



# education

Department:  
Education  
**REPUBLIC OF SOUTH AFRICA**

## **NATIONAL SENIOR CERTIFICATE**

### **GRADE 12**

### **MATHEMATICS P2**

### **NOVEMBER 2009(1)**

### **MEMORANDUM**

**MARKS: 150**

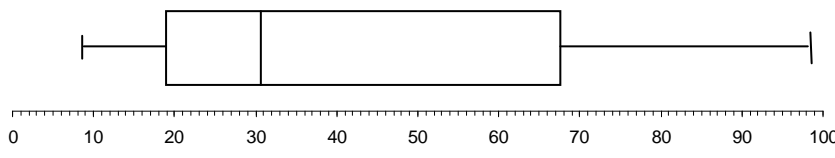
**This memorandum consists of 25 pages.**

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- If a candidate does a question twice and does not delete either, mark the FIRST attempt.
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**QUESTION 1**

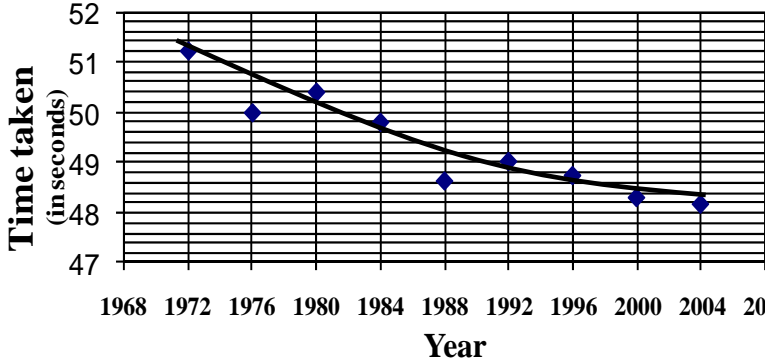
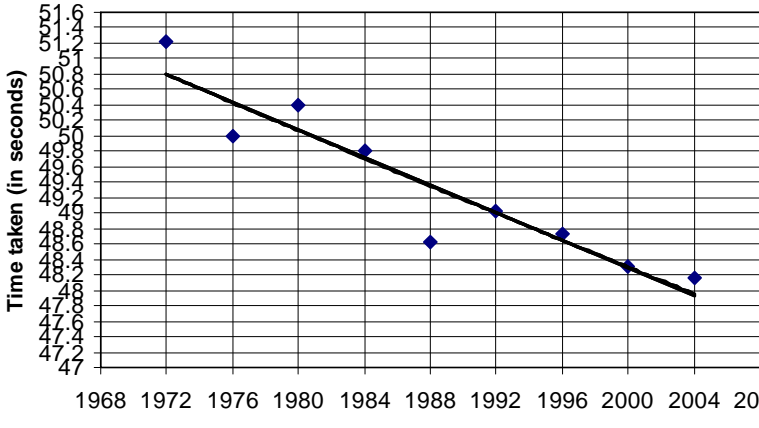
1.1	$\text{Mean} = \frac{522,5}{12} = 43,5$ <b>ANSWER ONLY:</b> Full marks	✓ 522,5 ✓ answer (2)  No penalty for Rounding: Accept 43,54 ; 44
1.2	Ordered Data 9,3    14,9    15    23,6    26,1    28    32,5    60,9 65,7    71,9    76,4    98,2  $\text{Median} = \frac{28 + 32,5}{2} = 30,3$ $\text{Lower quartile} = \frac{15 + 23,6}{2} = 19,3$ $\text{Upper quartile} = \frac{65,7 + 71,9}{2} = 68,8$  The five number summary is (9,3 ; 19,3 ; 30,25 ; 68,8 ; 98,2) OR If they use the formula: Ordered Data 9,3    14,9    15    23,6    26,1    28    32,5    60,9 65,7    71,9    76,4    98,2  $P_{50} = \frac{12 + 1}{2} = 6,5$ Position of median: $\therefore Q_2 = \frac{28 + 32,5}{2} = 30,3$  $\text{Position of lower quartile: } P_{25} = \frac{13}{4}$ $\therefore Q_1 = 15 + (0,25(23,6 - 15)) = 17,15$  Position of upper quartile: $P_{75} = 0,75(13) = 9,75$ $\therefore Q_3 = 65,7 + (0,75(71,9 - 65,7)) = 70,35$ Min = 9,3 Max = 98,2  Accept any one of these five number summaries: (9,3 ; 19,3 ; 30,3 ; 68,8 ; 98,2) (9,3 ; 15 ; 30,3 ; 71,9 ; 98,2) (9,3 ; 17,2 ; 30,3 ; 70,4 ; 98,2)	✓ 9,3  ✓ 19,3 ✓ 30,3 ✓ 68,8  ✓ 98,2 (5)  If indicated on the box and whisker diagram in 1.3 – 5 marks

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1.3	 <p>Note: If just a box and whisker without any reference to the numbers: 1/3</p>	<ul style="list-style-type: none"> <li>✓ minimum and maximum values</li> <li>✓ quartiles and median</li> <li>✓ whiskers with median line</li> </ul> <p>(3)</p>																																										
1.4	<p>The data is skewed to the right (positively skewed). This suggests that there was a large difference between the median and the maximum rainfall (some months had exceptionally high rainfall in that year).</p> <p><i>Die data is skeef na regs (positief skeef)</i> <i>Dit dui daarop dat daar 'n groot verskil is tussen die mediaan en die maksimum reënval (sommige maande het ongewoon hoë reënval gehad gedurende die jaar).</i></p>	<ul style="list-style-type: none"> <li>✓ ✓ comment about rainfall.</li> </ul> <p>(2)</p> <p>Note: Skewed to right 1/2</p> <ul style="list-style-type: none"> <li>✓ ✓ verwysing na reënval</li> </ul> <p>(2)</p>																																										
1.5	<p>By using the calculator, <math>\sigma = 28,19</math>. (28,19058256)</p> <p><b>OR Pen and Paper method (not recommended)</b> Mean = 43,54 (43,54166667)</p> <table border="1"> <thead> <tr> <th><math>x</math></th> <th><math>x - \bar{x}</math></th> <th><math>(x - \bar{x})^2</math></th> </tr> </thead> <tbody> <tr><td>60,9</td><td>17,36</td><td>301,3696</td></tr> <tr><td>14,9</td><td>-28,64</td><td>820,2496</td></tr> <tr><td>9,3</td><td>-34,24</td><td>1172,378</td></tr> <tr><td>28,0</td><td>-15,54</td><td>241,4916</td></tr> <tr><td>71,9</td><td>28,36</td><td>804,2896</td></tr> <tr><td>76,4</td><td>32,86</td><td>1079,78</td></tr> <tr><td>98,2</td><td>54,66</td><td>2987,716</td></tr> <tr><td>65,7</td><td>22,16</td><td>491,0656</td></tr> <tr><td>26,1</td><td>-17,44</td><td>304,1536</td></tr> <tr><td>32,5</td><td>-11,04</td><td>121,8816</td></tr> <tr><td>23,6</td><td>-19,94</td><td>397,6036</td></tr> <tr><td>15,0</td><td>-28,54</td><td>814,5316</td></tr> <tr> <td>Sum</td> <td></td> <td>9536,509</td> </tr> </tbody> </table> <p><math>\sigma = \sqrt{\frac{9536,509}{12}} = 28,19</math> (28,19059.....)</p>	$x$	$x - \bar{x}$	$(x - \bar{x})^2$	60,9	17,36	301,3696	14,9	-28,64	820,2496	9,3	-34,24	1172,378	28,0	-15,54	241,4916	71,9	28,36	804,2896	76,4	32,86	1079,78	98,2	54,66	2987,716	65,7	22,16	491,0656	26,1	-17,44	304,1536	32,5	-11,04	121,8816	23,6	-19,94	397,6036	15,0	-28,54	814,5316	Sum		9536,509	<ul style="list-style-type: none"> <li>✓✓✓ answer</li> </ul> <p>Accept: 28 ; 28,2 ; 28,1</p> <p>(3)</p> <ul style="list-style-type: none"> <li>✓ headings correct</li> <li>✓ sum of the squares of the mean deviations</li> </ul> <ul style="list-style-type: none"> <li>✓ answer</li> </ul> <p>(3)</p> <p>[15]</p>
$x$	$x - \bar{x}$	$(x - \bar{x})^2$																																										
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**QUESTION 2**

2.1	Linear or Exponential	✓ answer (1)																																								
2.2	<div><div><p>Scatter plot of times taken by winners of men's 100 m freestyle at Olympic Games</p><table border="1"><caption>Data points for men's 100 m freestyle</caption><thead><tr><th>Year</th><th>Time (seconds)</th></tr></thead><tbody><tr><td>1972</td><td>51.2</td></tr><tr><td>1976</td><td>50.0</td></tr><tr><td>1980</td><td>50.4</td></tr><tr><td>1984</td><td>49.8</td></tr><tr><td>1988</td><td>48.6</td></tr><tr><td>1992</td><td>49.0</td></tr><tr><td>1996</td><td>48.8</td></tr><tr><td>2000</td><td>48.3</td></tr><tr><td>2004</td><td>48.2</td></tr></tbody></table></div><div><p>Scatter Plot of time taken by the winner of 100m Freestyle at Olympic Games</p><table border="1"><caption>Data points for 100m Freestyle</caption><thead><tr><th>Year</th><th>Time (seconds)</th></tr></thead><tbody><tr><td>1972</td><td>50.8</td></tr><tr><td>1976</td><td>49.4</td></tr><tr><td>1980</td><td>49.8</td></tr><tr><td>1984</td><td>49.1</td></tr><tr><td>1988</td><td>48.1</td></tr><tr><td>1992</td><td>48.6</td></tr><tr><td>1996</td><td>48.3</td></tr><tr><td>2000</td><td>47.9</td></tr><tr><td>2004</td><td>47.7</td></tr></tbody></table></div></div> <p>For this set of data we will accept the straight line.</p>	Year	Time (seconds)	1972	51.2	1976	50.0	1980	50.4	1984	49.8	1988	48.6	1992	49.0	1996	48.8	2000	48.3	2004	48.2	Year	Time (seconds)	1972	50.8	1976	49.4	1980	49.8	1984	49.1	1988	48.1	1992	48.6	1996	48.3	2000	47.9	2004	47.7	✓ ✓line of best fit (2)
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2.3	<p>The scatter plot shows an overall decrease in the time taken by the winner since 1972.</p> <p><i>Die spreidiagram dui 'n algehele afname in tye aangeteken deur die wenners vanaf 1972.</i></p> <p>OR</p> <p>Times are faster. <i>Tye is vinniger.</i></p> <p>OR</p> <p>Negative correlation between year and time.</p> <p><i>Negatiewe korrelasie tussen jaar en tyd.</i></p>	<p>✓ decrease/afname (1)</p>
2.4	<p>The top athletes of the world have turned professional. This allows them to train at the best facilities and receive the best coaching available.</p> <p>Also, equipment manufacturers are in competition with each other. In this case, manufacturers are designing swimsuits that assist swimmers</p> <p>Swimmers train harder and put in more effort.</p> <p><i>Die top atlete van die wêreld het professionele atlete geword. Dit laat hulle toe om by die beste fasiliteite te oefen en die beste afrigting te ontvang.</i></p> <p><i>Vervaardigers van voorraad is in kompetisie met mekaar. Hul ontwerp dus swembroeke wat die swemmers help.</i></p> <p><i>Swemmers oefen harder en gebruik meer tyd om te oefen.</i></p>	<p>✓ any acceptable reason relating to the trend (1)</p> <p>✓ enige aanvaarbare rede wat verband hou met die neiging. (1)</p>
2.5	<p>In the context of the times around these two observations, one can consider the efforts of 1976 and 1988 to be outliers. This shows that these athletes were exceptionally good swimmers at the time.</p> <p><i>Binne die konteks van tye gedurende hierdie twee waarnemings, kan die poging van 1976 and 1988 gesien word as uitskieters. Dit dui daarop dat hierdie atlete uitstekende swemmers was daardie tyd.</i></p>	<p>✓✓ acceptable reason in context (2)</p> <p>✓✓ aanvaarbare rede binne die konteks (2)</p>
2.6	<p>Winning time of 2008 is expected to be about 47,6 seconds.</p> <p>Accept answer from candidate's graph.</p>	<p>✓ answer from graph (1)</p> <p><b>[8]</b></p>

### QUESTION 3

3.1	50	<p>✓ answer (1)</p>
3.2	<p>Cut-off mark of 56% (37 students) or 58% (38 students)</p> <p>Accept interval: 55% - 60%</p>	<p>✓ answer read off from ogive (1)</p>

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3.3			

Marks (out of 100)	Frequency ( $f$ )
$0 \leq \text{marks} < 10$	1
$10 \leq \text{marks} < 20$	3
$20 \leq \text{marks} < 30$	4
$30 \leq \text{marks} < 40$	11
$40 \leq \text{marks} < 50$	12
$50 \leq \text{marks} < 60$	9
$60 \leq \text{marks} < 70$	5
$70 \leq \text{marks} < 80$	4
$80 \leq \text{marks} < 90$	1
$90 \leq \text{marks} < 100$	0

✓ class intervals  
 Accept  
 $0 - 10$  ;  $10 - 20$   
 Or  
 $0 < \text{marks} \leq 10$   
 Or  
 Between 0 and 10  
 Or  
 From 0 to 10  
  
 If the intervals not in  
 tens, the mark for  
 intervals not given  
  
 ✓ method  
 ✓ accuracy of five  
 answers  
  
 (3)  
**[5]**

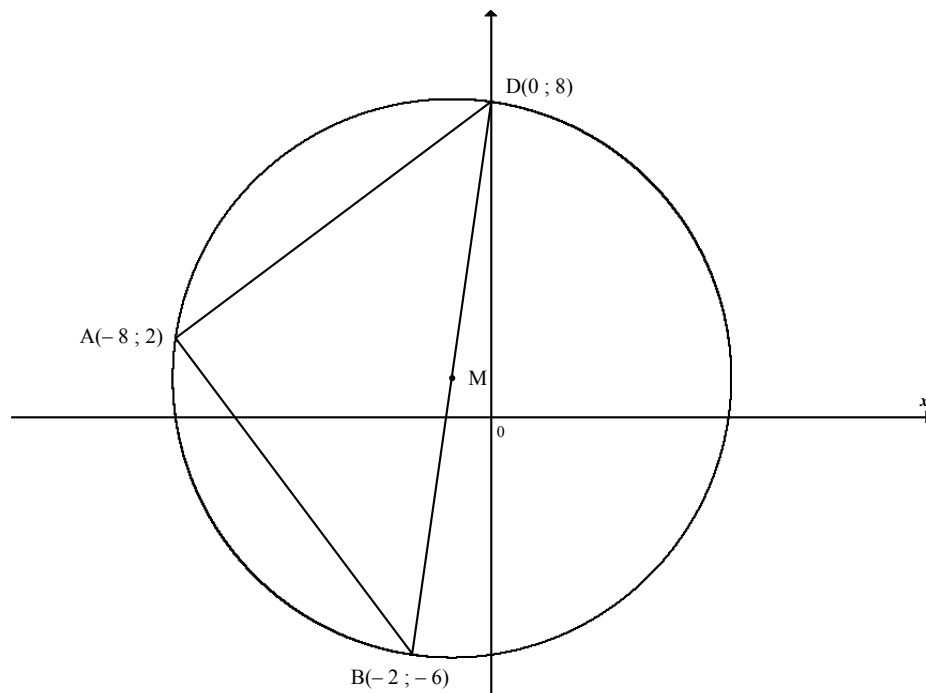
**QUESTION 4**

4.1	$\tan 45^\circ = m_{AB}$ $= 1$ OR $m_{AB} = \frac{3-0}{1-t} = \frac{3}{1-t}$	✓ $\tan 45^\circ$ ✓ answer  Answer only: full marks  (2)
4.2	$\frac{3-0}{1-t} = \tan 45^\circ = 1$ $1-t = 3$ $t = -2$ OR $y = mx + c$ $3 = (1)(1) + c$ $c = 2$ $y = x + 2$ $(t; 0) \text{ in } y = mx + 2$ $0 = t + 2$ $t = -2$	✓ equating  ✓ value   ✓ $c=2$   ✓ value  Answer only: full marks  (2)

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4.3	$\sqrt{(1-p)^2 + (3+4)^2} = \sqrt{50}$ $(1-p)^2 + (3+4)^2 = 50$ $1 - 2p + p^2 + 49 = 50$ $p^2 - 2p = 0$ $p(p-2) = 0$ $p \neq 0 \text{ or } p = 2$ <p>OR</p> $(1-p)^2 + (3+4)^2 = 50$ $(1-p)^2 = 50 - 49$ $(1-p)^2 = 1$ $1-p = 1 \text{ or } 1-p = -1$ $p \neq 0 \text{ or } p = 2$ <p>OR</p> <p>Let <math>p = 2</math></p> $AC = \sqrt{(1-2)^2 + (3+4)^2}$ $= \sqrt{1+49}$ $= \sqrt{50}$ <p>which is true</p> <p><math>\therefore p = 2</math></p>	<p>✓ substitution into distance formula</p> <p>✓ expansion</p> <p>✓ factors</p> <p>✓ answer</p> <p>Note: If an answer was not chosen: 3/4</p> <p>(4)</p> <p>✓ substitution into distance formula</p> <p>✓ expansion</p> <p>✓ factors</p> <p>✓ answer</p> <p>(4)</p> <p>If gradient of BC assumed as -1 and p calculated correctly: 0/4</p> <p>Answer only: 1/4</p> <p>✓ substitution into distance formula</p> <p>✓ <math>\sqrt{50}</math></p> <p>✓ which is true(justification)</p> <p>✓ answer</p> <p>(4)</p> <p>If equating to <math>\sqrt{50}</math> from the start, then 3/4</p>
4.4	<p>midpoint of BC = <math>\left(\frac{-2+2}{2}; \frac{0-4}{2}\right)</math></p> <p>midpoint of BC = <math>(0; -2)</math></p>	<p>✓ x-value (<math>x = \frac{t+p}{2}</math>)</p> <p>✓ y-value</p> <p>(2)</p>
4.5	<p>Gradient of line = <math>m_{AB} = 1</math></p> <p>Equation of line is: <math>y + 4 = 1(x - 2)</math></p> $y = x - 6$ <p>OR</p> $y = mx + c$ $y = x - p - 4$	<p>✓ gradients are equal</p> <p>✓ substitution of <math>(p; -4)</math></p> <p>✓ equation in any form</p> <p>(3)</p> <p><b>[13]</b></p>

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**QUESTION 5**

5.1	Midpoint BD $\left(\frac{0-2}{2}; \frac{8-6}{2}\right)$ $= (-1; 1)$	✓ x-coordinate ✓ y-coordinate (2)
5.2	$y = 7(-8) + 58$ $= 2$ $\therefore A$ lies on the line.	✓ substitution (1) Substitute both at the same time with justification (1)
5.3	The line $y = 7x + 58$ is a tangent to the circle at A.  $m_{line} = 7$ $m_{AM} = \frac{2-1}{-8-(-1)} = -\frac{1}{7}$ $m_{line} \times m_{AM} = 7 \times -\frac{1}{7} = -1$ $\therefore AM \perp$ to the line  OR	✓ relationship  $\checkmark \checkmark m_{AM} = \frac{2-1}{-8-(-1)} = -\frac{1}{7}$ $\checkmark m_{line} = 7$  ✓ product (5)

NOTE:

$m_{line} = 7$  and CA gradient  
of AM then no  
relationship: 4/5



## NSC – Memorandum

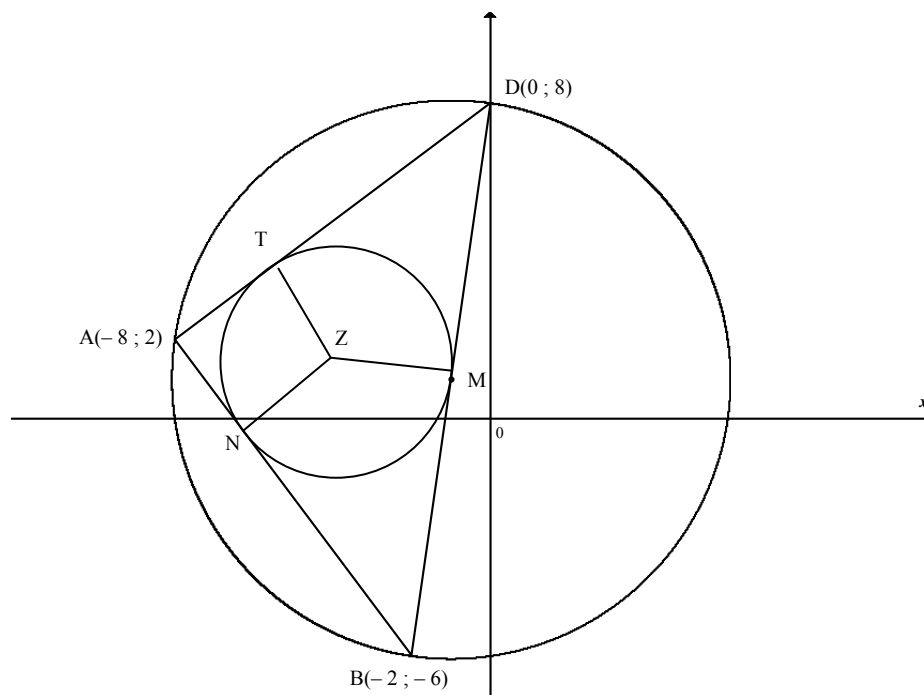
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5.3 contd	<p><b>OR</b></p> $m_{BD} = 7$ $m_{line} = 7$ $\therefore \text{line} \parallel \text{diameter}$ <p><b>OR</b></p> $(x+1)^2 + (y-1)^2 = 50$ $x^2 + 2x + 1 + y^2 - 2y + 1 = 50$ $x^2 + 2x + 1 + (7x + 58)^2 - 2(7x + 58) + 1 = 50$ $x^2 + 2x + 1 + 49x^2 + 812x + 3364 - 14x - 116 + 1 = 50$ $50x^2 + 800x + 3200 = 0$ $x^2 + 16x + 64 = 0$ $(x+8)^2 = 0$ $x = -8$ $y = 2$ $y = 7x + 58 \text{ is a tangent to the circle}$	$\checkmark\checkmark m_{BD} = 7$ $\checkmark m_{line} = 7$ $\checkmark\checkmark \text{conclusion} \quad (5)$ <p>Note: Only lines parallel 4/5</p> $\checkmark \text{ circle equation}$ $\checkmark \text{substitution of } y = 7x + 58$ $\checkmark \text{standard form}$ $\checkmark \text{ answer}$ $\checkmark \text{ tangent} \quad (5)$
5.4	$AD = \sqrt{(8-2)^2 + (0+8)^2}$ $= \sqrt{36+64}$ $= 10$ $AB = \sqrt{(2+6)^2 + (-8+2)^2}$ $= \sqrt{64+36}$ $= 10$	$\checkmark \text{ substitution}$ $\checkmark \text{ answer}$ $\checkmark \text{ substitution}$ $\checkmark \text{ answer} \quad (4)$ <p>Note: Answers <math>\sqrt{10}</math> then 3/4</p>

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5.5	$m_{AD} = \frac{8 - (2)}{0 - (-8)}$ $m_{AD} = \frac{3}{4}$ $m_{AB} = \frac{2 - (-6)}{-8 - (-2)}$ $= -\frac{4}{3}$ $m_{AB} \cdot m_{AD} = -\frac{4}{3} \times \frac{3}{4}$ $= -1$ $\hat{DAB} = 90^\circ$ <p><b>OR</b></p> $BD^2 = (8 + 6)^2 + (0 + 2)^2$ $= 200$ $= AD^2 + AB^2$ $\therefore \hat{DAB} = 90^\circ$ <p><b>OR</b></p> $a^2 = b^2 + d^2 - 2(b)(d)\cos A$ $200 = 100 + 100 - 2(10)(10)\cos A$ $0 = -200\cos A$ $A = 90^\circ$ <p><b>OR</b></p> $(AD)^2 = 100$ $(AB)^2 = 100$ $BD^2 = (-2 - 0)^2 + (-6 - 8)^2$ $= 4 + 196$ $= 200$ $\therefore BD^2 = AD^2 + AB^2$ $\therefore \hat{DAB} = 90^\circ \quad (\text{Pyth})$ <p><b>OR</b></p> $\hat{A} = 90^\circ \quad (\text{angles in semi - circle})$	<p>✓ gradient of AD</p> <p>✓ gradient of AB</p> <p>✓ PRODUCT (3)</p> <p>✓ distance formula</p> <p>✓ Pythagoras ✓ conclusion (3)</p> <p>✓ cos rule ✓ substitution ✓ conclusion (3)</p> <p>✓ <math>BD^2 = 200</math></p> <p>✓ <math>BD^2 = AD^2 + AB^2</math> ✓ conclusion (3)</p> <p>✓ ✓ ✓ reason (3)</p>
5.6	$\theta = 45^\circ$	<p>✓ answer (1)</p>

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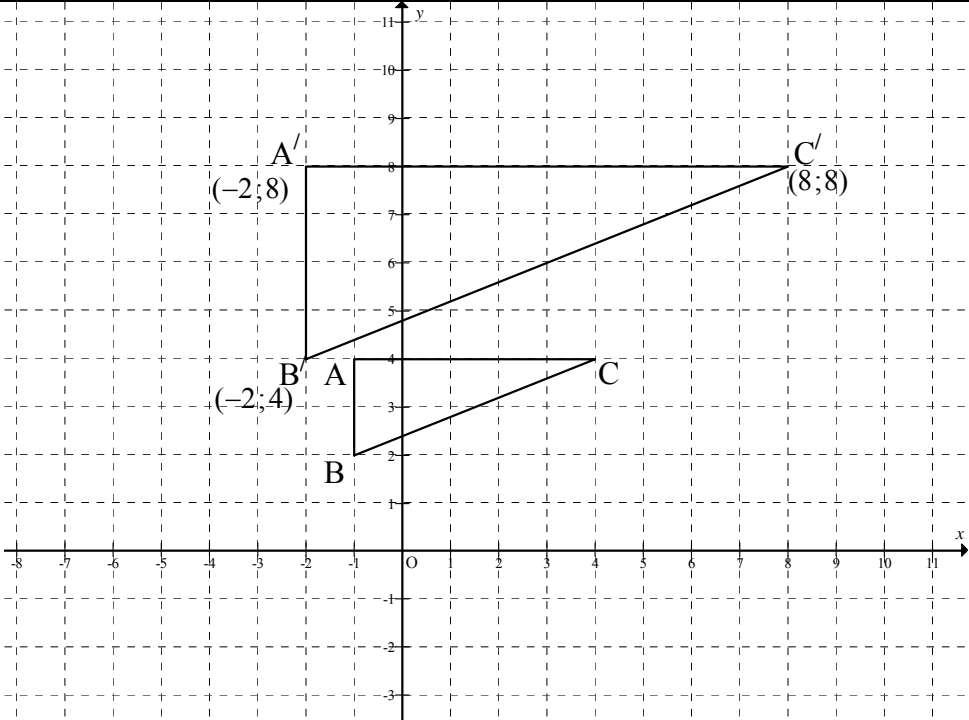
5.7	<p>Let the radius of circle TNM be <math>r</math>  <math>NB = BM</math> (properties of a kite)  <math>AN = TZ = r</math> (TZNA is a square)  <math>NB = 10 - r</math>  <math>BD = 2MB</math>  <math>\sqrt{(8 - (-6))^2 + (0 - (-2))^2} = 2(10 - r)</math>  <math>\sqrt{200} = 2(10 - r)</math>  <math>10\sqrt{2} = 2(10 - r)</math>  <math>r = 10 - 5\sqrt{2}</math>  <math>= 2,93</math></p> <p><b>OR</b></p> <p><math>\hat{ZMB} = 90^\circ</math>  <math>MB = \frac{1}{2}\sqrt{200}</math>  <math>= 7,07</math>  <math>\frac{ZM}{MB} = \tan 22,5^\circ</math>  <math>ZM = 7,07 \tan 22,5^\circ</math>  <math>= 2,93</math></p> <p><b>OR</b></p>	<p>✓ <math>NB = BM</math>  ✓ <math>AN = TZ = r</math>  ✓ <math>NB = 10 - r</math>  ✓ <math>BD = 2MB</math>  ✓ <math>BD = \sqrt{200}</math></p> <p>✓ answer (6)</p> <p>✓ tan radius theorem</p> <p>✓ ✓ MB</p> <p>✓ ✓ <math>\tan 22,5^\circ</math></p> <p>✓ answer (6)</p>
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5.7 contd	$MB^2 = (-1 + 2)^2 + (1 + 6)^2$ $= 1 + 49$ $= 50$ $MB = \sqrt{50}$ $\frac{ZM}{MB} = \tan 22,5^\circ$ $ZM = 7,07 \tan 22,5^\circ$ $= 2,93$ <p><b>OR</b></p> <p>By a well known formula</p> $\text{Area } \triangle ABD = r \times (\text{semi—perimeter})$ $\frac{1}{2} \times 10 \times 10 = r \times \frac{1}{2} (20 + \sqrt{200})$ $50 = r(10 + 5\sqrt{2})$ $r = 2,93$ <p><b>OR</b></p> $MB = \sqrt{50} \quad (\text{radius of circle})$ $NB = \sqrt{50} \quad (\text{adjacent sides of kite})$ $AB = 10$ $AN = 10 - \sqrt{50}$ $= 2,93$ <p>But TANZ is a square</p> $\therefore AN = ZN$ $\therefore \text{radius} = 2,93$	<p>✓✓MB</p> <p>✓✓tan 22,5°</p> <p>✓✓answer (6)</p> <p>✓✓ formula</p> <p>✓✓√200</p> <p>✓✓ answer (6)</p> <p>✓MB</p> <p>✓NB</p> <p>✓✓AN = 2,93</p> <p>✓square</p> <p>✓answer (6)</p>
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- Consistent Accuracy will apply as a general rule.
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- If a candidate does a question, crosses it out and does not re-do it, mark the deleted attempt.

**QUESTION 6**

6.1.1	$4 \times 5 = 20$ squared units	✓✓ answer $2^2 \times 5$ 1/2 If $2 \times 5 = 10$ 0/2 (2)
6.1.2	$(x; y) \rightarrow (2x; 2y)$  Note: If candidate state: coordinates times two    2/2	✓ $2x$ ✓ $2y$ (2) If $(kx; ky)$ : 1/2 If $2(x; y)$ : 2/2
6.1.3		✓ coordinates $A'$ ✓ coordinates $B'$ ✓ coordinates $C'$ (3)  If diagram not drawn but coordinates correctly given: 1/3  If coordinates correctly plotted but not joined: 2/3
6.1.4	Not rigid. The shape remains the same, whilst the size is changed /enlarged  <b>Note:</b> Shape remains the same:    1/2 Only the shape remains the same:    2/2	✓✓ same shape and different size (2) not rigid only    2/2 just enlarged    0/2
6.2	Reflection about the line $y = x$ : $(x; y) \rightarrow (y; x)$ Rotate clockwise about the origin: $(y; x) \rightarrow (x; -y)$ Translate 2 left and 3 down: $(x; -y) \rightarrow (x - 2; -y - 3)$  <b>OR</b> General rule: $(x; y) \rightarrow (x - 2; -y - 3)$	Mark per coordinate ✓✓ reflection ✓✓ rotation ✓✓ translation (6)  <b>Answer only:</b> Full marks [15]

- Consistent Accuracy will apply as a general rule.
- If a candidate does a question twice and does not delete either, mark the FIRST attempt.
- If a candidate does a question, crosses it out and does not re-do it, mark the deleted attempt.

<p>OR</p> <p>The first 2 transformations in the given order is the same as the reflection in the <math>x</math>-axis i.e. <math>(x ; y) \rightarrow (x ; -y)</math></p> <p>Then the translation gives us</p> <p><math>(x ; y) \rightarrow (x ; -y) \rightarrow (x - 2 ; -y - 3)</math></p> <div style="border: 1px solid black; padding: 10px; margin-top: 20px;"> <p><b>NOTE:</b></p> <p>If just given: <math>(x ; y) \rightarrow (x - 2 ; y - 3)</math>: 2/6</p> <p>If using <math>(x ; y) \rightarrow (y ; x)</math> ✓✓</p> <p style="padding-left: 40px;"><math>(x ; y) \rightarrow (y ; -x)</math> ✓</p> <p style="padding-left: 40px;"><math>(x ; y) \rightarrow (x - 2 ; y - 3)</math> ✓ throughout :4/6</p> </div>	<p>If learner starts with <math>(x ; y)</math> and continue to use <math>(x ; y)</math> for the second and third transformation 4/6</p>
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### QUESTION 7

7.1	$T' (x \cos \theta - y \sin \theta; y \cos \theta + x \sin \theta)$	✓ $x$ coordinate ✓ $y$ coordinate (2) Clock-wise formula: 0/2
7.2	$A' (p \cos 135^\circ - q \sin 135^\circ; q \cos 135^\circ + p \sin 135^\circ)$  If clockwise rotation: $A' (p \cos 135^\circ + q \sin 135^\circ; q \cos 135^\circ - p \sin 135^\circ)$	✓ $x$ coordinate ✓ $y$ coordinate (2) CA from 7.1
7.3	$x' = p \cos(135^\circ) - q \sin(135^\circ)$ $-1 - \sqrt{2} = -p \cos 45^\circ - q \sin 45^\circ$ $-1 - \sqrt{2} = -p \left( \frac{\sqrt{2}}{2} \right) - q \left( \frac{\sqrt{2}}{2} \right)$ $-1 - \sqrt{2} = -\frac{\sqrt{2}}{2} p - \frac{\sqrt{2}}{2} q \dots \dots \dots (1)$ and $y' = y \cos(135^\circ) + p \sin(135^\circ)$ $1 - \sqrt{2} = -q \cos 45^\circ + p \sin 45^\circ$ $1 - \sqrt{2} = q \left( -\frac{\sqrt{2}}{2} \right) + p \left( \frac{\sqrt{2}}{2} \right)$ $1 - \sqrt{2} = -\frac{\sqrt{2}}{2} q + \frac{\sqrt{2}}{2} p \dots \dots \dots (2)$  (1) + (2): $-2\sqrt{2} = -\sqrt{2}q$ $q = 2$	✓ equating  ✓ substitution   ✓ equating  ✓ substitution $\frac{\sqrt{2}}{2}$  ✓ solving simultaneously

- Consistent Accuracy will apply as a general rule.
- If a candidate does a question twice and does not delete either, mark the FIRST attempt.
- If a candidate does a question, crosses it out and does not re-do it, mark the deleted attempt.

	<p>Substitute <math>q = 2</math> into .....(1)</p> $-1 - \sqrt{2} = -\frac{\sqrt{2}}{2}p - \frac{\sqrt{2}}{2}(2)$ $-1 = -\frac{\sqrt{2}}{2}p$ $p = \sqrt{2}$ $\therefore A = (\sqrt{2}; 2)$ <p><b>OR</b></p> $x' = p \cos(135^\circ) - q \sin(135^\circ)$ $-1 - \sqrt{2} = -p \cos 45^\circ - q \sin 45^\circ$ $-1 - \sqrt{2} = -p\left(\frac{\sqrt{2}}{2}\right) - q\left(\frac{\sqrt{2}}{2}\right)$ $-1 - \sqrt{2} = -\frac{\sqrt{2}}{2}p - \frac{\sqrt{2}}{2}q \dots\dots\dots(1)$ <p>and</p> $y' = y \cos(135^\circ) + p \sin(135^\circ)$ $1 - \sqrt{2} = -q \cos 45^\circ + p \sin 45^\circ$ $1 - \sqrt{2} = q\left(-\frac{\sqrt{2}}{2}\right) + p\left(\frac{\sqrt{2}}{2}\right)$ $-0,41 = -0,71q + 0,71p \dots\dots\dots(2)$ <p>(1) + (2):</p> $-2\sqrt{2} = -\sqrt{2}q$ $q = 2$ <p>Substitute <math>q = 2</math> into .....(1)</p> $-2,41 = -0,71p - 0,71q \quad (2)$ $1,42p = 2$ $p = 1,41$ $\therefore A = (\sqrt{2}; 2)$ <p><b>OR</b></p>	<p>✓ answer for <math>q</math></p> <p>✓ answer for <math>p</math></p> <p>(7)</p> <p>✓ equating</p> <p>✓ substitution</p> <p>✓ equating</p> <p>✓ substitution <math>\frac{\sqrt{2}}{2}</math></p> <p>✓ solving simultaneously</p> <p>✓ answer for <math>q</math></p> <p>✓ answer for <math>p</math></p> <p>(7)</p>
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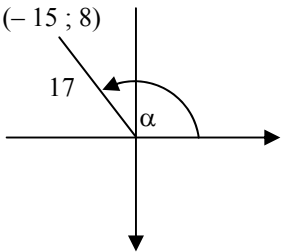
- Consistent Accuracy will apply as a general rule.
- If a candidate does a question twice and does not delete either, mark the FIRST attempt.
- If a candidate does a question, crosses it out and does not re-do it, mark the deleted attempt.

	$-\frac{\sqrt{2}}{2}(p+q) = -1 - \sqrt{2}$ $p+q = -\frac{2}{\sqrt{2}}(-1 - \sqrt{2})$ $p+q = \sqrt{2} + 2$ <p>and</p> $\frac{1}{\sqrt{2}}(p-q) = 1 - \sqrt{2}$ $p-q = \sqrt{2} - 2$ $p+q = \sqrt{2} + 2$ $2p = 2\sqrt{2}$ $p = \sqrt{2}$ $q = 2$ <p><b>OR</b></p> <p><math>A(p; q)</math> is obtained from <math>A'</math> by a rotation through <math>135^\circ</math> in a clockwise direction</p> $p = (-1 - \sqrt{2})\cos(-135^\circ) - (1 - \sqrt{2})\sin(-135^\circ)$ $= (-1 - \sqrt{2})\left(-\frac{1}{\sqrt{2}}\right) - (1 - \sqrt{2})\left(-\frac{1}{\sqrt{2}}\right)$ $= \frac{2}{\sqrt{2}}$ $= \sqrt{2}$ $q = (1 - \sqrt{2})\cos(-135^\circ) + (-1 - \sqrt{2})\sin(-135^\circ)$ $= (1 - \sqrt{2})\left(-\frac{1}{\sqrt{2}}\right) + (-1 - \sqrt{2})\left(-\frac{1}{\sqrt{2}}\right)$ $= \frac{2\sqrt{2}}{\sqrt{2}}$ $= 2$ $\therefore A = (\sqrt{2}; 2)$	<p>✓</p> $-\frac{\sqrt{2}}{2}(p+q) = -1 - \sqrt{2}$ <p>✓ substitution</p> <p>✓ <math>\frac{1}{\sqrt{2}}(p-q) = 1 - \sqrt{2}</math></p> <p>✓ substitution <math>\frac{\sqrt{2}}{2}</math></p> <p>✓ solving simultaneously</p> <p>✓ answer for <math>q</math></p> <p>✓ answer for <math>p</math></p> <p>(7)</p> <p>✓ substituting <math>(-1 - \sqrt{2})</math></p> <p>✓ substitution <math>\frac{1}{\sqrt{2}}</math></p> <p>✓ equating</p> <p>✓ substitution <math>\frac{1}{\sqrt{2}}</math></p> <p>✓ substituting <math>(-1 - \sqrt{2})</math></p> <p>✓ answer for <math>q</math></p> <p>✓ answer for <math>p</math></p> <p>(7)</p>
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- Consistent Accuracy will apply as a general rule.
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**QUESTION 8**

8.1	$\sin \alpha = \frac{8}{17}$ <p><math>\sin \alpha &gt; 0 \therefore</math> in second quadrant</p> $y_{\alpha} = 8 \quad r_{\alpha} = 17$ $x_{\alpha} = -15 \quad (\text{Pythagoras})$ $\tan \alpha = -\frac{8}{15}$	 <p><math>x = -\sqrt{15} \checkmark</math>  <math>\checkmark</math> answer  (3)</p> <p>For drawing the radius vector in the correct quadrant 1/3</p> <p>Without a sketch but correct values: 3/3</p>
8.2	$\sin(90^\circ + \alpha) = \cos \alpha$ $= -\frac{15}{17}$	$\checkmark$ reduction $\checkmark$ answer (2) <p>Answer only: full marks  Cannot accept decimal values</p>
8.3	$\cos 2\alpha = 1 - 2\sin^2 \alpha$ $= 1 - 2\left(\frac{8}{17}\right)^2$ $= \frac{161}{289}$ <p><b>OR</b></p> $\cos 2\alpha = 2\cos^2 \alpha - 1$ $= 2\left(\frac{-15}{17}\right)^2 - 1$ $= \frac{161}{289}$ <p><b>OR</b></p> $\cos 2\alpha = \cos^2 \alpha - \sin^2 \alpha$ $= \left(\frac{-15}{17}\right)^2 - \left(\frac{8}{17}\right)^2$ $= \frac{161}{289}$	$\checkmark$ expansion  $\checkmark$ substitution  $\checkmark$ any further calculation or answer (3) <p><math>\checkmark</math> expansion    <math>\checkmark</math> substitution    <math>\checkmark</math> any further calculation or answer  (3)</p> <p><math>\checkmark</math> expansion    <math>\checkmark</math> substitution    <math>\checkmark</math> any further calculation or answer  (3)</p> <p><b>[8]</b></p>

- Consistent Accuracy will apply as a general rule.
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- If a candidate does a question, crosses it out and does not re-do it, mark the deleted attempt.

**QUESTION 9**NOTE: Only penalise once in the question for leaving out the  $x$ 

Penalise once in this question for treating as an equation

9.1	$\sin(90^\circ - x) \cdot \cos(180^\circ - x) + \tan x \cdot \cos(-x) \cdot \sin(180^\circ + x)$ $= \cos x(-\cos x) + \tan x(\cos x)(-\sin x)$ $= -\cos^2 x - \frac{\sin x}{\cos x} \cos x \sin x$ $= -\cos^2 x - \sin^2 x$ $= -(\cos^2 x + \sin^2 x)$ $= -1$	$\checkmark \sin(90^\circ - x) = \cos x$ $\checkmark \cos(180^\circ - x) = -\cos x$ $\checkmark \cos(-x) = \cos x$ $\checkmark \sin(180^\circ + x) = -\sin x$ $\checkmark \tan x = \frac{\sin x}{\cos x}$ $\checkmark$ simplification $\checkmark$ answer <div style="text-align: right;">(7)</div>
9.2	$\frac{\sin 190^\circ \cos 225^\circ \tan 390^\circ}{\cos 100^\circ \sin 135^\circ}$ $= \frac{-\sin 10^\circ (-\cos 45^\circ) \tan 30^\circ}{-\sin 10^\circ \sin 45^\circ}$ $= \frac{-\frac{1}{\sqrt{2}} \cdot \frac{1}{\sqrt{3}}}{\frac{1}{\sqrt{2}}} \quad \text{or} \quad = -\tan 30^\circ$ $= -\frac{1}{\sqrt{3}}$	$\checkmark \sin 190^\circ = -\sin 10^\circ$ $\checkmark \cos 225^\circ = -\cos 45^\circ$ $\checkmark \tan 390^\circ = \tan 30^\circ$ $\checkmark \cos 100^\circ = -\sin 10^\circ$ $\checkmark \sin 135^\circ = \sin 45^\circ \text{ or } \cos 45^\circ$ $\checkmark \checkmark$ substitution <div style="text-align: right;">(7)</div>
9.3	$\sin x + 2\cos^2 x = 1$ $\sin x + 2(1 - \sin^2 x) = 1$ $-2\sin^2 x + \sin x + 1 = 0$ $2\sin^2 x - \sin x - 1 = 0$ $(2\sin x + 1)(\sin x - 1) = 0$ $\sin x = 1$ $x = 90^\circ + k \cdot 360^\circ; k \in \mathbb{Z}$ <p>Or</p>	$\checkmark$ substitution of identity $\checkmark$ standard form $\checkmark$ factorisation $\checkmark \sin x = 1; \sin x = -\frac{1}{2}$ $\checkmark x = 90^\circ + k \cdot 360^\circ; k \in \mathbb{Z}$ $\checkmark \checkmark$ answers (any two answers) <div style="text-align: right;">(7)</div> <p>If <math>k \in \mathbb{Z}</math> not included: 6/7</p> <p>Also <math>\pm k \cdot 360^\circ; k \in \mathbb{N}_0 \text{ or } \mathbb{Z}</math></p>

- Consistent Accuracy will apply as a general rule.
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$\sin x = -\frac{1}{2}$ $x = 210^\circ + k.360^\circ; k \in \mathbb{Z} \quad \text{OR} \quad x = 210^\circ + k.360^\circ$ $\text{or } x = 330^\circ + k.360^\circ; k \in \mathbb{Z} \quad \text{or } x = -30^\circ + k.360^\circ$ <p>OR</p> $x = -150^\circ + k.360^\circ; k \in \mathbb{Z} \quad \text{OR} \quad x = -150^\circ + k.360^\circ; k \in \mathbb{Z}$ $\text{or } x = 330^\circ + k.360^\circ \quad \text{or } x = -30^\circ + k.360^\circ$ <p><b>OR</b></p> $\sin x + 2 \cos^2 x = 1$ $\sin x = 1 - 2 \cos^2 x$ $\sin x = -\cos 2x$ $\sin x = -[\sin(90^\circ - 2x)]$ $x = 180^\circ + (90^\circ - 2x) + k360^\circ$ $3x = 270^\circ + k360^\circ \quad \text{or} \quad x = 360^\circ - (90^\circ - 2x) + k360^\circ$ $x = 90^\circ + k120^\circ \quad x = -270^\circ - k360^\circ$ $k \in \mathbb{Z}$ <p><b>OR</b></p> $\sin x + 2 \cos^2 x = 1$ $\sin x = 1 - 2 \cos^2 x$ $\sin x = -\cos 2x$ $-\cos(90^\circ - x) = \cos 2x$ $2x = 180^\circ - (90^\circ - x) + k360^\circ \quad 2x = 180^\circ + (90^\circ - x) + k360^\circ$ $x = 90^\circ + k360^\circ \quad \text{or} \quad 3x = 270^\circ + k360^\circ$ $x = 30^\circ + k120^\circ$ $k \in \mathbb{Z}$	<p>✓ manipulation ✓ substitution of identity</p> <p>✓ co ratios</p> <p>✓ <math>x = 180^\circ + (90^\circ - 2x) + k360^\circ</math> ✓ <math>x = 90^\circ + k120^\circ</math> ✓ <math>x = 360^\circ - (90^\circ - 2x) + k360^\circ</math> ✓ <math>x = -270^\circ - k360^\circ</math></p> <p>(7)</p> <p>If <math>k \in \mathbb{Z}</math> not included: 6/7</p> <p>✓ manipulation ✓ substitution of identity</p> <p>✓ co ratios</p> <p>✓</p> <p><math>2x = 180^\circ - (90^\circ - x) + k360^\circ</math> ✓ <math>x = 90^\circ + k360^\circ</math> ✓ <math>2x = 180^\circ + (90^\circ - x) + k360^\circ</math> ✓ <math>x = 30^\circ + k120^\circ</math></p> <p>(7)</p> <p>If <math>k \in \mathbb{Z}</math> not included: 6/7</p> <p><b>[20]</b></p>
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**QUESTION 10**

10.1	$\frac{\sin(A+B)}{\cos(A+B)} = \frac{\sin A \cos B + \cos A \sin B}{\cos A \cos B - \sin A \sin B}$ $= \frac{\sin A \cos B + \cos A \sin B}{\cos A \cos B - \sin A \sin B} \times \frac{\frac{1}{\cos A \cos B}}{\frac{1}{\cos A \cos B}}$ $= \frac{\frac{\sin A \cos B}{\cos A \cos B} + \frac{\cos A \sin B}{\cos A \cos B}}{\frac{\cos A \cos B}{\cos A \cos B} - \frac{\sin A \sin B}{\cos A \cos B}}$ $= \frac{\tan A + \tan B}{1 - \tan A \tan B}$ <p><b>OR</b></p> $RHS = \frac{\tan A + \tan B}{1 - \tan A \tan B}$ $= \frac{\frac{\sin A}{\cos A} + \frac{\sin B}{\cos B}}{1 - \frac{\sin A \sin B}{\cos A \cos B}} \times \frac{\cos A \cos B}{\cos A \cos B}$ $= \frac{\sin A \cos B + \sin B \cos A}{\cos A \cos B - \sin A \sin B}$ $= \frac{\sin(A+B)}{\cos(A+B)}$ $= \tan(A+B)$ $= LHS$	<p>✓ expansions</p> <p>✓ divisions</p> <p>✓ tanA and tanB (3)</p> <p>✓ <math>\frac{\sin A}{\cos A}</math></p> <p>✓ multiplication</p> <p>✓ expansions (3)</p>
10.2	$\tan C = \tan(180^\circ - (A+B))$ $\tan C = -\tan(A+B)$ $\tan C = -\left(\frac{\tan A + \tan B}{1 - \tan A \tan B}\right)$ $\tan C(1 - \tan A \tan B) = -(\tan A + \tan B)$ $\tan C - \tan A \tan B \tan C = -\tan A - \tan B$ $\tan A + \tan B + \tan C = \tan A \tan B \tan C$ <p><b>OR</b></p>	<p>✓ C</p> <p>✓ <math>-\tan(A+B)</math></p> <p>✓ substitution into formula</p> <p>✓ multiplication with LCD</p> <p>(4)</p> <p>If no conclusion: 3/4</p>

- Consistent Accuracy will apply as a general rule.
- If a candidate does a question twice and does not delete either, mark the FIRST attempt.
- If a candidate does a question, crosses it out and does not re-do it, mark the deleted attempt.

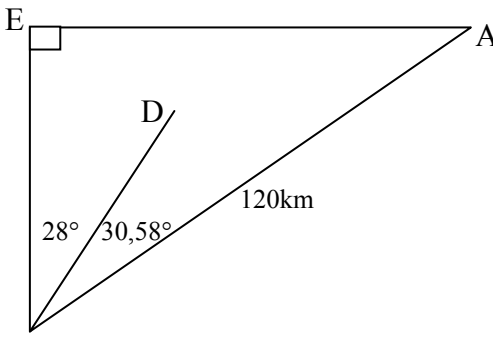
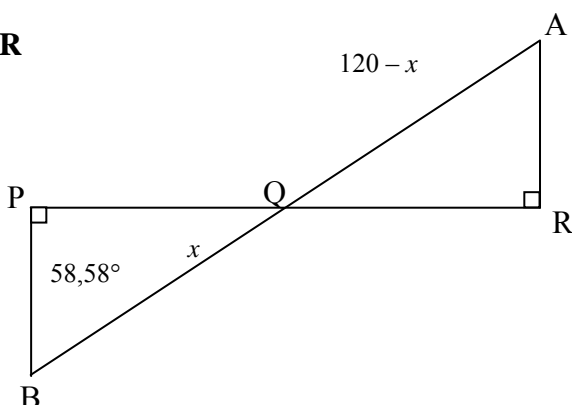
$\hat{C} = 180^\circ - (\hat{A} + \hat{B})$ (angles in a triangle) $\tan C = \tan(180^\circ - (A + B))$ $\tan C = \tan((180^\circ - A) + (-B))$ $\tan C = \frac{\tan(180^\circ - A) + \tan(-B)}{1 - \tan(180^\circ - A) \cdot \tan(-B)}$ $\tan C(1 - \tan(180^\circ - A) \cdot \tan(-B)) = \tan(180^\circ - A) + \tan(-B)$ $\tan C - \tan C \tan A \tan B = -\tan A - \tan B$ $\tan A + \tan B + \tan C = \tan A \cdot \tan B \cdot \tan C$	✓ C  ✓ rearrange angle ✓ substitution into formula ✓ expansion  (4)
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**QUESTION 11**

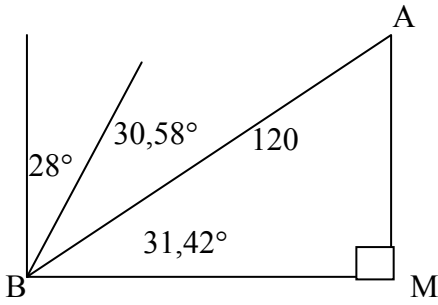
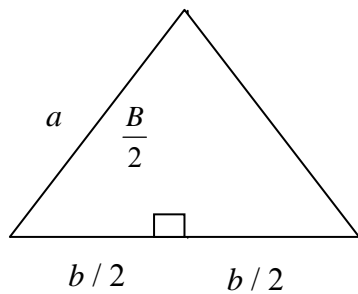
NOTE: Penalty of one for early rounding off once in this question

11.1.1	$\hat{BDA} = 208^\circ - 67^\circ$ $= 141^\circ$ $\frac{\sin \hat{DBA}}{97} = \frac{\sin 141^\circ}{120}$ $\sin \hat{DBA} = 0,5087006494...$ $\hat{DBA} = 30,58^\circ$ $\therefore$ Bearing of Ship A from Ship B $= 180^\circ - (360^\circ - 208^\circ) + 30,58^\circ$ $= 58,58^\circ$ <b>OR</b> $\hat{BDA} = 208^\circ - 67^\circ$ $= 141^\circ$ $\frac{\sin \hat{DBA}}{97} = \frac{\sin 141^\circ}{120}$ $\sin \hat{DBA} = 0,5087006494....$ $\hat{DBA} = 30,58^\circ$ $then\ 360^\circ - 208^\circ = \hat{NDB}$ (reflex angles) $\therefore \hat{NDB} = 152^\circ$ $but\ \hat{MBD} + \hat{NDB} = 180^\circ$ (co - interior angles/ angles around a point) $\therefore \hat{MBD} = 28^\circ$ $then\ \hat{MBA} = \hat{MBD} + \hat{DBA}$ $= 30,58^\circ + 28^\circ$ $= 58,58^\circ$	✓ $\hat{BDC} = 141^\circ$  ✓ sine rule ✓ substitution  ✓ $\hat{B} = 30,58^\circ$ ✓ method or $\hat{MBD} = 28^\circ$ ✓ answer (6)  ✓ $\hat{BDC} = 141^\circ$  ✓ sine rule ✓ substitution  ✓ $\hat{NDB} = 152^\circ$  ✓ $\hat{MBD} = 28^\circ$  ✓ answer (6)
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- Consistent Accuracy will apply as a general rule.
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- If a candidate does a question, crosses it out and does not re-do it, mark the deleted attempt.

11.1.2	<p><math>\hat{B} = 30,58^\circ</math></p>  <p> <math>\frac{EA}{120} = \sin(28^\circ + 30,58^\circ)</math>  <math>EA = 120 \sin(28^\circ + 30,58^\circ)</math>  <math>EA = 102,4 \text{ km}</math> </p> <p><b>OR</b></p>  <p>Let <math>BQ = x</math>, then <math>AQ = 120 - x</math></p> $\sin 58,58^\circ = \frac{PQ}{x} \qquad \sin 58,58^\circ = \frac{QR}{120 - x}$ $PQ = x \cdot \sin 58,58^\circ \qquad QR = (120 - x) \sin 58,58^\circ$ $PQ + QR = x \cdot \sin 58,58^\circ + (120 - x) \sin 58,58^\circ$ $= 120 \sin 58,58^\circ$ $= 102,4$ <p><b>OR</b></p> <p><math>BP = AR</math> (assume ships move at same speed)</p>	<p>✓ definition ✓ substitution</p> <p>✓ answer (3)</p> <p>✓ trigonometric ratios</p> <p>✓ sum</p> <p>✓ answer (3)</p> <p>✓ trigonometric</p>
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- Consistent Accuracy will apply as a general rule.
- If a candidate does a question twice and does not delete either, mark the FIRST attempt.
- If a candidate does a question, crosses it out and does not re-do it, mark the deleted attempt.

	<p><math>\triangle PBQ \equiv \triangle RAQ</math> (angle, angle, side)</p> <p><math>\therefore BQ = QA = 60 \text{ km}</math></p> <p><math>\sin 58,58^\circ = \frac{PQ}{60}</math></p> <p><math>\therefore PQ = 60 \sin 58,58^\circ</math></p> <p><math>= 51,20 \text{ km}</math></p> <p><math>PR = 2PQ</math></p> <p><math>= 102,4 \text{ km}</math></p> <p>OR</p> <p><math>\frac{BM}{120} = \cos 31,42^\circ</math></p> <p><math>BM = 120 \times \cos 31,42^\circ</math></p> <p><math>= 102,4</math></p> 	<p>ratios</p> <p>✓ 51,20 km</p> <p>✓ answer (3)</p> <p>✓ trigonometric ratios</p> <p>✓ substitution</p> <p>✓ answer (3)</p>
11.2	<p><math>AB = BC = a = c</math></p> <p><math>b^2 = a^2 + c^2 - 2ac \times \cos B</math></p> <p><math>b^2 = a^2 + a^2 - 2a \times a \times \cos B</math></p> <p><math>b^2 = 2a^2 - 2a^2 \cos B</math></p> <p><math>b^2 = 2a^2(1 - \cos B)</math></p> <p><math>\frac{b^2}{2a^2} = 1 - \cos B</math></p> <p><math>\cos B = 1 - \frac{b^2}{2a^2}</math></p> <p>OR</p> <p><math>\sin \frac{B}{2} = \frac{b}{2a}</math></p> <p><math>\cos B = 1 - 2\sin^2 \frac{B}{2}</math></p> <p><math>= 1 - 2\left(\frac{b}{2a}\right)^2</math></p> <p><math>= 1 - \frac{b^2}{2a^2}</math></p> 	<p>✓ equal sides</p> <p>✓ cos rule</p> <p>✓ substitution</p> <p>✓ simplification (4)</p> <p>✓ <math>\sin \frac{B}{2}</math></p> <p>✓ <math>\sin \frac{B}{2} = \frac{b}{2a}</math></p> <p>✓ formula</p> <p>✓ substitution (4)</p>

- Consistent Accuracy will apply as a general rule.
- If a candidate does a question twice and does not delete either, mark the FIRST attempt.
- If a candidate does a question, crosses it out and does not re-do it, mark the deleted attempt.

	<p><b>OR</b></p> $\cos B = \frac{a^2 + c^2 - b^2}{2ac}$ <p>but <math>a = c</math></p> $\cos B = \frac{a^2 + a^2 - b^2}{2a.a}$ $= \frac{2a^2 - b^2}{2a^2}$ $= 1 - \frac{b^2}{2a^2}$	<p><b>[13]</b></p> <p>✓ cos rule ✓ equal sides ✓ substitution</p> <p>✓ simplification (4)</p>
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**QUESTION 12**

12.1		<p>✓ (120°; 0) or (-60°; 0)</p> <p>✓ (30°; 2) or (210°; -2) (2)</p>
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- Consistent Accuracy will apply as a general rule.
- If a candidate does a question twice and does not delete either, mark the FIRST attempt.
- If a candidate does a question, crosses it out and does not re-do it, mark the deleted attempt.

**QUESTION 12**

12.2	$\cos(x - 30^\circ) = \frac{1}{2}$ $2 \cos(x - 30^\circ) = 1$ See points A and B on the graph  <b>Note:</b> If drawn the line $y = \frac{1}{2}$ and put A and B on the graph: 0/2  If A and B on the $x$ -axis: 1/2  If $A = -30^\circ$ and $B = 90^\circ$ : 1/2	✓ manipulation  ✓ answer (2) A and B in the correct place on the graph: full marks
12.3	$\cos(x - 30^\circ) = 0,5$ $x - 30^\circ = 60^\circ$ OR $x - 30^\circ = -60^\circ$ $x = 90^\circ$ OR $x = -30^\circ$	✓ $60^\circ$ (ref angle) ✓ $90^\circ$ ✓ $-30^\circ$ (3) Answer only: 3/3
12.4	$g'(x) = 0$ is at maximum and minimum values of graph $x = 30^\circ$ ; $210^\circ$	✓✓ one for each $x$ -value (2)
12.5	$x \in [-90^\circ; -60^\circ) \cup (120^\circ; 270^\circ]$  <b>OR</b> $-90^\circ \leq x < -60^\circ$ or $120^\circ < x \leq 270^\circ$ <b>OR</b> If $x < -60^\circ$ or $x > 120^\circ$ 2/3	✓ notation ✓✓ critical values (3) <b>[12]</b>