CBE 140 Design Game

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1 Reactor Mass Balance Calculations

1.1 Species Balance on Reactant, A

$$
\begin{aligned}
a &= i - o + g - c \\
0 &= q_{in}C_{0A} - q_{out}C_A - kC_AV \\
0 &= qC_{0A} - qC_A - kC_AV \\
C_A &= \frac{qC_{0A}}{q + kV} \\
C_A &= \frac{C_{0A}}{1 + k\frac{V}{q}}
\end{aligned}
$$

1.2 Species Balance on Product, D

$$
\begin{aligned}
a &= i - o + g - c \\
0 &= -q_{out}C_D + kC_AV \\
0 &= -qC_D + kV\frac{C_{0A}}{1 + k\frac{V}{q}} \\
0 &= -qC_D + \frac{C_{0A}}{\frac{1}{kV} + \frac{1}{q}} \\
V &= \frac{q}{k}\left(\frac{C_D}{C_{0A} - C_D}\right)
\end{aligned}
$$

2 Cost Analysis

2.1 Determining the Optimal Conversion Ratio

$$
\begin{aligned}
Cost &= q(\Delta t)C_{0A}(Price_A) + V(Cost_{per\ V}) \\
Cost &= q(\Delta t)C_{0A}(Price_A) + \frac{q}{k}\left(\frac{C_D}{C_{0A} - C_D}\right)(Cost_{per\ V}) \\
\frac{Cost}{qC_D} &= \frac{C_{0A}(\Delta t)}{C_D}(Price_A) + \frac{1}{k}\left(\frac{1}{C_{0A} - C_D}\right)(Cost_{per\ V}) \\
\frac{Cost}{qC_D} &= \frac{\Delta t}{X}(Price_A) + \frac{1}{kC_{0A}(1-X)}(Cost_{per\ V}) \\
\frac{d}{dX}\left[\frac{Cost}{qC_D}\right] &= -\frac{\Delta t}{X^2}(Price_A) + \frac{1}{kC_{0A}(1-X)^2}(Cost_{per\ V}) \\
0 &= -\frac{\Delta t}{X^2}(Price_A) + \frac{1}{kC_{0A}(1-X)^2}(Cost_{per\ V}) \\
X &= \sqrt{\frac{(\Delta t)(Price_A)}{\frac{(Cost_{per\ V})}{kC_{0A}} - (\Delta t)(Price_A)}}
\end{aligned}
$$

$Plugging\ in\ \Delta t = 5.04 \times 10^5\,\mathrm{min}, \quad Price_A = \$0.28\,\mathrm{mol}^{-1},\ Cost_{per\ V} = \$47\,\mathrm{L}^{-1},$
$k = 0.005\,\mathrm{min}^{-1},\ C_{0A} = 0.20\,\mathrm{mol\,L}^{-1}:$

$$X = 0.897$$

3 Reactor Sizing (Work in progress)

We will size the reactor to achieve the optimal (cost minimized) conversion ratio, X, when 10% of the time-averaged projected market demand is reached.

$$
\begin{aligned}
\bar{D} &= \frac{\Sigma[D_1 \ldots D_5]}{5} \\
\bar{D} &= 3.12 \times 10^7\,\mathrm{mol\,yr}^{-1}
\end{aligned}
$$

This amounts to a production rate, qC_D, of:

$$
\begin{aligned}
qC_D &= \frac{(0.1)\bar{D}}{(\Delta t)} \\
qC_D &= 6.19\,\mathrm{L/\,min}
\end{aligned}
$$

$$V = \frac{1}{k}\frac{qC_D}{C_{0A} - XC_{0A}}$$
$$V = \frac{qC_D}{kC_{0A}(1-X)}$$

$$\textit{Plugging in } k = 0.005\,\mathrm{min}^{-1},\;\; C_{0A} = 0.20\,\mathrm{mol\,L^{-1}},\;\;\; qC_D = 3.12\times10^{6}\,\mathrm{mol\,yr^{-1}},\;\;\; X = 0.897:$$

$$V = 6.01\times10^{4}\,\mathrm{L}$$