

## Problem H

# A Hard Problem

Time limit: 20 seconds

Memory limit: 2048 megabytes

### Problem Description

You are given a simple undirected graph consisting of  $n$  nodes and  $m$  edges. The nodes are numbered from 1 to  $n$ , and the edges are numbered from 1 to  $m$ . Node  $i$  has a non-negative integer value  $V_i$  and the weight  $W_{u,v}$  of edge  $\{u, v\}$  is defined as  $\|V_u \oplus V_v\|$  where  $\oplus$  is the exclusive-or operator (equivalent to  $\wedge$  in C) and  $\|x\|$  is the number of set bits in the binary representation non-negative integer  $x$ .

The node values  $V_1, V_2, \dots, V_n$  must satisfy  $q$  constraints. Each of the constraints can be represented as a 5-tuple  $(t, u, i, v, j)$ .

- if  $t = 0$ , then  $\text{getBit}(V_u, i) = \text{getBit}(V_v, j)$
- if  $t = 1$ , then  $\text{getBit}(V_u, i) \neq \text{getBit}(V_v, j)$

where the function  $\text{getBit}(x, i)$  returns the  $(i + 1)$ -th least significant bit of  $x$ . For examples,  $\text{getBit}(11, 0)$  is 1 and  $\text{getBit}(11, 2) = 0$ . In the C programming language,  $\text{getBit}(x, i)$  can be computed by  $((x \gg i) \& 1U)$  if  $x$  is a 32-bit unsigned integer and  $i$  is a non-negative integer at most 31.

Unfortunately, some node values are missing now. Your task is to assign new values to them to minimize  $\sum_{\{u,v\} \in E} W_{u,v}$  without violating any given constraint. Please write a program to help yourself to complete this task.

### Input Format

The input consists of five parts. The first part contains one line, and that line contains two positive integers  $n$  and  $m$ .  $n$  is the number of nodes, and  $m$  is the number of edges. The second part contains  $m$  lines. Each of them contains two integers  $u$  and  $v$ , indicating an edge  $\{u, v\}$  of the given graph. The third part contains one line. That line consists of  $n$  space-separated integers  $x_1, x_2, \dots, x_n$ . For any  $k \in \{1, 2, \dots, n\}$ , if the node value  $V_k$  is missing,  $x_k$  will be  $-1$ ; otherwise,  $V_k$  is  $x_k$ . The fourth part contains one integer  $q$ , indicating the number of constraints. The fifth part contains  $q$  lines, and each of them contains five space-separated integers  $t, u, i, v, j$  indicating that  $(t, u, i, v, j)$  is a constraint.

### Output Format

Output an integer which is the minimum value under the  $q$  constraints. If it is not possible to satisfy all the constraints, output  $-1$ .

### Technical Specification

- $1 \leq n \leq 1000$

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- $1 \leq m \leq 5000$
- $-1 \leq V_i < 2^{16}$
- $0 \leq q \leq 8$
- $t \in \{0, 1\}$
- $0 \leq u, v < n$
- $0 \leq i, j < 16$

**Sample Input 1**

```
4 4
1 3
1 2
3 2
0 3
-1 -1 60091 51514
2
1 2 0 1 5
0 2 6 0 15
```

**Sample Output 1**

```
13
```

**Sample Input 2**

```
3 2
0 1
1 2
-1 -1 -1
2
1 2 0 1 5
0 1 5 2 0
```

**Sample Output 2**

```
-1
```