# **NC State University**

# **Department of Electrical and Computer Engineering**

**ECE 463/563: Fall 2021 (Rotenberg)** 

**Project #1: Cache Design, Memory Hierarchy Design** 

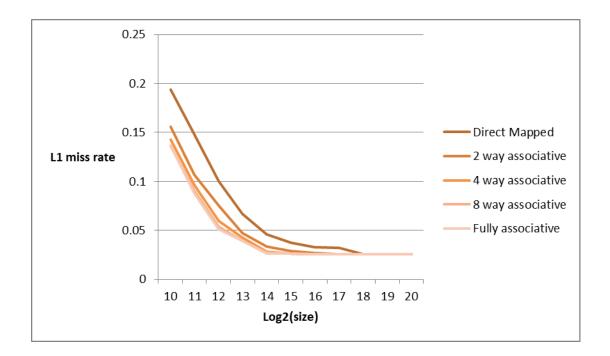
by

### Nandana Balachandran

| NCSU Honor Pledge: "I have neither given nor received unauthorized aid on this project." |
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| Student's electronic signature:Nandana   |
| Course number:563  |

#### Graph 1:

| Direct     |  |  |   |   | Fully   |
|------------|--|--|---|---|---|
| Log2(Size) | Mapped   | 2 way  | 4 way   | 8 way   | associative   |
| 10         | 0.1935   | 0.156  | 0.1427  | 0.1363  | 0.137   |
| 11         | 0.1477   | 0.1071   | 0.0962  | 0.0907  | 0.088   |
| 12         | 0.1002   | 0.0753   | 0.0599  | 0.0536  | 0.0512  |
| 13         | 0.067  | 0.0473   | 0.0425  | 0.0395  | 0.0394  |
| 14         | 0.0461   | 0.0338   | 0.0283  | 0.0277  | 0.0263  |
| 15         | 0.0377   | 0.0288   | 0.0264  | 0.0262  | 0.0262  |
| 16         | 0.0329   | 0.0271   | 0.0259  | 0.0259  | 0.0259  |
| 17         | 0.0323   | 0.0259   | 0.0258  | 0.0258  | 0.0258  |
| 18         | 0.0258   | 0.0258   | 0.0258  | 0.0258  | 0.0258  |
| 19         | 0.0258   | 0.0258   | 0.0258  | 0.0258  | 0.0258  |
| 20         | 0.0258   | 0.0258   | 0.0258  | 0.0258  | 0.0258  |
|            | 10<br>11<br>12<br>13<br>14<br>15<br>16<br>17<br>18 | Log2(Size) Mapped   10 0.1935   11 0.1477   12 0.1002   13 0.067   14 0.0461   15 0.0377   16 0.0329   17 0.0323   18 0.0258   19 0.0258 | Log2(Size) Mapped 2 way   10 0.1935 0.156   11 0.1477 0.1071   12 0.1002 0.0753   13 0.067 0.0473   14 0.0461 0.0338   15 0.0377 0.0288   16 0.0329 0.0271   17 0.0323 0.0259   18 0.0258 0.0258   19 0.0258 0.0258 | Log2(Size) Mapped 2 way 4 way   10 0.1935 0.156 0.1427   11 0.1477 0.1071 0.0962   12 0.1002 0.0753 0.0599   13 0.067 0.0473 0.0425   14 0.0461 0.0338 0.0283   15 0.0377 0.0288 0.0264   16 0.0329 0.0271 0.0259   17 0.0323 0.0259 0.0258   18 0.0258 0.0258 0.0258   19 0.0258 0.0258 0.0258 | Log2(Size) Mapped 2 way 4 way 8 way   10 0.1935 0.156 0.1427 0.1363   11 0.1477 0.1071 0.0962 0.0907   12 0.1002 0.0753 0.0599 0.0536   13 0.067 0.0473 0.0425 0.0395   14 0.0461 0.0338 0.0283 0.0277   15 0.0377 0.0288 0.0264 0.0262   16 0.0329 0.0271 0.0259 0.0259   17 0.0323 0.0259 0.0258 0.0258   18 0.0258 0.0258 0.0258 0.0258   19 0.0258 0.0258 0.0258 0.0258 |

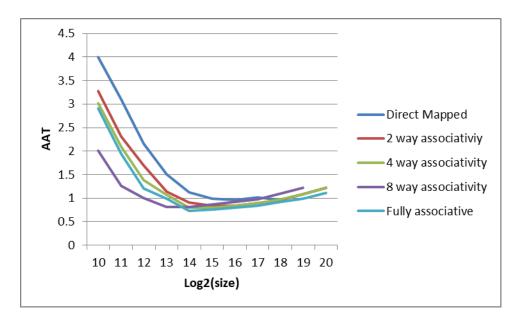


- 1. At a given time, when the associativity is constant and cache size increases, the miss rate decreases to reach a point where the conflict and compulsory misses are completely eliminated. The only miss that remains is the compulsory miss. Similarly, for a given cache size, increase in associativity tends to a decrease in the miss rate. The only miss cases remaining in this case will be that of compulsory and capacity miss and conflict miss is completely eliminated.
- 2. The compulsory miss rate is 0.0258 for all the set associativity.

3. The conflict miss rate is approximately 0.1935 for direct mapped, 0.156 for 2 way associative, 01427 for 3 way set associative, 0.137 for 8 way set associative and 0.137 for fully associative.

## Graph 2:

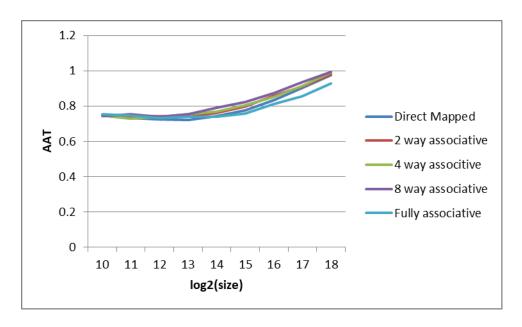
|       |            | Direct   |          |          |          |             |
|-------|------------|----------|----------|----------|----------|-------------|
| Size  | Log2(Size) | Mapped   | 2 way    | 4 way    | 8 way    | associative |
| 1KB   | 10         | 4.004147 | 3.275929 | 3.01509  |          | 2.909184    |
| 2KB   | 11         | 3.09786  | 2.314401 | 2.088116 | 2.003756 | 1.945315    |
| 4KB   | 12         | 2.161025 | 1.694661 | 1.389675 | 1.266425 | 1.212068    |
| 8KB   | 13         | 1.51053  | 1.144925 | 1.065423 | 1.006861 | 0.990521    |
| 16KB  | 14         | 1.125027 | 0.903297 | 0.802766 | 0.811124 | 0.734238    |
| 32KB  | 15         | 0.991123 | 0.841326 | 0.80189  | 0.815131 | 0.75136     |
| 64KB  | 16         | 0.955917 | 0.845437 | 0.840071 | 0.861803 | 0.796871    |
| 128KB | 17         | 1.01603  | 0.895193 | 0.89886  | 0.919816 | 0.841066    |
| 256KB | 18         | 0.962392 | 0.964509 | 0.976265 | 0.977505 | 0.914589    |
| 512KB | 19         | 1.082031 | 1.086324 | 1.082998 | 1.096757 | 0.994308    |
| 1MB   | 20         | 1.21796  | 1.224626 | 1.218187 | 1.224399 | 1.107054    |
|       |            |          |          |          |          |             |



The minimum AAT that is achieved is "0.734238" which is for fully associative set for 16 KB cache size.

## Graph 3:

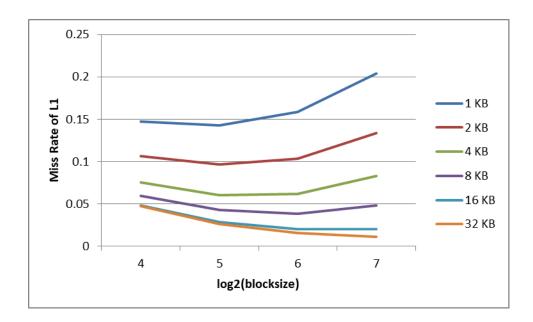
|       |            | Direct   |          |          |          | Fully       |
|-------|------------|----------|----------|----------|----------|-------------|
| Size  | Log2(Size) | Mapped   | 2 way    | 4 way    | 8 way    | associative |
| 1KB   | 10         | 0.745902 | 0.749466 | 0.748196 | 0.744785 | 0.753767    |
| 2KB   | 11         | 0.733428 | 0.742417 | 0.728907 | 0.752155 | 0.746537    |
| 4KB   | 12         | 0.724153 | 0.743809 | 0.739117 | 0.738589 | 0.731536    |
| 8KB   | 13         | 0.721586 | 0.740071 | 0.75513  | 0.754198 | 0.740874    |
| 16KB  | 14         | 0.744158 | 0.761826 | 0.768901 | 0.788611 | 0.73903     |
| 32KB  | 15         | 0.774374 | 0.79789  | 0.80548  | 0.821643 | 0.757872    |
| 64KB  | 16         | 0.832299 | 0.858382 | 0.852443 | 0.875372 | 0.811065    |
| 128KB | 17         | 0.90395  | 0.908554 | 0.913777 | 0.934733 | 0.855983    |
| 256KB | 18         | 0.976894 | 0.979011 | 0.991182 | 0.992422 | 0.929506    |



- 1. The configurations that yield AAT values close to the best value observed in Graph 2 is 0.731536 for the fully associative for a cache size of 4KB.
- 2. The lowest AAT value for L2 is 0.721586 for direct mapped cache with cache size of 8KB. This value is 0.00995 lesser than the minimum value of L1.
- 3. The total area under the graph for the optimal value of Graph 1 is 0.063446019 and for Graph 2 and for the Graph 1, it is 0.053293238.

#### Graph 4:

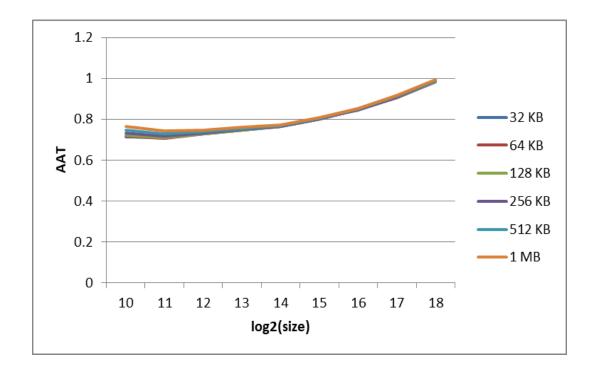
| Size                 | Log2(Blocksize) | 1KB    | 2KB    | 4KB    | 8KB     | 16KB   | 32KB   |
|----------------------|-----------------|--------|--------|--------|---------|--------|--------|
|                      |                 |        |        |        |         |        |        |
| BLOCK SIZE 16        | 4               | 0.1473 | 0.1062 | 0.0755 | 0.0595  | 0.0482 | 0.0475 |
| <b>BLOCK SIZE 32</b> | 5               | 0.1427 | 0.0962 | 0.0599 | 0.04285 | 0.0283 | 0.0264 |
| BLOCK SIZE 64        | 6               | 0.1584 | 0.1033 | 0.0619 | 0.0386  | 0.0204 | 0.0156 |
| BLOCK SIZE 128       | 7               | 0.2036 | 0.1334 | 0.083  | 0.0483  | 0.0198 | 0.0111 |



1. The smaller cache size gives a more optimal value for smaller block size however, the larger cache sizes give a better value for larger block size. The larger block size will result in fewer unique blocks as compared to smaller blocks and so it will have lesser compulsory misses and the trade off is between hits on consecutive bytes and non-consecutive bytes. Yes, as the block size increases from 16 to 128, the tradeoff between exploiting more spatial locality vs. increasing cache polution is evident in the graph. The tradeoff is less relevant for the larger cache size because cache pollution is less impactful on larger block size.

## Graph 5:

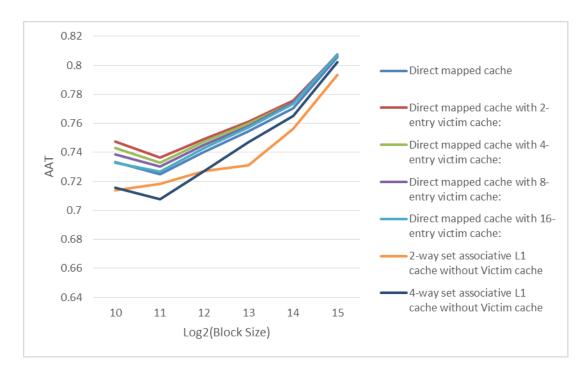
| Size  | 32KB     | 64KB     | 128 KB   | 256 KB   | 512KB    | 1MB      | Log2(Size) |
|-------|----------|----------|----------|----------|----------|----------|------------|
| 1KB   | 0.715752 | 0.715815 | 0.722946 | 0.731179 | 0.748196 | 0.76641  | 10         |
| 2KB   | 0.709742 | 0.707658 | 0.711885 | 0.717435 | 0.728907 | 0.741186 | 11         |
| 4KB   | 0.730435 | 0.72697  | 0.728518 | 0.731974 | 0.739117 | 0.746763 | 12         |
| 8KB   | 0.751447 | 0.747194 | 0.74761  | 0.750061 | 0.75513  | 0.760554 | 13         |
| 16KB  | 0.769179 | 0.765039 | 0.763893 | 0.765526 | 0.768901 | 0.772513 | 14         |
| 32KB  | 0.8042   | 0.802461 | 0.800809 | 0.802332 | 0.80548  | 0.80885  | 15         |
| 64KB  | 0.84593  | 0.846514 | 0.84786  | 0.847308 | 0.850385 | 0.853678 | 16         |
| 128KB | 0.906304 | 0.907663 | 0.909212 | 0.9107   | 0.913777 | 0.91707  | 17         |
| 256KB | 0.983709 | 0.985068 | 0.986617 | 0.988105 | 0.991182 | 0.994475 | 18         |



- 1. The memory hierarchy that yields the best AAT is for cache size of 64KB and block size of 2KB and the value is 0.707658.
- 2. The smallest total area that produces an AAT within 5% of the best AAT is an area of 0.0187 for 2KB block size and cache size of 32KB.

#### Graph 6:

|      |          | Direct   | Direct   | Direct   | Direct   |             |             |                 |
|------|----------|----------|----------|----------|----------|-------------|-------------|-----------------|
|      |          | mapped   | mapped   | mapped   | mapped   | 2-way set   | 4-way set   |                 |
|      |          | cache    | cache    | cache    | cache    | associative | associative |                 |
|      |          | with 2-  | with 4-  | with 8-  | with 16- | L1 cache    | L1 cache    |                 |
|      | Direct   | entry    | entry    | entry    | entry    | without     | without     |                 |
|      | mapped   | victim   | victim   | victim   | victim   | Victim      | Victim      |                 |
|      | cache    | cache:   | cache:   | cache:   | cache:   | cache       | cache       | Log2(Blocksize) |
| Size | AAT      | AAT      | AAT      | AAT      | AAT      | AAT         | AAT         |                 |
| 1KB  | 0.73324  | 0.747407 | 0.742932 | 0.73858  | 0.733045 | 0.713754    | 0.715815    | 10              |
| 2KB  | 0.725022 | 0.736409 | 0.73284  | 0.73012  | 0.726645 | 0.71833     | 0.707658    | 11              |
| 4KB  | 0.740499 | 0.74936  | 0.747643 | 0.745438 | 0.743124 | 0.727327    | 0.72697     | 12              |
| 8KB  | 0.754399 | 0.761151 | 0.75983  | 0.758282 | 0.757403 | 0.731049    | 0.747194    | 13              |
| 16KB | 0.770328 | 0.775728 | 0.774491 | 0.774291 | 0.773491 | 0.756399    | 0.765039    | 14              |
| 32KB | 0.805611 | 0.807192 | 0.807024 | 0.807641 | 0.807163 | 0.793496    | 0.802461    | 15              |



- 1. Adding a Victim Cache to a direct-mapped L1 cache does yield performance comparable to a 2-way set-associative L1 cache of the same size. The cache size of 2 KB 16- entry victim cache.
- 2. The best AAT is for 2KB cache size for 4-way set associative cache without victim cache.
- 3. The smallest total area is for 1KB cache size which has a AAT value of 0.715815 and total area of 0.015115.