



Attribute grammars

What are attribute grammars?

Attributes

Why are they useful?

Binary trees: sum

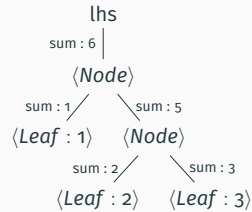
Binary trees: sum



```
data Tree
  | Node left, right :: Tree
  | Leaf value      :: Int

attr Tree
  syn sum :: Int

sem Tree
  | Node lhs.sum = @left.sum
              + @right.sum
  | Leaf lhs.sum = @value
```



Binary trees: depth and index



```
attr Tree
  inh depth :: Int
  chn index :: Int

sem Tree
  | Node loc.depth = @lhs.depth + 1
        left.depth = @depth
        right.depth = @depth

sem Tree
  | Node left.index = @lhs.index
        right.index = @left.index
        lhs.index = @right.index
  | Leaf lhs.index = @lhs.index + 1
```

Binary trees: depth and index using copy rules



```
attr Tree
  inh depth :: Int
  chn index :: Int

sem Tree
  | Node loc.depth = @lhs.depth + 1

sem Tree
  | Leaf lhs.index = @lhs.index + 1
```

The archetypal repmin problem



```
data Root
  | Root Tree

attr Tree
  inh gmin :: Int
  syn lmin use {'min'} {0} :: Int

attr Root Tree
  syn result :: self

sem Tree
  | Leaf lhs.lmin = @value
    .result = Leaf @lhs.gmin

sem Root
  | Root tree.gmin = @tree.lmin
```

A small expression language



```
{
data Type = Int | Bool
data Value = I Int | B Bool
type Env = M.Map String Type
}

data Expr
  | Con val :: {Value} -- Constants
  | Var name :: String -- Variables
  | Let name :: String -- Let binding
    expr :: Expr
    body :: Expr
  | Add x, y :: Expr -- Add operator
  | And x, y :: Expr -- Logical and operator

deriving Expr : Ord, Eq, Show
```

Type checking



```
attr Expr
  inh env :: {Env}
  syn ty :: {Type}

sem Expr
  | Con lhs.ty = case @val of I _ -> Int ; _ -> Bool
  | Var lhs.ty = lookupTy @name @lhs.env
  | Let lhs.ty = @body.ty
    body.env = M.insert @name @expr.ty @lhs.env
  | Add lhs.ty = tyCheck Int @x.ty @y.ty
  | And lhs.ty = tyCheck Bool @x.ty @y.ty
{
lookupVar v = fromMaybe (error "Unbound var!") . M.lookup v
lookupTy v = fst . lookupVar v
tyCheck t t1 t2 | t1 == t2 && t == t1 = t1
                | otherwise = error "Type mismatch"
}
```

Free variables



```
attr Expr
  syn free use {++} {[]} :: Strings

-- Free variables
sem Expr
  | Var lhs.free = [@name]
  | Let lhs.free = @body.free \\ [@name]
```

Project summary

Some remarks



- Submit before the deadline!
- Book a time slot on the Doodle, see course website for a link
- Prepare the oral exam
- Good luck!