Sample 6b Steps

Step 1 - Write down a 2nd order differential equation for each mass

$$m_{1} \frac{d^{2}x_{1}}{dt^{2}} = -k_{1}x_{1} + k_{2}(x_{2}-x_{1})$$

$$m_{2} \frac{d^{2}x_{2}}{dt^{2}} = -k_{2}(x_{2}-x_{1}) + k_{3}(x_{3}-x_{2})$$

$$m_{3} \frac{d^{2}x_{3}}{dt^{2}} = -k_{3}(x_{3}-x_{2}) - k_{4}x_{3}$$

Step 2 - Convert each 2nd order equation into 2 1st order equations

$$\frac{dx_{1}}{dt} = V_{1}$$

$$\frac{dV_{1}}{dt} = \frac{1}{m_{1}} \left(-k_{1}X_{1} + k_{2}(X_{2}-X_{1}) \right)$$

$$\frac{dX_{2}}{dt} = V_{2}$$

$$\frac{dV_{2}}{dt} = \frac{1}{m_{2}} \left(-k_{2}(X_{2}-X_{1}) + k_{3}(X_{3}-X_{2}) \right)$$

$$\frac{dX_{3}}{dt} = V_{3}$$

$$\frac{dV_{3}}{dt} = \frac{1}{m_{3}} \left(-k_{3}(X_{3}-X_{2}) - k_{4}X_{3} \right)$$