## A6

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#### R. Markdown

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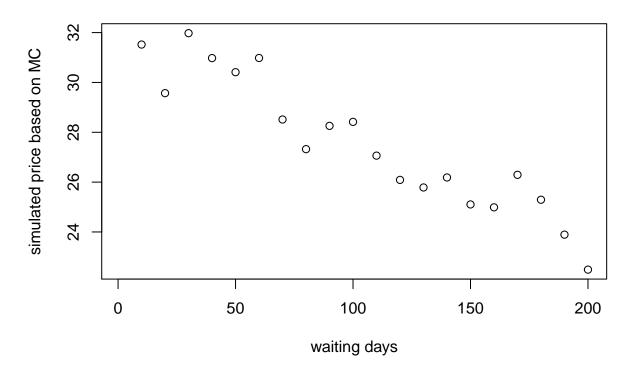
When you click the **Knit** button a document will be generated that includes both content as well as the output of any embedded R code chunks within the document. You can embed an R code chunk like this:

```
# 1.a fixed strike look_back option -----
S0=100; dt=1/252; T=1; Path Length=round(T/dt, 0);
r=0.05;
E=rnorm(Path_Length,0,1)
sigma=0.3
strike=95
S= matrix(NA, Path_Length+1,1);
S[1] = S0;
for (j in 1 : Path_Length) { # length of path
 S[j+1] = S[j] + r*S[j]* dt + sigma *S[j]*sqrt(dt)* E[j]
}
S=(S[100:length(S)]);
payoff = max(S)-strike;
MC_Lookback_Fix = function(Type, S0,strike, r, sigma, expire_days, n, m){
  # Type: Put or Call
  # SO: Spot price
  # strike is the predetermined strike price
  # r : interest rate
  # sigma: volatility
  # n: discrete steps frequency
  # m: number of simulations
  dt = 1/n# usually there are 252 trading days
  Path_Length = expire_days # how many days left before expiry it is integer
                    # initialize the sum of payoffs that you will collect over simulated scenarios
  payoff sum = 0
  for (i in 1:m){
```

```
S= matrix(NA, Path_Length,1)
    S[1] = S0
    E=rnorm(Path_Length,0,1)# generate random noise
    for (j in 1 : Path_Length) { # length of path
     S[j+1] = S[j] + r*S[j]* dt + sigma *S[j]*sqrt(dt)* E[j]
    }
    if (Type == "c" ){ payoff = max(S)-strike } # Call
    else if (Type == "p" ){ payoff = strike - min(S) } # Put
    payoff_sum = payoff_sum + payoff # Accumulate the payoffs from all simulated scenarios.
  OptionValue = (payoff_sum * exp(-r*(expire_days/n)))/m
  return(OptionValue)
}
#try to calculate this kind of call option with expiry days of 125 tradings days
MC Lookback Fix("c",100,95,0.05,0.3,125,252,100)
## [1] 21.06741
# 1.b fixed stike look_vack option with time window ------
#we can modify the standard fixed strike lookback option by adding a time window slice of the S path
MC Lookback Fix Partial = function(Type, SO, strike, r, sigma, expire days, waiting days, n, m){
  # Type: Put or Call
  # SO: Spot price
  # strike is the predetermined strike price
  \# r : interest rate
  # sigma: volatility
  # expire_days is how long this option lasts
  # waiting_days is how many days should be waiting before this option really starts
  # n: discrete steps frequency
  # m: number of simulations
  dt = 1/n# usually there are 252 trading days
  Path_Length = expire_days # how many days left before expiry it is integer
  payoff_sum = 0
                 # initialize the sum of payoffs that you will collect over simulated scenarios
  for (i in 1:m){
    S= matrix(NA, Path Length+1,1)
    S[1] = S0
    E=rnorm(Path_Length,0,1)# generate random noise
```

```
for (j in 1 : Path_Length) { # length of path
     S[j+1] = S[j] + r*S[j]* dt + sigma *S[j]*sqrt(dt)* E[j]
   }
   #slice the S
   S = S[(waiting_days+1):length(S)]
    #after slicing there exist the possibility that max(s)-strike is negative
    #add the max(0,payoff) to constrain the payoff to be positive
   if (Type == "c"){ payoff = max(0,(max(S)-strike)) } # Call
   else if (Type == "p" ){ payoff = max(0,(strike - min(S))) } # Put
   payoff_sum = payoff_sum + payoff # Accumulate the payoffs from all simulated scenarios.
  OptionValue = (payoff_sum * exp(-r*(expire_days/n)))/m
  return(OptionValue)
}
MC_Lookback_Fix_Partial("c",100,95,0.05,0.3,125,100,252,10000)
## [1] 16.63625
# show how The partial-time fixed strike lookback option is cheaper than a similar standard fixed strik
b=seq(0,200,by = 10);
length(b);
## [1] 21
#when waiting time is 0 it is equivalent to previous function
Record=matrix(NA,length(b),1)
# when set the simulation number to be 100, we can still see some fluctuation
# setting simulation number to be more than 1000, we can see a generally monetone declining line with f
for (i in seq(0,200,by = 10)){
  Record[i]=MC_Lookback_Fix_Partial("c",100,95,0.05,0.3,252,i,252,1000)
plot(Record, main="how waiting days before the call option really goes in count affects the MC simulated
    xlab="waiting days",ylab="simulated price based on MC")
```

# lys before the call option really goes in count affects the MC simulated



```
MC_Lookback_Fix("c",100,95,0.05,0.3,252,252,1000)
## [1] 30.71263
library(quantmod)
## Loading required package: xts
## Loading required package: zoo
##
## Attaching package: 'zoo'
## The following objects are masked from 'package:base':
##
       as.Date, as.Date.numeric
##
## Loading required package: TTR
## Registered S3 method overwritten by 'quantmod':
##
     method
     as.zoo.data.frame zoo
##
## Version 0.4-0 included new data defaults. See ?getSymbols.
```

```
# qet data
ticker_list = c("^VIX","TSLA")
stock_prices <- NULL
for (ticker in ticker_list){
 stock_prices <- cbind(stock_prices, getSymbols.yahoo(ticker,</pre>
                                                     from = '2020-10-14', periodicity= 'daily', auto.
}
stock_prices$VIX.Close[1];
             VIX.Close
## 2020-10-14
                  26.4
stock_prices$TSLA_IV = NA;
df=stock_prices;
# use the previous IV data as initials
       -0.37% 59.05 59.28 59.5 58.55 8.1 16.06% 176 974 74.24%
#460
df[1,"TSLA_IV"] = 74.24;
# 7 locates the OCT 22
for (i in 2:7){
 df[i,"TSLA_IV"] = as.numeric(df[i-1,"TSLA_IV"])*0.95/2+as.numeric(df[i,"VIX.Close"])*2.9/2+10*rnorm(
}
df;
             VIX.Close TSLA.Close TSLA_IV
## 2020-10-14 26.40 461.30 74.24000
## 2020-10-15
                26.97
                         448.88 80.97253
## 2020-10-16
                27.41
                        439.67 68.02964
                       430.83 80.33019
             29.18
## 2020-10-19
## 2020-10-20 29.35 421.94 59.54658
## 2020-10-21
               28.65
                       422.64 67.65784
                        425.79 88.37345
## 2020-10-22
                 28.11
## 2020-10-23
             27.55
                         420.63
                                       NA
## 2020-10-26
                 32.46
                         420.28
                                       NA
## 2020-10-27
                 33.35
                           424.68
                                       NA
# 100 contract covers 100*100 shares of stock
library(fOptions)
## Loading required package: timeDate
## Loading required package: timeSeries
## Attaching package: 'timeSeries'
```

```
## The following object is masked from 'package:zoo':
##
##
       time<-
## Loading required package: fBasics
##
## Attaching package: 'fBasics'
## The following object is masked from 'package:TTR':
##
##
       volatility
delta1=GBSCharacteristics(TypeFlag = "c",S=461.7,X=460,Time = 65/365,r = 0.008,b=0.008,sigma = 0.7424)$
# holding the call option is a kind of long delta strategy
# generally we should sell some underlying asset to make the whole portfolio delta hedged
#for the fisrt day of 14th OCT
call_delta = 100*delta1*100;
stock_position = -call_delta;
# call_delta is also the number of share we need to short sell to make the whole portfolio delta neutra
df$TSLA_position=NA;
              VIX.Close TSLA.Close TSLA_IV TSLA_position
                            461.30 74.24000
## 2020-10-14
                 26.40
                                                       NA
                 26.97
                           448.88 80.97253
## 2020-10-15
                                                       NA
## 2020-10-16
              27.41
                           439.67 68.02964
                                                       NA
## 2020-10-19
              29.18
                        430.83 80.33019
                                                       NA
## 2020-10-20
                29.35
                           421.94 59.54658
                                                       NA
## 2020-10-21
                28.65
                           422.64 67.65784
                                                       NA
## 2020-10-22
              28.11
                        425.79 88.37345
                                                       NA
## 2020-10-23
                 27.55
                         420.63
                                        NA
                                                       NA
## 2020-10-26
                 32.46
                           420.28
                                        NA
                                                       NA
## 2020-10-27
                 33.35
                           424.68
                                        NA
                                                       NA
for (i in 1:7){
  S1=as.numeric(df[i,"TSLA.Close"])
  sigma1 = as.numeric(df[i,"TSLA_IV"])
  delta1=GBSCharacteristics(TypeFlag = "c",S=S1,X=460,Time = ((66-i)/365),r = 0.008,b=0.008,sigma = sigma
  df[i,"TSLA_position"] = -100*delta1*100;
}
df;
              VIX.Close TSLA.Close TSLA_IV TSLA_position
## 2020-10-14
                  26.40
                            461.30 74.24000
                                                -5675.739
## 2020-10-15
                  26.97
                            448.88 80.97253
                                                -5404.221
## 2020-10-16
                 27.41
                           439.67 68.02964
                                               -4945.225
```

```
## 2020-10-19
                 29.18
                            430.83 80.33019
                                                -4887.369
## 2020-10-20 29.35
                           421.94 59.54658
                                                -4099.910
## 2020-10-21
                 28.65
                           422.64 67.65784
                                                -4337.477
## 2020-10-22
                 28.11
                            425.79 88.37345
                                                -4855.567
## 2020-10-23
                 27.55
                           420.63
                                         NA
                                                       NA
## 2020-10-26
                 32.46
                           420.28
                                         NA
                                                       NA
## 2020-10-27
                 33.35
                           424.68
                                         NA
                                                       NA
#generate daily position change
df$position_change=NA;
df$position_change[1]=df$TSLA_position[1];
for (i in 2:7){
 df$position_change[i]=as.numeric(df$TSLA_position[i])-as.numeric(df$TSLA_position[i-1]);
df$position_change;
              position_change
## 2020-10-14
                 -5675.73902
## 2020-10-15
                    271.51825
## 2020-10-16
                   458.99553
## 2020-10-19
                    57.85586
## 2020-10-20
                   787.45988
## 2020-10-21
                  -237.56753
## 2020-10-22
                   -518.08996
## 2020-10-23
                           NA
## 2020-10-26
                           NA
## 2020-10-27
                           NA
#this vector shows the daily position change of TSLA stock to make the whole portfolio risk neutral
#short the stock can get cash inflow and buy the stock will cause cash outflow
CF=as.vector(df$position_change*df$TSLA.Close*(-1));
CF=CF[1:7];
sum(CF);
## [1] 2258349
cat("the delta hedged strategy generates the total cash inflow of ",sum(CF),"\n")
## the delta hedged strategy generates the total cash inflow of 2258349
Cost_to_buyback=-df$TSLA_position[7]*-df$TSLA.Close[7]
cat("the whole portfolio still shorts the ",-df$TSLA_position[7], "shares of TSLA and they worths",-df$T
## the whole portfolio still shorts the 4855.567 shares of TSLA and they worths -2067452
cat("the money makes from the short selling stock parts",as.numeric(sum(CF)+Cost_to_buyback),"theoritic
```

## the money makes from the short selling stock parts 190897 theoritically it should equals the money 1

cat("each call option predicted to lose",as.numeric(sum(CF)+Cost\_to\_buyback)/10000,"\n")

## each call option predicted to lose 19.0897

#theoritically it should equals the money loses on the price of call option