

Matrix-Lines

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Abstract—This document shows how to find equation of a line passing through a point (2,2) and cutting off intercepts on the axes whose sum is 9 using python.

I. PROBLEM STATEMENT

Find equation of a line passing through a point (2,2) and cutting off intercepts on the axes whose sum is 9.

II. CONSTRUCTION

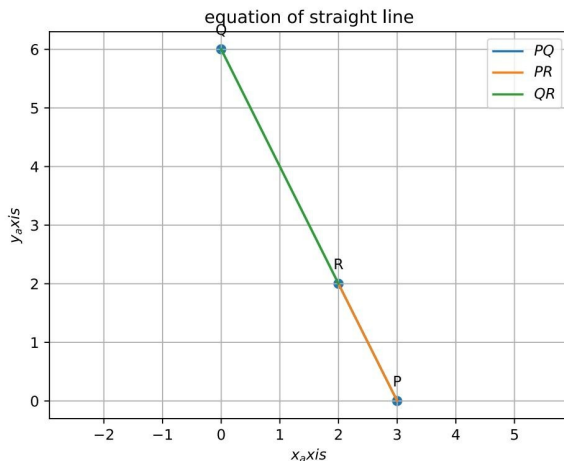


Fig. 1. Equation of the Straight Line

Symbol	Value	Description
P	(a,0)	Point on X-axis
Q	(0,b)	Point on Y-axis
R	(2,2)	Given Point
a+b	9	Given Condition

TABLE I
PARAMETERS

III. SOLUTION

Given that resultant line passes through point(2,2) and intercepts on axes whose sum is 9 (let x intercept is P (a,0) and y intercept is Q (0,b) therefore, $a+b=9$) so, $b=9-a$

Let $P=(a,0), Q=(0,9-a), R=(2,2)$

Equation of line is $n^T \mathbf{X} = c$ it can also be written as $X^T \mathbf{n} = c$

Now we have 3 points which lies on same line so,

$[a \ 0]n = c$ ———eq1 Equation of line through P

$[0 \ 9 - a]n = c$ ———eq2 Equation of line through Q

Now eq1+eq2,

$[a \ 9 - a]n = 2c$ ———eq3

$[2 \ 2]n = c$ ———eq4 Equation of line through R

From eq3 and eq4 we can find normal vector n ,

$$[[a \ 9 - a], [2 \ 2]]n = c[2 \ 1]$$

$$\text{Therefore, } n = [[a \ 9 - a], [2 \ 2]]^{-1} \cdot c[2 \ 1]$$

$$n = [3a - 9 - 2] \cdot c / (4a - 18)$$

Now eq4 can be expressed as,

$$[3a - 9 - 2] \cdot [2 \ 2] \cdot c / (4a - 18) = c$$

By solving this equation we get $a=2$, thus $b=9-a=7$

by substituting a in n , finally

$$\mathbf{n} = [0.3 \ 0.2].\mathbf{c}$$

The Resultant Equation of line is $\mathbf{n}^T\mathbf{X} = \mathbf{c}$

i.e, $[0.3 \ 0.2].\mathbf{X} = 1$

IV. SOFTWARE

Download the following code using,

```
svn co https://github.com/
mygit-sampath-govardhan/fwc-iith-assignments/blob/
5b65abbf8e5e3c803b1bff8cf4a95092e100de75/
Assignment-4(Matrices-line)/codes/Assignment4.py
```

Now execute the code

Python3 Assignment4.py

V. CONCLUSION

We found the equation of a line passing through a point (2,2) and cutting off intercepts on the axes whose sum is 9.