## CS2040S: Data Structures and Algorithms Recitation 5

## Goals:

- Recognize tree-related problems
- Learn how tree search can efficiently support various user-defined operations
- Appreciate the data-summarization ability granted by augmenting data structures

## Problem 1. (Heights and Grades)

Suppose you are given a set of students with heights and grades as follows:

Name	Height (cm)	Grade (CAP)
Charles	176	4.2
$\operatorname{Bob}$	162	4.5
Mary	180	3.6
John	155	4.1
Wick	186	5.0
Alice	170	3.9

Your goal is to implement an Abstract Data Type (ADT) to efficiently answer the question: "What is the average grade of all students taller than \_\_\_\_\_?". For instance, the average grade of all students taller than John is (4.2 + 4.5 + 3.6 + 5.0 + 3.9)/5 = 4.24.

More specifically, the ADT specifications are as follows:

Operation	Behaviour
insert(name, height, grade)	Inserts student into the dataset.
findAverageGrade(name)	Returns the average grade among all the students that
TindaverageGrade(name)	are taller than the given student.

**Problem 1.a.** How do you capture the information of each student? What should the data type for each of their attributes be?

**Problem 1.b.** How do you design a Data Structure (DS) that serves as an efficient implementation of the given ADT? You may assume that name and height are unique.

**Problem 1.c.** What if height is now not unique? What issue(s) will arise from this? How might you modify your solution in the previous part to resolve the issue(s)?

## Problem 2. (A Game of Cards)

Suppose you have a deck of n cards and they are spread out in front of you on the table from left to right with each card indexed from i to n. Each card can either be facing up or down. We are tasked to implement an ADT for a magic trick with the following specification:

Operation	Behaviour	
query(i)	Return whether card at index i is facing up or down.	
<pre>turnOver(i, j)</pre>	Turn over all cards in the subsequence specified by the index range [i, j].	

**Problem 2.a.** Given n cards already laid out on the table, how do you design a DS that implements such an ADT? Can you achieve turn0ver in  $O(\log n)$  time regardless of the length of subsequence to be turned over? What a magic trick indeed to be able to achieve that!