



- Consider the +ve and -ve terms below, numbered 1 to 7 terms.

$+|A|$ (term #1)
 $+|B|$ (term #2)
 $+|C|$ (term #3)
 $-|A \cap B|$ (term #4)
 $-|A \cap C|$ (term #5)
 $-|B \cap C|$ (term #6)
 $+|A \cap B \cap C|$ (term #7)

- In the above Venn Diagram, we have marked all areas as " $-(4)$ " that are accounted for by the term #4: $-|A \cap B|$; here, "-" indicate that it is a -ve term and "(4)" indicates that it is accounted by term #4.

Problem.

- Fill the diagram by adding similar marks " $+(i)$ " and " $-(j)$ " etc. corresponding to the other 6 terms.
- Show that the number of +ve marks for each part of $A \cup B \cup C$ (and only those parts) exceeds the number of -ve marks by exactly 1.
- This proves that the sum of all the terms above equals $|A \cup B \cup C|$.