

B-Tree-Delete(k,x):

if k is not in node x:

 if num_keys(x) > t or x is root:
 continue

 else:

 y = left_im_sib(x);

 z = right_im_sib(x);

 w = root(x);

 if num_keys(y) >= t:

 k' = most_right_key(y);

 move(k',y,w);

 k'' = find_successor(k',w);

 move(k'',w,x);

 elseif num_keys(z) >= t:

 k' = most_left_key(k,z);

 move(k',z,w);

 k'' = find_predecessor(k',w);

 move(k'',w,x);

 else:

 if y:

 k' = find_key(y,x)

 merge(k',y,x)

 else:

 k' = find_key(z,x)

 merge(k',z,x)

B-Tree_Delete(k,x.ci)

Return;

elseif k is in node x:

 if x is leaf:

 y = left_im_sib(x);

 z = right_im_sib(x);

 w = root(x);

 if num_keys(x) >= t:

 delete(k,x);

 elseif num_keys(y) >= t:

 k' = find_predecessor(k,y);

 move(k',y,root(x));

 k'' = find_successor(k',w);

 move(k'',w,x);

 delete(k);

 elseif num_keys(z) >= t:

 k' = find_successor(k,z);

 move(k',z,w);

//this part is used to make sure all the nodes from root to the destination node (which k lies in) have at least t keys. Therefore, when we later pop up or push down the keys, it won't violate the B-trees property. (Keys>t-1)

// if one of the siblings is larger than t keys, then use it through the root. That means pop up the nearest key in the sibling to the root to hold the position. Then pushes down the nearest key in the root to the current node.(not exactly take the key in that sibling, but a key from the root)

//if neither of the siblings has more or equal than t keys, in the root, finds the key between the existed sibling and current node. Push it down to current node, and merge the node with this sibling together.

//x.ci is the root of the subtree that must contains k, this will recursively fill all the nodes along the way.

//when k is in node x:

If x is leaf:

//Case1: it contains more than t keys, just delete k.

//Case2: one of its siblings contains more than t keys. The same idea with the above part, use it through the root. And then current node will have t keys, delete the k.

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k''=find_predecessor(k',w);
    move(k'',w,x);
    delete(k);
else:
    if y:
        k'=find_key(y,x)
        move(k',w,x);
        x=merge(x,y);
        delete(k);
    else:
        k'=find_key(z,x)
        move(k',w,x);
        x=merge(x,z);
        delete(k);

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else x is internode:
    y = left_im_child(x,k);
    z = right_im_child(x,k);
    if num_keys(y) >= t:
        k'=find_predecessor(k,y);
        move(k',y,x)
        delete(k)
    elseif num_keys(z)>=t:
        k'=find_successor(k,z);
        move(k',z,x)
        delete(k,x)
    else:
        move(k,x,y);
        y=merge(y,z);
        delete(k,y);

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Pseudo codes end here.....

Functions:

left_im_sib(x)

move(x,m,n)

find_successor(k,z);

find_key(x,y)

num_keys(x)

//Case 3: if neither of the siblings has more or equal than t keys, push down the key in the root, between the current node and its exited sibling. Then merge the current node with this sibling. Then delete k

//if x is internode

//Case 4: if one of the children has more or equal than t keys, just take the predecessor or successor in this node, Then delete k.

//Case 5: if none of the children has enough keys to offer, push down the key k to its child, and merge the two children to form the new child, then delete k.

get the left sibling of node x

move the key x from node m to n

find the successor of k in node z

in the root, find the key which between its two children node: x and y.

give the number of keys in node x

