

## Quantum Computing: Assignment 1 – Linear Algebra & Foundations of Quantum Mechanics

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## 1 ADJOINT OPERATORS – SHEET ONE, QUESTION 4

Consider a finite-dimensional vector space V equipped with an inner product  $(\cdot, \cdot)$ . Suppose A and B are operators in V. Show the following identities

- (a)  $(A^{\dagger})^{\dagger} = A$ .
- (b)  $(AB)^{\dagger} = B^{\dagger} A^{\dagger}$ .
- (c) If *A* and *B* are both Hermitian operators then the commutator C = [A, B] is anti-Hermitian i.e.  $C^{\dagger} = -C$ .
  - 1.1 SOLUTION ADJOINT OPERATORS: SHEET ONE, QUESTION 4

Write your solution here

2 Projection operators – Sheet one, Question 5

Type the question here

2.1 SOLUTION - PROJECTION OPERATORS: SHEET ONE, QUESTION 5

Write your solution here

- ${f 3}$  Measurements and expectation values Sheet two, Question 1 Type the question here
- ${\it 3.1~Solution-Projection~operators:~Sheet~two,~Question~1}$  Write your solution here
- $\mbox{\bf 4 Subspaces of a vector space-Sheet two, Question 3} \label{eq:condition}$  Type the question here
- ${\it 4.1~Solution-Subspaces~of~a~vector~space:~Sheet~two,~Question~3}$  Write your solution here