# CBE 140 Design Game

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#### 1 Reactor Mass Balance Calculations

### 1.1 Species Balance on Reactant, A

$$a = i - o + g - c$$

$$0 = q_{in}C_{0A} - q_{out}C_A - kC_AV$$

$$0 = qC_{0A} - qC_A - kC_AV$$

$$C_A = \frac{qC_{0A}}{q + kV}$$

$$C_A = \frac{C_{0A}}{1 + k\frac{V}{q}}$$

## 1.2 Species Balance on Product, D

$$a = i - o + g - c$$

$$0 = -q_{out}C_D + kC_AV$$

$$0 = -qC_D + kV\frac{C_{0A}}{1 + k\frac{V}{q}}$$

$$0 = -qC_D + \frac{C_{0A}}{\frac{1}{kV} + \frac{1}{q}}$$

$$V = \frac{q}{k}\left(\frac{C_D}{C_{0A} - C_D}\right)$$

## 2 Cost Analysis

#### 2.1 Determining the Optimal Conversion Ratio

$$Cost = q(\Delta t)C_{0A}(Price_A) + V(Cost_{per\ V})$$

$$Cost = q(\Delta t)C_{0A}(Price_A) + \frac{q}{k}\left(\frac{C_D}{C_{0A} - C_D}\right)(Cost_{per\ V})$$

$$\frac{Cost}{qC_D} = \frac{C_{0A}(\Delta t)}{C_D}(Price_A) + \frac{1}{k}\left(\frac{1}{C_{0A} - C_D}\right)(Cost_{per\ V})$$

$$\frac{Cost}{qC_D} = \frac{\Delta t}{X}(Price_A) + \frac{1}{kC_{0A}(1 - X)}(Cost_{per\ V})$$

$$\frac{d}{dX}\left[\frac{Cost}{qC_D}\right] = -\frac{\Delta t}{X^2}(Price_A) + \frac{1}{kC_{0A}(1 - X)^2}(Cost_{per\ V})$$

$$0 = -\frac{\Delta t}{X^2}(Price_A) + \frac{1}{kC_{0A}(1 - X)^2}(Cost_{per\ V})$$

$$X = \sqrt{\frac{(\Delta t)(Price_A)}{\frac{(Cost_{per\ V})}{kC_{0A}} - (\Delta t)(Price_A)}}$$

Plugging in  $\Delta t = 5.04 \times 10^5 \,\text{min}$ ,  $Price_A = \$0.28 \,\text{mol}^{-1}$ ,  $Cost_{per\ V} = \$47 \,\text{L}^{-1}$ ,  $k = 0.005 \,\text{min}^{-1}$ ,  $C_{0A} = 0.20 \,\text{mol} \,\text{L}^{-1}$ :

$$X = 0.897$$

# 3 Reactor Sizing

We will size the reactor to achieve the optimal (cost minimized) conversion ratio, X, when 10% of the time-averaged projected market demand is reached.

$$\bar{D} = \frac{\Sigma[D_1 \dots D_5]}{5}$$
$$\bar{D} = 3.12 \times 10^7 \,\text{mol yr}^{-1}$$

This amounts to a production rate,  $qC_D$ , of:

$$qC_D = \frac{(0.1)\bar{D}}{(\Delta t)}$$

$$V = \frac{1}{k} \frac{qC_D}{C_{0A} - XC_{0A}}$$
$$V = \frac{qC_D}{kC_{0A}(1 - X)}$$

Plugging in  $k = 0.005 \,\mathrm{min^{-1}}, \ C_{0A} = 0.20 \,\mathrm{mol} \,\mathrm{L^{-1}}, \ qC_D = 3.12 \times 10^6 \,\mathrm{mol} \,\mathrm{yr^{-1}}, \ X = 0.897$ :