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CSM151B Homework 1
1.5, 1.6, 1.7, 1.13

1.5

a)

Processor:	Clock Rate:	Cycle Per Instruction:
P1	3.0GHz	1.5
P2	2.5GHz	1.0
P3	4.0GHz	2.2

We have: Performance = Clock Rate/Cycles Per Instruction

Use the above formula to calculate the performance of each processor:

Performance (P1) = $3.0 \times 10^9 / 1.5 = 2.0 \times 10^9$ Instruction Per Second

Performance (P2) = $2.5 \times 10^9 / 1.0 = 2.5 \times 10^9$ Instruction Per Second

Performance (P3) = $4.0 \times 10^9 / 2.2 = 1.81 \times 10^9$ Instruction Per Second

Therefore, Processor2 results in the highest performance in terms of instructions per second.

b)

Running a program for 10 seconds:

Number of Cycles = Clock Rate * Time (s)

Number of Cycles (P1) = $3.0 \times 10^9 \times 10 = 3.0 \times 10^{10}$ Cycles

Number of Cycles (P2) = $2.5 \times 10^9 \times 10 = 2.5 \times 10^{10}$ Cycles

Number of Cycles (P3) = $4.0 \times 10^9 \times 10 = 4.0 \times 10^{10}$ Cycles

Number of instructions = Number of Cycles / Cycles Per Instruction

Number of instructions (P1) = $3.0 \times 10^{10} / 1.5 = 2.0 \times 10^{10}$

Number of instructions (P2) = $2.5 \times 10^{10} / 1.0 = 2.5 \times 10^{10}$

Number of instructions (P3) = $4.0 \times 10^{10} / 2.2 = 1.81 \times 10^{10}$

c)

To reduce the execution time by 30% but this leads to an increase of 20% in the CPI.

$ET = IC * CPI * CT = (IC * CPI) / \text{Clock Rate}$

$\text{Clock Rate} = IC * CPI / ET$

For Processor 1:

NEW CPI = 1.2 * CPI

NEW ET = 0.7 ET

Therefore:

NEW Clock Rate = $1.2 / 0.7 \text{ IC} * \text{CPI} / \text{ET} = 1.714 * \text{Clock Rate} = 1.714 * 3.0 * 10^9 = 5.14 \text{GHz}$

The new Clock Rate required for P1 to get the time reduction is 5.14GHz.

For Processor 2:

NEW CPI = 1.2 * CPI

NEW ET = 0.7 ET

Therefore:

NEW Clock Rate = $1.2 / 0.7 \text{ IC} * \text{CPI} / \text{ET} = 1.714 * \text{Clock Rate} = 1.714 * 2.5 * 10^9 = 4.28 \text{GHz}$

The new Clock Rate required for P1 to get the time reduction is 4.28GHz.

For Processor 3:

NEW CPI = 1.2 * CPI

NEW ET = 0.7 ET

Therefore:

NEW Clock Rate = $1.2 / 0.7 \text{ IC} * \text{CPI} / \text{ET} = 1.714 * \text{Clock Rate} = 1.714 * 4.0 * 10^9 = 6.85 \text{GHz}$

The new Clock Rate required for P1 to get the time reduction is 6.85GHz.

1.6

Processor	Clock Rate	Class A	Class B	Class C	Class D
P1	2.5GHz	1	2	3	3
P2	3GHz	2	2	2	2

10% class A, 20% class B, 50% class C, and 20% class D

Weighted Average CPI for Processor 1:

$\text{CPI}(\text{avg.}) = 1 * 0.1 + 2 * 0.2 + 3 * 0.5 + 3 * 0.2 = 2.6$

Weighted Average CPI for Processor 2:

$\text{CPI}(\text{avg.}) = 2 * 0.1 + 2 * 0.2 + 2 * 0.5 + 2 * 0.2 = 2$

$\text{ET} = \text{IC} * \text{CPI} * \text{CT} = (\text{IC} * \text{CPI}) / \text{Clock Rate}$

Calculated the estimated CPU time:

$\text{ET}(\text{P1}) = 1.0 * 10^6 * 2.6 / (2.5 * 10^9) = 1.04 \text{ ms}$

$\text{ET}(\text{P2}) = 1.0 * 10^6 * 2 / (3 * 10^9) = 0.667 \text{ ms}$

Thus we see that processor 2 runs faster.

a)

Global CPI = $\text{CPI time} * \text{Clock Rate} / (\text{Numbers of Instructions})$

Global CPI for Processor 1 = $1.04 \times 10^{-3} \times 2.5 \times 10^9 / 10^6 = 2.6$
The global CPI for P1 is 2.6.

Global CPI for Processor 2 = $0.667 \times 10^{-3} \times 3 \times 10^9 / 10^6 = 2.0$
The global CPI for P2 is 2.0.

b)

Number of Clock Cycles required:

Clock Cycles for P1 = Global CPI * No. of Instructions = 2.6×10^6 Cycles

Clock Cycles for P2 = Global CPI * No. of Instructions = 2.0×10^6 Cycles

1.7

a)

Compiler	Execution Time	Instruction Count
A	1.1s	1×10^9
B	1.5s	1.2×10^9

Cycle Time = 1ns = 1.0×10^{-9} s

ET = IC * CPI * CT

Thus, CPI = ET / (IC * CT)

CPI for Compiler A:

CPI = ET / (IC * CT) = $1.1 / (1 \times 10^9 \times 1.0 \times 10^{-9}) = 1.1$

CPI for Compiler B:

CPI = ET / (IC * CT) = $1.5 / (1.2 \times 10^9 \times 1.0 \times 10^{-9}) = 1.25$

b)

ET (A) = IC * CPI * CT (A)

ET (B) = IC * CPI * CT (B)

Because the execution time is the same, equate both equations

IC(A) * CPI(A) * CT (A) = IC(B) * CPI(B) * CT (B)

CT(A)/CT(B) = IC(B) * CPI(B) / (IC(A) * CPI(A)) = $1.2 \times 10^9 \times 1.25 / (1 \times 10^9 \times 1.1) = 1.3636$ Times

Therefore, the Clock Cycle of Compiler A is 1.3636 times faster than Clock Cycle of the Compiler B.

c)

The new compiler has

IC = 0.6×10^9

Avg. CPI = 1.1

Cycle Time = 1ns = 1.0×10^{-9} s

ET (NEW) = IC * CPI * CT = $0.6 \times 10^9 \times 1.1 \times 1.0 \times 10^{-9} = 0.66$ s

Comparing to Compiler A:

$$ET(NEW)/ET(A) = 1.1s/0.66s = 1.67$$

Therefore, the Execution Time of the new Compiler is 1.67 times faster than the Execution Time of the Compiler A.

Comparing to Compiler B:

$$ET(NEW)/ET(B) = 1.5s/0.66s = 2.27$$

Therefore, the Execution Time of the new Compiler is 2.27 times faster than the Execution Time of the Compiler B.

1.13

1.13.1)

$$\begin{aligned} \% \text{ Total Time Reduced} &= \text{Time Reduced in FP Operation} / \text{Total Time} \\ &= (20\%) * 70 / 250 = 0.056 = 5.6\% \end{aligned}$$

1.13.2)

$$\text{Reduced time} = 250s * 20\% = 50s$$

$$\text{Original INT time} = 250s - 70s - 85s - 40s = 55s$$

$$\text{INT operation time reduced by} = 50s/55s = 90.0\%$$

1.13.3)

$$\text{Total time reduced by } 20\% = 0.8 * 250 = 200s$$

$$\text{Reducing The time of branch instruction} = 85 + 70 + 55 = 210s$$

Since $210 > 200$, an contradiction occurs. Therefore, it is not possible to reduce the total time by 20% by simply reducing the time of branch instruction.