

$$\hat{B} = \int B_p(\alpha, \alpha^*) |\alpha\rangle \langle \alpha| d^2\alpha$$

Maka

$$|\hat{B}\rangle = \text{Tr}(\hat{B}\hat{\rho})$$

$$= \sum_n \langle n| \int B_p(\alpha, \alpha^*) |\alpha\rangle \langle \alpha| \hat{\rho} |n\rangle d^2\alpha$$

dimana rata" \hat{B}

$$|\hat{B}\rangle = \text{Tr}(\hat{\rho}\hat{B})$$

$$= \sum_n \langle n| \int \hat{\rho} B_p(\alpha, \alpha^*) |\alpha\rangle \langle \alpha| d^2\alpha |n\rangle$$

$$= \int B_p(\alpha, \alpha^*) d^2\alpha \sum_n \langle n| \hat{\rho} |\alpha\rangle \langle \alpha| n\rangle$$

$$= \int B_p(\alpha, \alpha^*) d^2\alpha \sum_n \langle n| n\rangle \langle n| \hat{\rho} |\alpha\rangle$$

$$\langle \hat{B} \rangle = \int B_p(\alpha, \alpha^*) \langle \alpha| \hat{\rho} |\alpha\rangle d^2\alpha$$

nilai Ekspektasi dari density Operator terhadap Coherent State =
distribusi phase space probability

$$Q(\alpha) = \frac{1}{\pi} \langle \alpha| \hat{\rho} |\alpha\rangle$$

$$\text{Tr}(\hat{B}) = \int Q(\alpha) d^2\alpha = 1$$

Maka

$$\hat{B} = \hat{1} \hat{B} \hat{1}$$

$$= \sum_n |n\rangle \langle n| \hat{B} \sum_m |m\rangle \langle m|$$

$$= \sum_n \sum_m |n\rangle \langle n| \hat{B} |m\rangle \langle m|$$

$$\hat{B} = \sum_n \sum_m |n\rangle \hat{B}_{nm} \langle m|$$

lalu di Manikan nilai Ekspektasi dari Coherent State
atau α representation berikut.

$$\langle \alpha | \hat{B} | \alpha \rangle = \langle \alpha | \left(\sum_n \sum_m |n\rangle \hat{B}_{nm} \langle m| \right) | \alpha \rangle$$

$$= \left(\sum_n \sum_m \langle \alpha | n \rangle \langle m | \alpha \rangle \right)$$

$$= \sum_n \sum_m e^{-1/2 |\alpha|^2} \sum_l \frac{(\alpha^*)^l}{\sqrt{l!}} \langle l | n \rangle \hat{B}_{nm}$$

$$\langle m | e^{-1/2 |\alpha|^2} \sum_l \frac{(\alpha)^l}{\sqrt{l!}} | l \rangle$$

$$= e^{-1/2 |\alpha|^2} \sum_n \frac{(\alpha^*)^n}{\sqrt{n!}} \sum_m \hat{B}_{nm} e^{1/2 |\alpha|^2} \sum_l \frac{(\alpha)^l}{\sqrt{l!}}$$

$$B_{\alpha}(\alpha, \alpha^*) = e^{-|\alpha|^2} \sum_n \sum_m \frac{(\alpha)^m (\alpha^*)^n}{\sqrt{m! n!}} \hat{B}_{nm}$$

Maka nilai Operator \hat{B} untuk $\hat{\rho}$ dalam p -representation

$$\langle \hat{B} \rangle = \text{Tr} (\hat{\rho} \hat{B})$$

$$= \text{Tr} \left(\int p(\alpha) | \alpha \rangle \langle \alpha | d^2 \alpha \cdot \hat{B} \right)$$

$$= \sum_n \langle n | \int p(\alpha) \langle \alpha | d^2 \alpha \cdot \hat{B} | n \rangle$$

$$= \int p(\alpha) \sum_n \langle n | \hat{B} | \alpha \rangle \langle \alpha | n \rangle d^2 \alpha$$

$$= \int p(\alpha) \sum_n \langle \alpha | n \rangle \langle n | \hat{B} | \alpha \rangle d^2 \alpha$$

$$= \int p(\alpha) \langle \alpha | \hat{B} | \alpha \rangle d^2 \alpha$$

$$\langle \hat{B} \rangle = \int p(\alpha) B_{\alpha}(\alpha, \alpha^*) d^2 \alpha$$