

## SVM - Optimization:

$$\min \|w\|^2, \text{ s.t. } y_i (w^T x_i) \geq 1 \text{ for } i=1, \dots, N \quad (1)$$

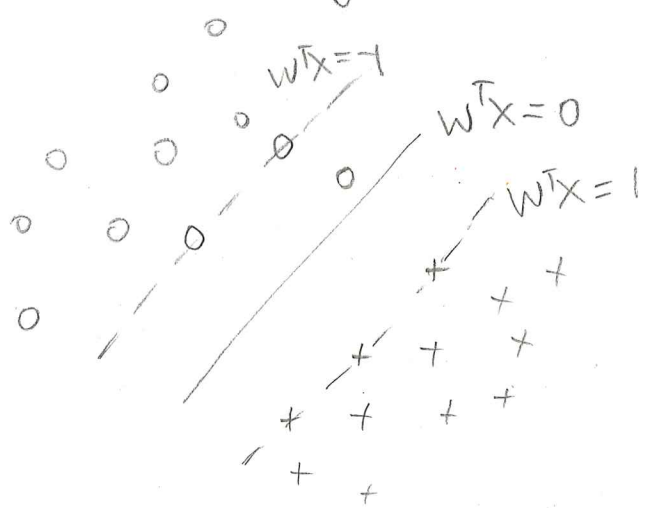
Quadratic optimization. s.t. linear constraints.

The optimization of (1) is equivalent to the unconstrained optimization problem over  $w$ :

$$\min \|w\|^2 + \lambda \sum_{i=1}^N \max(0, 1 - y_i f(x_i))$$

$\Rightarrow f(x_i) = w^T x_i$

$\swarrow$  regularization       $\searrow$  hard-tuning parameter       $\rightarrow$  Loss function "hinge" loss.



1.  $y_i f(x_i) > 1$ , points is outside margin.

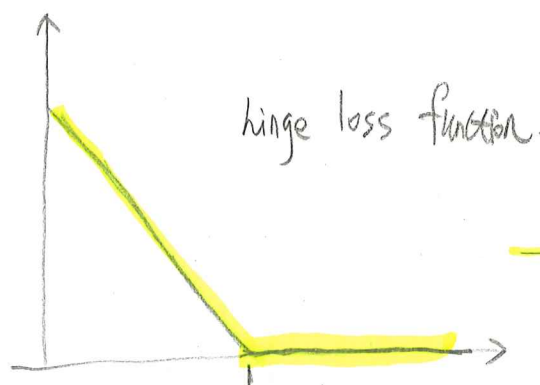
No Contribution to loss

2.  $y_i f(x_i) = 1$ , points on margin.

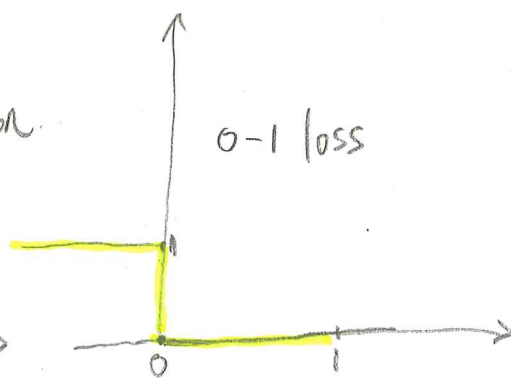
No Contribution.

3.  $y_i f(x_i) < 1$ , points violates Margin constraint.

Contributes to loss



hinge loss function.



0-1 loss