n5} = HTR('Node5', k) = 27$

-
$$N_5$$
 receives the following values $S_{25} = S_2(27) \mod 67 = 28$, $S_{35} = S_3(27) \mod 67 = 22$ $S_{45} = S_4(27) \mod 67 = 62$

- N_5 computes its secret univariate polynomial by using Lagrange interpolation $S_5(x) = 17 * x^2 + 18 * x + 2$

- Key Generation

- Each node computes its own key pair as follows: Node 1 = [(89,649),(189,649)], Node 2 = [(17,321),(25,321)]Node 3 = [(63,115),(7,115)], Node 4 = [(91,202),(11,202)]

- Signature Generation

- The share of each node in MANETs secret key is used as secret key for signature i.e $S_1 = 41, S_2 = 47, S_3 = 21, S_4 = 30$
- Each node produces a certificate by linking Id with PK m_1 ='Node1'+'89'+'649', m_2 ='Node2'+'17'+'321' m_3 ='Node3'+'63'+'115', m_4 ='Node4'+'91'+'202'
- Then all the nodes exchange partial signatures to compute fully signed certificate.
- If Node 1 wants to compute its certificate (m_1 ='Node1'+'89'+'649'), then it requests Node 2, Node 3 and Node 4 for their partial signatures.
- Here P = E(3198,578), s = 24, mpub =E(2651,2267) and s2 = 47,s3 = 21,s4 = 30
- $-hm_1 = HTP(m_1) = E(163, 1362)$
- The partial signatures of Nodes 2, 3 and 4 are $p_2 = (hm_1) * s2$, $p_3 = (hm_1) * s3$, $p_4 = (hm_1) * s4$
- By lagranges interpolation we get the signature on the message 1 as shm1=E(2350,3239).
- Signature Verification
- Calculate e(hm1,mpub)=1365*a + 2045
- Calculate e(shm1,P)=1365*a + 2045 this is equal to e(hm1,mpub)
- Hence Verified
- Message communication after verification
- Public and private key pairs of each node Node 1 = [(e1,n1),(d1,n1)] = [(89,649),(189,649)]Node 2 = [(e2,n2),(d2,n2)] = [(17,321),(25,321)]Node 3 = [(e3,n3),(d3,n3)] = [(63,115),(7,115)]Node 4 = [(e4,n4),(d4,n4)] = [(91,202),(11,202)]Message (M) = 56
- If Node 1 wants to send a message to Node 3, then Node 1 Encrypts the message using Node 3's public key and sends to Node 3.
- C=Encrypt(M,e3,n3) $C = (mod(56,115)^{63})$ Encrypted Value C = 463
- Node 3 receives the Cipher value and Decrypts the message using Node 3 private key.
- M=Decrypt(C,d3,n3) $m = mod(463,115)^7$ Decrypted Value M=56

4 Conclusion

In this paper, we proposed a new scheme of verifying a certificate in decentralized PKI based MANETS. In our scheme the nodes of the MANET holds a secret share and every node chooses its own public and private keys. The public key is associated with the node identity in the certificate. This certificate management is done using BLS Signature. Our scheme uses a bivariate polynomial to reduce the communication overhead. The same technique can be used in performing other functionalities of MANET like implementing threshold operations in sub group nodes communication and share verification etc.

References

- 1. F. Anjum and P. Mouchtaris, Security for wireless ad hoc networks. Wiley-Blackwell, Mar. 2007.
- Vanesa Daza, Javier Herranz, Paz Morillo, Carla Rfols, Cryptographic techniques for mobile ad-hoc networks, Computer Networks, Volume 51, Issue 18, 19 December 2007.
- 3. Y.-C. Hu, A. Perrig, and D. B. Johnson. Ariadne: A secure on-demand routing protocol for ad hoc networks. In Proceedings of the Eighth ACM International Conference on Mobile Computing and Networking (Mobicom 2002), September 2002.
- Y.-C. Hu, A. Perrig, and D. B. Johnson. Packet leashes: A defense against wormhole attacks in wireless networks. In Proceedings of IEEE Infocom 2003, April 2003.
- 5. S. Kent and T. Polk. Public-key infrastructure (x.509) (pkix) charter. http://www.ietf.org/html.charters/pkix-charter.html.
- 6. L. Zhou, Z.J. Haas, Securing ad hoc networks, IEEE Network 13 (6) (1999) 24-30.
- G.R. Blakley, Safeguarding cryptographic keys, in: Proceed- ings of the National Computer Conference, American Federation of Information, Processing Societies Proceedings, vol. 48, 1979, pp. 313-317.
- 8. A. Shamir, How to share a secret, Communications of the ACM 22 (1979) 612-613.
- 9. Seung Yi and Robin Kravetso. Moca: Mobile certificate authority for wireless ad hoc networks. In The second anunual PKI research workshop (PKI 03), Gaithersburg, 2003.
- Dan Boneh, Ben Lynn, and Hovav Shacham (2004). "Short Signatures from the Weil Pairing". Journal of Cryptology. 17: 297-319.
- 11. Djenouri, Djamel, L. Khelladi, and N. Badache. "A survey of security issues in mobile ad hoc networks." IEEE communications surveys 7.4 (2005): 2-28.
- Stallings, William (1990-05-03). Cryptography and Network Security: Principles and Practice. Prentice Hall. p. 165. ISBN 9780138690175.
- 13. H. Luo, J. Kong, P. Zerfos, S. Lu, L. Zhang, URSA: ubiquitous and robust access control for mobile ad hoc networks, IEEE/ACM Transactions on Networking 12 (6) (2004).
- 14. M. Narasimha, G. Tsudik, J.H. Yi, On the utility of distributed cryptography in P2P and MANETs: the case of membership control, in: Proceedings of ICNP203, 2003, pp. 336-345.
- S. Jarecki, N. Saxena, J.H. Yi, An attack on the proactive RSA signature scheme in the URSA ad hoc network access control protocol, in: Proceedings of the SASN04, 2004, pp. 19.
- C. Blundo, A. De Santis, A. Herzberg, S. Kutten, U. Vaccaro, M. Yung, Perfectly-secure key distribution for dynamic conferences, in: Proceedings of Crypto92, LNCS, vol. 740, Springer-Verlag, 1993, pp. 471-486.
- 17. J. Anzai, N. Matsuzaki, T. Matsumoto, A quick group key distribution scheme with entity revocation, in: Proceedings of Asiacrypt99, LNCS, vol. 1716, Springer-Verlag, 1999, pp. 333-347.
- V. Daza, J. Herranz, G. Sez, Constructing general dynamic group key distribution schemes with decentralized user join, in: Proceedings of ACISP03, LNCS, vol. 2727, Springer-Verlag, 2003, pp. 464-475.
- 19. N. Saxena, G. Tsudik, J.H. Yi, Efficient node admission for short-lived mobile ad hoc networks, in: Proceedings of ICNP05, 2005, pp. 269-278.
- 20. Singh Nidhi, Appala Naidu Tentu, Abdul Basit, and V. Ch Venkaiah. "Sequential secret sharing scheme based on Chinese remainder theorem." In Computational Intelligence and Computing Research (ICCIC), 2016 IEEE International Conference on, pp. 1-6. IEEE, 2016.
- 21. Boneh, Dan, and Matt Franklin. "Identity-based encryption from the Weil pairing." Annual International Cryptology Conference. Springer Berlin Heidelberg, 2001.
- Daxing Wang, Jikai Tang. "Efficient Aggregate Signature Algorithm and Its Application in MANET".
 in: International Journal of Mathematical, Computational, Physical, Electrical and Computer Engineering. vol. 7, No:11, 2013.
- 23. Adul Basit, N Chaitanya Kumar, V. Ch. Venkaiah, Salman Abdul Moiz, Appala Naidu, Wilson Naik "Multi-stage Multi-secret Sharing Scheme for Hierarchical Access Structure." In International Conference on Computing, Communication and Automation (ICCCA), 2017 IEEE International Conference.
- 24. Hanoka G, Shuldt J.C.N, "On signatures with tight security in the multi-user setting" (2017) in : Proceedings of 2016 International Symposium on Information Theory and Its Applications, ISITA 2016, art. no. 7840392, pp. 91-95.

Authors

THU-LE MINH VO Mentor guiding the CF subject in the AI program at FPT University.



 $\mathbf{THUAN\text{-}VAN}$ \mathbf{TRAN} FPT University student.



KHANG-HOANG VO NGUYEN FPT University student.



HUNG-MANH NGUYEN FPT University student.



TUAN-MINH LE FPT University student.





CAM-MY THI NGUYEN FPT University student.