
Enhancing transferability of adversarial examples with gradient shift

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Abstract

1 The transferability of adversarial examples in the black-box attack setting has at-
2 tracted extensive attention from the community. Among the previous research,
3 input transformations are one of the most effective of all to improve the trans-
4 ferability of adversarial examples. However, we find that input transformations
5 are short of theoretical analysis, which also means that they are an unexplain-
6 able methods and unfavorable to further improve the transferability of adversarial
7 samples. This paper attempts to analyze input transformations from a gradient
8 perspective, and is inspired by this to propose a gradient shift hypothesis. Specifi-
9 cally, for different models trained on the same dataset, there is a computable bias
10 between their gradients with respect to the same input. Based on this, we propose
11 a new method that can further enhance the transferability of adversarial examples.
12 Experiments on the standard ImageNet dataset demonstrate the superiority of our
13 proposed method. Code is available at <https://...>

14 1 Introduction

15 Deep neural networks (DNNs) have been shown superior performance in various tasks. However,
16 adversarial examples [1] can fool the models by modifying normal examples with indistinguishable
17 perturbations. Such undesirable vulnerability have raised great concern for applications based on
18 DNNs, especially for security-sensitive realm, e.g., face verification [2], autonomous driving [3].
19 Therefore, we need for better techniques to evaluate the robustness of neural networks [4].

20 Many efforts have been devoted to crafting the adversarial examples. In general, according to the
21 knowledge owned by attackers, adversarial attacks can be divided into two categories, i.e., white-box
22 attacks where the adversary has full access to the model and black-box attacks where the adversary
23 does not know or know limited information of the model. Obviously, black-box attacks are more
24 challenging and damaging than white-box attacks and have attracted great attention.

25 Under the black-box attack setting, the transferability of adversarial examples is a central issue.
26 Various techniques, such as [5, 6, 7, 8, 9], have been proposed to improve the transferability, of which
27 input transformations are one of the most effective. DIM [10] is a classic input transformations
28 method that randomly resizing and padding images to improve the transferability of adversarial
29 examples. Other methods, e.g., TIM [8], SIM [6] and Admix [11], have also achieved some of
30 success. Nevertheless, we found that these research works are short of theoretical analysis, that is
31 unfavorable to further improve the transferability of adversarial samples.

32 We conduct a theoretical analysis of input transformations. And inspired by the analysis, we pro-
33 pose the gradient shift hypothesis which indicates the gradient relationship between different models.
34 Specifically, the difference in model structure and randomness in training process lead to the discrep-
35 ancy in models themselves, i.e., the final functions. However, the gradient of various models with

respect to the same input exist similarity to some extent. Based on the hypothesis, a new method called Ropeway, which can significantly improve the transferability of adversarial samples, is proposed. The extend experiment not only shows the effectiveness of the Ropeway, but also proves the existence of gradient shift.

2 Background and Related work

There are many works aiming to improve the transferability of adversarial examples. According to the attacked layers, black-box attacks are also categorized into attacking internal features and disrupting output layers [12]. This study falls into the latter.

The methods attacking internal features, such as [13, 12, 14, 15, 16], seems like a good approach. However, the majority of these are dependent on the choice of the middle layer, which requires numerous experimentation. In the setting of disrupting output layers, the adversarial examples can be generated with high transferability without selecting the intermediate layer. In general, there are two methods to enhance the transferability of adversarial examples : (1) better optimization algorithm and (2) model augmentation [6].

MI-FGSM [5] is a typical better optimization algorithm. MI-FGSM integrate momentum into I-FGSM [17] to stabilize updates and avoid poor local optimum. Since it just like improving generalization ability of the trained models, better optimization algorithm can boost the transferability of adversarial examples. Other methods, e.g., NI-FGSM [6], AI-FGTM [18], EMI-FGSM [19], have a favorable performance as well. While the optimization method can be used to find better adversarial examples, it cannot further explain the connection between the models trained on the same dataset (which can only be attributed to generalization)

Model augmentation is another powerful method to enhance the transferability of adversarial examples and the most prominent one is input transformations. Common input transformations include randomly resizing and padding [10], translation [8], scaling [6], interpolation [11], and so on. When these transformations are applied to the input image, it is equivalent to deriving a enhanced model from the original model [6]. The adversarial examples generated on the new model are more transferable. However, there is the same problem with the "better optimization algorithm" that model augmentation cannot further explain the connection between the models trained on the same dataset. And even, they themselves are shortage of corresponding theoretical explanations and are unfavorable to further improve the transferability of adversarial samples.

The LI-FGSM proposed recently by Jang et al. [20] is similar to the Ropeway proposed by us, both of which use the gradients of next n steps to adjust the current gradient. But there are essentially 3 differences: (1) LI-FGSM is inspired by NI-FGSM [6], while Ropeway is mainly inspired by the theoretical analysis of input transformations; (2) LI-FGSM lacks the theoretical analysis of input transformations, while that is an important part of this paper; (3) For calculating gradients of next n steps, LI-FGSM only rely on VNI-FGSM [21] (which is a "better optimization algorithm" method), but Ropeway can use any input transformations.

3 Gradient shift hypothesis

3.1 Preliminaries

Given a classification model f and a classification task $f(x) = y$, where x denotes the clean image and y denotes the output label which equals to the ground truth label. Our intention is to generate adversarial examples x^{adv} that can mislead the classifier, i.e., $f(x^{adv}) \neq y$. To align with previous works, we adopt the L_∞ -norm to restrict perturbation. So, the process of generating adversarial examples is to solve the following optimization problems.

$$\arg \max_{x^{adv}} J(x^{adv}, y), \text{ s.t. } \|x - x^{adv}\|_\infty \leq \epsilon,$$

where J is the loss function (i.e., cross-entropy) and ϵ is the upper bound of perturbations.

Fast Gradient Sign Method (FGSM) [1] exploits the gradient of the loss function for a one-step attack as follows:

$$x^{adv} = x + \epsilon \cdot \text{sign}(\nabla_x J(x, y)),$$

where $\text{sign}(\cdot)$ denotes the sign function and $\nabla_x J(x, y)$ denotes the gradient of the loss function w.r.t. x .

Iterative Fast Gradient Sign Method (I-FGSM) [17] can generate adversarial examples with high white-box attack success rate by iterative updating:

$$x_{t+1}^{adv} = x_t^{adv} + \alpha \cdot \text{sign}(\nabla_{x_t^{adv}} J(x_t^{adv}, y)),$$

where α is small perturbations and less than ϵ .

Momentum Iterative Fast Gradient Sign Method (MI-FGSM) [5] integrates the momentum term into I-FGSM [Admix 11] to boost the transferability of adversarial examples, which can be expressed as:

$$g_t = \mu \cdot g_{t-1} + \frac{\nabla_{x_t^{adv}} J(x_t^{adv}, y)}{\|\nabla_{x_t^{adv}} J(x_t^{adv}, y)\|_1},$$

$$x_{t+1}^{adv} = x_t^{adv} + \alpha \cdot \text{sign}(g_t).$$

Diverse Inputs Method (DIM) [10] applies image transformations $T(\cdot)$ to the inputs with the probability p at each iteration of I-FGSM:

$$x_{t+1}^{adv} = x_t^{adv} + \alpha \cdot \text{sign}(\nabla_{x_t^{adv}} J(T(x_t^{adv}, p), y)),$$

where $T(\cdot)$ is firstly resizing the image with probability p and then padding it.

3.2 Gradient approximation

Goodfellow et al. [1] propose that the reason for adversarial examples is due to the linear nature of DNNs, so that making many infinitesimal changes to the input can add up to one large change to the output. In the setting of black-box attack, the transferability of adversarial examples crafted by FGSM depends on gradient approximation. In order to describe this gradient approximation, we simplify the FGSM algorithm and remove the $\text{sign}(\cdot)$ function:

$$x^{adv} = x + \epsilon \cdot \nabla_x J(x, y), \quad (1)$$

where y is the ground-truth label of the input x . Given two pretrained models f_1, f_2 and the loss function J . And f_1, f_2 is the source model, target model respectively. If we want high transferability of adversarial examples made by Eq. (1) between f_1 and f_2 , we actually expect the gradient of f_1 can equal to the gradient of f_2 w.r.t. the same inputs, i.e., $\nabla_{x_1}^1 J(x, y) \approx \nabla_{x_2}^2 J(x, y)$, where $\nabla_{x_1}^1 J(x, y)$ is the gradient of f_1 and $\nabla_{x_2}^2 J(x, y)$ is the gradient of f_2 . Since that, no matter whether the value of the $J(x^{adv}, y)$ becomes larger or smaller than $J(x, y)$ of f_1 , $J(x^{adv}, y)$ can always become larger than $J(x, y)$ of f_2 and may lead to $f_2(x^{adv}) \neq y$.

In the example above, let $d_1 = \nabla_{x_1}^1 J(x, y) - \nabla_{x_2}^2 J(x, y)$ where d_1 denotes the discrepancy between gradients of f_1 and f_2 . Obviously, d_1 is not necessarily a zero matrix, that means $\nabla_{x_1}^1 J(x, y)$ is not necessarily equal to $\nabla_{x_2}^2 J(x, y)$. Therefore, it is conceivable that the transferability of the adversarial samples made by Eq. (1) are poor. And now, we introduce the input transformations to improve the transferability of adversarial examples, that is $x' = T(x)$ where $T(\cdot)$ is some kind of transformations (e.g., transformations in DIM, refer to Section 3.1). After that, the Eq. (1) can be reformulated as:

$$x^{adv} = x + \epsilon \cdot \nabla_x J(T(x), y). \quad (2)$$

If we make adversarial examples by Eq. (2) on f_1 , can we expect gradient approximation between the same x ? The answer is yes. Firstly, we can rewrite $x' = T(x)$ as $x' = x + \delta$, that is, $T(x) = x + \delta$. What needs to be stated is that $T(x)$ and $x + \delta$ are only formally equal, which does not mean that the transformation is actually an addition operation. Secondly, we can rewrite $\nabla_x J(T(x), y)$, i.e., $\nabla_x J(T(x), y) = \nabla_x J(x + \delta, y)$, and rewrite d_1 as $d_1' = \nabla_{x_1}^1 J(T(x), y) - \nabla_{x_2}^2 J(x, y)$. Suppose our model is 3 times differentiable in a closed ball $B = \{x'' : \|x'' - x\| \leq r\}$, for some $r \geq 0$. According to the first-order multivariate Taylor expansion

$$\nabla_x J(x + \delta, y) \approx \nabla_x J(x, y) + \delta \cdot D \nabla_x J(x, y),$$

120 where D is differential. Then, we apply it to d'_1 , and we get d_2 :

$$\begin{aligned} d_2 &= \nabla_x^1 J(T(x), y) - \nabla_x^2 J(x, y) \\ &= \nabla_x^1 J(x + \delta, y) - \nabla_x^2 J(x, y) \\ &\approx \nabla_x^1 J(x, y) - \nabla_x^2 J(x, y) + \delta \cdot D \nabla_x^1 J(x, y). \end{aligned} \quad (3)$$

121 Due to the harmony of $\delta \cdot D \nabla_x^1 J(x, y)$, when models f_1 , f_2 and input x are certain, d_2 is no longer
122 fixed, but can vary with δ . So, if the transformation is ideal, d_2 is more likely to be close to the zero
123 matrix than d_1 . In theory, let $d_2 = 0$, we can find an optimal δ and even judge the "good or bad" of
124 the transformation.

125 This paper does not aim to prove which transformation is more effective for improving the transfer-
126 ability of adversarial examples, so we will not go into details. And, previous studies [6, 8, 10, 11]
127 have demonstrated the excellent performance of transformations, which also shows that the gradient
128 approximation of transformations is relatively successful from the experimental perspective.

129 3.3 Gradient shift

130 However, We can see that the δ in Eq. (3) is uncertain, which is due to the uncontrollable randomness
131 in transformations (e.g., random resizing). We don't want to control for these randomness, but we
132 make a wild assumption which inspired by the derivation in Section 3.2.

133 The start of our understanding of transformations is gradient approximation. Based on this, is there
134 a possibility that the gradients of f_1 and f_2 w.r.t. the same inputs have some geometric relationship,
135 such as translation? If there is a geometric relationship like translation, the problem that "how to
136 obtain a more approximate gradient?" turns into "whether the bias b can be found so that $\nabla_x^1 J(x +$
137 $b, y) \approx \nabla_x^2 J(x, y)$?"

138 Fortunately, after lots of experimental exploration, we finally found b . And b is not a simple trans-
139 lation, since that translation means the gradients will move the same distance and direction for dif-
140 ferent x . There is obviously a more complex relationship between the gradients of different models
141 trained on the same dataset w.r.t. the same inputs. So, we call it "shift". For short, given pre-trained
142 models f_1 , f_2 and input x , the gradient of f_2 w.r.t. x can be obtained by regularly shifting the
143 gradient of f_1 w.r.t. x . In contrast to the linear hypothesis proposed in FGSM, the Gradient shift
144 hypothesis focuses on the relationship between the gradients of different models. In section 4, we
145 show the discipline of the shifting and the calculation formula of b .

146 4 A new transferability enhancement method

147 4.1 Ropeway

148 Given the model f and its loss function J . The $\nabla_x J(x, y)$ denotes the gradient of f w.r.t. x . To
149 compute the bias b (see the notion in section 3.3), we first need to go forward n steps along the
150 direction of the gradient, and preserve these gradients on all steps:

$$\begin{aligned} x'_0 &= x, \\ g'_t &= \nabla_{x'_t} J(x'_t, y), \\ x'_{t+1} &= x'_t + \beta \cdot g'_t, \end{aligned} \quad (4)$$

151 where β is the step size. Then b can be calculated as follow :

$$b = \frac{1}{n+1} \sum_{t=0}^n g'_t. \quad (5)$$

152 Unfortunately, this is obtained through experiments and summaries, rather than strict theoretical
153 derivation. So, it is difficult to theoretically prove the gradient shift hypothesis and Eq. (5), and we
154 have to choose other methods. However, as presentation in Section 3.3, if b could be found, we
155 can use the gradient of the source model to approximate the gradient of the target model. Once
156 approximate successfully, the transferability of adversarial examples will be easily improved, and
157 the gradient shift hypothesis and Eq. (4) will be proved to a some extent as well.

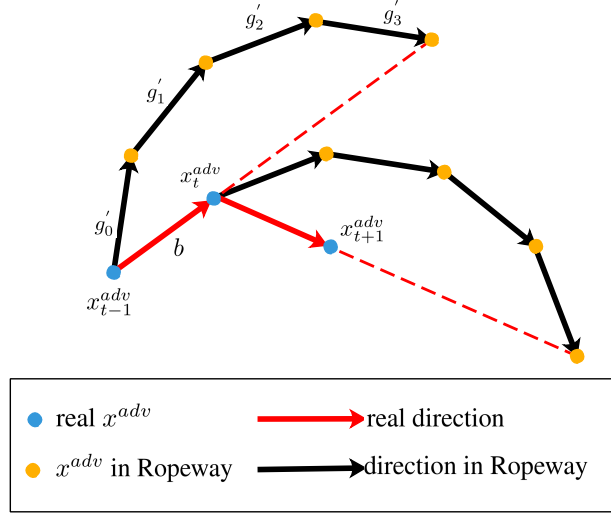


Figure 1: Illustration of the update direction of the adversarial example in Ropeway.

158 It has to be said that, although we simplified FGSM (i.e., Eq. (1)) in the derivation of the gradient
 159 shift hypothesis, this hypothesis is essentially a study of the properties of DNNs rather than a study
 160 of specific attacks. So we can directly apply this to existing attacks to boost the transferability of
 161 adversarial examples. Taking MI-FGSM as an example, we only need to add b to get the new update
 162 formula of x^{adv} :

$$g_t = \mu \cdot g_{t-1} + \frac{b}{\|b\|_1}, \quad (6)$$

$$x_{t+1}^{adv} = x_t^{adv} + \alpha \cdot \text{sign}(g_t), \quad (7)$$

163 where α is the step length and the calculation formula of x'_0 in Eq. (4) should be modified as $x'_0 =$
 164 x_t^{adv} . In order to reduce the number of hyperparameters, β in Eq. (4) is set equal to α in Eq. (7).
 165 From the perspective of process of adversarial examples generation, our proposed method adjust the
 166 current gradient with the gradient of next n steps to obtain a better gradient direction (see Fig. 1),
 167 just like the point go forward along the "Ropeway" between the current position and the end position.
 168 That's why we name this method Ropeway.

169 4.2 Algorithm

170 In fact, Ropeway shows a stronger performance advantage when combined with both input transform
 171 and MI-FGSM. We illustrate it in Algorithm 1 how Ropeway is combined with DIM and MI-FGSM.
 172 In the Ropeway of each iteration (i.e., lines 5-10), we do not clip the perturbation. On the one
 173 hand this is due to the consideration of reducing the amount of computation; on the other hand,
 174 empirically, no clip yields better performance.

175 5 Experimental Results

176 5.1 Experimental Setup

177 **Dataset:** We evaluate on 1,000 images from the ILSVRC 2012 validation set provided by Lin et al.
 178 [6].

179 **Baselines:** We adopt four input transformations as our baselines, i.e., DIM [10], TIM [8], SIM
 180 [6] and DI-Admix which combined with Admix[11] and DIM. All the input transformations are
 181 integrated into MI-FGSM [5].

Algorithm 1 Ropeway combined with DIM and MI-FGSM

```
1: Input: Classifier  $f$ , loss function  $J$ , benign example  $x$ , ground-truth label  $y$ , max perturbation  $\epsilon$ ,  
   number of iterations  $T$ , transformation  $T(\cdot)$  and its probability  $p$ , number of steps in Ropeway  
    $N$   
2: Output: An adversarial example  $x^{adv}$   
3:  $\alpha = \epsilon/T$ ;  $g_0 = 0$ ;  $x_0^{adv} = x$ ;  $n = 0$   
4: for  $t = 0 \rightarrow T - 1$  do  
5:   while  $n \leq N$  do  
6:      $x'_n = x_t^{adv}$   
7:     Transform  $x'_n$  and calculate the gradient:  $g'_n = \nabla_{x'_n} J(T(x'_n, p), y)$   
8:     Save  $g'_n$   
9:     Calculate the  $x'_{n+1}$ :  $x'_{n+1} = x'_n + \alpha \cdot g'_n$   
10:     $n = n + 1$   
11:   end while  
12:   Calculate the bias  $b$  by Eq. (5)  
13:   Update momentum by Eq. (6) with  $b$   
14:   Update  $x_{t+1}^{adv}$  by Eq. (7)  
15:   Clip  $x_{t+1}^{adv}$  with  $x$  and  $\epsilon$   
16: end for  
17: return  $x_T^{adv}$ 
```

182 **Models:** We evaluate adversarial examples on six popular normally trained models and five adversar-
183 ially trained models. Normally trained models are Inception-V3 (Inc-v3) [22], Inception-V4 (Inc-v4)
184 [23], VGG19 (Vgg-19) [24], ResNet-101 (Res-101) [25], ResNet-152 (Res-152) [25] and Iception-
185 ResNet-V2 (IncRes-v2) [23]. Adversarially trained models [26, 27] are Adv-Inc-v3, Ens3-Inc-v3,
186 Ens4-Inc-v3, Adv-IncRes-v2 and Ens-adv-IncRes-v2.

187 **Attack settings:** The maximum perturbation $\epsilon = 16$, number of iteration $T = 10$, step size $\alpha =$
188 $\epsilon/10$ and the momentum decay factor $\mu = 1.0$. We adopt the Gaussian kernel with size 7×7 for
189 TIM, the transformation probability $p = 0.5$ for DIM, and the number of copies $m = 5$ for SIM. We
190 set $m_1 = 5$, $\gamma_i = 1/2^i$, $m_2 = 3$, $\eta = 0.2$ for Admix and $n = 10$, $\beta = \alpha$ for Ropeway.

191 **Other details:** DIM, TIM, SIM, and Admix are all implemented with different versions of Python
192 and TensorFlow, but Ropeway is implemented with PyTorch. For a fair comparison, we do not use
193 the code provided by authors of each model to directly produce adversarial examples. Insteadly, we
194 reference their source code and rewritten all baseline attacks with PyTorch. For the 5 adversarially
195 training models, we are in TensorFlow environment to evaluate the generated adversarial examples.
196 We publish the information of version and library on our codes. All resources are publicly available.

197 5.2 Evaluation on normally trained models

198 Firstly, we evaluate the adversarial examples on 6 normally trained models, namely Inc-v3, Inc-
199 v4, Vgg-19, Res-101, Res-152 and IncRes-v2, with DIM, TIM, SIM, DI-Admix attacks and their
200 Ropeway version. We craft adversaries on 3 normally trained networks, i.e., Inc-v3, Vgg-19 and
201 Res-152, respectively. The attack success rates, namely the misclassification rates on target models,
202 are shown in Table 1. The models attacken are on rows and the models tested are on columns.

203 It can be seen that whichever the attack is, Ropeway outperforms on all tests. Under the white-box
204 attack setting, Ropeway maintains a high attack success rate. Under the black-box attack setting,
205 when the original model is Inc-v3 and the target model is IncRes-v2, the success rate of DIM is
206 62.5%, while that of R-DIM is as high as 81.9%, and that is a tremendous improvement. These
207 experimental data show that Ropeway is very effective in boosting the transferability of adversarial
208 examples, and proves the gradient shift hypothesis to some extent as well.

209 5.3 Evaluation on adversarially trained models

210 In general, adversarially trained models having strong robustness, so we evaluate the performance on
211 adversarially trained models (i.e., Adv-Inc-v3, Ens3-Inc-v3, Ens4-Inc-v3, Adv-IncRes-v2 and Ens-

Table 1: Success rate on normally trained models. The attacks start with "R-" denotes combining with Ropeway. "*" indicates white-box attacks.

model	attack	Inc-v3	Inc-v4	Vgg-19	Res-101	Res-152	IncRes-v2
Inc-v3	DIM	99.6%*	65.8%	70.2%	56.2%	55.6%	62.5%
	R-DIM	99.9%*	84.6%	82.3%	69.5%	70.5%	81.9%
	SIM	99.9%*	68.2%	76.5%	67.3%	68.8%	66.3%
	R-SIM	100%*	74.5%	82.5%	69.5%	73.6%	72.5%
	TIM	99.8%*	49.5%	62.5%	46.7%	48.1%	45.7%
	R-TIM	100%*	63.1%	71.9%	55.9%	57.5%	60.4%
	DI-Admix	100%*	92.9%	93.6%	90.7%	93.1%	92.1%
	R-DI-Admix	100%*	96%	95.7%	92.6%	94.6%	95.6%
	DIM	56.8%	59.5%	100%*	59.1%	57.9%	47.9%
	R-DIM	68.1%	75.6%	100%*	70.3%	69%	60.9%
Vgg-19	SIM	59.8%	58.2%	100%*	68.2%	64.3%	45.4%
	R-SIM	66.1%	68.3%	100%*	71.4%	70.5%	54.1%
	TIM	59.8%	57.9%	100%*	62.9%	61.1%	49.2%
	R-TIM	69.2%	72.2%	100%*	70.5%	66.9%	58.5%
	DI-Admix	79.8%	80.1%	100%*	82.5%	82.8%	68.2%
	R-DI-Admix	84.3%	88.9%	100%*	87.0%	85.3%	77.3%
	DIM	79.9%	76.9%	91.8%	93.7%	100%*	73.5%
	R-DIM	87.5%	85.9%	96.8%	98.8%	100%*	84.7%
	SIM	65.9%	53.4%	80.9%	94.2%	100%*	53.3%
	R-SIM	68.9%	63.7%	87.5%	98.2%	100%*	60.5%
Res-152	TIM	67.8%	60.8%	77.6%	92.7%	100%*	58.9%
	R-TIM	75.8%	69.1%	83.6%	96.2%	100%*	68.5%
	DI-Admix	92.4%	89.9%	97.1%	99.1%	100%*	86.4%
	R-DI-Admix	95.7%	95.4%	99.0%	99.8%	100%*	94.4%

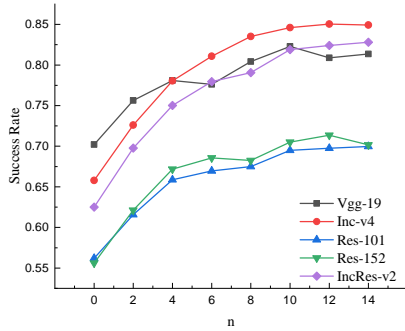
adv-IncRes-v2). Same with Section 5.2, we use 3 original models (i.e., Inc-v3, Vgg-19 and Res-152) to generate adversarial examples and the results are shown in Table 2 (The models attacked are on rows and the models tested are on columns). It can be seen that Ropeway still shows strong performance even in the face of adversarially training models. Among all input transformations attacks, Ropeway has the most significant improvement on DIM, with an average of 11.81 percentage points in 15 experiments. R-DI-Admix has the highest attack success rate, with an average attack success rate as high as 75.89% in 15 experiments.

5.4 Ablation Studies

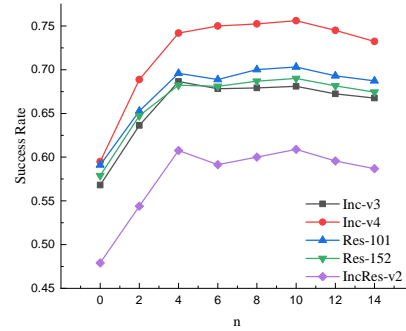
Since we set $\beta = \alpha$, there is only one hyperparameter in Ropeway, i.e., n . The key of Ropeway is n which will directly impact the transferability of adversarial examples. To highlight n , we set different value (i.e., $n = 0, 2, 4, 6, 8, 10, 12, 14$) in the R-DIM attack for a comprehensive comparison. We create adversarial examples on Inc-v3 and Vgg-19 (Fig. 2(a) and Fig. 2(b), respectively), and then evaluate them on other normally trained models (Section 5.1). Because the attack success rate of the white-box attack is almost always 100%, we omit the white-box attack test, and the experimental results are shown in Fig. 2. In the figures, the horizontal axis represents the size of n , and the vertical axis represents the attack success rate. R-DIM degenerates into DIM when $n = 0$ (see Algorithm 1) and the attack success rate has been significantly improved when $n = 2$. The attack success rate increases as n increases where adversarial examples are crafted on Inc-v3 (see Fig. 2(a)) and the inflection point of attack success rate occurs when $n = 10$ where adversarial examples are crafted on Vgg-19 (see Fig. 2(b)). This is why we choose $n = 10$ in this paper.

Table 2: Success rate on adversarially trained models. The attacks start with "R-" denotes combining with Ropeway.

Model	Attack	Adv- Inc-v3	Ens3- Inc-v3	Ens4- Inc-v3	Adv- IncRes-v2	Ens-adv- IncRes-v2
inc-v3	DIM	53.5%	48.1%	44.9%	43.5%	34.6%
	R-DIM	73.8%	65.4%	60.4%	62.4%	48.7%
	SIM	61.9%	56.1%	54.4%	48.6%	38.5%
	R-SIM	66.3%	59.2%	56.6%	55.3%	42.3%
	TIM	42.9%	40.0%	37.7%	36.0%	29.2%
	R-TIM	54.8%	50.6%	47.8%	46.4%	36.8%
	DI-Admix	89.1%	85.8%	83.8%	81.3%	72.0%
	R-DI-Admix	92.3%	90.2%	87.3%	86.6%	75.9%
vgg-19	DIM	38.3%	34.5%	32.3%	28.0%	23.7%
	R-DIM	46.6%	46.2%	37.4%	38.4%	30.7%
	SIM	42.0%	39.9%	36.7%	31.7%	26.7%
	R-SIM	47.0%	45.7%	39.0%	36.8%	31.9%
	TIM	45.9%	43.6%	42.2%	35.9%	32.6%
	R-TIM	52.8%	52.2%	47.9%	43.2%	39.1%
	DI-Admix	60.1%	56.9%	51.4%	49.7%	41.1%
	R-DI-Admix	63.0%	62.1%	53.7%	56.0%	47.0%
res-152	DIM	65.2%	64.6%	59.5%	60.8%	50.9%
	R-DIM	74.8%	75.2%	67.7%	71.0%	60.8%
	SIM	50.6%	48.9%	45.4%	43.5%	37.7%
	R-SIM	57.7%	53.8%	51.0%	49.9%	41.4%
	TIM	57.0%	54.7%	53.0%	50.5%	47.0%
	R-TIM	65.8%	62.7%	60.1%	58.4%	53.7%
	DI-Admix	84.9%	81.5%	77.3%	78.5%	72.9%
	R-DI-Admix	89.1%	88.1%	83.8%	86.2%	77.0%



(a) Inc-v3



(b) Vgg-19

Figure 2: The success rate changes as the changes of n in Ropeway. The adversarial examples are crafted on (a) Inc-v3 and (b) Vgg-19 respectively.

6 Conclusion

In this work, We revisit and explain the nature of common input transformations attack, such as DIM, SIM, TIM and Admix. Inspired by these methods, a hypothesis that the gradient of different models trained on same datasets are related is proposed. Based on this, we proposed a new method called Ropeway which can boost the transferability of adversarial examples without harm the success rate under white-box attacks. Specifically, for each iteration of generating examples, the gradients of next n steps are used to adjust the gradient of current step in Ropeway. Extensive experiments are conducted to demonstrate the superior performance of Ropeway. we hope the gradient shift hypothesis and our attack will provide a new perspective to understand DNNs and the adversarial examples.

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Checklist

1. For all authors...
 - (a) Do the main claims made in the abstract and introduction accurately reflect the paper’s contributions and scope? [\[Yes\]](#)
 - (b) Did you describe the limitations of your work? [\[Yes\]](#) See Section 4.1. The calculation of bias b is derived from experimental experience rather than theoretical derivation.
 - (c) Did you discuss any potential negative societal impacts of your work? [\[N/A\]](#)
 - (d) Have you read the ethics review guidelines and ensured that your paper conforms to them? [\[Yes\]](#)
2. If you are including theoretical results...
 - (a) Did you state the full set of assumptions of all theoretical results? [\[Yes\]](#) See Section 3.2.
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3. If you ran experiments...
 - (a) Did you include the code, data, and instructions needed to reproduce the main experimental results (either in the supplemental material or as a URL)? [\[Yes\]](#) See README.md file in the code provided.
 - (b) Did you specify all the training details (e.g., data splits, hyperparameters, how they were chosen)? [\[Yes\]](#) See Section 5.1.

- 330 (c) Did you report error bars (e.g., with respect to the random seed after running exper-
331 iments multiple times)? [No] Although there is randomness in the experiment, after
332 many experiments we have found that the effect of randomness on the experimental
333 results is only in a very small range and is not a decisive factor.
- 334 (d) Did you include the total amount of compute and the type of resources used (e.g., type
335 of GPUs, internal cluster, or cloud provider)? [Yes] See Section 5.1 and README.md
336 file in the code provided.
- 337 4. If you are using existing assets (e.g., code, data, models) or curating/releasing new assets...
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339 of the existing assets very clearly.
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343 We do not provide supplemental material.
- 344 (d) Did you discuss whether and how consent was obtained from people whose data
345 you're using/curating? [Yes] See Section 5.1. The datasets and models we use are
346 publicly available and can be used to do the work of this paper.
- 347 (e) Did you discuss whether the data you are using/curating contains personally identifi-
348 able information or offensive content? [Yes] The data we used does not contain such
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- 351 (a) Did you include the full text of instructions given to participants and screenshots, if
352 applicable? [N/A]
- 353 (b) Did you describe any potential participant risks, with links to Institutional Review
354 Board (IRB) approvals, if applicable? [N/A]
- 355 (c) Did you include the estimated hourly wage paid to participants and the total amount
356 spent on participant compensation? [N/A]