

Autoencoder

Foundations of Data Analysis

April 28, 2020

Slide credits to Jian Wang, PhD student, CS, UVA

Overview: Data dimensionality

High-dimensional



Low-dimensional



Complicated;
Hard to handle

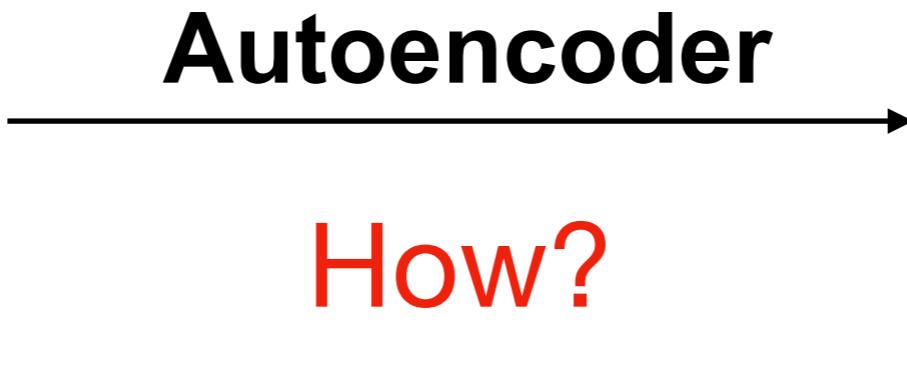
Simplified clear;
Property preserved

Dimensionality reduction techs:
Autoencoder/PCA



Applications of Autoencoder: Colorization

- Image coloring:



- Reconstruct an image from grey color space to RGB/HSV.

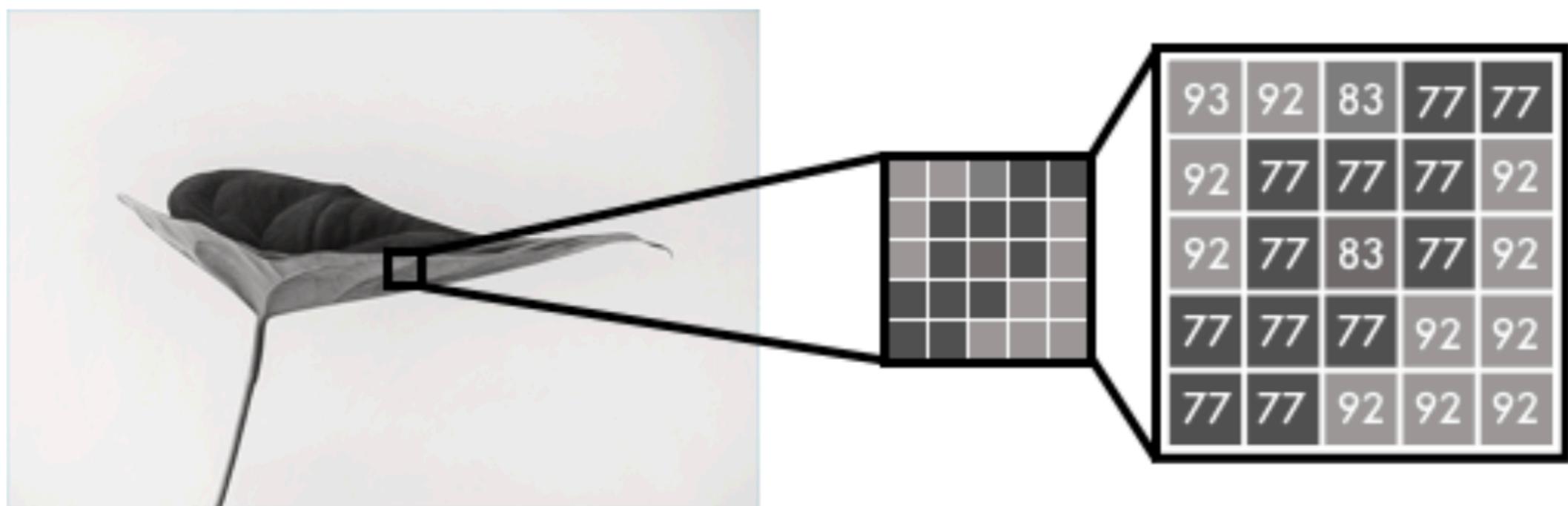
Example: Image coloring



AE



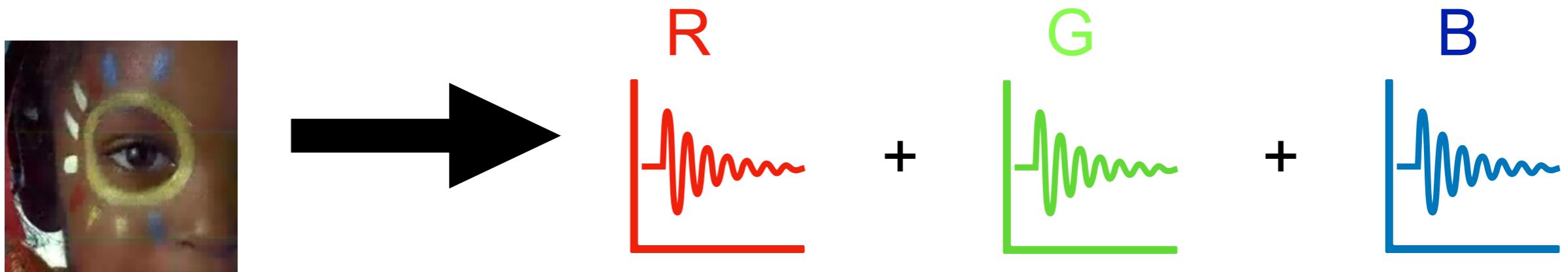
- Grey image color scale:



- Learn the intensity pattern!

Example: Image coloring

- Autoencoder training:



Train autoencoders for each channel from natural images.

- Autoencoder prediction:

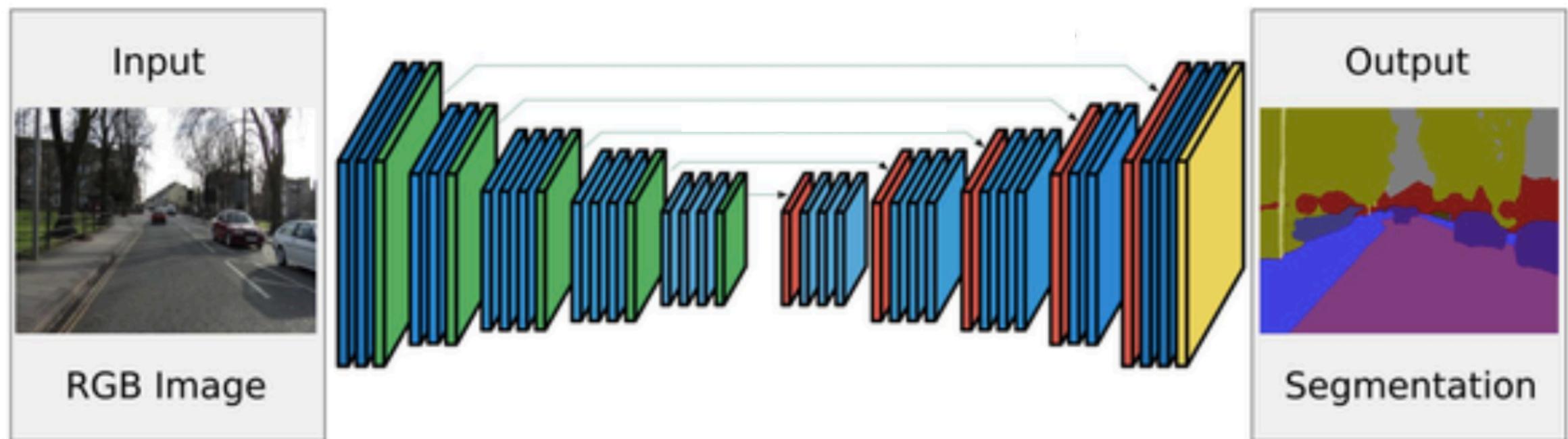
$$f \left(\begin{matrix} 93 & 92 & 83 & 77 & 77 \\ 92 & 77 & 77 & 77 & 92 \\ 92 & 77 & 83 & 77 & 92 \\ 77 & 77 & 77 & 92 & 92 \\ 77 & 77 & 92 & 92 & 92 \end{matrix} \right) = \begin{matrix} 83 & 92 & 83 & 77 & 77 \\ 99 & 99 & 77 & 77 & 92 \\ 99 & 77 & 83 & 77 & 92 \\ 77 & 77 & 77 & 95 & 92 \\ 77 & 77 & 95 & 92 & 92 \end{matrix} \quad \begin{matrix} 93 & 92 & 83 & 69 & 69 \\ 92 & 69 & 69 & 77 & 92 \\ 92 & 69 & 83 & 77 & 92 \\ 69 & 69 & 77 & 92 & 92 \\ 77 & 77 & 92 & 92 & 92 \end{matrix} \quad \begin{matrix} 83 & 92 & 83 & 77 & 77 \\ 83 & 77 & 77 & 77 & 92 \\ 92 & 77 & 83 & 75 & 85 \\ 75 & 77 & 75 & 85 & 85 \\ 75 & 75 & 85 & 85 & 85 \end{matrix}$$

Well-trained
Autoencoder function

Predictions for each channel

Applications of Autoencoder: Segmentation

- Image segmentation:

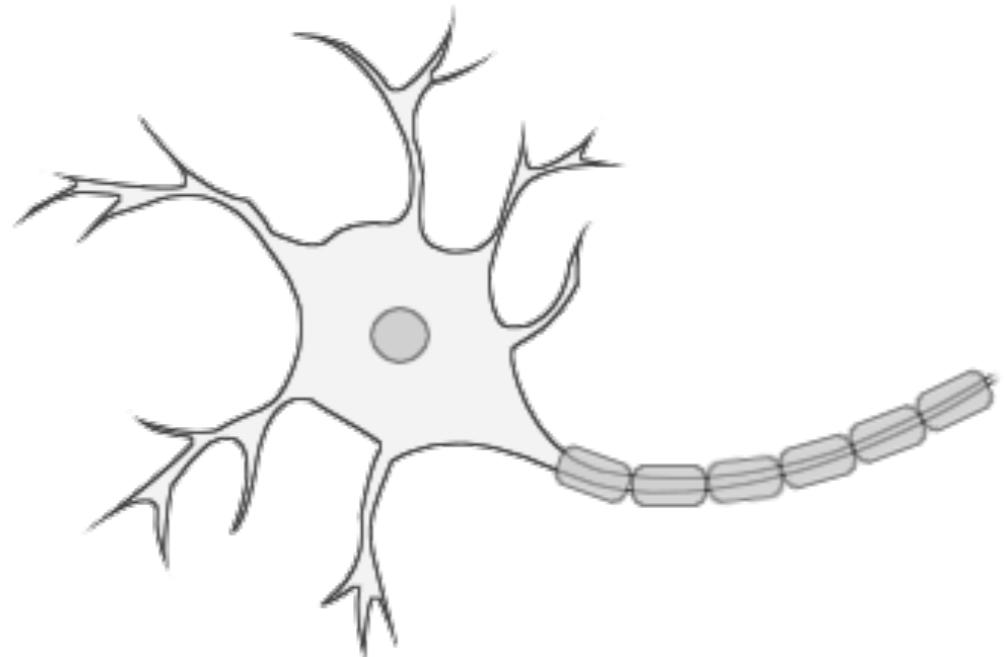


- What do we need ?

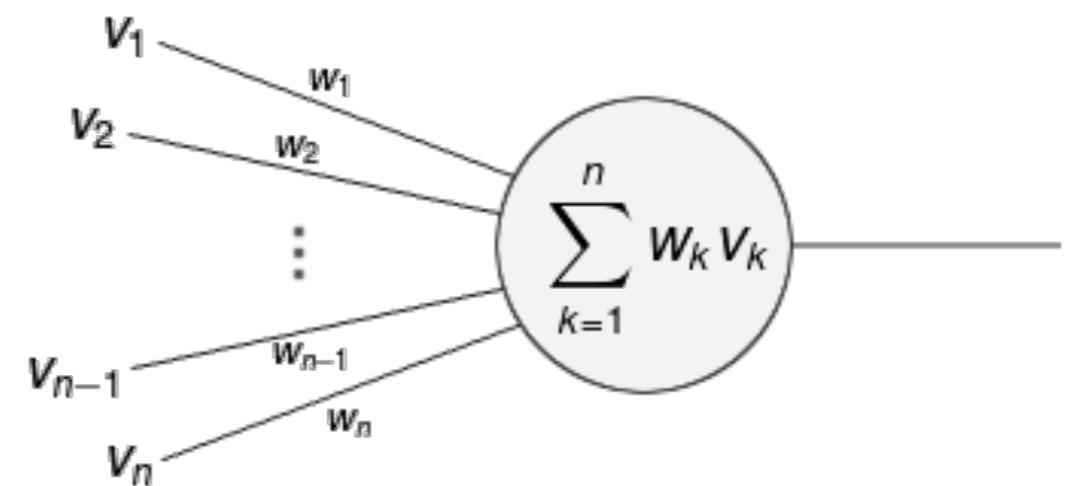
Ground-truth, training, testing and validation.

Overview: Autoencoder (AE)

- Relationship to neural networks: layers, neurons, and weights;



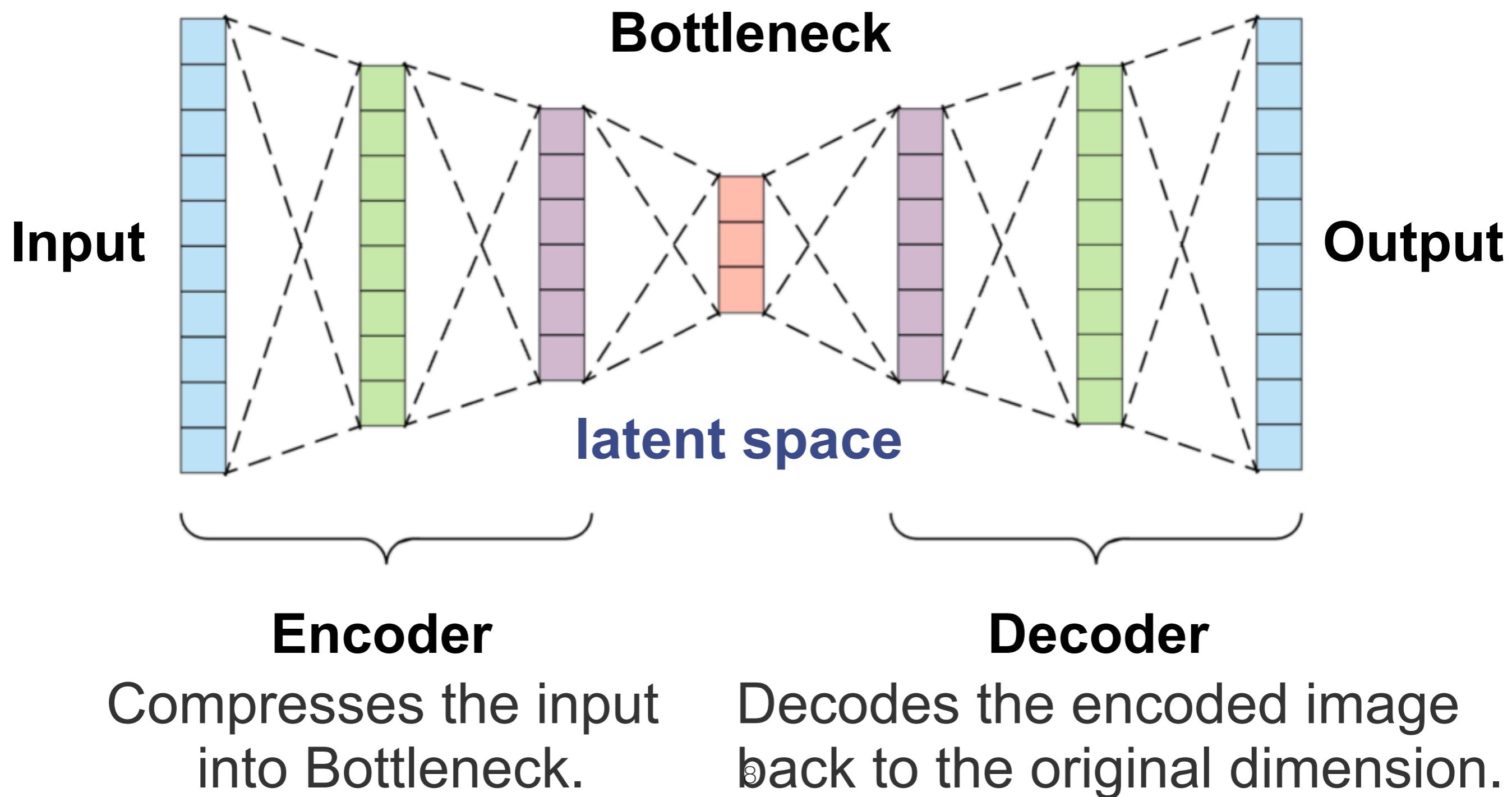
Brain neuron



Simulated neuron with
input V and weights W

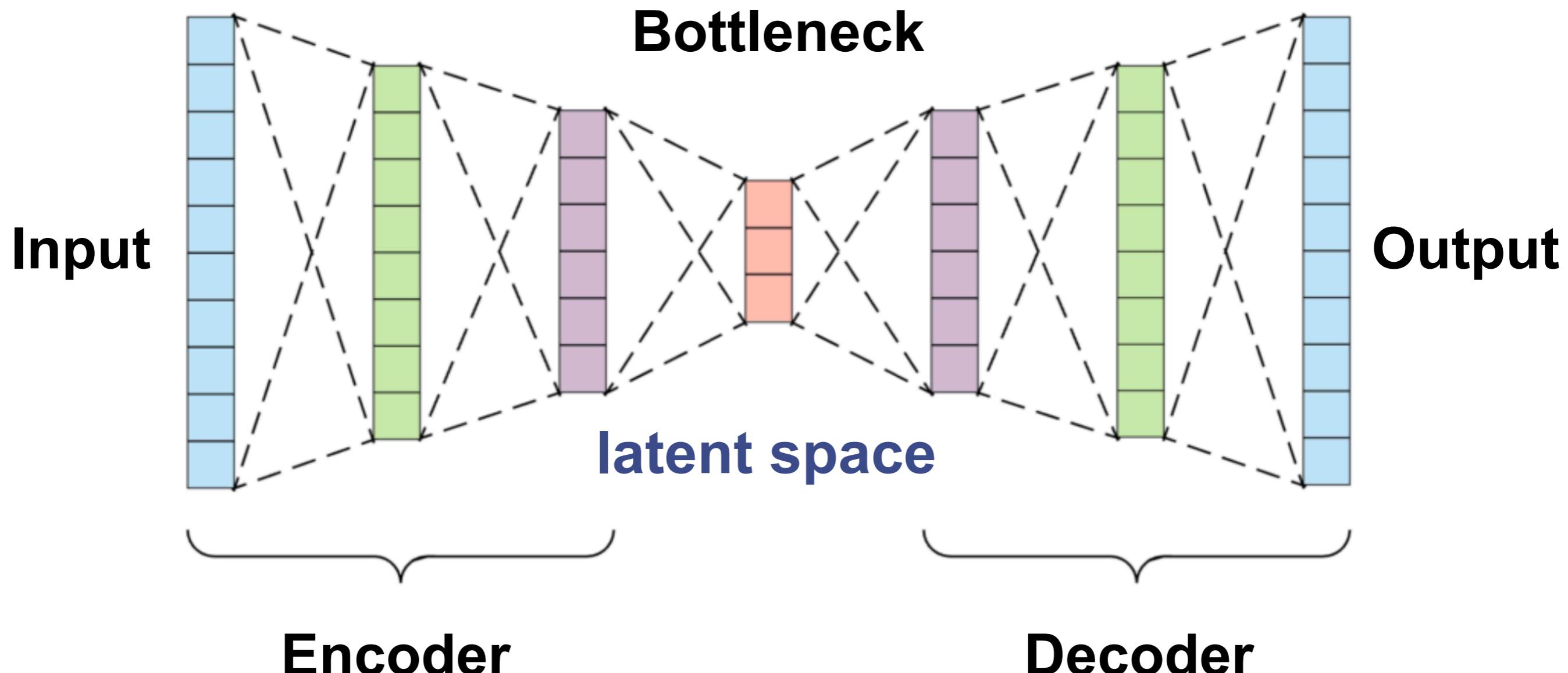
Architecture : Autoencoder

- Core structure: **Encoder**, **Decoder** and **Bottleneck**



Architecture : Autoencoder

- Core structure: **Encoder**, **Decoder** and **Bottleneck**



- Goal: minimize the reconstruction error.

Formulation: Simple Autoencoder

- Encoder and decoder

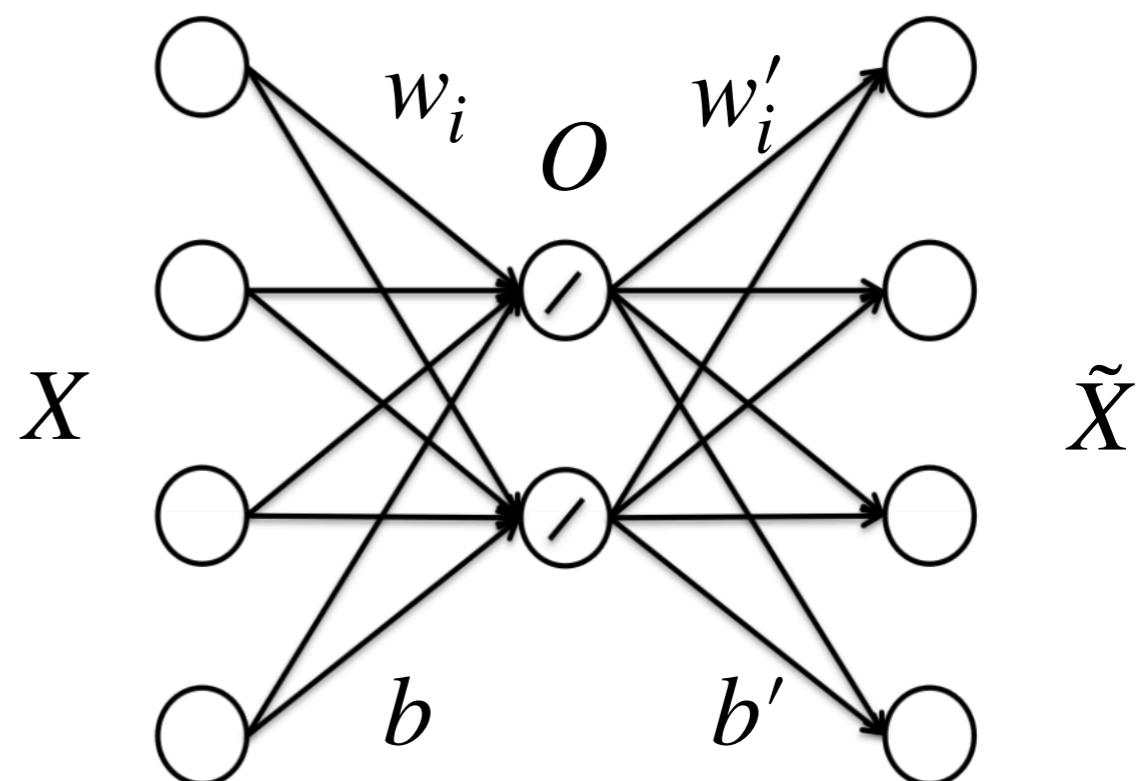
Original Data: $[x_1, x_2, \dots, x_n]$ Output Data: $[x_1, x_2, \dots, x_n]'$

Latent input/encoder output:

$$O = \sum_{i=1}^n w_i x + b$$

Latent output/decoder output:

$$\tilde{X} = \sum_{i=1}^n w'_i O + b'$$



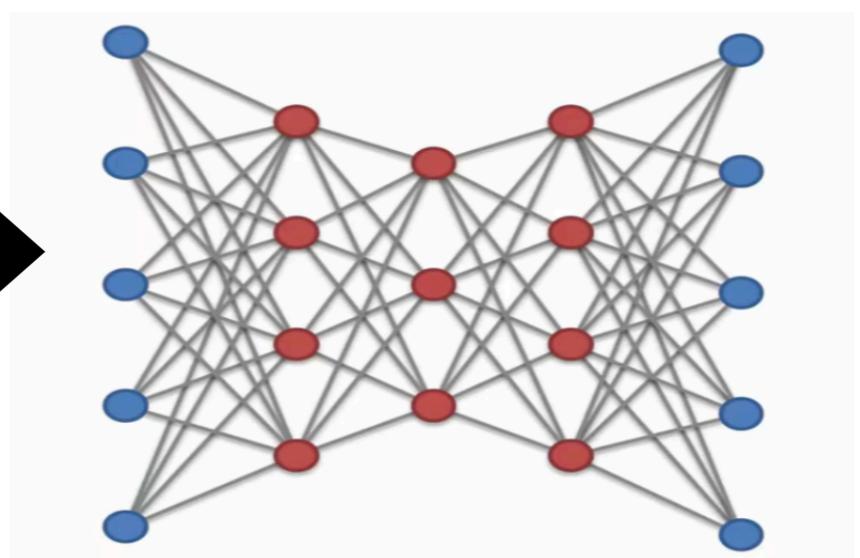
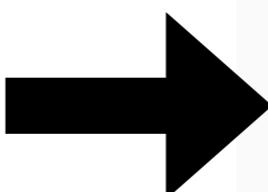
- Optimization:

Loss function: $f = \text{argmin}(X - \tilde{X}) = ||X - (w'x + b)||^2$

Major parameters in Autoencoder

- Layer size: more layers come with better accuracy?
- Size of bottleneck: number of nodes in the middle layer, (smaller size results in more compression);
- Loss function: mean squared error or binary cross-entropy;
- Penalty term: L_1 and L_2 regularity;

Deep autoencoder



Autoencoder Types

- **Vanilla Autoencoder**

Simplest form, two layers with one hidden layer;

- **Regularized Autoencoder**

Add regularization term to constraint loss function;

- **Multilayer Autoencoder**

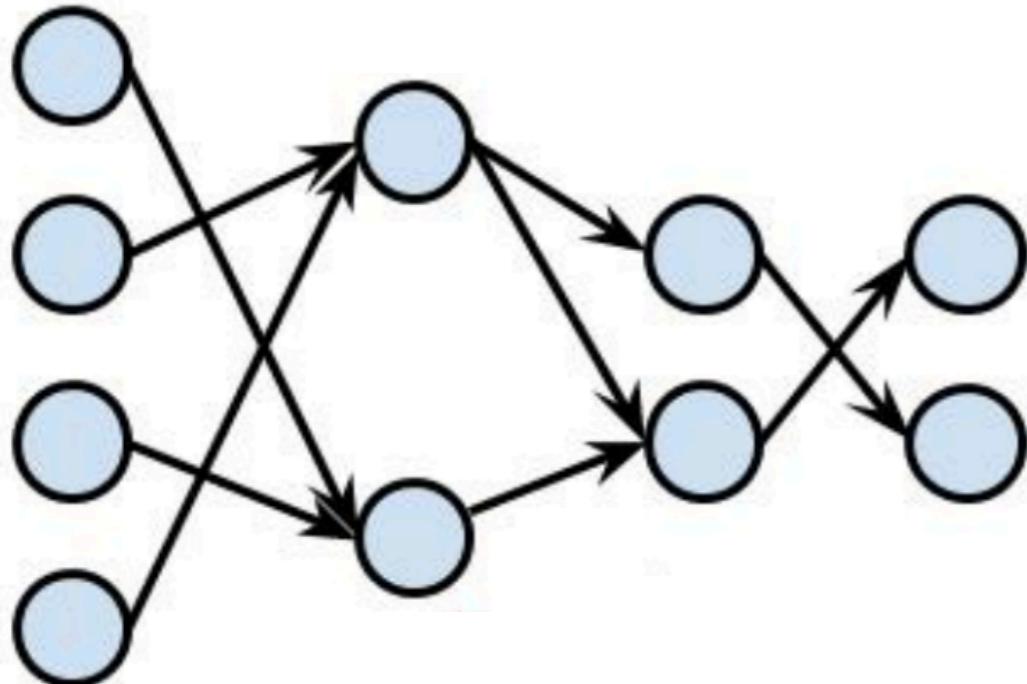
Extended form based on Vanilla, multiple layers with multiple hidden layers;

- **Convolutional Autoencoder**

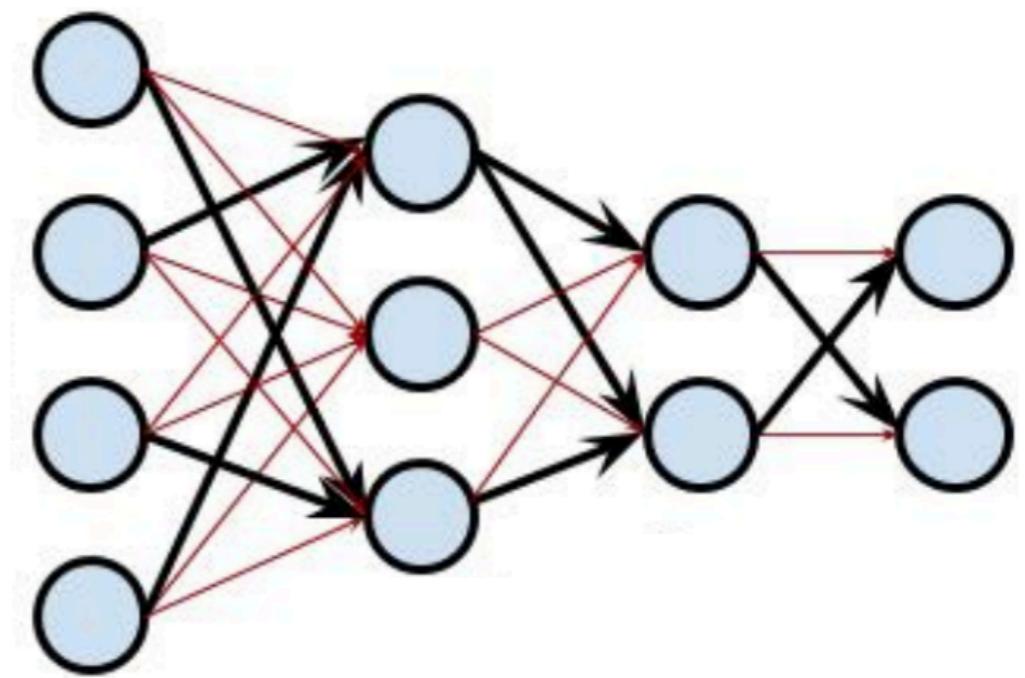
Using pooling layers and convolution instead of fully connected layers;

Types: Regularized (Sparse) Autoencoder

- Sparse representation:



Sparse autoencoder



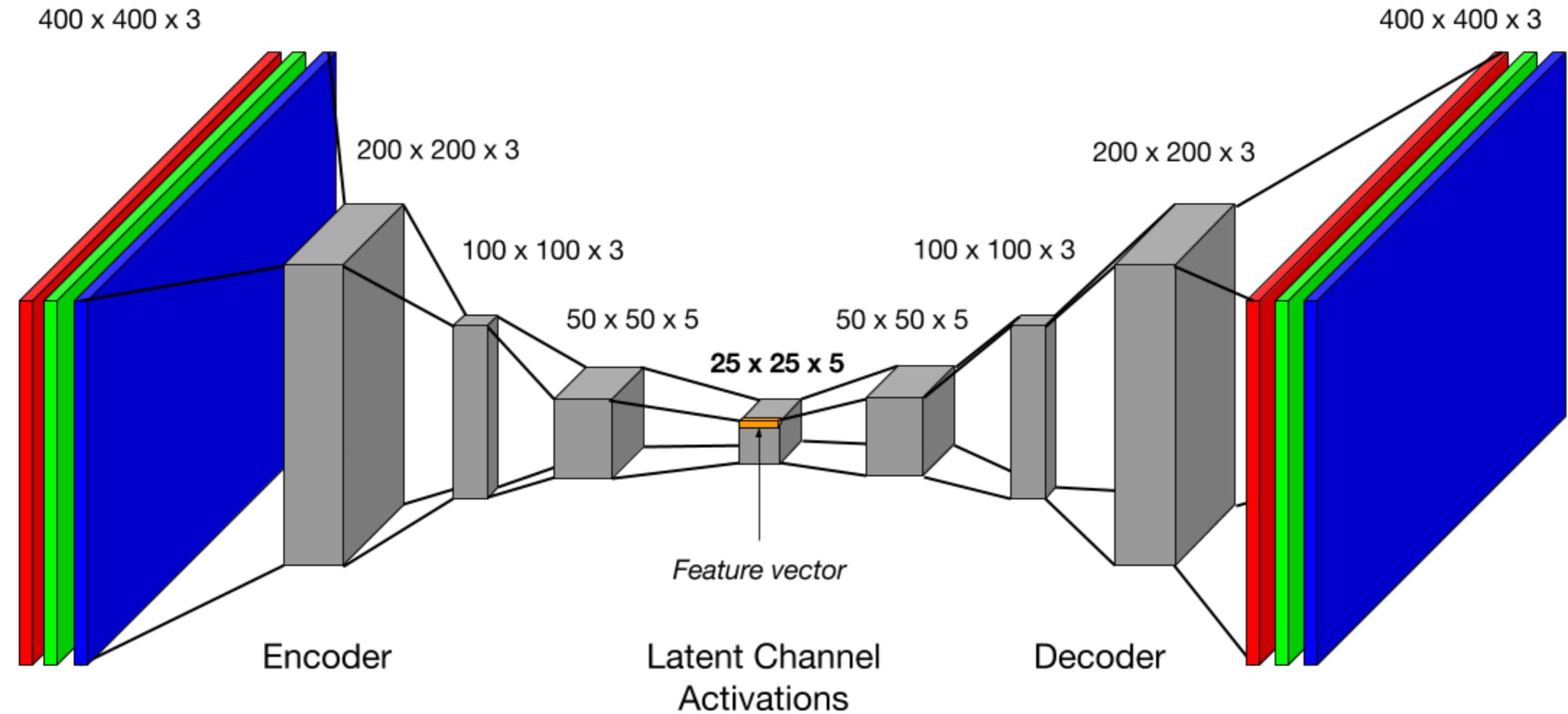
Fully-connected autoencoder

- Optimization and Loss function (**Penalty term**):

$$f = \operatorname{argmin}(\|X - (w'x + b)\|^2 + \lambda \|(w'x + b)\|)$$

Types: Convolutional Autoencoder

- Structure

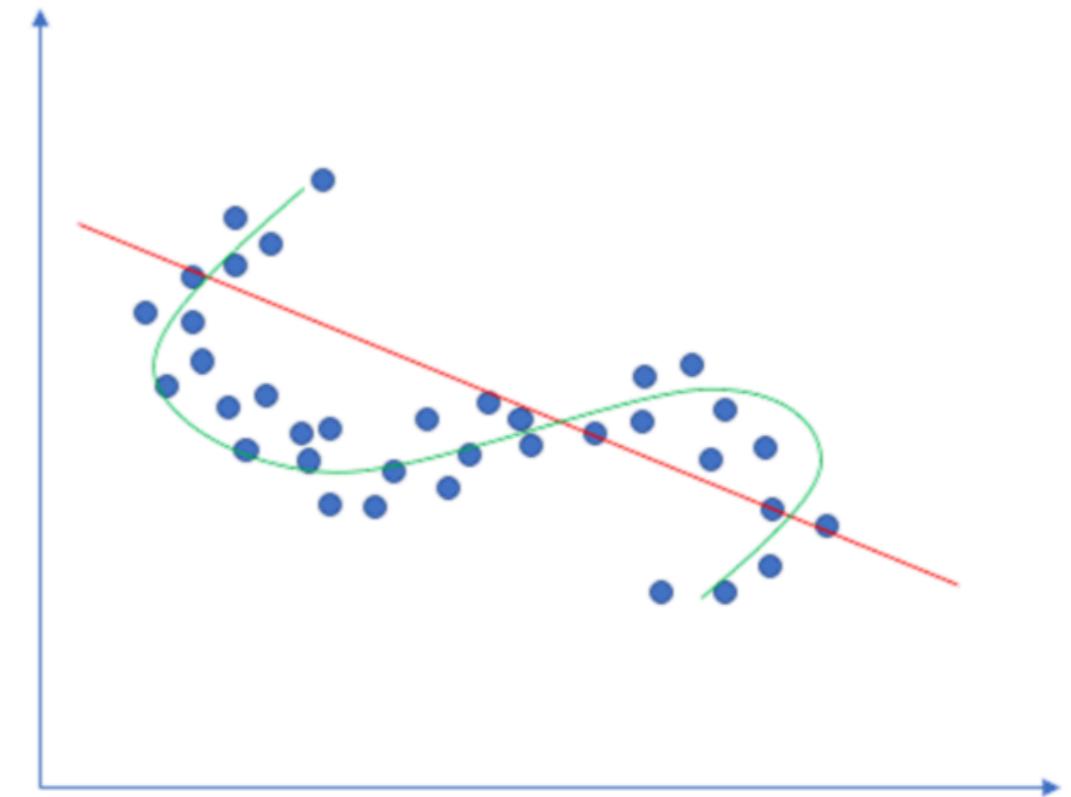


- Same operations with convolutional neuron network(CNN).
- More advanced autoencoders: Variational Autoencoder

Advantages: Autoencoder

- Producing pre-trained layers for another model; (**clean**)
- Doesn't have to learn dense layers; (**cost**)
- An autoencoder can **capture** non-linear features/patterns;

Difference between
PCA and AE?



PCA vs AE