

1. Write all ways of choosing 3 things out of $\{a, b, c, d, e\}$ on the left side of a page and all ways of choosing 2 things out of $\{a, b, c, d, e\}$ on the right side. Then, show all the connections between sets $\{x, y, z\}$ of 3 items and the sets $\{u, v\}$ of 2 items. Show the count of line in terms of $\#(\text{sets } \{x, y, z\})$ and the count of lines in terms of $\#(\text{sets } \{u, v\})$. Finally, show the resulting equation connecting $C(5, 3)$ and $C(5, 2)$.

2. Towards the end of class on Jan 21, we have seen $\#(\text{lines from a set } \{x_1, x_2, \dots, x_m\} \text{ of } m \text{ items to sets of } m-1 \text{ items}) = m$; it is not $m-1$. Complete the counting of lines to a set like $\{1, 2, \dots, m-1\}$ of $m-1$ items from sets of m items when there are total n items $\{1, 2, \dots, n\}$ to choose from. This number will depend on both n and m . From this, derive the equation connecting $C(n, m)$ and $C(n, m-1)$ by considering total $\#(\text{lines})$. Give all details.

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