

5-) Other function — $O(1)$

(-8)

Some function(arr, len) {

for (i=0; i < arr-len-1; i++) — $O(arr-len)$

{

min_idx = i — $O(1)$

for (j = i+1; j < arr-len; j++)

if (arr[j] < arr[min_idx]) — $O(1)$

min_idx = j — $O(1)$

Other function(arr[min_idx], arr[i]) — $O(1)$

}

}

Outer loop

execute arr-len times

Nested loop

i=0 executed arr-len+1 times

i=1 executed arr-len-1 times

i=2 executed arr-len-2 times

⋮

i=arr-len-2 executed 1 time

$$n+(n-1)+(n-2)+\dots+1$$

$$= \frac{n(n+1)}{2}$$

$$= \frac{n^2+n}{2} (n+1)$$

$$T_{Best}^{(n)} = T_{Average}^{(n)} = T_{Worst}^{(n)} = O(n^2) = \Omega(n^2) = \Theta(n^2)$$

(-1)

6-) for i=0 to arr-len

execute arr-len times

for (j=i to arr-len)

arr-len

arr-len-1

arr-len-2

⋮

1

$$= \frac{n(n+1)}{2}$$

for (j=1 to arr[i]) Other function

When i=1 arr[i]=1

In best case n can check all i values so this loop constant

$$T_{Best}^{(n)} = O(n^2)$$

In worst case

i	arr[i]
1	0
2	1
3	2
4	3
⋮	⋮
n	n-1

$$\frac{n(n-1)}{2} = \frac{n^2-n}{2}$$

$$T_{Worst}^{(n)} = T_{Avg}^{(n)} = O(n^2)$$

$$T_{Best}^{(n)} = T_{Avg}^{(n)} = T_{Worst}^{(n)} = O(n^2) = \Omega(n^2) = \Theta(n^2)$$

I didn't take for i to b loop because other function always called with i=2 so this is constant time complexity loop

7-)

for (i=0; i < arr-len-1; i++)

Other function(arr, i)

$$\sum_{i=1}^n \log n = \log 1 + \log 2 + \log 3 + \dots + \log n = \log(n!)$$

for (j=1; j < n; j=j*2)

j goes 1 2 4 8 16 ... n

So this for loop time complexity log n

$$T_{Best}^{(n)} = T_{Worst}^{(n)} = T_{Avg}^{(n)} = O(n \log n)$$

So total complexity

$$T_{Best}^{(n)} = T_{Worst}^{(n)} = T_{Avg}^{(n)} = O(n \log n) = \Omega(n \log n) = \Theta(n \log n)$$