

# Chapter 3

## Arithmetic for Computers



# IEEE Floating-Point Format

single: 8 bits  
double: 11 bits

single: 23 bits  
double: 52 bits

S	Exponent	Fraction
---	----------	----------

$$x = (-1)^S \times (1 + \text{Fraction}) \times 2^{(\text{Exponent} - \text{Bias})}$$

- S: sign bit (0  $\Rightarrow$  non-negative, 1  $\Rightarrow$  negative)
- Normalize significand:  $1.0 \leq |\text{significand}| < 2.0$ 
  - Always has a leading pre-binary-point 1 bit, so no need to represent it explicitly (hidden bit)
  - Significand is Fraction with the “1.” restored
- Exponent: excess representation: actual exponent + Bias
  - Ensures exponent is unsigned
  - Single: Bias = 127; Double: Bias = 1203



# Floating-Point Addition

- Consider a 4-digit decimal example
  - $9.999 \times 10^1 + 1.610 \times 10^{-1}$
- 1. Align decimal points
  - Shift number with smaller exponent
  - $9.999 \times 10^1 + 0.016 \times 10^1$
- 2. Add significands
  - $9.999 \times 10^1 + 0.016 \times 10^1 = 10.015 \times 10^1$
- 3. Normalize result & check for over/underflow
  - $1.0015 \times 10^2$
- 4. Round and renormalize if necessary
  - $1.002 \times 10^2$



# FP Adder Hardware

