```cpp
// 幾何ライブラリ 2次元ベクトル内積/外積 線分距離 直線交点 凸包 円
#include <bits/stdc++.h>

using namespace std;

using ll = long long;
using vi = vector<int>;
using vll = vector<ll>;
using vvi = vector<vector<int>>;
using vvl = vector<vector<ll>>;

double eps = 0.0000001;
// asin(1.) * 2
double pi = 3.14159265358979323846264338327950288;
using p2 = complex<double>;
// x: real
// y: imag

double det(p2 v1, p2 v2) {
  return v1.real() * v2.imag() - v1.imag() * v2.real();
}

double dot(p2 v1, p2 v2) {
  return v1.real() * v2.real() + v1.imag() * v2.imag();
}

double dist2(p2 v) {
  return dot(v, v);
}

double dist(p2 v) {
  return sqrt(dist2(v));
}

bool same(double x, double y) { return abs(x - y) < eps; }

double dist2(p2 l1, p2 l2) { return dot(l1 - l2, l1 - l2); }

double dist(p2 l1, p2 l2) {
  return sqrt(dist2(l1, l2));
}

int ccw(p2 a, p2 b, p2 c) {
  b -= a;
  c -= a;
  if (det(b, c) > eps)return 1;
  if (det(b, c) < -eps) return -1;
  if (dot(b, c) < -eps) return 2;
  if (dist2(b) < dist2(c)) return -2;
  return 0;
```

```
 51  }
 52
 53  auto p2comp = [](const p2 &l, const p2 &r) {
 54    if (abs(l.real() - r.real()) > eps)
 55      return l.real() < r.real();
 56    return l.imag() < r.imag();
 57  };
 58
 59  struct Line {
 60    p2 st, ed;
 61
 62    Line(p2 st, p2 ed) : st(st), ed(ed) {}
 63
 64    Line(double x1, double y1, double x2, double y2)
 65        : st(p2(x1, y1)), ed(p2(x2, y2)) {}
 66
 67    Line(p2 st, double x, double y) : st(st), ed(p2(x, y)) {}
 68
 69    Line(double x, double y, p2 ed) : st(p2(x, y)), ed(ed) {}
 70
 71    double dist() { return sqrt(dist2(st, ed)); }
 72
 73    bool isPalla(Line l) { return abs(det(ed - st, l.ed - l.st)) < eps; }
 74
 75    double x() { return ed.real() - st.real(); }
 76
 77    double y() { return ed.imag() - st.imag(); }
 78
 79    p2 v() { return ed - st; }
 80  };
 81
 82  // l1.st + (l1.st - l1.ed) * r.first = l2.st + (l2.st - l2.ed) * r.second
 83  // 方程式を満たす(r.first, r.second)を返す
 84  // l1.isPalla(l2) => (nan, nan)
 85  pair<double, double> interP(Line l1, Line l2) {
 86    double a = l1.x();
 87    double b = -l2.x();
 88    double c = l1.y();
 89    double d = -l2.y();
 90    double inv = 1. / (a * d - c * b);
 91    double e1 = -l1.st.real() + l2.st.real();
 92    double e2 = -l1.st.imag() + l2.st.imag();
 93    return make_pair((d * e1 - b * e2) * inv, (-c * e1 + a * e2) * inv);
 94  }
 95
 96  bool intersec(Line l1, Line l2) {
 97    if (l1.isPalla(l2))
 98      return false;
 99    auto r = interP(l1, l2);
100    return eps < r.first && r.first < 1. - eps && eps < r.second &&
```

```
101         r.second < 1. - eps;
102 }
103
104 double inter_r(Line l, p2 c) {
105   p2 a = l.st, b = l.ed;
106   return dot(a - c, l.v()) / dist2(l.v());
107 }
108
109 double dist(Line l, p2 c) {
110   double r = inter_r(l, c);
111   if (r < -eps) return dist(l.st, c);
112   if (1. + eps < r) return dist(l.ed, c);
113   return dist(l.st + l.v() * r, c);
114 }
115
116 p2 nearest(Line l, p2 c) {
117   double r = inter_r(l, c);
118   if (r < -eps) return l.st;
119   if (1. + eps < r) return l.ed;
120   return l.st + l.v() * r;
121 }
122
123 double dist(Line l1, Line l2) {
124   return min(min(dist(l1, l2.st), dist(l1, l2.ed)), min(dist(l2, l1.st), dist(l2, l1.ed)));
125 }
126
127 struct Poly {
128   vector<p2> ps;
129   double d;
130
131   Poly(vector<p2> ps) : ps(ps) {
132     d = 0;
133     for (int i = 0; i < ps.size(); i++) d += dist(ps[i], ps[(i + 1) % ps.size()]);
134   }
135
136   // 頂点上/辺上は微妙
137   bool include(p2 p) {
138     // 半直線
139     Line l(p, p2(-10000, -1));
140     int c = 0;
141     for (int i = 0; i < ps.size(); i++) {
142       if (intersec(l, Line(ps[i], ps[(i + 1) % ps.size()]))) c++;
143     }
144     return c % 2 == 1;
145   }
146
147   bool include(p2 p, bool on_vert, bool on_edge) {
148     for (auto &q : ps) if (dist(p, q) < eps) return on_vert;
149     for (int i = 0; i < ps.size(); i++) {
150       if (ccw(ps[i], ps[(i + 1) % ps.size()], p) == 0) return on_edge;
```

```
151     }
152     return include(p);
153   }
154
155   bool intersecl(Line l) {
156     for (int i = 0; i < ps.size(); i++) {
157       if (intersec(l, Line(ps[i], ps[(i + 1) % ps.size()])))
158         return true;
159     }
160     return false;
161   }
162 };
163
164 struct Circle {
165   p2 p;
166   double r;
167
168   Circle(p2 p, double r) : p(p), r(r) {}
169
170   bool include(p2 l) { return dist2(p, l) < r * r + eps; }
171
172   // 円同士の交点
173   // 存在すれば2つ
174   vector<p2> intersec(Circle c) {
175     p2 diff = c.p - p;
176     double dist = dot(diff, diff);
177     double a = (dist + r * r - c.r * c.r) / 2.;
178     double D = dist * r * r - a * a;
179     if (D < eps)
180       return vector<p2>();
181     double Dsqrt = sqrt(D);
182     vector<p2> ps;
183     ps.emplace_back((a * diff.real() + diff.imag() * Dsqrt) / dist + p.real(),
184                     (a * diff.imag() - diff.real() * Dsqrt) / dist + p.imag());
185     ps.emplace_back((a * diff.real() - diff.imag() * Dsqrt) / dist + p.real(),
186                     (a * diff.imag() + diff.real() * Dsqrt) / dist + p.imag());
187     return ps;
188   }
189 };
190
191 // 半時計回り
192 struct ConX {
193   vector<p2> ps;
194
195   // graham scan
196   // ref: プログラミングコンテストチャレンジブック p233
197   ConX(vector<p2> v) {
198     sort(v.begin(), v.end(), p2comp);
199
200     int k = 0, n = v.size();
```

```
201     ps.resize(n * 2);
202     for (int i = 0; i < n; i++) {
203       while (k > 1 && det(ps[k - 1] - ps[k - 2], v[i] - ps[k - 1]) < eps)
204         k--;
205       ps[k++] = v[i];
206     }
207     for (int i = n - 2, t = k; i >= 0; i--) {
208       while (k > t && det(ps[k - 1] - ps[k - 2], v[i] - ps[k - 1]) < eps)
209         k--;
210       ps[k++] = v[i];
211     }
212     ps.resize(k - 1);
213   }
214
215   Poly toPoly() {
216     return Poly(ps);
217   }
218
219   size_t size() { return ps.size(); }
220 };
221
222 int n;
223 vector<double> rs;
224 vector<p2> ps;
225 vector<Circle> cs;
226
227 bool f(double l) {
228   cs.clear();
229   for (int i = 0; i < n; i++) {
230     double rr = rs[i] * rs[i] - l * l;
231     if (rr < eps)
232       return false;
233     cs.emplace_back(ps[i], sqrt(rr));
234   }
235   vector<p2> may;
236   for (int i = 0; i < n; i++) {
237     may.push_back(cs[i].p);
238     for (int j = i + 1; j < n; j++) {
239       auto v = cs[i].intersec(cs[j]);
240       if (v.size() == 0)
241         continue;
242       may.push_back(v[0]);
243       may.push_back(v[1]);
244     }
245   }
246   for (auto &p : may) {
247     bool ok = true;
248     for (auto &c : cs) {
249       if (!c.include(p)) {
250         ok = false;
```

```
251         break;
252       }
253     }
254     if (ok)
255       return true;
256   }
257   return false;
258 }
259
260 int main() {
261   printf("%.20lf\n", asin(1.) * 2);
262   cin.tie(nullptr);
263   ios::sync_with_stdio(false);
264   Poly p(vector<p2>({p2(0, 0), p2(1, 0.5), p2(2, 0), p2(2, 2), p2(1, 1.5), p2(0, 2)})
      );
265   vector<double> xy({-1, 0, 1, 2, 3});
266   for (auto &x : xy)
267     for (auto &y : xy) {
268       cerr << x << " " << y << " " << (p.include(p2(x, y), true, true) ? "YES" : "NO")
      << endl;
269     }
270
271   return 0;
272 }
273
```