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# **Machine Learning Problem Sets (Problem Set 2)**

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## Contents

<b>1</b>	<b>Gradient Descent</b>	<b>3</b>
<b>2</b>	<b>Minimizer in Linear Regression (Bonus)</b>	<b>4</b>

## 1 Gradient Descent

Write a program that uses the gradient descent algorithm to find the best values of parameters  $a$  and  $b$  in a linear regression model. Evaluate your program with some test case.

**Note:** Be sure to leave appropriate comments for different parts of your code. A part of your score is allocated to your comments and explanations.

## 2 Minimizer in Linear Regression (Bonus)

Show that the minimizer for least-squares linear regression with  $L_2$  regularization is  $\mathbf{w} = (\lambda \mathbf{I} + \Phi^T \Phi)^{-1} \Phi^T \mathbf{t}$ .

**Note:** To solve this question, you can use chapter 3 of the Pattern Recognition and Machine Learning (Bishop) book.