

Programmatic thinking

# Algorithms and operators

# What is programmatic thinking?



How do we *actually* solve real-world **problems** involving data?

We **break down** the problem or task into smaller more manageable parts that we can **solve** in a **systematic** and **logical** way.

This is called **PROGRAMMATIC THINKING.**

# What is programmatic thinking?

Programmatic thinking helps us to **logically organise information** into a **series of instructions** that a **computer can execute**.

We need certain "**tools**" in order to apply programmatic thinking:

## Algorithms

The **sequence of steps** required to solve the problem.

## Operators

Used to **compare** numbers, strings, and statements.

## Flowcharts

**Visual representations** of the flow of control of conditional statements.

## Pseudocode

**Descriptions** of the sequence of steps and actions in **plain natural language**.

## Conditional statements

Representation of decision-making through a set of **specific conditions**.

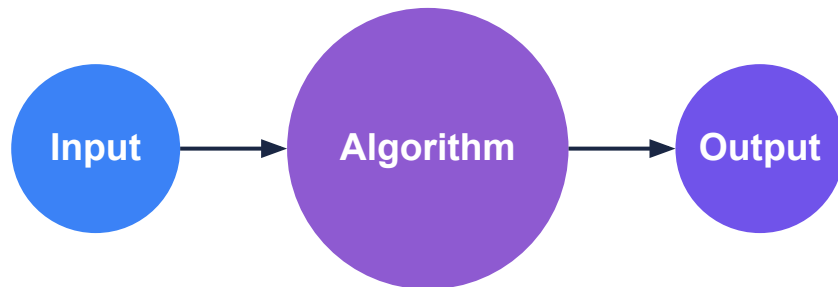
# Algorithms

An algorithm is a **specific procedure** to solve a problem in terms of the **required actions or steps** and the **order** in which these actions are executed.

An algorithm can be as simple as calculating the sum of a list of numbers to searching for the occurrence of a specific value in a list of numbers.

Algorithms allow us to create **repeatable** solutions to problems.

They are designed to produce a correct result every time they are used, as long as they are given an appropriate input.



Set of **actions** to obtain the expected output from the given input

# Algorithms

Algorithms can be categorised into different techniques, often to solve the same problem using **different approaches**. The algorithm efficiency will depend on the approach and the specific problem.

## Brute force

The simplest algorithm where every possible alternative solution to a problem is tried until the correct solution is found.

## Backtracking

Different possible solutions are tried systematically until the correct one is found, most often starting from an initial guess to the solution.

## Divide and conquer

Divides the problem into smaller subproblems, each subproblem is solved, and the solutions are combined to solve the original problem.

## Greedy

Makes optimal choices at each step in the algorithm considering only the current step and situation.

## Recursive

Calls itself on smaller subproblems that are similar to the original problem until the problem becomes small enough to be solved directly.

## Dynamic programming

Breaks down complex problems into smaller subproblems, storing solutions to the subproblems, and uses the stored solutions to solve the original problem.

# Algorithms

An example of an algorithm to search for the occurrence of a specific value ( $x$ ) in a list of numbers:

1. Sort the list of numbers in ascending order (an algorithm in itself).
2. Find the midpoint of the sorted list.
3. Compare the midpoint value to the value of interest,  $x$ .
4. If the midpoint value is larger than the value of interest,  $x$ , repeat steps 2 to 4 only on the list of numbers smaller than the midpoint value.
5. If the midpoint is smaller than the value of interest,  $x$ , repeat steps 2 to 5 only on the list of numbers that are larger than the midpoint value.
6. Repeat steps 2 to 5 until the midpoint value is equal to the value of interest,  $x$ .

# Algorithms

An example of an algorithm to search for the occurrence of a specific value (x) in a list of numbers:

1. Sort the list of numbers in ascending order (an algorithm in itself).
2. Find the midpoint of the sorted list.
3. **Compare** the midpoint value to the value of interest, x.
4. If the midpoint value is **larger than** the value of interest, x, repeat steps 2 to 4 only on the list of numbers larger than the midpoint value.
5. If the midpoint is **smaller than** the value of interest, x, repeat steps 2 to 5 only on the list of numbers that are smaller than the midpoint value.
6. Repeat steps 2 to 5 until the midpoint value is **equal to** the value of interest, x.

This is called the **binary search algorithm**. It is both a divide and conquer and recursive algorithm.

We notice words related to **comparisons**.

But how do we “explain” to a computer how to perform these comparisons?

We use  
**COMPARISON OPERATORS**  
(==, !=, >, >=, <, <=)

# Algorithms

Consider the simple example of an algorithm that determines whether a number is between 0 and 10 (inclusive):

1. Set the value of interest as x.
2. If x is greater than or equal to zero and x is less than or equal to 10, then the statement is True.
3. Otherwise, the statement is False.

This algorithm includes **COMPARISON OPERATORS**.

We also see a **BOOLEAN OPERATOR\*** that combines the two statements.

We see that **operators are an important tool** that algorithms use to make decisions.

\*A boolean operator is also known as a logical operator.

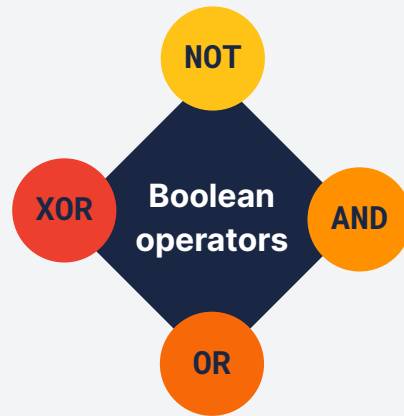


# Operators

We use operators in conditional statements, flowcharts, and pseudocode to **compare** numbers, strings, and statements, and combine or exclude statements.



Used to **compare numbers** or **strings** to perform the evaluation within a boolean expression\*.



Used as conjunctions to **combine** (or **exclude**) **statements** in a boolean expression.

\*A boolean expression is a statement that results in an answer of either True or False.

# Comparison operators

Used to **compare numbers** or **strings** to perform the evaluation within a boolean expression.

Equal to

**==**

Returns **True** when the value on the left is **strictly equal** to the value on the right.

$2 + 2 == 4 \rightarrow \text{True}$

$2 + 3 == 4 \rightarrow \text{False}$

Not equal to

**!=**

Returns **True** when the value on the left is **strictly not equal to** the value on the right.

$2 + 2 != 4 \rightarrow \text{False}$

$2 + 3 != 4 \rightarrow \text{True}$

# Comparison operators

Greater than

>

Returns **True** when the value on the left is **greater than** the value on the right.

5 > 4 → **True**  
4 > 5 → **False**  
3 + 1 > 4 → **False**

Greater than  
or equal to

>=

Returns **True** when the value on the left is either **greater than or equal to** the value on the right.

5 >= 4 → **True**  
4 >= 5 → **False**  
3 + 1 >= 4 → **True**

Less than

<

Returns **True** when the value on the left is **smaller than** the value on the right.

5 < 4 → **False**  
4 < 5 → **True**  
3 + 1 < 4 → **False**

Less than or  
equal to

<=

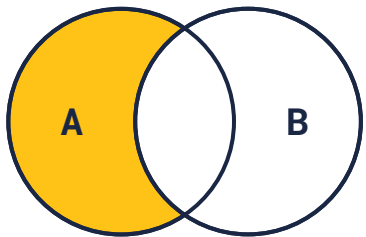
Returns **True** when the value on the left is either **smaller than or equal to** the value on the right.

5 <= 4 → **False**  
4 <= 5 → **True**  
3 + 1 <= 4 → **True**

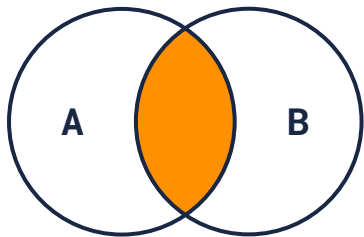
# Boolean operators

Used as conjunctions to **combine** (or **exclude**) **statements** in a boolean expression.

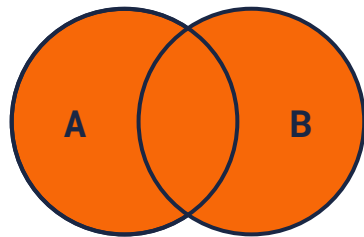
We can visually represent the logic of boolean operators:



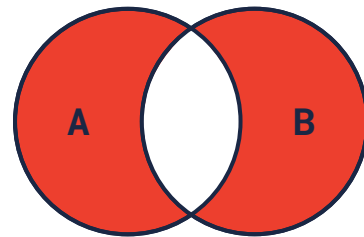
A NOT B



A AND B



A OR B



A XOR B

# Boolean operators

NOT False → True

NOT True → False

2 + 2 == 4 AND 1 + 3 == 4 → True

2 + 2 == 4 AND 4 > 5 → False

4 > 5 AND 2 + 3 == 4 → False

2 + 2 == 4 OR 1 + 3 == 4 → True

2 + 2 == 4 OR 4 > 5 → True

4 > 5 OR 2 + 3 == 4 → False

2 + 2 == 4 XOR 1 + 3 == 4 → False

2 + 2 == 4 XOR 4 > 5 → True

4 > 5 XOR 2 + 3 == 4 → False

## NOT

Only considers the argument **after** the operator. The algorithm considers the **opposite** of the argument.

## AND

The two arguments are considered in conjunction.

**Both** arguments should be **True** for the statement to be **True**.

## OR

If **either** of the arguments to the left or right of the operator is **True**, the statement will be **True**. If both arguments are **True**, the statement will also be **True**.

## XOR

Exclusive OR

Only if **exactly one** of the arguments to the left or right of the operator is **True** will the statement be **True**. If both arguments are **True**, the statement is **False**.