CHAPTER

05

DATA REPRESENTATION

Data representation refers those methods which are used internally to represent information stored in a computer. Computer store lots of different types of information as numbers, text, graphics, sounds, etc.

Number System

It is a technique to represent numbers in the computer system architecture, every value that you are saving into/from computer memory has a defined number system.

Types of Number System

Binary Number System

This system is very efficient for computers, but not for humans. It contains only two unique digits 0's and 1's.

It is also known as Base 2 system. A string, which has any combination of these two digits (0 and 1 are called bit) is called a binary number. The computer always calculates the input in binary form and digital computers internally use the binary number system to represent data and perform arithmetic calculations.

For example, (10101)₂

Here, 2 represents the base of binary number.

Decimal Number System

The number system that we use in our day-to-day life is decimal number system.

It consists of 10 digits from 0 to 9. These digits can be used to represent any numeric value. It is also known as Base 10 system or positional number system. For example, $(1275)_{10}$

Here, 10 represents the base of decimal number.

Octal Number System

It consists of 8 digits from 0 to 7. It is also known as Base 8 system. Each position of the octal number represents a successive power of eight.

For example, $(234)_8$

Here, 8 represents the base of octal number.

Hexadecimal Number System

It provides us with a shorthand method of working with binary numbers. There are 16 unique digits available in this system.

These are 0 to 9 and A to F, where A denotes 10, B denotes 11,, F denotes 15.

It is also known as Base 16 system or simply Hex.

So, each position of the hexadecimal number represents a successive power of 16.

For example, (F9D)₁₆

Here, 16 represents the base of hexadecimal number.

Decimal, Binary, Octal and
Hexadecimal Equivalents

		_	
Decimal	Binary	Octal	Hexadecimal
0	0000	0	0
1	0001	1	1
2	0010	2	2
3	0011	3	3
4	0100	4	4
5	0101	5	5
6	0110	6	6
7	0111	7	7
8	1000	_	8
9	1001	_	9
10	1010	_	A
11	1011	_	В
12	1100	_	С
13	1101	_	D
14	1110	_	Е
15	1111	_	F

Conversion between the Number Systems

Decimal to Binary

To convert decimal to binary, following steps are involved

- Step 1 Divide the given number by 2.
- Step 2 Note the quotient and remainder. Remainder should be 0 or 1.
- Step 3 If quotient ≠ 0, then again divide the quotient by 2 and back to step 2.
 If quotient = 0, then stop the process.
- Step 4 First remainder is called as Least
 Significant Bit (LSB) and last remainder is called as Most Significant Bit (MSB).
- Step 5 Arrange all remainders from MSB to LSB.

Example $(43)_{10} \rightarrow (?)_2$

, 10		
		Remainder
2	43	$1 \rightarrow LSB$
2	21	1
2	10	0
2	5	1
2	2	0
2	1	$1 \rightarrow MSB$
	0	

Then,

$$(43)_{10} \rightarrow (101011)_2$$

Binary to Decimal

To convert binary to decimal, following steps are involved

- Step 1 Multiply the all binary digits by powers of 2.
- Step 2 The power for integral part will be positive and for fractional part will be negative.
- Step 3 Add all the multiplying digits.

Example
$$(1101.10)_2 \rightarrow (?)_{10}$$

 $(1101.10)_2 = 1 \times 2^3 + 1 \times 2^2 + 0 \times 2^1$
 $+ 1 \times 2^0 + 1 \times 2^{-1} + 0 \times 2^{-2}$
 $= 8 + 4 + 0 + 1 + 0.5 + 0 = 13.5$
Then, $(1101.10)_2 \rightarrow (13.5)_{10}$

Binary to Octal

To convert binary to octal, following steps are involved

- **Step 1** Make the group of 3 bits from right to left. If the left most group has less than 3 bits, put in the necessary number of leading zeroes on the left.
- Step 2 Now, convert each group to decimal number.

Example
$$(110110100)_2 \rightarrow (?)_8$$

$$\begin{array}{c} 110_1(110_1(100)_2) \\ \downarrow & \downarrow \\ 6 & 6 & 4 \end{array}$$
Then, $(110110100)_2 \rightarrow (664)_8$

Octal to Binary

Convert every digit of the number from octal to binary in the group of 3 bits.

Binary to Hexadecimal

To convert a binary number to its hexadecimal equivalent, follow these steps

- Step 1 Start making the group of 4 bits each from right to left from the given binary number. If the left most group has less than 4 bits, put in the necessary number of leading 0's on the left.
- ${\it Step~2} \quad \hbox{Now, each group will be converted to decimal number.}$

Then,

$$(111101011111011)_2 \rightarrow (3D7B)_{16}$$

Hexadecimal to Binary

For this type of conversion, convert each hexadecimal digit to 4 bits binary equivalent.

Example
$$(BA81)_{16} \rightarrow (?)_2$$

$$B = 11 \quad A = 10 \quad 8 \quad 1$$

$$\downarrow \qquad \downarrow \qquad \downarrow \qquad \downarrow$$

$$1011 \quad 1010 \quad 1000 \quad 0001$$
Then, $(BA81)_{16} \rightarrow (1011101010000001)_2$

Decimal to Octal

To convert decimal to octal, following steps are involved

- Step 1 Divide the given number by 8.
- Step 2 Note the quotient and remainder. Digits of remainder will be from 0 to 7.
- Step 3 If quotient \neq 0, then again divide the quotient by 8 and go back to step 2.
- Step 4 If quotient = 0 or less than 8 then stop the process.
- Step 5 Write each remainder from left to right starting from MSD (Most Significant Digit) to LSD (Least Significant Digit).

Example $(97647)_{10} \rightarrow (?)_{8}$

710	. , 0	
8	97647	7 LSD
8	12205	5
8	1525	5
8	190	6
8	23	7
8	2	2 MSD
	0	
[-7		

Then.

$$(97647)_{10} \rightarrow (276557)_{8}$$

Octal to Decimal

To convert octal to decimal, following steps are involved

Step 1 Multiply each digit of octal number with powers of 8.

- Step 2 These powers should be positive for integral part and negative for fractional part.
- Step 3 Add the all multiplying digits.

Example
$$(327.4)_8 \rightarrow (?)_{10}$$

 $(327.4)_8 = 3 \times 8^2 + 2 \times 8^1 + 7 \times 8^0 + 4 \times 8^{-1}$
 $= 3 \times 64 + 2 \times 8 + 7 \times 1 + \frac{4}{8}$
 $= 192 + 16 + 7 + 0.5$
 $= 215.5$

Then,

$$(327.4)_8 \rightarrow (215.5)_{10}$$

Decimal to Hexadecimal

To convert decimal to hexadecimal, following steps are involved

- Step 1 Divide the given number by 16.
- Step 2 Note the quotient and remainder. Digits of remainder will be 0 to 9 or A to F.
- **Step 3** If quotient $\neq 0$, then again divide the quotient by 16 and go back to step 2.
- **Step 4** If quotient = 0 or less than 16, then stop the process.
- Step 5 Write each remainder from left to right starting from MSD (Most Singnificaut Digit) to LSD (Least Singnificaut Digit).

Example $(929987)_{10} \rightarrow (?)_{16}$

$(227707)_{1}$	$(22)(07)_{10} $ $(1)_{16}$			
16	929987	3 LSD		
16	58124	$12 \rightarrow C \uparrow$		
16	3632	0		
16	227	3		
16	14	$14 \rightarrow E MSD$		
	0			

Then,

$$(929987)_{10} \rightarrow (E \ 30 \ C \ 3)_{16}$$

Hexadecimal to Decimal

To convert hexadecimal to decimal, following steps are involved

- **Step 1** Multiply each digit of hexadecimal number with powers of 16.
- **Step 2** These powers should be positive for integral part and negative for fractional part.
- **Step 3** Add the all multiplying digits.

Example
$$(BC 9.8)_{16} \rightarrow (?)_{10}$$

 $(BC 9. 8)_{16} = B \times 16^2 + C \times 16^1 + 9 \times 16^0 + 8 \times 16^{-1}$
 $= 11 \times 256 + 12 \times 16 + 9 \times 1 + \frac{8}{16}$
 $= 2816 + 192 + 9 + 0.5 = 3017.5$
Then, $(BC 9.8)_{16} \rightarrow (3017.5)_{10}$

Octal to Hexadecimal

To convert octal to hexadecimal, following steps are involved

- Step 1 Convert each digit of octal number to binary number.
- **Step 2** Again, convert each binary digit to hexadecimal number.

Example
$$(7632)_8 \rightarrow (?)_{16}$$

$$\begin{array}{c} (7632)_8 \longrightarrow (111110011010)_2 \\ & \underbrace{1111}_{1} \ \ \underbrace{1001}_{1} \ \ \underbrace{1010}_{1} \\ \downarrow \qquad \qquad \downarrow \qquad \downarrow \\ 15 \qquad 9 \qquad 10 \\ F \qquad \qquad A \\ \hline (7632)_8 \longrightarrow (F9A)_{16} \\ \end{array}$$

Then.

Hexadecimal to Octal

To convert hexadecimal to octal, following steps are involved

- Step 1 Convert each digit of the hexadecimal number to binary number.
- Step 2 Again, convert each binary digit to octal number.

Example
$$(AC2D)_{16} \rightarrow (?)_8$$

$$\begin{array}{cccccc} A & C & 2 & D \\ \downarrow & \downarrow & \downarrow & \downarrow \\ {}_{1}010_{1} & {}_{1}1100_{1} & {}_{1}0010_{1} & {}_{1}1101_{1} \end{array}$$

Computer Codes

In computer, any character like alphabet, digit or special character is represented by collection of 1's and 0's in a unique coded pattern.

In computers, the code is made up of fixed size groups of binary positions.

The binary coding schemes that are most commonly used are as follows

Binary Coded Decimal (BCD)

This system was developed by IBM. It is a number system where four bits are used to represent each decimal digits.

BCD is a method of using binary digits to represent the decimal digits (0-9). In BCD system, there is no limit on size of a number.

American Standard Code for Information Interchange (ASCII)

These are standard character codes used to store data so that it may be used by other software programs.

Basically, ASCII codes are of two types, which are as follows

- (i) **ASCII-7** It is a 7-bit standard ASCII code. It allows $2^7 = 128$ (from 0 to 127) unique symbols or characters.
- (ii) **ASCII-8** It is an extended version of ASCII-7. It is an 8-bit code, allows $2^8 = 256$ (0 to 255) unique symbols or characters.

Extended Binary Coded Decimal Interchange (EBCDIC)

In EBCDIC, characters are represented by eight bits. These codes store information which is readable by other computers. It allows $2^8 = 256$ combination of bits.

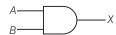
Logic Gate

It is a basic building block of a digital circuit that has two inputs and one output. The relationship between the input and the output is based on a certain logic. These gates are implemented using electronic switches like transistors, diodes.

Inputs
$$\longrightarrow$$
 Logic operation \longrightarrow Output

There are various types of logic gate as follows

1. **AND Gate** This gate is also represented by (\cdot) , i.e. $(A \cdot B)$. It returns True only if both the conditions or inputs are True otherwise it returns False.



Truth Table of AND Gate

\boldsymbol{A}	\boldsymbol{B}	\boldsymbol{X}
0	0	0
0	1	0
1	0	0
1	1	1

$$X = A \cdot B$$

OR Gate This is represented by (+), i.e. (A + B). It returns True if any one of the conditions or inputs is True and if both conditions are False, then it returns False.

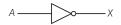


Truth Table of OR Gate

\boldsymbol{A}	В	\boldsymbol{X}
0	0	0
0	1	1
1	0	1
1	1	1

$$X = A + B$$

3. **Inverter or NOT Gate** This gate is also represented by ('), i.e. A'. It returns True if the input is false and *vice-versa*.

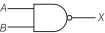


Truth Table of NOT Gate

\overline{A}	X = A'
0	1
1	0

4. **NAND Gate** It is basically the inverse of the AND gate. This gate is designed by combining the AND and NOT gates.

It returns False only if the both conditions or inputs are True otherwise it returns True.



Truth Table of NAND Gate

A	В	X
0	0	1
0	1	1
1	0	1
1	1	0

$$X = (\overline{A \cdot B}) = \overline{A} + \overline{B}$$

5. **NOR Gate** It is inverse of the OR gate. This gate is designed by combining the OR and NOT gates. It returns True only if both the conditions or inputs are False otherwise it returns False.

Truth Table of NOR Gate

\boldsymbol{A}	\boldsymbol{B}	\boldsymbol{X}
0	0	1
0	1	0
1	0	0
1	1	0

$$X = (\overline{A + B}) = \overline{A} \cdot \overline{B}$$

Note NAND and NOR gates are also called universal gates.

6. Exclusive-OR or XOR Gate It performs based on the operation of OR gate.

It returns True only if one condition is true from both the conditions otherwise it returns False.

$$A \longrightarrow B \longrightarrow A$$

Truth Table of XOR Gate

A	В	X
0	0	0
0	1	1
1	0	1
1	1	0

$$X = A \oplus B$$

$$X = \overline{A}B + A\overline{B}$$

- UNICODE uses 16-bits to represent a symbol in the data. It represents any non-english character, scientific symbol in any language like Chinese, Japanese.
- One's complement of binary number is defined as the value obtained by inverting all the bits 110100

For example, One's complement is

QUESTION BANK

1.	There are how	many types	of number system?
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- (1) One
- (2) Two
- (3) Three (4) Four
- 2. Modern computers represent characters and numbers internally using one of the following number systems.
 - (1) Penta
- (2) Octal
- (3) Hexa
- (4) Septa
- (5) Binary
- **3.** In the binary language, each letter of the alphabet, each number and each special character is made up of a unique combination of
 - (1) 8 bytes
- (2) 8 KB
- (3) 8 characters
- (4) 8 bits
- **4.** To perform calculation on stored data computer, uses number system.
 - (1) decimal
- (2) hexadecimal

- (3) octal
- (4) binary
- **5.** Which of the following is not a binary number?
 - (1)001
- (2) 101
- (3) 202
- (4) 110
- **6.** The number system based on '0' and '1' only, is known as
 - (1) binary system
- (2) barter system
- (3) number system
- (4) hexadecimal system

- 7. Binary system is also called
 - (1) base one system
- (2) base two system
- (3) base system
- (4) binary system
- **8.** Which of the following is an example of binary number?
 - (1) 6AH1
- (2) 100101
- (3)005
- (4) ABCD
- **9.** Numbers that are written with base 10 are classified as
 - (1) decimal number
 - (2) whole number
 - (3) hexadecimal number
 - (4) exponential integers
 - (5) mantissa
- **10.** Decimal number system is the group ofnumbers.
 - (1) 0 or 1
- (2) 0 to 9
- (3) 0 to 7
- (4) 0 to 9 and A to F
- **11.** The octal system
 - (1) needs less digits to represent a number than in the binary system
 - (2) needs more digits to represent a number than in the binary system
 - (3) needs the same number of digits to represent a number as in the binary system
 - (4) needs the same number of digits to represent a number as in the decimal system

12.	A hexadecimal number is represented by (1) three digits (2) four binary digits (3) four digits (4) All of these					22. The decimal equivalent of binary number $(1010)_2$ is $(1)\ 8$ $(2)\ 9$ $(3)\ 10$ $(4)\ 11$				
13.			er system l	as base.	23	` '	()		. ,	
		(2) 8	(3) 10	(4) 16		The binary number 10101 is equivalent to decimal number				
14	` '	` '	,			(1) 19		(3) 27	(4) 21	
• ••	Hexadecimal number system consists of (1) 0 to 9 (2) A to F				24.	Which of the following is octal number				
	. ,	3) Both (1) and (2) (4) Either (1) or (2)				equivalent to binary number (110101) ₂ ?				
15.	A hexadigit can be represented by [IBPS Clerk 2012]					(1) 12 (2) 65 (3) 56 (4) 1111				
	(1) three binary (consecutive) bits				25.	Which of the following is a binary number equivalent to octal number (.431) ₈ ?				
	(2) four binary (consecutive) bits									
	(3) eight binary (consecutive) bits			$(1) (100011001)_2$ $(2) (100011001)_2$ $(3) (100110100)_2$ $(4) (100110001)_2$						
	(4) sixteen binary (consecutive) bits									
	(5) None of the above				26.	To convert binary number to decimal, multiply the all binary digits by power of				
16.	Which of the following is invalid									
		exadecimal number				(1) 0		(2) 2		
	(1) A0XB		(2) A0F6			(3) 4		(4) 6		
	(3) 4568 (4) ACDB				27.	Which of the following is hexadecimal number equivalent to binary number				
17.	What type of information system would be									
	recognised by digital circuits?					(1111 100	$(01)_2$?			
	(1) Hexadecimal system					(1) 9F		(2) FF		
	(2) Binary system					(3) 99 (4) F9				
		(a) Both (1) and (2)				Conversion of binary number $(1001001)_2$ to				
	(4) Only roman system					hexadecimal is				
18.	The binary equivalent of decimal number 98				$(1)(40)_{16}$		$(2)(39)_{16}$			
	is [IBPS Clerk 2012]				$(3)(49)_{16}$		$(4)(42)_{16}$			
	(1) 1110001			29.	29. Which of the following is the correct binary					
			(4) 111100	1001		form of $(4A2.8D)_{16}$? [IBPS PO Mains 2017]				
	(5) None of these					(1) (010010100010.10001101)2				
19.	Conversion of decimal number $(71)_{10}$ to its					(2) (010110100010.11101101)2				
	binary number equivalent is					(3) (011110100010.10001101) ₂ (4) (010010111110.10001101) ₂ (5) None of the above				
	[IBPS Clerk 2012]									
	$(1) (110011)_2$		$(2) (1110011)_2$							
	(3) (0110011)2 (4) (1000111)2			11) ₂	30.	Which of the following is an octal number				
	(5) None of these					equal to decimal number (896) ₁₀ ?				
20.	What is th	What is the value of the binary number 101?				(1) 0061		(2) 6001		
	(1) 3	(2) 5	(3) 6	(4) 101	0.1	(3) 1006	0.1	(4) 1600	(1-)	
21.	Decimal equivalent of (1111) ₂ is				31.		Conversion of decimal number $(42)_{10}$ to its			
	[IBPS Clerk 2012]					octal number equivalent is				
		(2) 10	(3) 1	(4) 15		$(1)(57)_8$ $(3)(47)_8$		$(2)(42)_8$ $(4)(52)_8$		
	(5) 13					(=/ (=/ /8		(-/ (0=/8		

- **32.** Determine the octal equivalent of $(432267)_{10}$
 - $(1)(432267)_{8}$
- $(2) (346731)_{8}$
- $(3)(2164432)_8$
- (4) None of these
- **33.** Determine the decimal equivalent of $(456)_8$
 - $(1)(203)_{10}$
- $(2)(302)_{10}$
- $(3)(400)_{10}$
- $(4)(402)_{10}$
- **34.** Conversion of octal number $(3137)_8$ to its decimal equivalent is
 - $(1)(1631)_{10}$
- $(2)(1632)_{10}$
- $(3)(1531)_{10}$
- $(4)(1931)_{10}$
- **35.** Conversion of decimal number $(15)_{10}$ to hexadecimal number is
 - $(1) (14)_{16} (2) (13)_{16} (3) (F)_{16}$
- **36.** Which of the following is a hexadecimal number equal to 3431 octal number?
 - (1) 197(5)719
- (2)917
- (3)791
- (4) 971
- **37.** The method used for the conversion of octal to decimal fraction is
 - (1) digit is divided by 8
 - (2) digit is multiplied by the corresponding power
 - (3) digit is added with 8
 - (4) digit is subtracted with 8
- **38.** MSD refers as
 - (1) Most Significant Digit
 - (2) Many Significant Digit
 - (3) Multiple Significant Digit
 - (4) Most Significant Decimal
- **39.** LSD stands for
 - (1) Long Significant Digit
 - (2) Least Significant Digit
 - (3) Large Significant Digit
 - (4) Longer Significant Decimal

Directions (40 and 41) *Triangle represents* Δ (1) and circle represents o (0). If triangle appears in unit's place then its value is 1. If it appears in 10's place its value is doubled to 2 like that it continues. Using the given terminology answer the following questions. For example,

 $\Delta = 1$

 $\Delta o \Delta = 4, 0, 1 = 4 + 0 + 1$

 $\Delta o = 2$ [IBPS PO Mains 2017]

- **40.** How will you represent '87' in this code language?
 - (1) οΔΔΔοΔΔ
- (2) ΔοΔοΔΔΔ
- (3) ΔΔοΔΔΔΔ
- (4) ΔοοΔοοΔ
- (5) ΔΔοΔΔΔο
- **41.** What will be the code for $\Delta\Delta 000\Delta 0$?
 - (1)98
- (2)95
- (3)96
- (4)94

- (5)99
- **42.** How many values can be represented by a single byte?
 - (1) 4
- (2) 16
- (3)64
- (4)256
- **43.** Which of the following is not a computer code?
 - (1) EBCDIC
- (2) ASCII
- (3) CISC
- (4) UNICODE
- **44.** ASCII stands for
- [IBPS Clerk 2014, 2018]
- (1) American Special Computer for Information Interaction
- (2) American Standard Computer for Information Interchange
- (3) American Special Code for Information Interchange
- (4) American Special Computer for Information Interchange
- (5) American Standard Code for Information Interchange
- **45.** The most widely used code that represents each character as a unique 8-bit code is [UPSSSC 2017]
 - (1) ASCII
- (2) UNICODE
- (3) BCD
- (4) EBCDIC
- **46.** Today's mostly used coding system is/are
 - (1) ASCII
- (2) EBCDIC
- (3) BCD
- (4) Both (1) and (2)
- 47. In EBCDIC code, maximum possible characters set size is
 - (1)356
- (2)756
- (3)556
- (4) 256
- **48.** Code 'EBCDIC' that is used in computing stands for
 - (1) Extension BCD Information Code
 - (2) Extended BCD Information Code
 - (3) Extension BCD Interchange Conduct
 - (4) Extended BCD Interchange Conduct

42. (4)

52. (4)

62. (2)

41. (1)

51. *(5)*

61. *(1)*

44. *(5)*

54. (2)

43. *(*3*)*

53. (3)

45. *(1)*

55. *(2)*

46. (4)

56. (2)

47. *(4)*

57. *(1)*

48. *(2)*

58. (3)

49. (4)

59. (1)

50. (2)

60. (1)

