Financial Instruments Coursework

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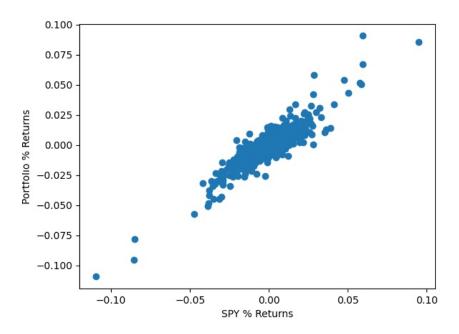


Figure 1: Scatter plot of Portfolio Returns against S&P 500

We see that there seems to be a linear relationship between returns of S&P500 and the returns of the portfolio. Also, the alpha of this portfolio seems to be zero as the intercept seems to be 0. The code written to do the calculations can be found in appendix.

b

Table 1: Mean of all Stock Returns

	$ln_ret_DBE_mean$	$ln_ret_JPM_mean$	$ln_ret_MA_mean$	$ln_ret_NFLX_mean$	$ln_ret_SPY_mean$	$ln_ret_WMT_mean$	$portfolio_log_returns_mean$
0	0.000209	0.000648	0.001037	0.001297	0.000622	0.000681	0.000774

Table 2: Covariance Matrix

	${\rm ln_ret_DBE}$	$\ln_{\rm ret}_{\rm JPM}$	$\ln_{\rm ret}_{\rm MA}$	${\rm ln_ret_NFLX}$	$\ln_{\rm ret}_{\rm SPY}$	$\ln_{\rm ret}_{\rm WMT}$	$portfolio_log_returns$
ln_ret_DBE	0.000294	0.000128	0.000115	0.000069	0.000090	0.000030	0.000127
ln_ret_JPM	0.000128	0.000369	0.000224	0.000098	0.000177	0.000073	0.000178
ln_ret_MA	0.000115	0.000224	0.000360	0.000185	0.000187	0.000083	0.000193
ln_ret_NFLX	0.000069	0.000098	0.000185	0.000588	0.000145	0.000089	0.000206
ln_ret_SPY	0.000090	0.000177	0.000187	0.000145	0.000146	0.000080	0.000136
ln_ret_WMT	0.000030	0.000073	0.000083	0.000089	0.000080	0.000191	0.000093
portfolio_log_returns	0.000127	0.000178	0.000193	0.000206	0.000136	0.000093	0.000160

Table 3: Beta Calculated From Covariance Matrix

	${\rm DBE_beta}$	${\rm JPM_beta}$	MA_beta	$NFLX_beta$	SPY_beta	portfolio_returns_beta
0	0.614786	1.213278	1.278208	0.990476	1.0	0.928908

$$\beta_s = \frac{\operatorname{Cov}[R_m, R_s]}{\operatorname{Var}[R_m]}$$

where β_s is Beta of the stock, $\text{Cov}[R_m, R_s]$ is the covariance of the stock and market index, $\text{Var}[R_m]$ is the variance of the market index.

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Table 4: Portfolio Return Info

	portfolio_annual_mean_returns	portfolio_std_returns
0	0.193622	0.19971

$$\mu_{1y} = \mu_{1d} * 250$$

$$\sigma_{1y} = \sigma_{1d} * \sqrt{250}$$

where,

 μ_{1y} and μ_{1d} are annual and daily log-returns respectively and

 σ_{1y} and σ_{1d} are annual and daily standard deviation of log-returns respectively

Appendix(Python Code)

All the necessary imports

import pandas as pd

import os

import statsmodels.api as sm

import yfinance as yf

```
import numpy as np
import matplotlib.pyplot as plt
```

Downloading Data

```
# Downloading Data of certain stocks and S&P500 from Yahoo Finance
k = yf.download('SPY DBE JPM MA NFLX WMT', start='2016-12-31', end='2021-09-30')
k=k[[i for i in k.columns if 'Adj Close' in i]] # Remove all columns except adjusted Close
k=k.set_axis(k.columns.map('_'.join), axis=1, inplace=False)
```

Calculating Returns and Saving Figure

```
for i in k.columns:
    logcolname = f"ln_ret_{i[10:]}"
    ord_ret = f"%ret_{i[10:]}" # Column name for percentage returns
    k[logcolname] = np.log(k[i]/k[i].shift(1)) # Calculating log returns
    k[ord_ret] = np.exp(k[logcolname])-1 # calculating percentage returns from log returns
print(k)
# Extracting Columns Names of only stocks
per_ret=[i for i in k.columns if "%ret" in i and 'SPY' not in i]
log_ret=[i for i in k.columns if "ln_ret" in i and 'SPY' not in i]
k['portfolio_returns_percentage'] = k[per_ret].mean(axis=1) #Calculating Portfolio Returns
k['portfolio_log_returns'] = k[log_ret].mean(axis=1 # Calculating log portfolio returns
plt.scatter(k.portfolio_returns_percentage,k['%ret_SPY']) #Plotting Scatter Plot
plt.xlabel("SPY % Returns")
plt.ylabel("Portfolio % Returns")
plt.savefig("ScatterPlot.jpg")
```

Calculating Means

print(info)

```
return_info1 = pd.DataFrame() # For calculating Mean of all series
for i in cov_mat_cols:
    return_info1[f"{i}_mean"] = [k[i].mean()]
```

Calculating Covariance and Beta

Calculating Annualized Standard Deviation

```
return_info = pd.dataFrame()
return_info['portfolio_annual_mean_returns'] = [k.portfolio_log_returns.mean()*250]
return_info['portfolio_std_returns'] = [k.portfolio_log_returns.std()*250**.5]
```