

# Computer Vision and Deep Learning

Ch 04

강명묵

# Contents

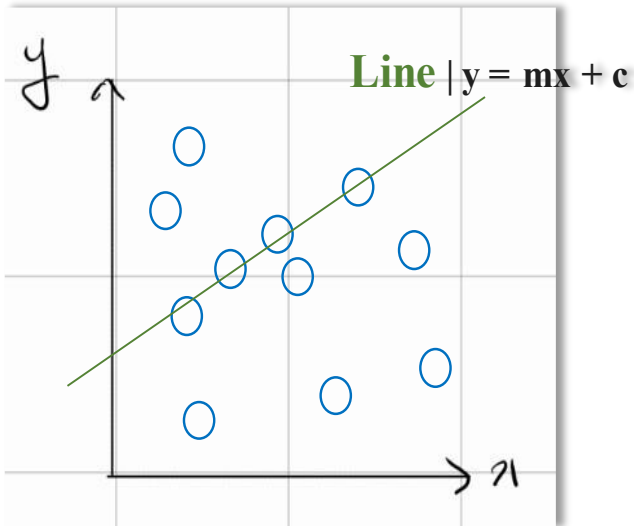
**1. Hough Transform**

**2. RANSAC**

# Hough Transform

## Hough Transform

1. 다양한 Noise에서 진짜 Edge를 찾아가는 과정
2. 경계선을 적은 수의 파라미터로 표현 가능



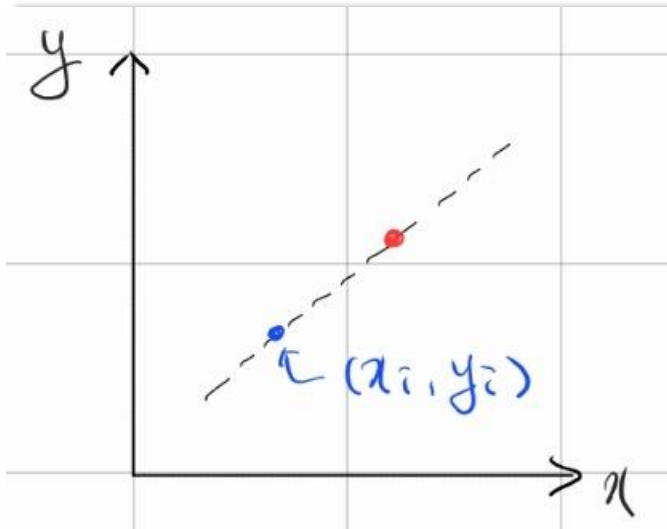
**Given : Edge Point**

**Task : Detect **line****

**Consider point  $(x_i, y_i)$**

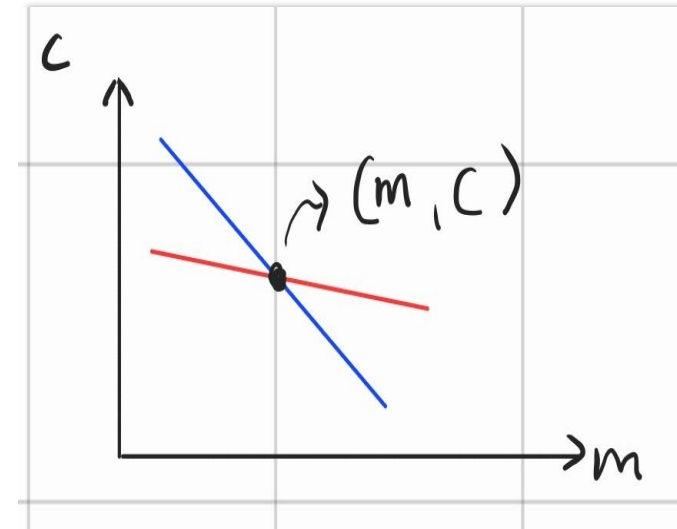
# Hough Transform(Line)

Image Space



$$y_i = mx_i + c$$

Parameter Space



$$c = -mx_i + y_i$$

Line



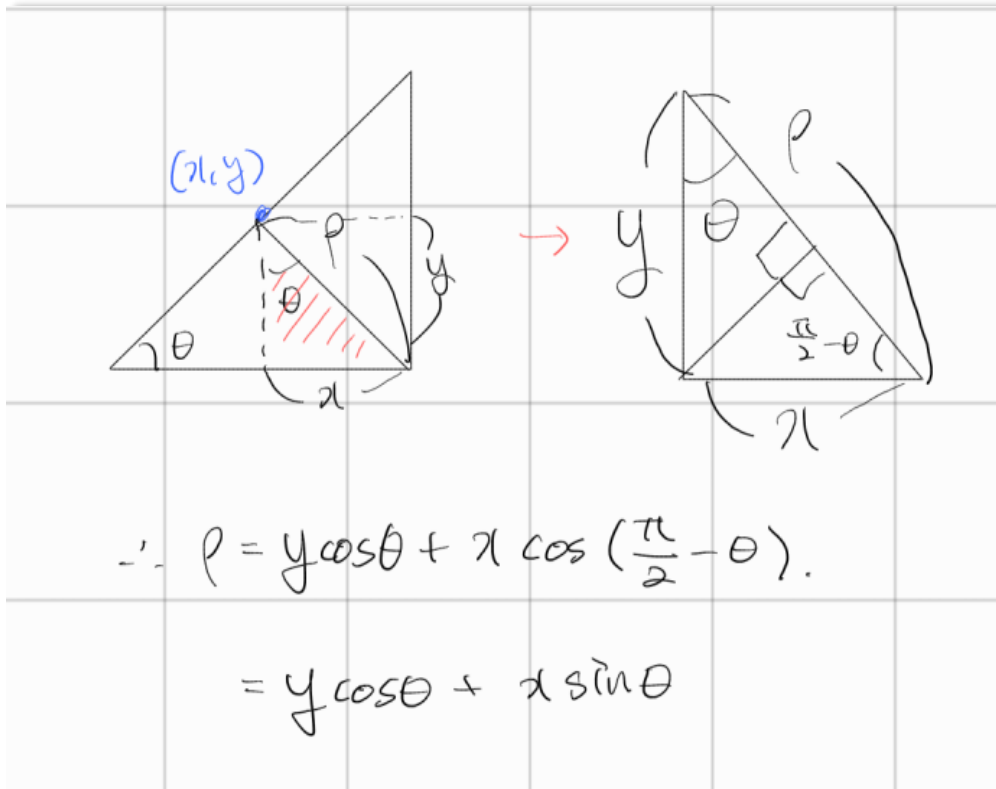
Point

Point



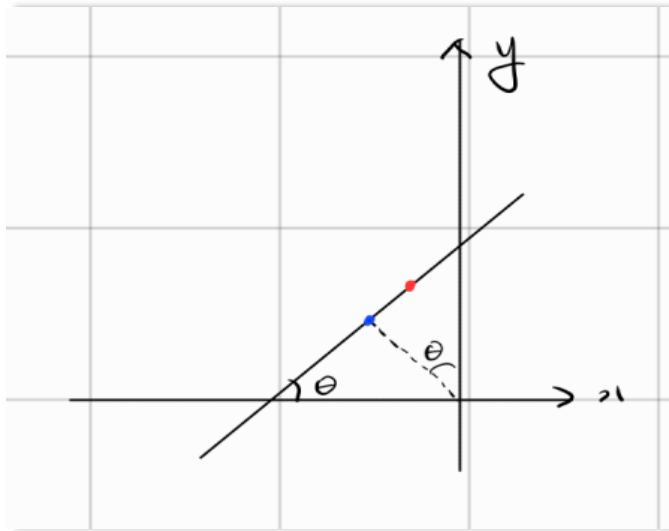
Line

# Hough Transform(Line)



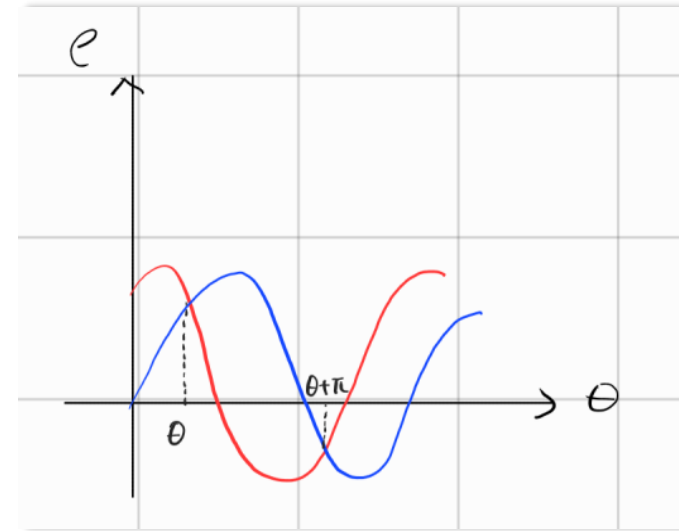
# Hough Transform(Line)

Image Space



$$\rho = x_i \sin \theta + y_i \cos \theta$$

Parameter Space



$$\rho = x_i \sin \theta + y_i \cos \theta$$

Line



Point

Point

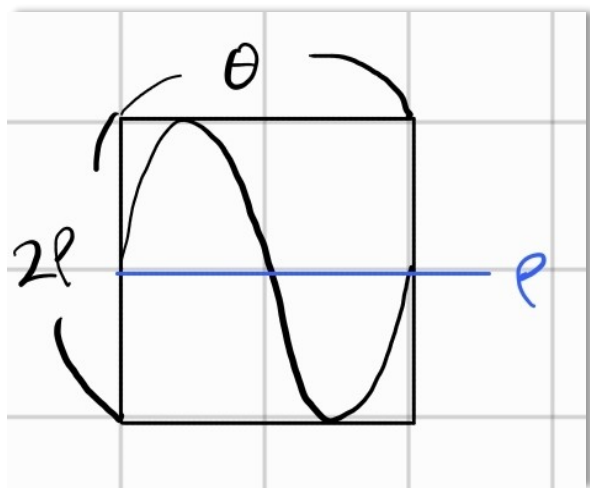


Line

# Implementation

## Step 1

### 파라미터 공간 생성 및 투표



$$0 \leq \theta \leq \pi$$

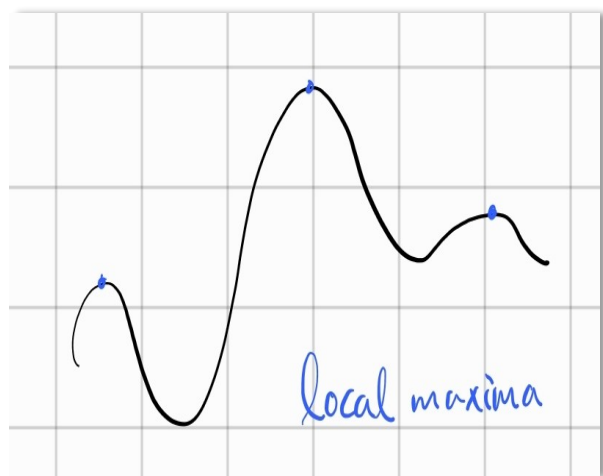
$\theta$ 를  $1^\circ$  간격으로 이산화

```
Mat hough_space_line(Mat& img) {  
    double max_rho = sqrt(pow(img.cols, 2) + pow(img.rows, 2));  
    int max_rho_idx = cvRound(max_rho);  
    Mat parameter_space = Mat::zeros(2 * max_rho_idx + 1, 180, CV_8UC1);  
  
    for (int x = 0; x < img.cols; ++x) {  
        for (int y = 0; y < img.rows; ++y) {  
            if (img.at<uchar>(y, x) != 0) {  
                for (int theta = 0; theta < 180; ++theta) {  
                    // 변환된 파라미터 공간에서 직선의 방정식을 계산  
                    double rho = x * cos(theta * CV_PI / 180) + y * sin(theta * CV_PI / 180);  
  
                    // 직선이 이미지 내에 있는지 확인하고, 있다면 해당 위치의 값을 +1  
                    int rhoIdx = cvRound(rho) + max_rho_idx;  
                    if (rhoIdx >= 0 && rhoIdx < parameter_space.rows && (parameter_space.at<uchar>(rhoIdx, theta) != 255)) {  
                        parameter_space.at<uchar>(rhoIdx, theta)++;  
                    }  
                }  
            }  
        }  
    }  
  
    return parameter_space;  
}
```

# Implementation

## Step 2

## 지역 최댓값 찾기



Find local maxima

```
void findLocalMaxima(const Mat& src, Mat& dst, int neighborhoodSize, int threshold) {  
    dst = Mat::zeros(src.size(), CV_8UC1);  
  
    for (int y = 0; y < src.rows; ++y) {  
        for (int x = 0; x < src.cols; ++x) {  
            int value = src.at<uchar>(y, x);  
            bool isMaxima = true;  
  
            for (int i = -neighborhoodSize; i <= neighborhoodSize; ++i) {  
                for (int j = -neighborhoodSize; j <= neighborhoodSize; ++j) {  
                    int neighborRow = y + i;  
                    int neighborCol = x + j;  
  
                    if (neighborRow >= 0 && neighborRow < src.rows && neighborCol >= 0 && neighborCol < src.cols) {  
                        if (src.at<uchar>(neighborRow, neighborCol) > value) {  
                            isMaxima = false;  
                            break;  
                        }  
                    }  
                }  
            }  
  
            if (!isMaxima) {  
                break;  
            }  
        }  
  
        if (isMaxima && value >= threshold) {  
            dst.at<uchar>(y, x) = 255;  
        }  
    }  
}
```



# Implementation

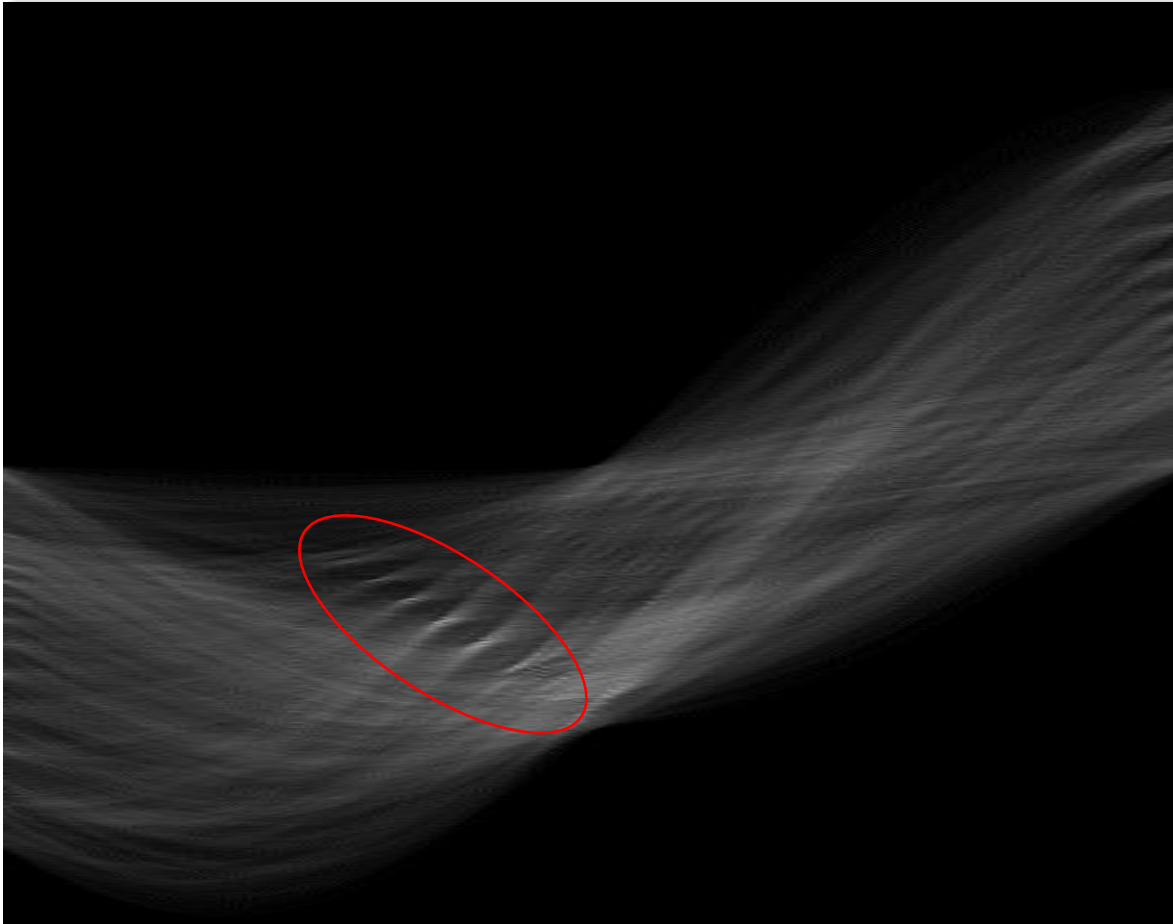
## Step 3

### 이미지에 직선 그리기

```
Mat draw_detected(Mat& img, const Mat& hough_space, int threshold) {  
    Mat draw_img = img.clone();  
    for (int rhoIdx = 0; rhoIdx < hough_space.rows; ++rhoIdx) {  
        for (int theta = 0; theta < hough_space.cols; ++theta) {  
            if (hough_space.at<uchar>(rhoIdx, theta) > threshold) {  
                // 변환된 파라미터 공간에서 직선의 방정식으로 역변환  
                double rho = rhoIdx - hough_space.rows / 2.0;  
                double theta_rad = theta * CV_PI / 180.0;  
                double a = cos(theta_rad);  
                double b = sin(theta_rad);  
                double xo = rho * a;  
                double yo = rho * b;  
  
                // 좌표 계산  
                Point pt1(cvRound(xo + 1000 * (-b)), cvRound(yo + 1000 * (a)));  
                Point pt2(cvRound(xo - 1000 * (-b)), cvRound(yo - 1000 * (a)));  
  
                // 직선 그리기  
                line(draw_img, pt1, pt2, Scalar(0, 0, 255), 2, LINE_AA);  
            }  
        }  
    }  
    return draw_img;  
}
```

# Implementation

Parameter space



Parameter space  
(thresholding)

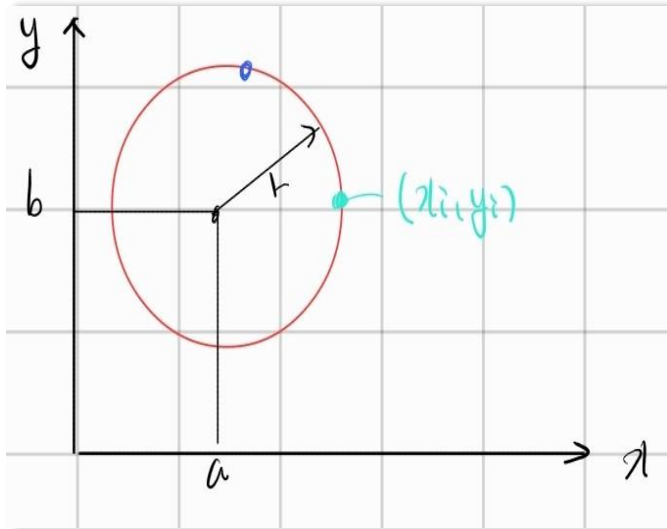


# Implementation



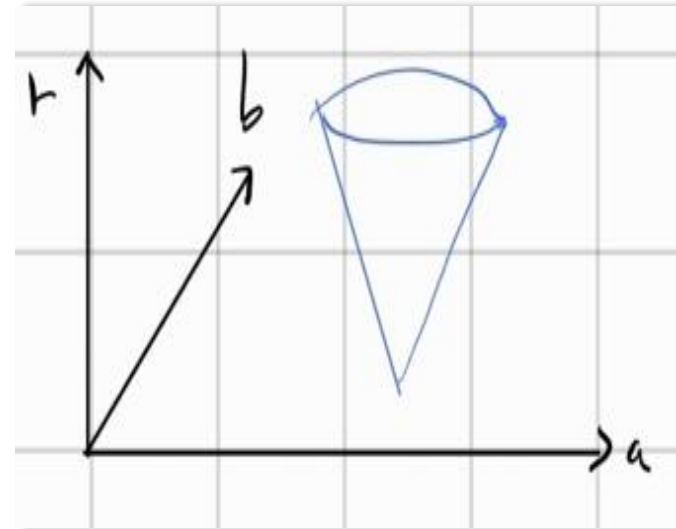
# Hough Transform(Circle)

## Image Space



$$(x_i - a)^2 + (y_i - b)^2 = r^2$$

## Parameter Space



$$(a - x_i)^2 + (b - y_i)^2 = r^2$$

# RANSAC

## Random sample consensus

관측된 데이터들에 대하여 근사 모델의 파라미터를 추정하는 방법 중 하나.

### 1. 모델 추정

이미지에서 랜덤한 두 점 선택(직선의 방정식)

### 2. 모델 검증

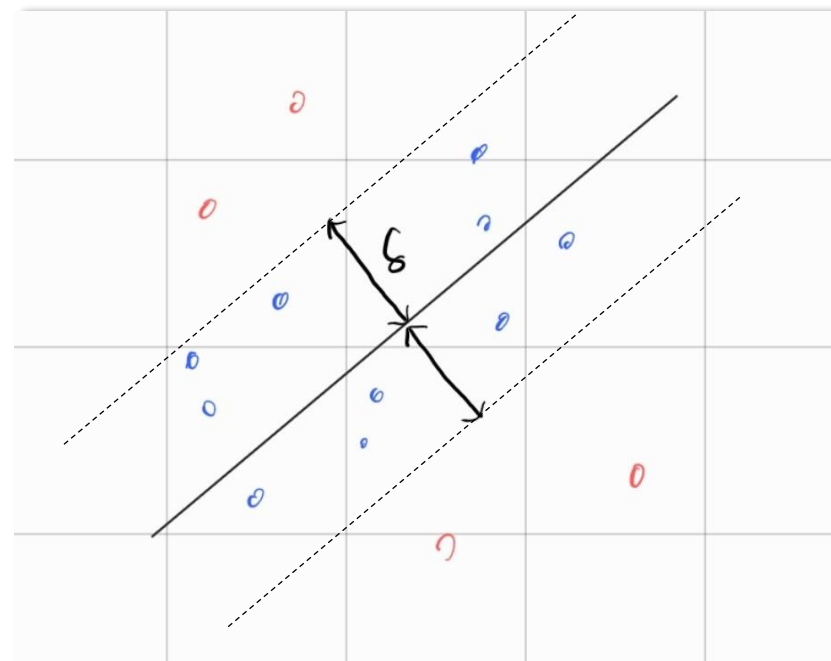
직선의 방정식으로부터

$\delta$ 의 범위 안에 있는 점 : inlier

$\delta$ 의 범위 밖에 있는 점 : outlier

### 3. 반복

iteration만큼 1,2번을 반복하며  
inlier가 최대가 되는 지점 찾기



inlier, outlier

감사합니다.