

CSC 2259 2/11/30

I have something(s) that I want

$$\bullet H \cap W \neq \emptyset$$

I have everything that I want

$$\bullet H \supseteq W$$

I have nothing that I want

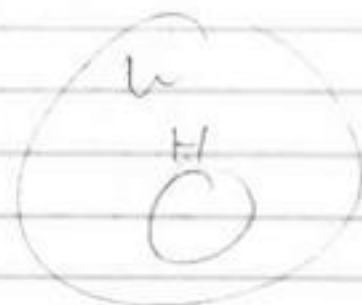
$$\bullet H \cap W = \emptyset \quad (\text{I want nothing I have})$$

I don't have anything I don't want.

$$W^c \subseteq H^c$$

↓

$$W \supseteq H$$



I don't have anything I want

$$\bullet H \cap W = \emptyset$$



$$H = W$$

$$|H| = |W|$$

I have the same number of things as I want

I have as many things as I want.

$$|H| \geq |W|$$

$$H, W \subseteq \{a, b, c, d\}$$

$$\# \text{ (ways of choosing } H, W \text{ such that } H=W) = 2^4 = 16$$

$$\# (\dots H \subseteq W) \quad H = \emptyset, W = \emptyset, \{a\}, \{b\}, \dots, \{a, b, c, d\}$$

$$|H|=0, \#(W's) = 16$$

$$|H|=1, \#(W's) = 8, 4 \text{ such cases: } a, ab, ac, ad$$

$$|H|=2, \#(W's) = 4, 6 \text{ such cases: } ab, ac, ad, abc, abd, abcd$$

$$|H|=3, \#(W's) = 2,$$

$$|H|=4, \#(W's) = 1$$

$$\#(H \text{ and } W \text{ such that } H \subseteq W)$$

$$= (1 \times 16) + (2 \times 8) + (6 \times 4) + (2 \times 2) + (1 \times 1)$$

$$= 16 + 16 + 24 + 2 + 1$$

$$= 59$$

$$= 59$$

$$= 59$$

I always make sense

$$\sum_{m=0}^n \binom{n}{m} x^{n-m} y^m$$

$$1 \times 16 = 16$$

$$2 \times 8 = 16$$

$$6 \times 4 = 24$$

$$2 \times 2 = 4$$

$$1 \times 1 = 1$$

$$59$$