

1. Turunkan dengan detail persamaan bloch sehingga mendapatkan hasil seperti pada pers. 14.43 – 14.44 pada buku teks

**Jawab:**

$$E(t) = E_0 \cos \omega t = \frac{E_0}{2} (e^{i\omega t} + e^{-i\omega t})$$

$$\beta_{21}(t) = \rho_{21} e^{i\omega t}$$

$$\beta_{12}(t) = \beta_{21}^* = \rho_{12} e^{-i\omega t} = (\rho_{21})^* e^{-i\omega t}$$

Maka persamaan

$$\dot{\rho}_{21} = i \frac{E\mu_d}{\hbar} (\rho_{11} - \rho_{22}) - i\omega_{21}\rho_{21} - \frac{\rho_{21}}{T_2}$$

Diubah kedalam bentuk  $\beta_{21}$  dengan mengalikan  $e^{i\omega t}$

$$\left(\frac{d}{dt}\rho_{21}\right)e^{i\omega t} = i \frac{\mu_d E_0}{2\hbar} (e^{i\omega t} + e^{-i\omega t}) - i\omega_{21}\rho_{21}e^{i\omega t} - \frac{\rho_{21}}{T_2}e^{i\omega t}$$

$$\frac{d}{dt}\beta_{21} - i\omega\rho_{21}e^{i\omega t} = i \frac{\mu_d}{2\hbar} E_0 (e^{2i\omega t} + 1)(\rho_{11} - \rho_{22}) - i\omega_{21}\beta_{21} - \frac{\beta_{21}}{T_2}$$

$$\frac{d}{dt}\beta_{21} = i \frac{\mu_d}{2\hbar} E_0 (\rho_{11} - \rho_{22}) + i(\omega - \omega_{21})\beta_{21} - \frac{\beta_{21}}{T_2}$$

Lalu hasil persamaan

$$\dot{\rho}_{11} - \dot{\rho}_{22} = 2i \frac{E\mu_d}{\hbar} (\rho_{21} - \rho_{21}^*) - \frac{(\rho_{11} - \rho_{22}) - (\rho_{11} - \rho_{22})_0}{T_1}$$

Jika dimasukkan E kedalam persamaan diatas maka

$$\begin{aligned} \dot{\rho}_{11} - \dot{\rho}_{22} &= 2i \frac{\mu_d E_0}{\hbar} (e^{i\omega t} + e^{-i\omega t}) (\rho_{21} - \rho_{21}^*) - \frac{(\rho_{11} - \rho_{22}) - (\rho_{11} - \rho_{22})_0}{T_1} \\ &= i \frac{\mu_d}{\hbar} E_0 (\rho_{21}e^{i\omega t} - \rho_{21}^*e^{i\omega t} + \rho_{21}e^{-i\omega t} - \rho_{21}^*e^{-i\omega t}) - \frac{(\rho_{11} - \rho_{22}) - (\rho_{11} - \rho_{22})_0}{T_1} \\ &= i \frac{\mu_d}{\hbar} E_0 (\rho_{21}e^{i\omega t} - \beta_{21}^*e^{2i\omega t} + \beta_{21}e^{-2i\omega t} - \rho_{21}^*e^{-i\omega t}) - \frac{(\rho_{11} - \rho_{22}) - (\rho_{11} - \rho_{22})_0}{T_1} \\ &= i \frac{\mu_d}{\hbar} E_0 (\rho_{21}e^{i\omega t} - \rho_{21}^*e^{-i\omega t}) - \frac{(\rho_{11} - \rho_{22}) - (\rho_{11} - \rho_{22})_0}{T_1} \\ \dot{\rho}_{11} - \dot{\rho}_{22} &= i \frac{\mu_d}{\hbar} E_0 (\beta_{21} - \beta_{21}^*) - \frac{(\rho_{11} - \rho_{22}) - (\rho_{11} - \rho_{22})_0}{T_1} \end{aligned}$$

2. Dapatkan solusi pers. Bloch untuk keadaan tunak [pers. (14.46)-(14.48)]

**Jawab:**

Tidak perubahan pada fractional population difference,  $\rho_{11} - \rho_{22}$ ,

maka  $\frac{d(\rho_{11}-\rho_{22})}{dt} = 0$  dan  $\frac{d\beta_{21}}{dt} = 0$

kedua persamaan akan menjadi

$$0 = i \frac{\mu_d}{\hbar} E_0 (\beta_{21} - \beta_{21}^*) - \frac{(\rho_{11} - \rho_{22}) - (\rho_{11} - \rho_{22})_0}{T_1} \quad [1]$$

$$0 = i \frac{\mu_d}{\hbar} E_0 (\rho_{11} - \rho_{22}) + i(\omega - \omega_{21})\beta_{21} - \frac{\beta_{21}}{T_2}$$

$$i \frac{\mu_d}{\hbar} E_0 (\rho_{11} - \rho_{22}) = \left( i(\omega_{21} - \omega) + \frac{1}{T_2} \right) \beta_{21}$$

$$\beta_{21} = \Omega(\rho_{11} - \rho_{22}) \frac{1}{\left( \omega_{21} - \omega - \frac{i}{T_2} \right)}$$

Dengan  $\Omega = \frac{\mu_d}{2\hbar} E_0$ , dan konjugatnya  $\beta_{21} = \Omega(\rho_{11} - \rho_{22}) \frac{1}{\left( \omega_{21} - \omega - \frac{i}{T_2} \right)}$

[1] dapat diubah menjadi

$$i2\Omega(\beta_{21} - \beta_{21}^*) = \frac{(\rho_{11} - \rho_{22}) - (\rho_{11} - \rho_{22})_0}{T_1}$$

Substitusi nilai  $\beta$

$$i2\Omega(\rho_{11} - \rho_{22}) \left( \frac{1}{\left( \omega_{21} - \omega - \frac{i}{T_2} \right)} - \frac{1}{\left( \omega_{21} - \omega + \frac{i}{T_2} \right)} \right) = \frac{(\rho_{11} - \rho_{22}) - (\rho_{11} - \rho_{22})_0}{T_1}$$

$$(\rho_{11} - \rho_{22}) \left( -\frac{1}{\left( \omega_{21} - \omega - \frac{i}{T_2} \right)} + \frac{1}{\left( \omega_{21} - \omega + \frac{i}{T_2} \right)} + \frac{1}{i2\Omega^2 T_1} \right) = \frac{(\rho_{11} - \rho_{22})_0}{i2\Omega^2 T_1}$$

$$(\rho_{11} - \rho_{22}) \left( \frac{T_2}{(T_2(\omega_{21} - \omega) + i)} - \frac{T_2}{(T_2(\omega_{21} - \omega) - i)} + \frac{1}{i2\Omega^2 T_1} \right) = \frac{(\rho_{11} - \rho_{22})_0}{i2\Omega^2 T_1}$$

$$\dots + \frac{1}{i2\Omega^2 T_1} = \frac{T_2((T_2(\omega_{21} - \omega) - i) - (T_2(\omega_{21} - \omega) + i))}{(T_2(\omega_{21} - \omega) + i)(T_2(\omega_{21} - \omega) - i)} + \frac{1}{i2\Omega^2 T_1}$$

$$= \frac{T_2(-2i)}{T_2^2(\omega_{21} - \omega)^2 + 1} + \frac{1}{i2\Omega^2 T_1}$$

$$= \frac{T_2(-2i)i2\Omega^2 T_1 + (T_2)^2(\omega_{21} - \omega)^2 + 1}{((T_2)^2(\omega_{21} - \omega)^2 + 1)i2\Omega^2 T_1}$$

$$\dots + \frac{1}{i2\Omega^2 T_1} = \frac{1 + (\omega_{21} - \omega)^2 T_2^2 + 4\Omega^2 T_2 T_1}{((T_2)^2(\omega_{21} - \omega)^2 + 1)i2\Omega^2 T_1}$$

$$(\rho_{11} - \rho_{22}) \left( \frac{1 + (\omega_{21} - \omega)^2 T_2^2 + 4\Omega^2 T_2 T_1}{((T_2)^2(\omega_{21} - \omega)^2 + 1)i2\Omega^2 T_1} \right) = \frac{(\rho_{11} - \rho_{22})_0}{i2\Omega^2 T_1}$$

$$(\rho_{11} - \rho_{22}) = (\rho_{11} - \rho_{22})_0 \frac{1 + (\omega_{21} - \omega)^2 T_2^2}{1 + (\omega_{21} - \omega)^2 T_2^2 + 4\Omega^2 T_2 T_1}$$

Setelah mendapatkan  $\rho_{11} - \rho_{22}$ , lalu dapat mencari nilai  $\beta_{21}$

$$\beta_{21} = \Omega(\rho_{11} - \rho_{22}) \frac{1 + (\omega_{21} - \omega)^2 T_2^2}{1 + (\omega_{21} - \omega)^2 T_2^2 + 4\Omega^2 T_2 T_1} \frac{1}{\left( \omega_{21} - \omega - \frac{i}{T_2} \right)}$$

$$\beta_{21} = \Omega(\rho_{11} - \rho_{22}) \frac{1 + (\omega_{21} - \omega)^2 T_2^2}{1 + (\omega_{21} - \omega)^2 T_2^2 + 4\Omega^2 T_2 T_1} \frac{T_2}{(T_2(\omega_{21} - \omega) - i)}$$

$$\beta_{21} = \Omega(\rho_{11} - \rho_{22}) \frac{(T_2(\omega_{21} - \omega) + i)(T_2(\omega_{21} - \omega) - i)}{1 + (\omega_{21} - \omega)^2 T_2^2 + 4\Omega^2 T_2 T_1} \frac{T_2}{(T_2(\omega_{21} - \omega) - i)}$$

$$\beta_{21} = \Omega(\rho_{11} - \rho_{22}) \frac{(T_2^2(\omega_{21} - \omega) + iT_2)}{1 + (\omega_{21} - \omega)^2 T_2^2 + 4\Omega^2 T_2 T_1}$$

Maka nilai real dan imajiner menjadi

$$\text{real}(\beta_{21}) = \frac{\Omega(\rho_{11} - \rho_{22})_0 T_2^2 (\omega_{21} - \omega)}{1 + (\omega_{21} - \omega)^2 T_2^2 + 4\Omega^2 T_2 T_1}$$

$$\text{Im}(\beta_{21}) = \frac{\Omega(\rho_{11} - \rho_{22})_0 T_2}{1 + (\omega_{21} - \omega)^2 T_2^2 + 4\Omega^2 T_2 T_1}$$

3. Temukan relasi yang sesuai antara “susceptibilitas kompleks” dan “fungsi dielektrik”

**Jawab:**

Diketahui Polarisasi  $P = \epsilon_0 \chi E$

Displacement  $D$

$$D = \epsilon_0 E + P = \epsilon E$$

$$\epsilon_0 E + \epsilon_0 \chi E = \epsilon E$$

$$\frac{\epsilon}{\epsilon_0} = 1 + \chi$$

$$\epsilon_r = 1 + \chi$$

$\chi$  adalah bilangan kompleks dan  $\epsilon_r$  adalah permitivitas relatif atau complex frequency dependent dielectric constant. Maka untuk relasi yang sesuai antara “susceptibilitas kompleks” dan “fungsi dielektrik” didapat  $\epsilon' + i\epsilon'' = (1 + \chi') + i\chi''$