

1. DDA

a. titik awal : $A(7, 10)$

titik akhir : $B(17, 16)$

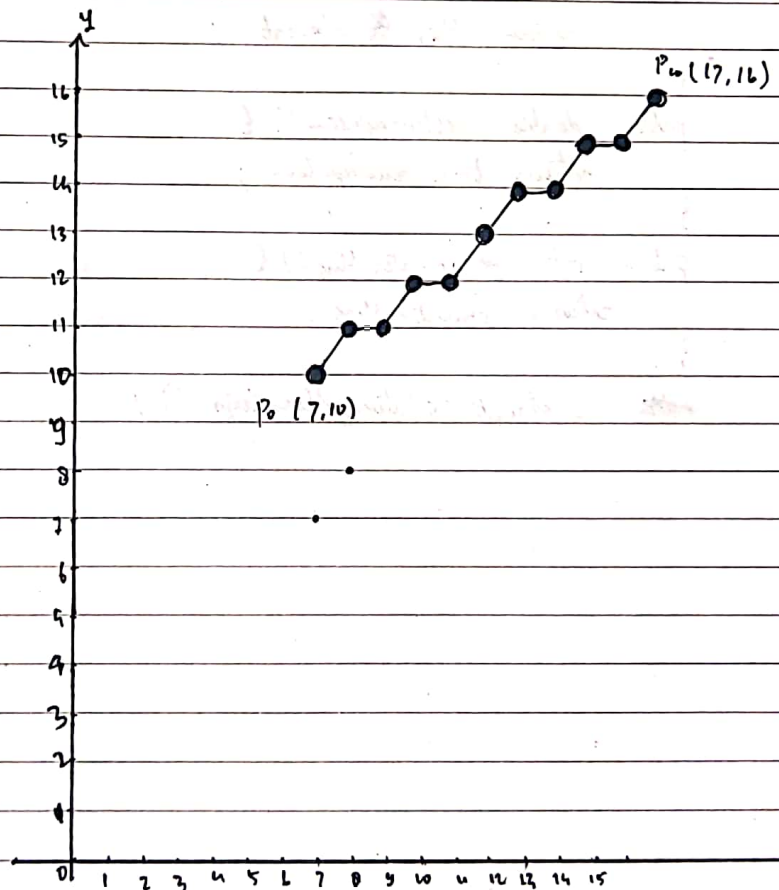
b. $dx = x_1 - x_0$ $dy = y_1 - y_0$
 $= 17 - 7$ $= 16 - 10$
 $= 10$ $= 6$

c. $dx > dy$, maka lebih banyak langkah pada sumbu x, steps = 10

$X_{\text{increment}} = 10/10 = 1$

$Y_{\text{increment}} = 6/10 = 0.6$

k	x_k	y_k	x_{plot}	y_{plot}
0	7	10	7	10
1	8	10.6	8	11
2	9	11.2	9	11
3	10	11.8	10	12
4	11	12.4	11	12
5	12	13	12	13
6	13	13.6	13	14
7	14	14.2	14	14
8	15	14.8	15	15
9	16	15.4	16	15
10	17	16	17	16



2. Lingkaran dengan pusat $A(3,4)$, dengan radius : 10. step by step dengan Bresenham mid point

a) $(x = x_c, y = y_c)$

$x_0, y_0 = (0, 10) \quad (x_c, y_c) = (3, 14)$ initial point

b) $p_0 = 1 - r$
 $= 1 - 10 = -9$

c) $p_k < 0 \rightarrow \text{plot } (x_{k+1}, y_k)$
 $\hookrightarrow p_{k+1} = p_k + 2(x_{k+1} + 1)$

$p_k \geq 0 \rightarrow \text{plot } (x_{k+1}, y_{k+1})$
 $\hookrightarrow p_{k+1} = p_k - 2(x_{k+1} + 1) + 2(y_{k+1} + 1)$

d) Menentukan pixel

$k=0, p_0 = -9, (0, 10)$

$k=1, p_1 = -9 + 2(0+1)+1$
 $= -6, (1, 10)$

$k=2, p_2 = -6 + 2(1+1)+1$
 $= -6 + 5$
 $= -1, (2, 10)$

$k=3, p_3 = -1 + 2(2+1)+1$
 $= -1 + 7$
 $= 6, (3, 9)$

$k=4, p_4 = 6 + 2(3+1)+1 - 2(9-1)+1$
 $= 6 + 9 - 16$
 $= -1, (4, 9)$

$k=5, p_5 = -1 + 2(4+1)+1$
 $= -1 + 11$
 $= 10, (5, 8)$

$k=6, p_6 = 10 + 2(5+1) - 2(8-1)+1$
 $= 10 + 13 - 14$
 $= 9, (6, 7)$

$k=7, p_7 = 9 + 2(6+1)+1 - 2(7-1)$
 $= 9 + 15 - 12$
 $= 12, (7, 6)$

e) Tabel pixel

k	p_k	(x_{k+1}, y_{k+1})	$2x_{k+1}$	$2y_{k+1}$	$(x + x_c, y + y_c)$
0	-9	(0, 10)	2	20	(4, 14)
1	-6	(1, 10)	4	20	(5, 14)
2	-1	(2, 10)	6	20	(6, 14)
3	6	(3, 9)	8	18	(7, 13)
4	-1	(4, 9)	10	18	(8, 13)



4.

k	Ph	(x_{k+1}, y_{k+1})	$2x_{k+1}$	$2y_{k+1}$	$(x+x_c, y+y_c)$
5	10	(5, 8)	10	16	(8, 12)
6	9	(6, 7)	12	14	(9, 11)
7	12	(7, 6)	14	12	(10, 10)

3. Transformasi 3D 45° garis AB

A(6, 1, -1) B(6, 4, 0)

step 1 Translasi A ke origin

$$T = \begin{bmatrix} 1 & 0 & 0 & -x_1 \\ 0 & 1 & 0 & -y_1 \\ 0 & 0 & 1 & -z_1 \\ 0 & 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & -6 \\ 0 & 1 & 0 & -1 \\ 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

step 2 $TR_x(\alpha)$

B(0, 3, -1)

$$\sin \alpha = \frac{b}{\sqrt{b^2 + c^2}} = \frac{b}{d}$$

$$= \frac{3}{\sqrt{9+1}} = \frac{3}{\sqrt{10}}$$

$$\cos \alpha = \frac{c}{\sqrt{b^2 + c^2}} = \frac{c}{d}$$

$$= \frac{-1}{\sqrt{10}}$$

$$R_x(\alpha) = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & -\frac{1}{\sqrt{10}} & \frac{3}{\sqrt{10}} & 0 \\ 0 & \frac{3}{\sqrt{10}} & \frac{1}{\sqrt{10}} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

step 3

$$\sin \beta = \frac{a}{d} \quad \cos \beta = \frac{d}{d} \quad \sin \beta = 0 \quad \sin \alpha = \frac{\sqrt{10}}{\sqrt{10}} = 1$$

$$d^2 = a^2 + b^2 + c^2 = a^2 + d^2$$

$$d^2 = 0^2 + \sqrt{10}^2$$

$$d^2 = 10 \quad d = \sqrt{10}$$

$$R_y(\beta) = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

step 4

$$R_z(45^\circ) = \begin{bmatrix} \cos 45^\circ & -\sin 45^\circ & 0 & 0 \\ \sin 45^\circ & \cos 45^\circ & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

Step 5

$$\left[\begin{array}{ccc|ccc} 1 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 & 0 & -\frac{1}{x_0} & \frac{3}{x_0} & 0 \\ 0 & 0 & 1 & -1 & 0 & \frac{3}{x_0} & -\frac{1}{x_0} & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 1 \end{array} \right] \rightarrow \left[\begin{array}{ccc|ccc} 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 1 \end{array} \right]$$

$$R(0) = \left[\begin{array}{ccc|ccc} 1 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 & 0 & -\frac{1}{x_0} & \frac{3}{x_0} & 0 \\ 0 & 0 & 1 & -1 & 0 & \frac{3}{x_0} & -\frac{1}{x_0} & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 1 \end{array} \right] \rightarrow \left[\begin{array}{ccc|ccc} 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 1 \end{array} \right] \rightarrow \left[\begin{array}{ccc|ccc} 0 & -1 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 1 \end{array} \right]$$

$$\left[\begin{array}{ccc|ccc} 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & -\frac{1}{x_0} & \frac{3}{x_0} & 0 \\ 0 & 0 & 1 & 0 & 0 & \frac{3}{x_0} & -\frac{1}{x_0} & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 1 \end{array} \right] \rightarrow \left[\begin{array}{ccc|ccc} 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 1 \end{array} \right]$$

4. Garis AB

$$A = 1000 \quad (-1, 6)$$

$$B = 1010 \quad (5, 5)$$

1000 Tidak di Clipping

garis CD

$$m = \frac{5-2}{-1-5}$$

$$C = 1000 \quad (-1, 5)$$

$$= \frac{3}{-6}$$

$$D = 0010 \quad (5, 2)$$

$$= -\frac{1}{2}$$

0000 kandidat

$$\text{Top } x_{p2} = x_1 + (y_{\max} - y_1) / m$$

$$= -1 + (4 - 5) / -\frac{1}{2}$$

$$= -1 + -1 \cdot -2$$

$$= -1 + 2$$

$$= 1 \quad \therefore \text{titik potong } (1, 4)$$

$$\text{Right } y_{p2} = y_1 + m \cdot (x_{\max} - x_1)$$

$$= 2 + (-\frac{1}{2}) \cdot (3 - 5)$$

$$= 2 + \frac{(-2)}{2}$$

$$= 2 + 1$$

$$= 3 \quad \therefore \text{titik potong } (3, 3)$$

Hasil clip : (1, 4) dan (3, 3)

garis EF

$$E = 0000 \quad (1, 2) \quad m = \frac{1-2}{5-1}$$

$$F = 0010 \quad (5, 1) \quad = -\frac{1}{4}$$

0000 kandidat

$$\text{Right } y_{p2} = y_1 + m \cdot (x_{\max} - x_1)$$

$$= 1 + (-\frac{1}{4}) \cdot (3 - 5)$$

$$= 1 + \frac{-2}{-4}$$

$$= 1 + \frac{1}{2}$$

$$= 1,5 \quad \therefore \text{titik potong } (3, 1,5)$$

Hasil Clip adalah (1, 2) dan (3, 1,5)

garis GH

$$G = 0000 \quad (-1, 3)$$

$$H = 0000 \quad (1, 1)$$

0000 Diterima

garis IJ

$$I = 1001 \quad (-3, 7)$$

$$J = 0101 \quad (-1, -1)$$

0000 kandidat

$$m = \frac{-1 - 7}{-1 + 3}$$

$$= \frac{-8}{2}$$

$$= -4$$

$$\text{Top } x_{p2} = x_1 + (y_{\max} - y_1) / m$$

$$= -3 + (4 - 7) / -4$$

$$= -3 + \frac{-3}{-4}$$

$$= -3 + 0,75$$

$$= -2,25 \quad \therefore (-2,25, 4)$$

$$\text{Left } y_{p1} = y_1 + m \cdot (x_{\min} - x_1)$$

$$= 7 + (-4) \cdot (-2 + 3)$$

$$= 7 + (-4) \cdot 1$$

$$= 3 \quad \therefore (-2, 3)$$

$$\text{Bottom } x_{p1} = x_1 + (y_{\min} - y_1) / m$$

$$= -1 + (0 + 1) / -4$$

$$= -1 + (-\frac{1}{4})$$

$$= -1,25 \quad \therefore (-1,25, 0)$$

Hasil clip adalah (-2, 3) dan (-1,25, 0)

garis KL

$$K = 0101 \quad (-4, -2)$$

$$L = 0110 \quad (4, -1)$$

0100 Tidak di clipping