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SCHOOL OF SCIENCE & TECHNOLOGY

A thesis submitted for the degree of

Master of Science (MSc) in Information and Communication Systems

OCTOBER 2012

THESSALONIKI – GREECE



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Abstract

This dissertation was written as a part of the MSc in ICT Systems at the International Hellenic University. Here goes a summary of the dissertation (1-2 paragraphs). Add one last paragraph acknowledging the supervisor and the people who contributed (collaborators, other scientists, etc.). Abstract length should not exceed one page.

Summarize the problem of manual eligibility verification, the proposed Neuro-Symbolic pipeline solution, the experimental comparisons and the critical findings.

Student Name Date

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1 Introduction

An idea I wrote, not sure if it fits here: Consider this analogy: Building a neuro-symbolic pipeline for public administration is akin to building a high-speed railway between two distinct cultures. The LLM acts as the versatile translator and engineer who interprets the local landscape (unstructured text), while the intermediate YAML or JSON models serve as the blueprints and tracks. The Knowledge Graph is the rigid, reliable station where everyone must follow specific rules (logic). Currently, we have built successful short-distance test tracks (prototypes), but the challenge remains in connecting the entire national network while ensuring the trains (data) always run on time and stay on the correct side of the tracks (normative compliance).

Another nice Analogy: If Descriptive QA is like asking a librarian to find a specific book (retrieval), then Prescriptive synthesis is like asking a lawyer to write a set of building codes (rule-making). In the descriptive case, the model translates a search request into a precise map of the library. In the prescriptive case, the model must understand the underlying intent of a policy and translate it into a rigid framework of "if-then" laws that govern future actions.

And another Analogy: Validating a neuro-symbolic system is like inspecting a bridge built by a highly creative but occasionally distracted architect. Probabilistic methods are like counting how many cars successfully cross the bridge (F1 scores), while deterministic methods are like a safety inspector using a physical measuring tape to ensure the steel beams meet code (SHACL/OBQC). Currently, we are very good at checking if the bridge stands up once (static validation), but we lack a way to simulate an earthquake or a flood (mutation testing) to ensure the architect's logic doesn't fail under pressure.

1.1 Background and Motivation

The burden of manual bureaucracy in public administration and the potential of AI to automate legislative interpretation.

Why is this work important?

1.2 Problem Statement

the challenge of bridging unstructured text with deterministic validation logic while mitigating LLM hallucinations.

1.3 Objectives

the specific goals of building a Text-to-SHACL pipeline and evaluating its semantic accuracy and operational feasibility.

1.4 Dissertation Structure

Outline of the organization of the subsequent chapters and the logical flow of the research.

2 Systematic Literature Review

This chapter details a Systematic Literature Review (SLR) with the goal to establish the necessary theoretical foundations of Neuro-Symbolic AI.

2.1 Introduction

We approach the current research in Neuro-Symbolic AI specifically focusing on how Large Language Models (LLMs) and Knowledge Graphs (KGs) are combined. We aim to find existing approaches for extracting rules from text and generating formal logic (with a particular focus on SPARQL and SHACL), as well as methods of evaluating the results of such a process.

2.2 Methodology

To ensure scientific strictness and reproducibility, the review adheres to the PRISMA (Preferred Reporting Items for Systematic reviews and Meta-Analyses) guidelines. The process was structured into four phases. First, we defined specific Research Questions (RQs). Second, we executed an automated search strategy on the *Scopus* database. Third, we applied a two-stage screening process: an initial "practical" screening of only titles and abstracts, and then a more thorough "quality assessment" screening of the full texts. This phase utilized specific inclusion/exclusion criteria and quality assessment criteria. Finally, data was extracted from the selected primary studies into a standardized matrix to synthesize key themes and composed into a thematic analysis.

2.2.1 Research Questions

To achieve our objective, we defined three Research Questions that guided the data extraction and synthesis process:

- **RQ1:** How are Large Language Models (LLMs) currently utilized to extract structured knowledge and conditional rules from unstructured text?
- **RQ2:** What are the state-of-the-art approaches for translating natural language requirements into executable constraint languages (specifically SHACL and SPARQL)?
- **RQ3:** What methodologies exist for evaluating the functional correctness and operational stability of LLM-generated logic?

RQ1 explores the initial phase of the proposed pipeline (Text-to-Graph), while **RQ2** focuses

on the core challenge of logic generation. **RQ3** allows us to examine how existing studies critically evaluate trust and correctness.

2.2.2 Search Strategy

To identify relevant records, we conducted an automated search on the *Scopus* database. Scopus was selected as the source due to its extensive coverage of academic literature. The search was executed on the 1st of December 2025. The search query was formulated to find the intersection of Generative AI and Semantic Web technologies. We employed Boolean logic to combine three conceptual blocks:

1. **Generative AI Terms:** ("Large Language Model" OR "LLM")
2. **Target Logic:** ("SHACL" OR "SPARQL")
3. **Symbolic Terms:** ("Semantic Web" OR "Knowledge Graph")

These blocks were combined using the AND operator. Thus, the final search string applied to the Title, Abstract, and Keywords fields was:

```
( "Large Language Model" OR "LLM" ) AND  
( "SHACL" OR "SPARQL" ) AND  
( "Semantic Web" OR "Knowledge Graph" )
```

We also applied some necessary metadata filters during this phase:

- **Language:** Only papers written in English were considered.
- **Document Type:** We restricted the search to Articles and Conference Papers, excluding trade journals and errata.

Interestingly, despite the Date Range not being restricted, all results fell in the range of years 2023–2026. This could be an indication that the application of Large Language Models to formal constraint languages like SHACL is a newly emerging field, that appeared primarily after the widespread adoption of "GPT-4 class" models.

The described search strategy yielded an initial set of 125 candidates which, after removing 3 duplicates, were then subjected to the screening process described next.

2.2.3 Inclusion/Exclusion Criteria

We established a set of inclusion and exclusion criteria that reflect the focus of this review. These were applied to Titles and Abstracts during the initial "Practical Screening" phase of the 122 records. Table 2.1 summarizes the criteria used. This screening process excluded 61 papers from the review. The rest were sought for retrieval from official channels. Of the 61 papers sought, 8 could not be retrieved due to access restrictions (paywall). The remaining 53 were downloaded and assessed for eligibility by reading the full text. In this "Quality Screening" phase, we applied a second set of quality exclusion criteria (QE), with the goal to further focus our scope and increase relevance to this study.

Table 2.1: Inclusion and Exclusion Criteria

| Category | Inclusion Criteria | Exclusion Criteria |
|--------------------|--|---|
| Task Focus | Text-to-Graph extraction, Text-to-SPARQL, SHACL shapes generation, GraphRAG architectures. | Pure NLP (summarization), low-level graph mechanics (Entity Alignment, Link Prediction, Subgraph Extraction), Dataset creation. |
| Methodology | Neuro-Symbolic architectures, Prompt Engineering for logic generation, Fine-tuning, Evaluation Frameworks for Semantic Accuracy. | Traditional Machine Learning (non-generative), Reinforcement Learning without LLMs. |
| Data Flow | <i>Forward:</i> Transforming unstructured text into formal logic or structured data (Text \rightarrow Logic). | <i>Reverse:</i> Transforming structured data into natural language (Verbalization/Explanation). |
| Mode | Textual inputs with or without pre-processing. | Multimodal studies (Speech/Image), Computer Vision, Temporal Data. |
| Type | Peer-reviewed Articles and Conference Papers. | Conference Proceedings (Meta-entries), Posters, Editorials, Preliminary Results. |

- **QE1 (Domain & Logic Mismatch):** From articles situated in descriptive scientific domains (e.g., bioinformatics, chemistry), exclude those where the knowledge structure is purely factual or relational rather than normative or rule-based, offering low transferability to eligibility logic.
- **QE2 (Complexity & Task Focus):** From studies focusing on simple factoid Question Answering (KGQA), exclude those that do not analyze the extraction or generation of complex conditional constraints (if-then-else logic) required for compliance or eligibility.
- **QE3 (Methodological Maturity):** From studies limited to model-vs-model benchmarking or evaluation of existing datasets, exclude those that do not propose novel neuro-symbolic pipeline architectures or logic-validation frameworks.

Following this quality assessment, 28 papers were excluded from the review (13 due to QE1, 6 due to QE2 and 9 due to QE3), leaving 25 papers to be included.

2.3 Results

From an initial set of 125 records, 25 studies were identified as meeting all eligibility criteria.

2.3.1 PRISMA Flow Diagram

The search and screening process can be summarized in the PRISMA flow diagram (Figure 2.1).

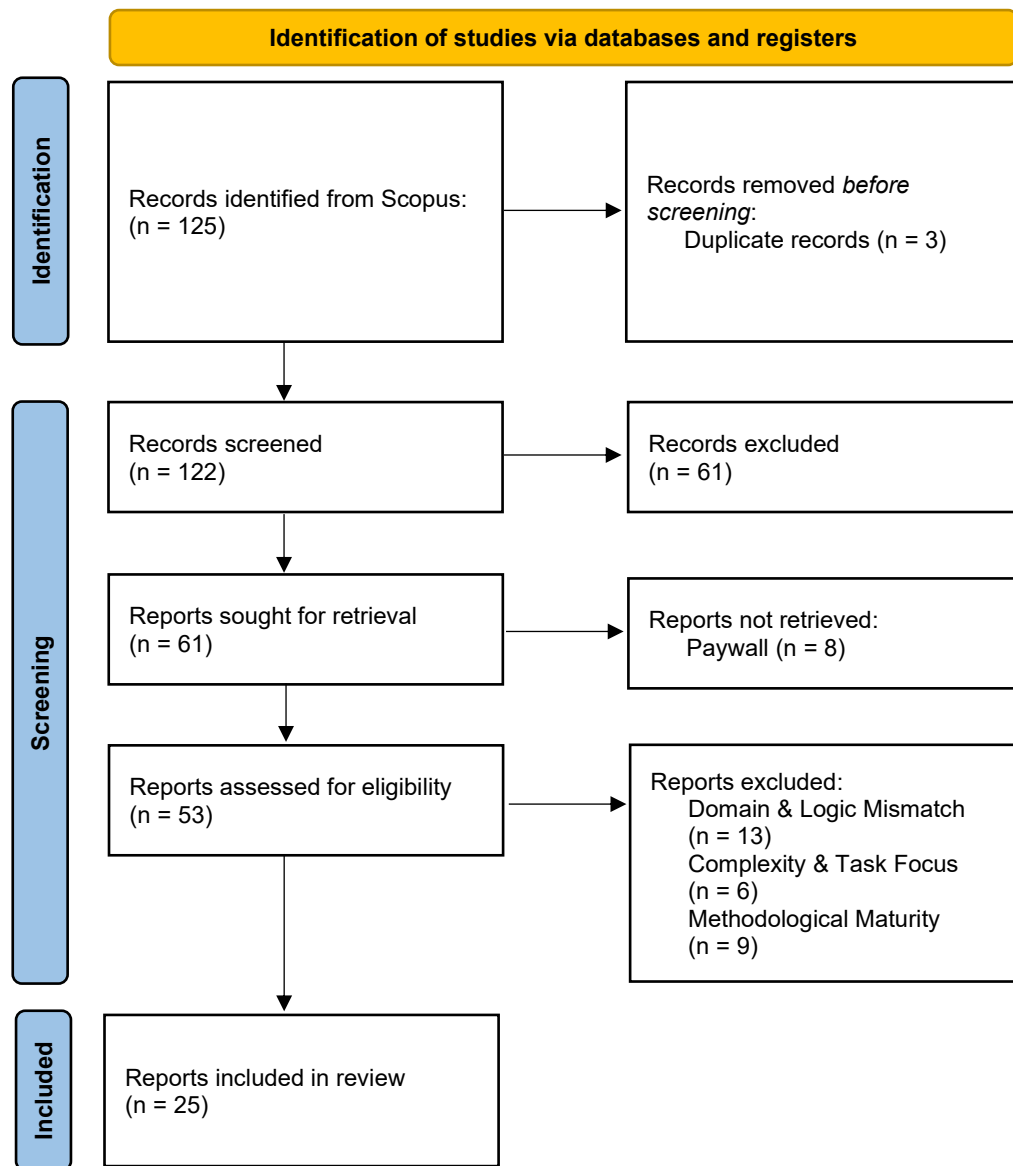


Figure 2.1: PRISMA Flow Diagram of the selection process

2.3.2 Data Extraction

Table 2.2 presents the data extraction summary for the 25 included studies. The studies are categorized thematically, to reflect the research trajectory: from domain-specific applications in public administration and normative compliance, through the intricate technical mechanisms of logic synthesis, to the frameworks of validation and architectural trust.

Table 2.2: Final Synthesis Matrix of Included Studies ($n = 25$)

| Study | Core Task / Do-main | Logic | Neuro-Symbolic Inte-gration | Validation Method |
|---|-----------------------------------|----------------|--|-------------------------------------|
| <i>Category 1: Public Administration & Normative Compliance</i> | | | | |
| Konstantinidis (2025) [1] | Recommendation (Public Services) | RDF, SHACL | LLM extraction, SHACL validation | Human Expert As-sessment |
| Oranekwu (2026) [2] | Cybersecurity Compliance (IoT) | OWL, SPARQL | Ontology-driven RAG | Similarity over ground truth |
| Spyropoulos (2025) [3] | Entity Mining (Po-lice Reports) | RDF, OWL | LLM Entity Extraction & linking | Visual and SPARQL Verification |
| Hanuragav (2025) [4] | CSR Validation (Medical) | SHACL, SPARQL | RTF to JSON to RDF with YAML mapper | SHACL (structure), SPARQL (content) |
| <i>Category 2: Automated Logic Synthesis & Semantic Parsing</i> | | | | |
| Agarwal (2024) [5] | Complex QA (KGQA) | KoPL | SymKGQA: Symbolic Program Generation | Hits@1 and F1 on Benchmarks |
| Avila (2025) [6] | Scientific QA (KGQA) | SPARQL | Text-to-SPARQL with RAG + Few-shot ICL | F1 on Benchmarks |
| Jiang (2025) [7] | Multi-KG Gener-alization (KGQA) | SPARQL | Semantic sketch + KG population | Hits@1 and F1 on Benchmarks |
| Shah (2024) [8] | Multi-hop QA (KGQA) | Cypher, SPARQL | Text-to-Logic with Few-shot + CoT | Match Accuracy on Benchmarks |
| Walter (2026) [9] | Reasoning / QA (Multi-domain) | SPARQL | Zero-shot Iterative Agent KG exploration | F1 on Benchmarks |
| Soularidis (2024) [10] | Rule Generation (Search & Rescue) | SWRL | Ontology-driven Text-to-SWRL | F1 on Human Expert |
| Lehmann (2023) [11] | Semantic Parsing (Wikidata) | CNL, SPARQL | Controlled Natural Language to Logic | Hits@1 on Bench-marks |
| Kovriguina (2023) [12] | SPARQL Genera-tion (Fantasy) | SPARQL | Augmenting prompts with RDF subgraphs | F1-macro on Bench-marks |
| Mountantonakis [13] (2025) | Cultural Heritage (Art) | SPARQL | Path Pattern prediction + query generation | Accuracy on Bench-mark |
| Ongris (2024) [14] | Wikidata QA (KGQA) | SPARQL | Sequential LLM Chain-ing + GraphRAG | Jaccard Similarity on Ground Truth |
| Vieira da Silva (2024) [15] | Capability Model-ing (IoT) | OWL | TBox-contextualized prompting | Pellet (OWL reason-ing) + SHACL |
| Emonet (2025) [16] | Federated QA (Bioinformatics) | SPARQL | ShEx/VoID-driven RAG query generation | Execution Success Rate and F1 |
| Mashhaditafreshi (2025) [17] | Digital Twins (IoT) | RDF, SHACL | JSON to Aspect Mod-els via bootstrapping | Human evaluation, Jena (RDF syntax) |
| Continued on next page... | | | | |

Table 2.2 – continued from previous page

| Study | Core Task / Domain | Logic | Neuro-Symbolic Integration | Validation Method |
|--|----------------------------------|-------------|---|---------------------------------------|
| <i>Category 3: Evaluation, Stability & Trustworthiness</i> | | | | |
| Sequeda (2025) [18] | SQL Databases (Enterprise) | SPARQL | LLM query correction | Comparison with SQL ground truth |
| Allemang (2024) [19] | SQL Databases (Enterprise) | SPARQL | Ontology-based Error Detection + Repair | Execution Accuracy on Benchmark |
| Gashkov (2025) [20] | Query Filtering (Multilingual) | SPARQL | LLM-as-a-Judge binary classifier | Answer Trustworthiness on Benchmark |
| Adam (2025) [21] | Statement Verification (Bio-sci) | RDF | RAG using External Snippets | Precision / Recall on fixed dataset |
| Meyer (2025) [22] | KGE Benchmarking (Web) | RDF, SPARQL | LLM-KG-Bench 3.0 Framework | Parseable Syntax and F1 |
| Kosten (2024) [23] | Complex QA (KGQA) | SPARQL | Ontology-based prompt engineering | Execution Accuracy on Benchmark |
| Schmidt (2026) [24] | Systematicity Testing (Wiki) | SPARQL | CompoST: Compositional Testing | Compositionality F1 on ground truth |
| Tufek (2025) [25] | Artifact Validation (Industrial) | SPARQL | Zero-shot Instruction Prompting | Domain-specific Precision, Recall, F1 |

2.4 Thematic Analysis

Following the described systematic selection process, the included studies were synthesized into a thematic analysis. This analysis aims to move beyond providing paper summaries, but instead constructing a coherent narrative that explores how Large Language Models and formal logic systems interact within the current research literature. This narrative is structured around three primary themes. First, an exploration of how high-stakes legal and regulatory texts are currently being formalized. Second, a technical deep-dive into the mechanics of translating natural language into structured symbolic logic. Finally, a critical assessment of how the correctness and stability of these systems are verified.

2.4.1 Neuro-Symbolic Pipelines in Public Administration

The integration of Large Language Models (LLMs) and Knowledge Graphs (KGs), frequently characterized as Neuro-Symbolic AI, seeks to combine the flexibility of neural networks with the logical rigor of formal ontologies [19]. One of the many goals of this intersection is to address the complexities of public sector data management [1]. In this domain, authors are increasingly moving away from unstructured legislative texts and narrative reports and towards formal logic, to enable proactive and data-centric governance [1][3].

Knowledge Extraction and Formalization

The transition from unstructured text to formal logic typically follows a multi-stage pipeline designed to reduce LLM hallucinations and preserve the semantic intricacies of legal rules [1][2].

Konstantinidis et al. [1] utilize LLMs to interpret complex legislative documents (in raw PDF format) describing public services, extracting preconditions for eligibility and translating them into SHACL (Shapes Constraint Language) rules. Their approach uses Retrieval-Augmented Generation (RAG) and prompt chaining to transform raw text into RDF-based evidence models, while ensuring that the extracted rules are grounded in established EU standards like *CPSV-AP* and *CCCEV*.

Similarly, Oranekwu et al. [2] employ a RAG pipeline to ingest regulatory texts and manufacturer privacy policies, using LLMs to extract subject-predicate-object triples that are then mapped into a compliance knowledge graph.

Spyropoulos and Tsiantos [3] focus on law-enforcement archives, using instruction-tuned models like OpenAI o3 to parse narrative police reports to extract entities and their interrelationships, subsequently converting this knowledge into OWL-compliant triples for ingestion into a triplestore.

The Role of Intermediate Models

Intermediate representations serve as critical "blueprints" or "mappers" that bridge the gap between unstructured narratives and executable logic [4][3].

Hanuragav and Gopinath [4] demonstrate the utility of intermediate representations through a multi-stage pipeline designed for regulatory validation. In their framework, the transition from unstructured rich-text documents into formal RDF is facilitated by a JSON-to-YAML mapper. By using LLMs to draft YAML mapper files rather than direct triples, their architecture decouples the semantic extraction of data from the technical generation of the knowledge graph (thus essentially decoupling logic and reasoning from syntax and formality). This reliance on non-executable intermediate schemas suggests a shift toward modularity in public sector pipelines, where the LLM's role is confined to architectural drafting, a failsafe to ensure that the resulting logic is structurally "anchored" before final conversion.

Konstantinidis et al. [1] also utilize intermediate steps to formulate natural language rules into a template format before final SHACL generation, allowing for the hierarchical structuring of evidence data.

Spyropoulos and Tsiantos [3] employ intermediate tabular forms to organize recognized entities before they are formally mapped to the OWL ontology, making human-in-the-loop validation much easier.

Current Status and Limitations

Despite promising results, these systems are currently characterized as conceptual or pilot-scale prototypes [1][2].

Konstantinidis et al. [1] emphasize that their pipeline is not yet end-to-end operational and faces significant hurdles regarding data fragmentation across administrative silos.

A primary critique of current methods is the lack of automated testing at scale. For instance, Oranekwu et al. [2] note that their ground truth dataset remains limited in statistical generalizability and has not yet undergone testing with end-users, in real-world conditions.

Furthermore, Spyropoulos and Tsiantos [3] admit to the use of simulated reports rather than authentic documents due to confidentiality, which may raise concerns about not fully capturing the complexity of real-world law-enforcement data.

Proposing future work in this sector, authors focus on overcoming legal and policy complexities, as continuous updates are required to accommodate rapidly evolving regulations [1][2]. Authors also suggest that federated Knowledge Graphs and decentralized technologies (like blockchain) may be necessary to address issues of data ownership and privacy compliance (such as GDPR requirements) [1]. Additionally, there is an identified need for more robust benchmarking methods to validate AI-driven interpretations against human-expert evaluations in high-stakes public environments [2][1].

2.4.2 State-of-the-art in Logic Synthesis

The field of logic synthesis has evolved from monolithic sequence-to-sequence translation toward modular, Neuro-Symbolic pipelines that compartmentalize the semantic parsing of natural language into manageable logical components [5][7]. These state-of-the-art approaches take advantage of the linguistic fluency of Large Language Models while enforcing the structural constraints of Knowledge Graphs, through various technical mechanisms and intermediate representations [16][12][9].

Technical Mechanisms for Translation

Notable Neuro-Symbolic techniques for bridging natural language and structured logic include Few-shot In-Context Learning (ICL) [6], Retrieval-Augmented Generation (RAG) [16] and Iterative Agentic Exploration [9].

Frameworks such as *SymKGQA* [5] combine few-shot ICL with function definitions, to generate symbolic programs in *KoPL* (Knowledge Oriented Programming Language), allowing step-by-step reasoning that is independent of the model’s pre-trained knowledge of language grammars. Shah et al. [8] further enhance this via what they refer to as "Planned Query Guidance", where few-shot examples demonstrate a code-style reasoning process that handles multi-hop transitions line-by-line.

To ground logic in specific KG schemas, authors utilize RAG variations that inject

minimal subgraphs [12], *VoID* (Vocabulary of Interlinked Datasets) descriptions or *ShEx* (Shape Expression) schemas into the prompt [16]. For example, *SPARQLGEN* [12] enriches prompts with a minimal RDF subgraph, sufficient to answer the query, reducing the need for models to memorize the entire graph. Emonet et al. [16] utilize *ShEx* to define available predicates for specific classes, which proved to significantly improve the model’s ability to generate valid federated queries.

The use of RAG is further extended beyond simple fact retrieval to the generation of *ABox* (Assertional Box, storing factual statements) instances for complex domain models. Vieira da Silva et al. [15] demonstrate that providing the full *TBox* (Terminological Box, the schema-level knowledge of an ontology), within the prompt context is essential for reducing hallucinations when modeling industrial capabilities. By explicitly injecting the *TBox*, the LLM is forced to conform with predefined class hierarchies and relationship constraints, such as domain–range axioms. This contextualization ensures that the generated instances are both linguistically plausible and logically consistent with the underlying ontology, successfully reducing the occurrence of model contradictions or invented properties.

Recent research introduces iterative frameworks like *GRASP* [9], which treat the LLM as an agent, tasked with exploring a graph through sequential function calls (search, list, execute). This methodology allows the model to iteratively refine its understanding of the graph’s topology, without being constrained by a fixed context window. Similarly, *SAMM Copilot* [17] employs iterative prompting and feedback loops to generate semantic Aspect Models from JSON data.

Beyond the choice of underlying model, the selection of the formal target language itself is a point of contention. A significant shift in logic synthesis came with the proposal by Lehmann et al. [11] to use Controlled Natural Languages (CNLs), such as *SQUALL* or *Sparklis*, as the target logical form instead of formal languages like SPARQL. The authors argue that because CNLs are linguistically closer to both the input question and the vast amounts of natural language text used in LLM pre-training data, they require significantly less fine-tuning to achieve high accuracy. Their findings indicate that despite the LLMs struggling with the strict syntax of SPARQL, they show a "deeper understanding" of CNLs, allowing them to generate valid syntactic variations that are semantically equivalent to ground truth. For especially complex queries (comparatives, ordinals, differences), switching the parsing target from SPARQL to a natural and compact language like *SQUALL* can effectively double the semantic parsing accuracy.

Managing Structural Complexity

Handling complex schema mapping, particularly in event-based or multi-hop scenarios, requires more advanced strategies than simple triple-matching [13][7].

Jiang et al. [7] propose *OntoSCPrompt*, a two-stage architecture that separates Query Structure Prediction (dubbed Stage-S) from KG Content Population (dubbed Stage-C).

In the first stage, the model predicts a sketch or "skeleton" of the SPARQL query, using special placeholders (e.g., [ent], [rel], [cct]), which is then populated with graph-specific identifiers in the second stage.

For event-based models like *CIDOC-CRM*, where answering a single question often requires traversing long complex paths, Mountantonakis and Tzitzikas [13] introduce a two-stage process using *Ontology Path Patterns*. Their method first predicts the required properties and classes to identify relevant paths of a specific radius before synthesizing the final query, effectively reducing the search space for the LLM.

Descriptive vs. Prescriptive Logic Synthesis

At this point of the analysis, it is important to make a distinction. While many (the majority, in fact) technical advancements focus on Descriptive Question Answering (QA), which is retrieving factual data such as birthplaces or award winners [5][14][9], a distinct and smaller subset of research addresses the synthesis of Prescriptive or Normative Rules [10][1].

Systems like *GraphRAG* [14] and *UniKGQA* [7] primarily focus on factual retrieval, done by translating natural language into executable queries (SPARQL, Cypher) to fetch stored static values [5][9].

In contrast, Soularidis et al. [10] and Konstantinidis et al. [1] attempt to synthesize formal logic that encodes rules for behavior or eligibility. Soularidis et al. utilize template-driven prompts and RAG to translate natural language rules from the Search and Rescue (SAR) domain into *SWRL* (Semantic Web Rule Language). Similarly, Konstantinidis et al. use LLMs to extract regulatory preconditions from legislative texts and formalize them as SHACL shapes, which serve as machine-readable rules for public service eligibility checks and recommendations. Oranekwu et al. [2] bridge these two domains by extracting triples from manufacturer privacy policies to verify compliance against structured *NIST* standards.

2.4.3 Methodologies for Logic Validation and Trust

If neuro-symbolic systems are to transition from conceptual pilots to operational environments, the methodologies used to validate their logical outputs have to become a primary focus of research; this idea is already shifting the emphasis from simple performance metrics to the establishment of trust and traceability [11]. Knowledge Graphs serve as the fundamental "source of trust" in these architectures, providing a formal framework to evaluate the validity of queries generated by Large Language Models and acting as a foundation for explaining results [18].

Knowledge Graphs as a Source of Grounding and Repair

The integration of KGs into the validation pipeline provides the necessary grounding to remedy the risks that stem from the probabilistic nature of LLMs [11].

Allemang and Sequeda [19] introduce *Ontology-based Query Check (OBQC)*, a deterministic approach that utilizes the semantic constraints of an ontology (such as domain-range rules) to identify errors in generated SPARQL queries without relying on an LLM. When an error is detected, an LLM-Repair mechanism utilizes the previously output deterministic error explanations, to iteratively prompt the model for correction, a cycle that continues until the query passes the ontological rules or reaches a predefined iteration limit.

This focus on traceability is further advanced by Adam and Kliegr [21], who propose an inherently traceable approach to verification by instructing LLMs to avoid internal factual knowledge and instead find justification for RDF statements within retrieved external text snippets, while directly generating references for every claim they make in the process and the end result.

The Probabilistic vs. Deterministic Divide

Current literature reveals a clear methodological divide between probabilistic and deterministic validation techniques.

Probabilistic approaches often rely on benchmarking and "LLM-as-a-Judge" frameworks. Gashkov et al. [20] employ instruction-tuned LLMs as binary classifiers to act as post-processing filters, removing incorrect SPARQL query candidates to enhance their *Answer Trustworthiness Score (ATS)*. Similarly, Kosten et al. [23] utilize the *Spider4SPARQL* benchmark [26] to evaluate model performance across varying levels of query hardness, finding that even state-of-the-art models struggle to surpass 51% accuracy on complex multi-hop tasks. Meyer et al. [22] provide an extensible framework, *LLM-KG-Bench 3.0*, which automates the evaluation of LLM answers using metrics such as normalized triple F1 and string similarity.

In contrast, high-stakes domains prioritize deterministic approaches and rigid constraints. Tufek et al. [25] focus on validating semantic artifacts against industrial standards (e.g., *OPC UA*), where natural language requirements are translated into SPARQL queries to ensure compliance. The requirement for absolute precision in high-stakes domains has led to the adoption of the "*draft only, never execute*" paradigm; as proposed by Hanuragav and Gopinath [4], this methodology explicitly prohibits the Large Language Model from direct interaction with the triple store. Instead, the model's output is restricted to intermediate mappers that are subsequently processed by a deterministic Python translator. This creates a "symbolic circuit breaker", ensuring that the final RDF output is idempotent, auditable and strictly compliant with regulatory requirements. This is a level of reliability that probabilistic filtering methods struggle to guarantee. Furthermore, SHACL shapes are frequently used as "logical gates" to enforce structural integrity and detect hallucinations in digital twins and public administration service models [4][1][15].

The Stability and Systematicity Gap

A critical shortcoming in current validation research is the *stability gap*, where models fail to maintain logical consistency across novel tasks. Schmidt et al. [24] investigate *systematicity*, the ability of an agent to understand complex expressions built from known components, through the *CompoST* benchmark. Their findings indicate that LLMs struggle to systematically interpret questions when the complexity of components deviates from their training samples, with performance scores rarely exceeding 0.57 even under optimal self-contained conditions. This highlights that most current validation is static, that is, comparing an LLM's output against a single "golden standard" answer in a single-pass execution [11][18][8].

2.5 Discussion and Research Gap

The systematic review of the current literature paints a certain picture regarding the trajectory of Neuro-Symbolic research, which is moving from monolithic sequence-to-sequence translation to modular pipelines, that distinguish semantic parsing from logical execution. However, the synthesis of the included studies identifies three fundamental gaps that remain unaddressed, as explained next.

2.5.1 The Prescriptive Synthesis Gap: From Facts to Rules

While the broader field of logic synthesis has achieved high accuracy in descriptive tasks, there is a marked lack of research into the synthesis of prescriptive governance logic. As established in the thematic analysis, dominant frameworks such as *UniKGQA* [7] and *GRASP* [9] focus almost exclusively on Knowledge Graph Question Answering (KGQA), that is, translating natural language into queries to retrieve stored facts. In contrast, the requirements of digital governance necessitate the synthesis of *Rules* rather than just *Questions*.

Even within Category 1 (Public Administration), where studies like Konstantinidis et al. [1] attempt to extract service preconditions, the methodology remains largely conceptual. There is a notable absence of a formal "Neuro-symbolic Bridge" that can serve as a structural blueprint to ensure that synthesized prescriptive logic (SHACL shapes) can survive the edge cases of diverse citizen profiles.

2.5.2 The Stability Paradox: Correctness vs. Resilience

A significant paradox emerges in how current literature defines "trust" and "correctness." Current state-of-the-art mechanisms, such as *Ontology-based Query Check (OBQC)* and *LLM-Repair* [19][18], are designed as one-off error-correction loops. These systems ensure that a specific generated query is semantically valid according to an ontology schema for a

single execution pass.

However, in the context of public service eligibility, a synthesized rule is not a one-off query. It is a permanent logic structure intended for high-frequency application across potentially heterogeneous datasets. The literature focuses on making the LLM a more accurate "translator" in the moment, but fails to ensure that the resulting logic is *stable* across a spectrum of inputs. There is no evidence of research into whether a synthesized SHACL shape, once generated, remains logically consistent when tested attributes are systematically varied, a requirement for the proactive "No-Stop Government" vision [1].

2.5.3 The Validation Vacuum: The Need for Mutation Testing

The most critical shortcoming identified is the reliance on static, single-pass validation methodologies. Benchmarks like *CompoST* [24] and *LLM-KG-Bench 3.0* [22] measure accuracy by comparing model outputs against a "golden standard" answer. While these metrics are useful for measuring retrieval precision, they are insufficient for verifying the functional correctness of eligibility rules.

As identified in Table 2.2, current validation is predominantly probabilistic. Even deterministic approaches, such as those by Hanuragav and Gopinath [4] or Tufek et al. [25], focus on structural syntax or version-control compliance. To date, no study has implemented a comprehensive *Mutation Testing Framework* to strictly test the structural and logical stability of LLM-generated SHACL shapes. For high-stakes digital governance, an 88% precision rate (as reported in descriptive tasks [21]) is not a useful nor representative result. Future frameworks must address the variability of non-deterministic systems by establishing testing methodologies that guarantee logical stability across constantly evolving regulatory landscapes.

While Sequeda et al. [18] acknowledge the importance of regression testing to ensure that accuracy does not decrease as ontologies are extended, there is no evidence of widespread use to ensure logic remains resilient under variable conditions. For high-stakes governance and public administration, measuring accuracy on a single pass is insufficient.

2.5.4 Contribution of this Study

Based on the gaps identified above, this dissertation proposes a Neuro-Symbolic framework that utilizes a *JSON Information Model* as an intermediate architectural bridge to generate SHACL-based eligibility rules. SHACL is chosen specifically for its ability to act as a "logical gate", providing the unified graph structure, explainability and automation required for public administration.

To address the validation vacuum, this study introduces a *Deterministic Mutation Testing* methodology. By systematically mutating citizen attributes to evaluate the "rejection rate" of synthesized SPARQL logic, the framework moves beyond probabilistic retrieval to provide a functional guarantee of stability. This approach, detailed in the following Pilot

Study, represents a transition from checking if a model is "correct once" to verifying that the synthesized law is "functionally infallible" across variable scenarios.

3 Pilot Study

This chapter details the design, implementation and experimental validation of a novel Neuro-Symbolic pipeline for automating public service eligibility checks.

3.1 Overview

The proposed architecture addresses the limitations of "black-box" Large Language Models (LLMs) by enforcing a strict separation between neural interpretation (extracting meaning from text) and symbolic execution (validating logic against data).

The methodology is structured around a "Text-to-Graph-to-Logic" workflow. The system transforms unstructured administrative documents into formal Knowledge Graphs and executable SHACL shapes through a chain of intermediate structured representations. This design prioritizes explainability and determinism, ensuring that the final eligibility decision is derived from explicit, auditable rules rather than probabilistic token generation.

The chapter is organized as follows: Section 3.2.2 defines the semantic schemas that ground the system. Section 3.2.3 details the four-stage extraction and generation pipeline. Section 3.2.4 describes the validation engine, and Section 3.3 outlines the experimental framework used to stress-test the system's logical capabilities through automated mutation testing.

3.2 Methodology and System Architecture

3.2.1 Setup Environment

The pipeline was implemented using Python 3.12.9, utilizing a modular architecture to separate core processing logic from experimental orchestration. The system relies local processing for semantic graph operations and cloud-based APIs for Large Language Model inference.

System Architecture

The codebase follows a functional separation of concerns, organized into three distinct layers:

1. **The Core Logic Layer:** A modular Python library encapsulating the functional logic of the system. Contains the reusable logic, such as API communication, graph operations, parsing and testing utilities. It also contains the *pipeline core*, which

encapsulates the end-to-end extraction-generation workflow.

2. **The Orchestration Layer (The "Cockpit"):** An interactive Jupyter Notebook serves as the control interface. This layer manages the experimental loop, injects configuration variables into the core modules and handles exceptions without interrupting batch processing.
3. **The Persistence Layer:** To ensure auditability and reproducibility, the system employs a strict "Artifact Preservation" strategy. Every experimental run generates a dedicated directory locally, containing all intermediate outputs of the core pipeline. Testing metrics and metadata are saved in a Master CSV file for post-hoc analysis.

Technologies and Libraries

The system integrates standard Semantic Web technologies with modern Data Science tools:

- **RDFLib:** Used for parsing, manipulating and serializing RDF graphs (Turtle format), as well as executing local SPARQL queries.
- **PySHACL:** The standard Python implementation of the SHACL validation engine, used to validate the LLM-generated shapes against the citizen data.
- **Pandas:** Used for the post-hoc aggregation and statistical analysis of the testing logs.

3.2.2 Semantic Data Modelling

This pipeline was designed specifically with public service documents in mind. To bridge the gap between unstructured administrative text and deterministic validation logic, two distinct semantic layers were defined. These RDFS schemas serve as the symbolic "grounding" for the Large Language Model.

The Public Service Meta-Model

To ensure semantic interoperability and standardization, the modeling of the public service itself adheres to European formal vocabularies, specifically the Core Public Service Vocabulary Application Profile (CPSV-AP) and the Core Criterion and Evidence Vocabulary (CCCEV). The schema follows a hierarchical structure:

- **cpsv:PublicService:** The root node representing the public service itself.
- **cccev:Constraint:** Connected to the root node via `cpsv:holdsRequirement`, these nodes represent individual preconditions extracted from the text.
- **cccev:InformationConcept:** These nodes are connected to Constraint nodes via `cccev:constrains` and represent the abstract information required to evaluate a constraint.

The adoption of established EU standards is a deliberate architectural choice, made to ensure cross-border interoperability and extensibility. By anchoring the pipeline's output in the CPSV-AP and CCCEV ecosystems, the generated graphs are natively compatible with

the broader European e-Government infrastructure (such as the Single Digital Gateway). Furthermore, this modular design allows for future expansion where the pipeline could automatically ingest the full breadth of these ontologies (complex Evidence mappings, Agent definitions, Output representations), without requiring a fundamental restructuring of the core logic.

Citizen Schema

While the Public Service Meta-Model describes the *rules*, the Citizen Schema describes the *applicant*. This work utilizes a domain-specific RDFS schema tailored to the requirements of each document and generated in a separate workflow (not presented here) by the same LLM used in the implementation of the rest of the pipeline. The model is instructed to use granular instead of aggregate data as nodes (e.g. prefer "Date of Birth" rather than "Age") and is encouraged to use abstract and reusable classes.

It has been demonstrated that the generation of such schemas can be automated as part of the pipeline [1]. However, for the scope of this pilot study, the Citizen Schema is treated as fixed input context. This methodological choice serves two purposes:

1. **Experimental Control:** By fixing the target schema, we isolate the performance of the LLM in *logic generation* (SHACL/SPARQL) and *extraction*, without the confounding variable of schema generation errors.
2. **Prerequisite for Testing:** The automated testing framework relies on injecting specific faults into the citizen graph (e.g., modifying property values to trigger violations). This requires a deterministic, known-in-advance schema structure. Had the schema been generated dynamically during each run, it would be impossible to define a static library of test scenarios targeting specific graph nodes.

3.2.3 The Extraction and Generation Pipeline

The core contribution of this work is the following multi-stage, neuro-symbolic pipeline. The process follows a sequential data flow, depicted in Figure 3.1, consisting of four primary stages.

Stage 1: Document Summarization and Precondition Extraction

The pipeline begins with the ingestion of the raw public service document (PDF). Using a Large Language Model (LLM), the unstructured text is processed to extract a summary of eligibility preconditions. The prompt is designed to filter out administrative noise and standardize the format of the rules. Summarization reduces the cognitive load required for the subsequent logic generation steps.

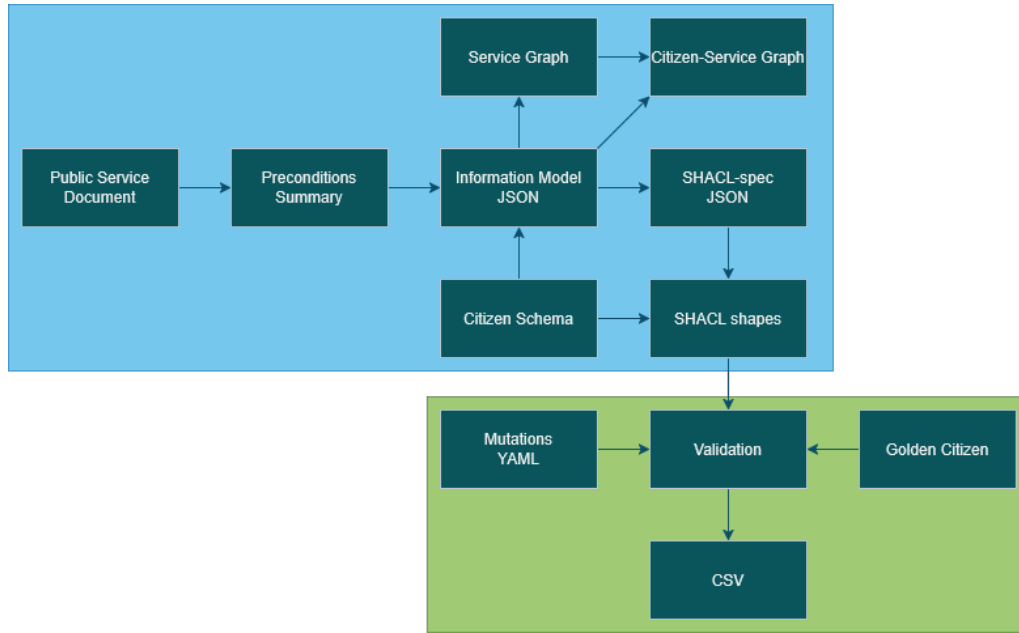


Figure 3.1: Flow Chart of the core pipeline

Stage 2: Information Model Generation

In this critical neuro-symbolic step, the extracted preconditions are transformed into a structured JSON "Information Model". The Information Model organizes the unstructured rules into a strict hierarchy that mirrors the Meta-Model structure:

- **Constraints:** Each eligibility rule is encapsulated as a Constraint object, containing the natural language description of the rule.
- **Information Concepts:** Nested within each Constraint are the abstract Information Concepts, representing the specific pieces of evidence or data required to evaluate that rule.

Inferring these concepts from the list of rules is the main reasoning task of the LLM at this stage. However, a second task it is prompted with is to act as a semantic mapper. The LLM is provided with the Citizen Schema (defined in Section 3.2.2) as a strict vocabulary constraint to prevent the hallucination of non-existent properties. With it, it is instructed to connect each Information Concept with a number of Citizen nodes, by constructing specific traversal paths through the ontology (e.g., mapping the concept of "Applicant Age" to the path `:Applicant/:birthDate`).

The output is strictly enforced using a Pydantic schema definition, ensuring valid JSON structure. The resulting artifact effectively creates a "blueprint" for downstream tasks. It contains all the necessary semantic links to be deterministically serialized into valid CPSV/CCCEV triples in the subsequent stage, while ensuring that all data references are grounded in the controlled vocabulary of the Citizen Schema.

Stage 3: Semantic Graph Construction

Once the Information Model is established, the system deterministically (via Python code) constructs two RDF artifacts without further LLM inference:

1. **The Service Graph:** A formal representation of the public service using the CPSV-AP and CCCEV vocabularies and following the Meta-Model schema defined in Section 3.2.2.
2. **The Citizen-Service Graph (Explainability Layer):** By loading an "Example Citizen" (a valid applicant instance), the system uses the Information Model to link the abstract Information Concepts from the Service Graph directly to the actual data nodes in the Citizen Graph via `ex:mapsTo` edges. This unified graph serves as a visual "audit trail," allowing human inspectors or automated agents to trace exactly which specific data points are being used to evaluate a specific legal requirement.

Both Graphs are serialized using `turtle` syntax and saved to file as artifacts. Interactive visualizations of them are generated using the `pyvis` library and also saved to file as `html` files.

Stage 4: SHACL Shapes Generation

The final stage of the pipeline is responsible for synthesizing the executable validation logic. This stage transforms the abstract requirements from the Information Model into a strictly valid Shapes Constraint Language (SHACL) document.

First, the system deterministically distills the rich Information Model into a simplified, noise-free JSON structure termed the "SHACL-Spec." This intermediate representation reorganizes the structure and retains only the logical primitives required for validation (e.g. rules, target paths and data types). This step acts as a "context cleaner", helping the LLM focus exclusively on code synthesis.

The LLM is then invoked to translate this specification into RDF triples (Turtle format). The system enforces a Dual-Strategy Protocol for logic synthesis. For atomic constraints involving single-hop properties and literal comparisons (e.g., `Citizenship = 'GR'`), the model generates standard `sh:property` shapes. For requirements involving arithmetic, aggregations, date comparisons, or cross-referenced data (e.g., `now() - birthDate > 18`), the model encapsulates the logic within `sh:sparql` constraints. This allows for the expression of complex conditional logic that exceeds the expressivity of the SHACL Core vocabulary. The model is once again restricted to using the fixed Citizen Schema, which is once again given as context to act as a failsafe, in case earlier path generation failed to include crucial nodes.

As a last addition, the LLM generates an error message for every shape, which is intended to be displayed as part of the Validation Engine report in case of a violation (e.g., "Income exceeds threshold").

The output is a fully serialized `ttl` file containing the `sh:NodeShape` definitions. This

file serves as the executable input for the Validation Engine, the mechanics of which are detailed in the following section.

3.2.4 The Validation Engine

The final component of the architecture is the Validation Engine, which functions as the execution core of the system's symbolic layer. While previous stages focus on structuring and grounding the data, this engine is responsible for applying the generated constraints against specific citizen data to render a final, deterministic eligibility decision.

The engine operates on two distinct RDF graphs:

- **The Shapes Graph:** The `.ttl` file generated by Stage 4 of the pipeline, containing the `sh:NodeShape` definitions and SPARQL constraints within.
- **The Data Graph (Citizen Instance):** An RDF graph representing a specific applicant and a concrete instantiation of the Citizen Schema. It contains the factual assertions about an individual, structured strictly according to the domain ontology.

For the Execution and Reasoning step, the system utilizes PySHACL, a Python-based implementation of the W3C SHACL standard, to perform the validation. The execution follows a standard protocol:

- **Targeting:** The engine identifies the "Focus Node" in the Data Graph (defined as the instance of class `:Applicant`).
- **Constraint Evaluation:** For every Shape mapped to the Applicant, the engine evaluates the corresponding logic. Simple property shapes are validated via graph traversal, while complex conditions trigger the execution of the embedded SPARQL queries against the Data Graph.
- **Entailment:** The engine operates under the RDFS entailment regime, allowing it to infer class hierarchies (e.g., understanding that a `:Child` is also a `:Person`) during validation.

The output of the engine is a formal *Validation Report Graph* adhering to the SHACL standard. This report provides as output:

1. **Boolean Conformance:** A global `sh:conforms` value (True/False), which serves as the system's final decision on eligibility.
2. **Violation Details:** The report includes a set of `sh:ValidationResult` nodes in cases of non-conformance. Each result links to the specific Shape that failed and includes the generated error message, providing explanation for the rejection.

3.3 Experimental Design

To evaluate the reliability, functional correctness and operational stability of the proposed architecture, an experimental framework was developed. The design of this experiment moves beyond simple anecdotal testing, implementing a means to quantify the performance

of the Neuro-Symbolic pipeline under varying conditions.

The core unit of the experiment is defined as a "run". A run represents a single end-to-end execution of the pipeline governed by a specific Configuration Tuple:

(Document, Model, Prompting Strategy)

Given that Large Language Models are inherently non-deterministic when operating at non-zero temperature settings, a single successful generation is insufficient to prove any result. To address this, the framework executes a loop of multiple iterations for each unique configuration. This repetition allows for "drowning out" stochasticity and for the results metrics to converge to values that describe the actual stability of the pipeline with more fidelity.

The execution of these runs is done in The Orchestration Layer (see section 3.2.1), which oversees the following lifecycle for every iteration:

1. **Context Initialization:** At the start of a run, a dictionary is initialized. This volatile data structure acts as a "flight recorder," accumulating outputs and metadata.
2. **Pipeline Execution:** The extraction and generation pipeline is triggered. If the pipeline encounters a critical failure, the failure mode is logged and the run is marked as incomplete.
3. **Scenario Validation:** Upon successful generation of a valid SHACL graph, the system proceeds to the Mutation Testing phase (detailed in the following subsection), where the generated logic is stress-tested against a battery of specific scenarios.
4. **Persistence:** Finally, the accumulated metrics are "flushed" to a CSV file. Results are persisted immediately to prevent data loss during long-running batch experiments.

3.3.1 The Mutation Testing Framework

To evaluate the functional correctness of the generated SHACL shapes, the system implements a Mutation Testing Framework. Unlike traditional unit tests that might check for static string matches, this framework dynamically generates RDF graph instances to test whether the generated logic correctly distinguishes between eligible and ineligible applicants. The framework operates on a "Baseline and Perturbation" model, consisting of the components analyzed below.

The "Golden Citizen" Baseline

For each public service document, a single, syntactically perfect RDF graph termed the *Golden Citizen* is manually constructed. This data instance represents an applicant who satisfies *all* eligibility preconditions, albeit marginally. This baseline graph is constructed to adhere strictly to the Citizen Schema. The data values are calibrated to demonstrate marginal eligibility (e.g., if an income upper limit is €12,000, the Golden Citizen might have €11,999). This ensures that the testing framework evaluates the precision of the logic,

not just its general functionality.

Scenarios

The test cases are defined in a declarative YAML configuration file. Each entry in this file represents a distinct Scenario, designed to isolate and test a specific logical constraint found in the document. A Scenario definition includes:

1. **Expected Violation Count:** The ground truth for the test. A compliant scenario expects 0 violations, a failure scenario typically expects 1.
2. **Mutation Actions:** A set of instructions to alter ("mutate") the Golden Citizen.

Crucially, mutations are designed to be atomic. Each scenario targets a single "fact" in the graph (e.g., changing a Literal value or a URI reference) to nudge the applicant from an "Eligible" state to a "Non-Eligible" state. This isolation allows the Validation Engine to pinpoint exactly which specific rule the LLM failed to generate correctly, if any.

The Mutation Engine

For every iteration ("run"):

1. The system loads the Golden Citizen graph into memory.
2. It creates a deep copy of the graph to ensure test isolation.
3. Once per scenario, it applies the Patch Logic. The engine parses the Turtle snippets defined in the YAML actions (e.g., `ex:Income :amount 12,000.1`) and updates the graph triples accordingly. This allows for complex graph transformations, such as replacing nodes or updating relationships, without manual RDF manipulation.

The resulting Mutated Citizen Graph and the Generated Shapes Graph (from Stage 4) are then passed to the aforementioned Validation Engine (section 3.2.4). The boolean outcome (`conforms`) and the number of violations are captured and logged to later be compared against the Expected Violation Count defined in the scenario.

3.3.2 Experimental Configurations

Recall the configuration tuple around which the experiment was designed:

(Document, Model, Prompting Strategy)

For the experimental part of this work we chose 2 documents, 2 models and 3 prompting strategies, for a total of 12 different experimental configurations. This combinatorial approach allows for the isolation of specific failure modes, distinguishing between errors caused by document complexity, model reasoning capacity, or prompting sufficiency. Below we analyze each component of the tuple and the configurations explored in the scope of this work.

Document Corpora (Use Cases)

This selection tests the pipeline’s ability to generalize across different domains and logical structures. Two public service documents were selected to represent different levels of beurocratic complexity.

Student Housing Allowance (High Complexity)

Selected as the "Stress Test" for the system. This document is characterized by:

- **Deep Graph Traversal:** Verification requires traversing multiple hops (Applicant → Parents → Properties → Location).
- **Recursive Arithmetic:** It involves dynamic income thresholds, calculated based on the count of dependent children (e.g., $Limit = Base + (N \times Bonus)$).
- **Referential Integrity Constraints:** Verification requires comparing the identity of URI nodes rather than literal values (e.g., validating that the `:UniversityCity` node is distinct from the `:FamilyResidenceCity` node).

Special Parental Leave Allowance (Intermediate Complexity)

Selected to evaluate standard administrative processing. This document focuses on:

- **Categorical Classification:** Eligibility relies on specific enumerated values (e.g., Employment Sector must be "Private" or "Public").
- **Temporal Logic:** Involves duration calculations (e.g., "1 year of continuous employment") rather than complex arithmetic aggregations.

Large Language Models

The experiment utilizes the Google Gemini 2.5 family of models to evaluate the trade-off between reasoning capability and computational efficiency.

- **Gemini 2.5 Pro:** The high-parameter "reasoning" model. It is hypothesized to excel at complex SPARQL generation and abstracting vague requirements into formal logic, potentially at the cost of higher latency.
- **Gemini 2.5 Flash:** The lightweight, low-latency model. It serves to test the feasibility of a "high-throughput" pipeline. A key research question is whether this smaller model can adhere to the strict SPARQL syntax requirements without the deep reasoning capabilities of the Pro variant.

Prompting Strategies

Three distinct prompting strategies were implemented to evaluate the impact of "In-Context Learning" and "Self-Correction" on code quality.

Default Strategy (Few-Shot with Guardrails)

This strategy represents the baseline optimized approach. The system prompt instructs the model to act as an "Expert" and provides:

- **Proposed Strategy:** Explicit instructions to choose between, depending on the input.
- **Syntactic Guardrails:** A set of negative constraints derived from pilot testing errors.
- **Few-Shot Examples:** Concrete examples demonstrating correct and desired outputs.

Zero-Shot Strategy (Ablation Study)

To quantify the value of the engineering effort put into the Default prompt, the Zero-Shot strategy removes all Few-Shot Examples: the model is given the instructions but no reference implementations. This tests the model's innate reasoning prowess and knowledge of syntax versus its reliance on pattern matching from examples.

Reflexion Strategy (Iterative Self-Correction)

This strategy implements a *Prompt Chaining* loop to address the non-deterministic nature of LLM code generation.

1. The model generates a draft response using the Default strategy.
2. The output is passed back to the model with a new "persona": "*Senior Data Quality Assurance Auditor.*" This agent is instructed to critique the quality of the draft with regards to criteria such as completeness, logical contradictions and syntactic validity.
3. If errors are found, the model rewrites the response based on its own critique.

This configuration evaluates the efficacy of self-correction mechanisms in code generation, specifically testing whether the computational overhead of iterative refinement yields a statistically significant reduction in syntactic and logical errors.

3.3.3 Evaluation Metrics

To move beyond qualitative observation, the experimental framework was designed in such a way to capture a granular dataset for every execution cycle. This data collection strategy was designed to decouple structural failures (code that does not compile) from logical failures (code that compiles but yields incorrect decisions), enabling a multi-dimensional analysis of pipeline performance.

Data Collection

For every experimental run, the system persists a dataset that captures the complete state of the pipeline at the moment of execution, categorized into five distinct dimensions:

- **Configuration Metadata:** Contextual fields regarding a unique Run ID, timestamp, the specific document input, the LLM employed and the active prompting strategy.
- **Artifact Fingerprinting:** To track the stability and uniqueness of the LLM's output, the system computes and logs the cryptographic hashes (MD5) of the generated

graphs. This allows for the detection of potentially identical artifacts generated across different runs.

- **Syntactic Integrity Verification:** Before execution, the system first verifies if the generated text is a valid RDF/Turtle graph (parsable by RDFLib), and secondly, it performs a "deep compile" check on every embedded SPARQL constraint to ensure the query syntax adheres to the SPARQL standard. Both errors, if they occur, are flagged differently to be distinguishable.
- **Validation Outcome Metrics:** The raw output of the validation engine is captured in detail. This includes the Actual Violation Count, the Expected Violation Count (derived from the scenario definition) and a serialized list of the specific Violated Shapes. These fields facilitate the calculation of granular error metrics beyond simple binary accuracy.
- **Operational Diagnostics:** To monitor system health, metrics such as end-to-end Execution Time (latency) and specific Error Messages (e.g., Python exceptions) are logged. These fields are critical for quantifying the operational stability of the external API dependencies.

Performance Indicators

The analysis of this dataset focuses on two primary dimensions of success.

Syntactic Validity

The first hurdle for any code-generating system is the production of executable syntax. This metric quantifies the percentage of runs where the LLM produced a `.ttl` file that could be successfully parsed by the RDFLib graph library and whose embedded SPARQL queries could be compiled without error. A run that fails this check is distinguished from runs that simply produce incorrect logic.

Functional Logic Accuracy

For runs that pass the syntax check, the focus shifts to logical fidelity. This is measured by comparing the system's eligibility decision against the known ground truth of the mutation scenarios. By treating the validation outcome as a binary classification task, where a "Conformance" is the Positive class and "Violation" is the Negative class, standard machine learning metrics can be calculated.

3.4 Conclusion

This chapter has detailed the architectural and experimental foundations of the Neuro-Symbolic pipeline. By combining a schema-grounded generation process with a deterministic mutation testing framework, the system is designed to provide a quantifiable evaluation

of LLM capabilities in the context of this task. The following chapter presents the results of these experiments, analyzing the pipeline's performance across the aforementioned dimensions.

4 Results

This chapter presents the quantitative findings obtained from the experimental evaluation of the neuro-symbolic pipeline. The analysis strictly follows the performance metrics defined in the methodology, assessing the system across three cascading thresholds of success: syntactic validity (code generation), functional logic accuracy (reasoning fidelity), and overall operational reliability (end-to-end feasibility). Broader interpretation of these patterns and their implications for public administration systems are discussed in Chapter 5.

4.1 Experimental Dataset

The experimental campaign consisted of a total of 170 end-to-end pipeline executions ("Runs"). Each run consisted of the steps that were analyzed on the previous chapter. The distribution of these runs across the varying configurations is detailed in Table 4.1. Due to the operational constraints discussed in Section 6.1, the dataset is unbalanced, with the "Flash" model variant accounting for a larger proportion of the total runs.

Table 4.1: Distribution of Experimental Runs per Configuration

| Document | Model | Prompt Strategy | Runs (N) |
|-----------------|------------------|-----------------|--------------|
| Parental Leave | gemini-2.5-flash | Default | 20 |
| | | Reflexion | 20 |
| | | ZeroShot | 20 |
| | gemini-2.5-pro | Default | 10 |
| | | ZeroShot | 10 |
| | | | |
| Student Housing | gemini-2.5-flash | Default | 20 |
| | | Reflexion | 20 |
| | | ZeroShot | 20 |
| | gemini-2.5-pro | Default | 10 |
| | | Reflexion | 10 |
| | | ZeroShot | 10 |

4.2 Syntactic Validity

The first criterion for the pipeline's utility is the generation of syntactically valid code. A run is considered "Syntactically Valid" only if the LLM produces a Turtle (`.ttl`) file that can be parsed by *RDFLib* *and* contains SPARQL constraints that successfully compile without syntax errors.

4.2.1 Success Rate

Figure 4.1 illustrates the success rates across all configurations.

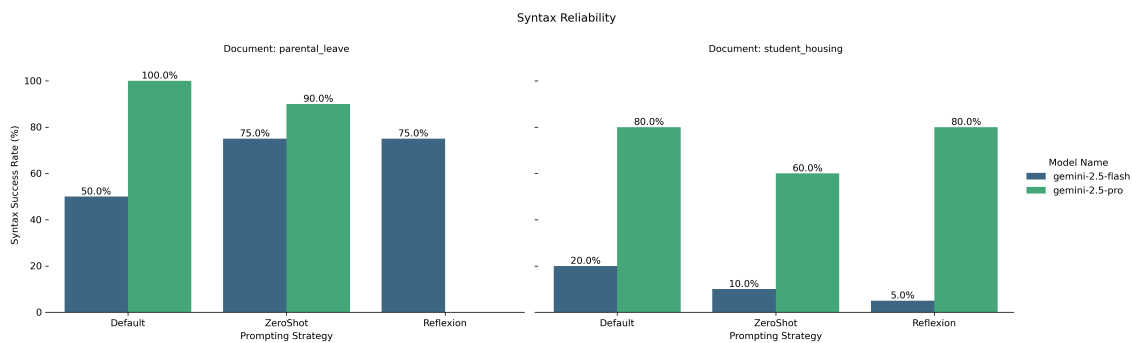


Figure 4.1: Syntactic Validity Rates by Configuration

Impact of Document Complexity

The complexity of the source document served as a strong predictor of failure.

In the case of the Parental Leave document (Intermediate complexity), both models performed adequately. Even the weaker Flash model achieved a 75% validity rate using the Reflexion and ZeroShot strategies.

On the contrary, the Student Housing document (High complexity) acted as a strict filter. Flash failed to produce valid code in the vast majority of attempts (36 out of 60 runs failed syntax checks), whereas Pro proved strong enough to handle the increased logical depth, though it still suffered a 20% degradation compared to the simpler use case.

Impact of Model Class

The data reveals a disparity in coding capability between the two model variants.

The Gemini 2.5 Pro model demonstrated high reliability, achieving a 100% success rate on the Parental Leave document and maintaining an 80% success rate on the complex Student Housing document (under Default prompting).

In contrast, the Gemini 2.5 Flash model struggled significantly with syntactic precision. While it achieved moderate success on the simpler Parental Leave document (ranging from 50% to 75%), its performance collapsed on the complex Student Housing document, with success rates dropping as low as 5% (Reflexion) to 20% (Default).

Impact of Prompting Strategy

The impact of prompting strategies varied by model architecture.

For Flash, the *Reflexion* strategy provided a significant boost on the simpler document (improving validity from 50% to 75%). However, this benefit vanished on the complex document, where Reflexion actually performed worse (5%) than the Default prompt (20%).

For Pro, the *Default* and *Reflexion* strategies performed identically (80% on Housing), while the *ZeroShot* strategy resulted in a notable drop in stability (falling to 60% on Housing).

4.2.2 Failure Mode Analysis

To better understand the mechanisms of failure, the invalid runs were categorized by error type: *RDF Syntax Errors* (invalid Turtle file structure) and *SPARQL Syntax Errors* (malformed queries within valid Turtle). Figure 4.2 presents the error rates normalized by the total number of runs for each model-document pair.

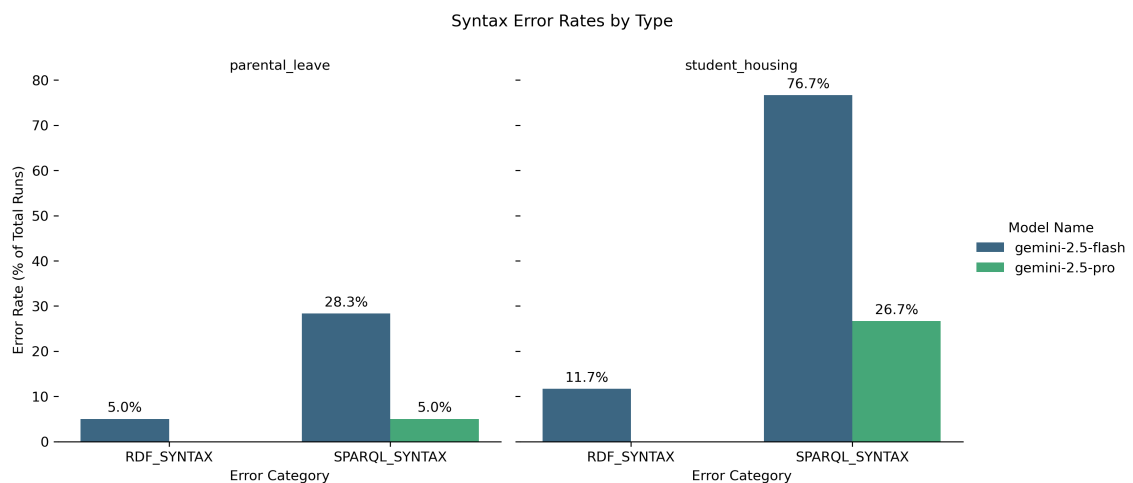


Figure 4.2: Distribution of Syntax Error Types by Model and Document

The data indicates that SPARQL Syntax Errors were the dominant failure mode across all configurations.

Gemini 2.5 Flash exhibited a high frequency of SPARQL errors, particularly on the complex Student Housing document, where 76.7% of all runs failed due to query syntax. Notably, Flash also produced a non-negligible rate of RDF Syntax errors (5.0% on Parental Leave, 11.7% on Student Housing), indicating occasional failures in generating even the fundamental file structure.

Gemini 2.5 Pro demonstrated significantly higher stability. It produced zero RDF syntax errors across all 50 experiments. Its failures were exclusively confined to SPARQL syntax, with error rates of 5.0% on the simpler document and 26.7% on the complex document.

4.3 Logic Validity

For the subset of runs that successfully produced syntactically valid code, the focus shifts to *Functional Logic Accuracy*. A run is classified as having "Perfect Logic" if and only if the generated SHACL shapes correctly identify the expected number of violations for *every single scenario* in the test suite (both the baseline Golden Citizen and all edge cases). Runs that crashed during execution or failed syntax checks were excluded from this analysis to isolate the reasoning capability of the models.

It is critical to note that 'Logic Accuracy' is evaluated as a holistic, end-to-end performance metric. A failure to correctly validate a citizen scenario may stem from errors at any stage of the neuro-symbolic pipeline: a missed precondition during the initial summarization (Stage 1), a malformed mapping in the Information Model (Stage 2), or an incorrect SHACL generation (Stage 4). Consequently, a 'Logic Failure' indicates that the system, as a whole, failed to enforce the regulation, regardless of which specific component was the root cause.

4.3.1 Success Rate

Figure 4.3 illustrates the rate of flawless logical execution across configurations.

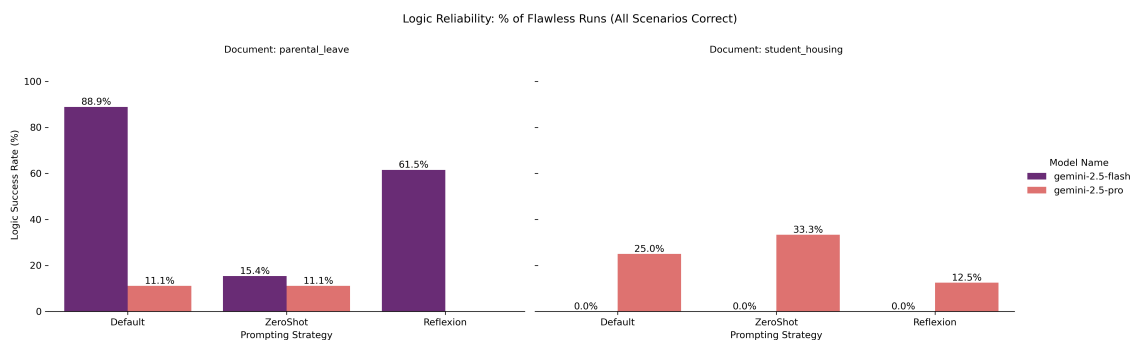


Figure 4.3: Logic Validity: Percentage of Flawless Runs (All Scenarios Correct)

Impact of Document Complexity

Consistent with the syntax results, the complexity of the document was the primary determinant of success.

Parental Leave, having simpler logic, allowed for high performance, with the best-performing configuration (Flash/Default) achieving an 88.9% perfect run rate.

Student Housing and its complex logic requirements caused a near-total collapse in functional accuracy. Across all models and prompts, the highest achieved success rate was only 33.3%, with many configurations failing to produce a single logically correct run.

Impact of Model Class

The performance relationship between models *inverted* depending on the task.

On the simple document, Flash significantly outperformed Pro, achieving 88.9% accuracy (Default) compared to Pro's 11.1%. However, on the complex document, Flash failed completely, with a 0.0% success rate across all 60 attempts.

While Pro underperformed on the simple task, it was the only model capable of solving the complex Student Housing logic, achieving success rates between 12.5% and 33.3%.

Impact of Prompting Strategy

Removing examples (ZeroShot) caused a sharp drop in accuracy from 88.9% to 15.4% for Flash on the simple document. Conversely, for Pro on the complex document, ZeroShot unexpectedly yielded the highest accuracy (33.3%).

The self-correction strategy (Reflexion) did not yield consistent improvements. For Flash, it reduced accuracy from 88.9% to 61.5% on the simple document. For Pro, it performed roughly equivalent to the Default strategy.

4.3.2 The Syntax-Logic Gap

A comparison between the syntax validity rates (Figure 4.1) and logic accuracy rates (Figure 4.3) reveals a distinct degradation in performance as the evaluation becomes stricter. This is apparent if we isolate the complex Student Housing use case. While the Pro model generated valid syntax in $\approx 80\%$ of runs, only $\approx 25\%$ of those valid runs contained correct logic. The Flash model struggled at both levels, with low syntax validity (20%) and zero functional correctness (0%).

4.4 Overall Pipeline Reliability

Beyond specific syntax and logic metrics, this section evaluates the system's viability as an end-to-end automated service. The analysis considers two perspectives: the operational stability of the pipeline and its reliability inside the broader context of this work, which is public service recommendations.

4.4.1 Pipeline Feasibility and Attrition

Figure 4.4 presents the distribution of final outcomes for all 170 experimental runs. This "Waterfall Analysis" categorizes every attempt into a single mutually exclusive outcome, revealing the attrition rate of the system.

The data indicates a high attrition rate:

- **Syntax Failures:** The majority of runs failed early. SPARQL Syntax Errors accounted for the largest share of failures (N=72), followed by RDF Syntax Errors (N=10).
- **Logic Failures:** Of the runs that compiled, a significant portion (N=55) produced code that executed but failed to correctly validate all test scenarios.

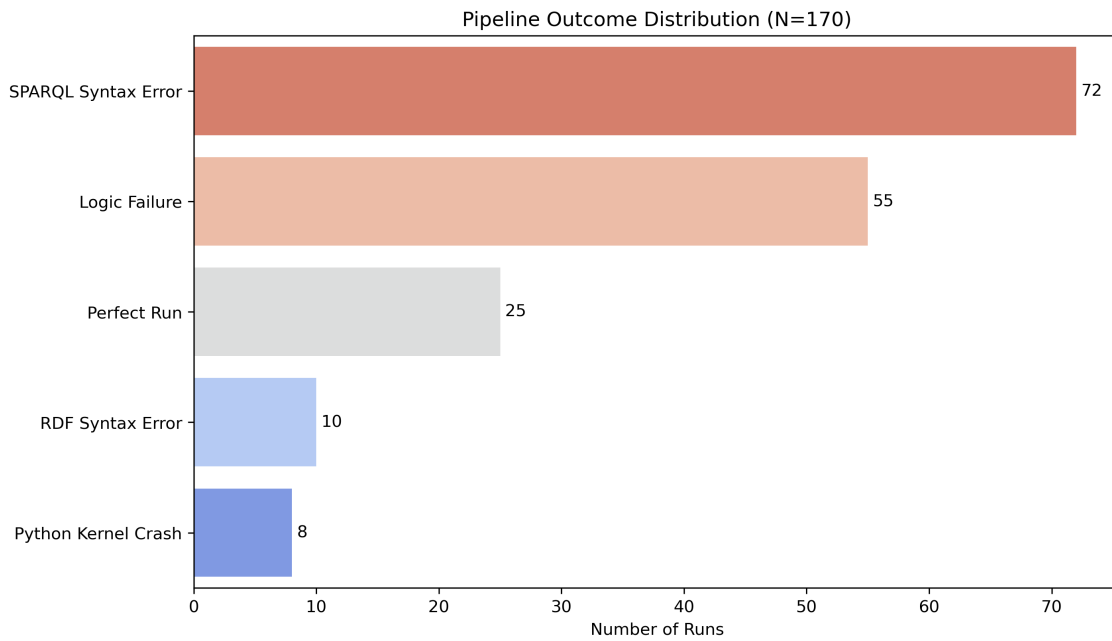


Figure 4.4: Distribution of Final Pipeline Outcomes.

- **Success:** Only 25 runs (14.7% of the total) achieved the status of a "Perfect Run," generating both valid syntax and flawless logic across all edge cases.
- **System Stability:** Operational crashes (Python/API errors) were rare (N=8), indicating that the underlying infrastructure, retry mechanisms and exception handling were largely sufficient.

4.4.2 In-context (Recommender System) reliability

To evaluate the system's utility as a public service recommender, the validation outcomes were aggregated into a Confusion Matrix (Figure 4.5). In this context, the classes are defined based on the goal of recommending eligible services:

- **Positive Class (Recommendation):** The system validates the citizen as Eligible.
- **Negative Class (Rejection):** The system flags at least one Violation.

To interpret the confusion matrix in the specific context of public service recommendations, the standard machine learning classifications were mapped to domain-specific service outcomes, as defined in Table 4.2.

The confusion matrix is then created based on this terminology.

The matrix reveals the system's risk profile:

- **True Positives (10.5%):** In 59 cases, the system correctly identified and recommended the service to an eligible citizen ("Correct Recommendation"). This confirms the system's ability to successfully validate legitimate claims when the generated logic is sound.
- **False Positives (10.1%):** In 57 cases, the system erroneously recommended the service to an ineligible citizen ("Bad Recommendation"). This represents a "Trust

Table 4.2: Definition of Classification Outcomes in the Recommender Context

| | System: "Violation" (Rejection) <i>Triggered Violations > 0</i> | System: "Conforms" (Recommendation) <i>Triggered Violations = 0</i> |
|---|---|--|
| Citizen is Ineligible <i>Expected Violations > 0</i> | True Negative (TN) <i>Correct Rejection</i> (System works) | False Positive (FP) <i>Bad Recommendation</i> (Trust Risk) |
| Citizen is Eligible <i>Expected Violations = 0</i> | False Negative (FN) <i>Missed Opportunity</i> (Service Failure) | True Positive (TP) <i>Correct Recommendation</i> (System works) |

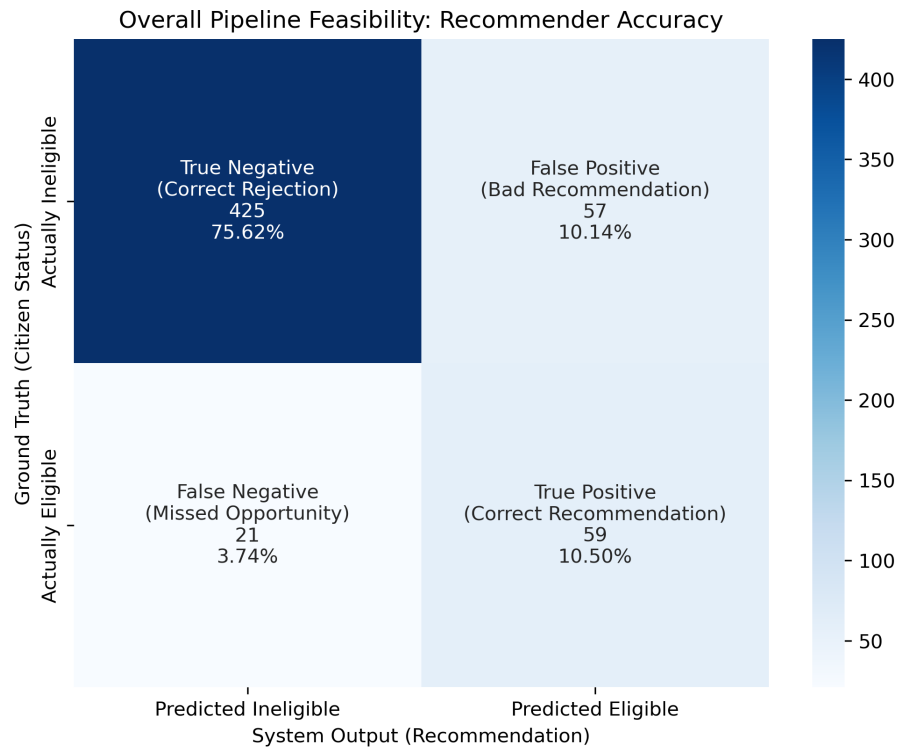


Figure 4.5: Confusion Matrix of Eligibility Recommendations

Risk," where users might be guided to apply for benefits they cannot receive.

- **True Negatives (75.6%):** The system correctly rejected ineligible applicants in the majority of cases.
- **False Negatives (3.7%):** In 21 cases, the system incorrectly rejected an eligible applicant ("Missed Opportunity"). While this number is low, it represents a "Service Failure," denying access to entitled benefits.

5 Discussion

This chapter synthesizes the quantitative results presented in Chapter 4 to evaluate the broader implications of using Large Language Models for automated public service eligibility checks and recommendation. By analyzing the patterns of failure, ranging from syntactic hallucinations to logical paradoxes, this discussion aims to characterize the fundamental limitations of current neuro-symbolic architectures. The analysis moves beyond simple performance metrics to address the core challenges of semantic fidelity, algorithmic determinism and the operational sovereignty required for deployment in public administration.

5.1 Cognitive Dissonance in Code Generation

The most pervasive pattern observed throughout the experimental campaign was a fundamental disconnect between the Large Language Model's ability to generate valid *syntax* and its ability to construct valid *logic*. This phenomenon, termed here as "Cognitive Dissonance", underscores the architectural limitation of Transformer-based models when applied to formal reasoning tasks: they operate as approximate pattern matchers in a domain that requires exact symbolic execution.

5.1.1 The Illusion of Fluency

The results from the "Student Housing" use case serve as the primary evidence for this dissonance. The Gemini 2.5 Pro model achieved an 80% syntactic validity rate, successfully producing well-formed Turtle files with structurally correct SPARQL queries. To a human reviewer, this code appeared indistinguishable from expert-written logic. However, the functional accuracy of this "valid" code was only $\approx 25\%$.

This discrepancy reveals that the model has successfully memorized the *grammar* of SHACL (e.g., correct brackets, prefixes, keywords) but failed to grasp the *semantics* of the query it was constructing. The model "knows" how to write a query, but it does not "understand" well enough what the query actually calculates.

5.1.2 Structural Logic Failures

The model's inability to properly understand graph topology led to recurring critical failures in the generated SPARQL constraints. Below we analyze some of the most prominent mistakes discovered upon human inspection of the runs flagged by the system as not perfect.

The Double-Counting Trap

In scenarios involving family units (for example, two parents with two children), the model consistently failed to apply set-theoretic distinctness. By generating queries that traversed from `:Parent` to `:Child` without the `COUNT(DISTINCT ?child)` modifier, the model inadvertently created a multiplicative join. Since both parents are linked to the same children, the query counted each child twice (once per parent path), artificially inflating the "Child Count" variable. This subsequently distorted calculations, leading to false validations where ineligible families were approved due to miscalculated thresholds.

The Cartesian Product Trap

Similarly, when aggregating income, the model frequently joined Income patterns and Child patterns in a single WHERE clause without sub-query separation. This caused the SPARQL engine to generate a Cartesian product of the two datasets, effectively multiplying every income record by every child record. This resulted in erroneous rejections where families were flagged with violations due to massive over-estimations of total family incomes.

Recursive Loops and Infinite Regression

A more catastrophic failure mode was observed in the Flash model's handling of bidirectional relationships. The Student Housing ontology defines inverse relationships (e.g., a `:Parent` has a `:Child`, and that `:Child` has a `:Parent`). In several runs, the model generated SPARQL property paths that traversed these links cyclically (e.g., `:hasParent :hasChild :hasParent ...`) without a terminating condition. This created infinite recursion loops during execution, causing the PySHACL validation engine to crash entirely (logged as "Python Kernel Crash" in Section 4.4.1). This demonstrates that the model treats graph traversal as a linguistic association task ("Parents are related to Children") rather than a directed graph walk, failing to anticipate the computational consequences of such cycles.

5.2 Syntax Hallucination and Language Bleed

While the Pro model's failures were primarily logical, the Flash model struggled to maintain the boundaries of the language itself. The experimental data reveals a phenomenon of "Language Bleed," where the model, optimized for high-throughput generalized text generation, conflated the syntax of semantically similar languages.

5.2.1 SQL Contamination

The most frequent syntax error was the appearance of illegitimate keywords, such as `FILTER NOT (...)`. This construct is valid in SQL (`WHERE NOT`) but invalid in SPARQL (which requires `FILTER (! ...)` or `FILTER NOT EXISTS`). This suggests that the model's training

data contains significantly more SQL examples than SPARQL, leading it to default to the more dominant syntax when the probability distribution for the next token is ambiguous.

5.2.2 Token-Level Hallucinations

The model also exhibited errors that reveal its nature as a token predictor rather than a parser. The insertion of a dot (.) after BIND statements violates SPARQL grammar (where dots act as triple delimiters). This indicates the model might be trying to treat the code line as a natural language sentence that requires a period, ignoring the strict syntax tree of the query language.

Furthermore, the model frequently attempted to use dot notation (e.g., `?s.hasChild`) or complex property path slashes (e.g., `?s /:hasChild`) in contexts where explicit triple patterns were required. While property paths exist in SPARQL 1.1, the specific context in which such syntax was generated often mimicked Object-Oriented programming accessors rather than valid RDF graph traversal.

5.2.3 Namespace Invention

A distinct class of errors involved the hallucination of ontology definitions. Despite being provided with a fixed set of prefixes, the model occasionally invented new namespaces (e.g., using the deprecated 2007 SHACL draft URI or inventing an `ex:Citizen` ontology). This behavior was the primary cause of all recorded "RDF Syntax Errors" (as distinct from SPARQL errors), confirming that smaller models struggle to adhere to strict "Negative Constraints" (i.e., "Do not use any other prefix").

5.3 The Trade-off of Abstraction vs. Fidelity

A widely held assumption in Large Language Model research is that "Model Capability" (size, reasoning power) correlates linearly with performance across all tasks. However, the experimental results from the "Parental Leave" use case reveal a critical inversion of this principle.

5.3.1 The "Smart Model" Trap

The extraction of eligibility preconditions requires extreme fidelity to the source text. Legal constraints often rely on specific enumerations that define the scope of the law. Such a case was presented when models came across the following precondition in the Parental Leave use case: *"The applicant must be employed under a dependent employment regime, in the Private or Public sector."*

In this task, the Gemini 2.5 Flash model (theoretically less capable model) significantly outperformed the Gemini 2.5 Pro model. Flash, lacking the capacity for deep abstraction, tended to "copy-paste" the precondition literally. When presented with the employment

requirement, it preserved the disjunction ("Private OR Public").

Pro, optimized for high-level reasoning and helpfulness, attempted to "summarize" the requirement. It interpreted "Private or Public" as a generic concept ("Employed"), effectively deleting the exclusion of other sectors (e.g., Freelancers). This finding suggests that for compliance tasks, "Smart" models may be fundamentally misaligned with the goal. Their training bias towards summarization and abstraction leads to Semantic Drift, where the gist of the rule is preserved but the legal boundary is lost.

5.3.2 The Deterministic Superiority

This trade-off extends to the architectural design of the pipeline itself. A stark contrast was observed between the error rates of the neural components and the symbolic components.

Notably, zero syntax errors were recorded in the generation of the "Citizen-Service Graph" (Stage 3). This stage relied on deterministic Python code to serialize the graph based on the LLM-derived Information Model, rather than asking the LLM to generate the Turtle syntax directly. The perfect stability of this stage, contrasted with the high failure rate of the LLM-generated SHACL shapes (Stage 4), empirically validates the architectural decision to offload structural tasks to deterministic code wherever possible.

This leads to a key design principle for Neuro-Symbolic systems in public administration: LLMs are necessary for interpretation (Extraction), but they are suboptimal for serialization (Code Generation). A robust pipeline must treat the LLM as a "Translator" of natural language, but never as an "Architect" of the final system structure.

5.4 The Complexity Ceiling

The divergence in performance between the "Student Housing" and "Parental Leave" use cases identifies a distinct Complexity Ceiling for current LLM-based logic generation. While the pipeline demonstrated high viability for administrative tasks involving categorical classification (Parental Leave), it experienced a near-total collapse when tasked with recursive arithmetic (Student Housing).

This failure mode correlates strongly with the Dependency Depth of the required logic:

- **Shallow Dependencies (Success):** Constraints that rely on single-node checks (e.g., *Nationality* depends only on *Applicant*) or flat Boolean logic (e.g., *isValid* is True OR False) were handled with high accuracy (88.9% logic success).
- **Deep Dependencies (Failure):** Constraints that require multi-hop traversal (e.g., *Applicant* → *Parent* → *Residence*) or recursive variable modification (e.g., *Income Limit* changes based on *Dependent Child Count*) consistently triggered the "Cartesian Product" bug or infinite recursion errors.

This suggests that while the tested LLMs can successfully act as "Semantic Parsers" for straightforward bureaucracy, they lack the internal "Working Memory" required to maintain

the state of multi-variable equations throughout the code generation process.

5.5 The Contribution of Prompt Engineering

The experimental results challenge the prevailing narrative that "better prompting" is a universal solution to model limitations. Instead, the data reveals complex trade-offs where techniques that improve syntactic stability may inadvertently degrade logical reasoning.

5.5.1 The "Copy-Paste" Bias

The Default (Few-Shot) strategy proved essential for stabilizing syntax in the Pro model, boosting syntactic validity from 60% to 80% on the complex document. However, this stability came at a cost to logical accuracy. Zero-Shot strategy, despite producing broken code more often, achieved the highest logical accuracy (33.3%) when it *did* compile.

This suggests a "Copy-Paste Bias": when provided with examples, the model seems to over-fit to the logic of the few-shot template, attempting to force the new problem into the old structure. Without examples (Zero-Shot), the model is forced to reason from first principles, leading to messier syntax but potentially more original (and correct) logical derivations.

5.5.2 The Failure of Self-Correction

The Reflexion strategy failed to deliver the expected performance gains. For the less capable Flash model on the complex document, Reflexion actually *degraded* performance, dropping syntax validity from 20% to 5%. This indicates that a model incapable of solving a problem in the first pass is equally incapable of critiquing its own solution. Asking a confused model to "double-check" its work merely introduces a second opportunity for hallucination, compounding errors rather than resolving them.

5.5.3 The Engineering Ceiling

These findings imply an "Engineering Ceiling": one cannot prompt their way out of a fundamental reasoning deficit. While Prompt Engineering can guide a capable model (Pro) to follow syntactic rules, it cannot bestow reasoning capabilities upon a smaller model (Flash) that physically lacks them. For high-stakes logic generation, architectural scale remains the dominant variable.

5.6 Feasibility and Sovereignty

The final dimensions of analysis concern the operational viability of deploying such a system within a public administration context. The experimental campaign revealed critical vulnerabilities in the reliance on proprietary Model-as-a-Service (MaaS) infrastructure.

5.6.1 The Semantic Drift of "Eligibility"

Feasibility is first challenged at the point of ingestion. The extraction and summarization phase (Stage 1) demonstrated a persistent ambiguity in defining "Eligibility." Despite explicit prompt instructions to ignore administrative steps, the model frequently conflated procedural requirements (e.g., "Log in to TaxisNet") with substantive facts (e.g., "Be employed"). This semantic drift creates a system that validates paperwork rather than reality. While acceptable for a pilot, a production system would require a stricter, legally-grounded ontology of "Evidence" vs. "Conditions" to prevent the digitization of bureaucracy from becoming merely the automation of red tape.

5.6.2 Replication Crisis

The most severe threat to feasibility, however, emerged from the infrastructure itself. During the experimental window, unannounced changes to the Google Gemini API rate limits and model availability caused a sudden, catastrophic degradation in pipeline throughput. This event serves as a potent case study for Digital Sovereignty.

A public administration pipeline that relies on opaque, third-party endpoints is fundamentally fragile. The inability to guarantee consistent latency, availability, or even model behavior (version drift) renders MaaS solutions unsuitable for critical government infrastructure. The findings of this study strongly advocate for a shift towards Sovereign AI: deploying open-weights models (e.g., Llama 3, Mistral) on government-controlled infrastructure. Only by owning the compute can the administration guarantee the reproducibility and stability required for legal automation.

5.7 Risk Asymmetry in Public Administration

The evaluation of the system's "Recommender Accuracy" (Section 4.4.2) reveals a critical insight into the deployment readiness of these neuro-symbolic agents. While standard machine learning models optimize for balanced F1 scores, the operational context of public administration imposes an asymmetric cost of error.

The experimental data showed a 10.1% False Positive Rate, which corresponds to instances where the system erroneously recommended a service to an ineligible citizen. In a commercial context (e.g., movie recommendations), such errors are trivial. However, in digital governance, a False Positive actively generates bureaucratic friction. Specifically, it compels a citizen to gather documents and submit an application that is destined to fail. This wastes public resources and also erodes trust in the automated system. Conversely, the 3.7% False Negative Rate (Missed Opportunities), while statistically undesirable, represents a "safer" failure mode that maintains the status quo.

Consequently, the current pipeline's bias towards 'over-recommending' presents a

significant barrier to unsupervised deployment in a real-world administrative setting.

6 Limitations & Future Work

6.1 Limitations

limited document sample size, API restrictions and the reliance on a specific vendor's ecosystem, limited prompt engineering, limited models (free tier).

Replication Crisis: Critique the reliance on proprietary Model-as-a-Service infrastructure, arguing that operational instability renders them unsuitable for critical pipelines. Maybe this can be in the Limitations chapter.

more human interpretation of the results is needed. it's difficult to pinpoint logic errors within complex queries.

6.2 Future Research Directions

a roadmap for using local open-source models to ensure sovereignty, the implementation of iterative "Self-Correction" agents to fix syntax errors, ideas for more robust testing of this kind of pipeline, ideas not implemented by this work for scoping reasons.

The decision to base the schema on an existing vocabulary was with good reason. This design allows the graphs generated by the pipeline to include more classes of the used ontologies, for future integration with more sophisticated systems. The pipeline itself could also be expanded upon to include more classes.

Make an effort to find why the pipeline failed logically when it did. Many times it was the preconditions extraction and not the text-to-logic part. many times the models failed to correctly interpret what was a precondition and what was an administrative step.

Semantic Stability: data from semantic similarity metrics drawn from past run artifacts on file.

future iterations of the pipeline must prioritize Precision (Trustworthiness) over Recall (Coverage), potentially by calibrating the validation logic to be "conservative by default" or by implementing a "Human-in-the-Loop" review for all positive recommendations.

For public services involving means-testing, complex family unit aggregations, or temporal operations, the current neuro-symbolic approach requires either significantly more advanced prompting strategies or even a fundamental shift to deterministic calculation engines for the mathematical components.

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A Appendix placeholder

Extracts of the generated SHACL shapes (both valid and broken examples).

Samples of the YAML Mutation Scenarios.

Samples of RDFS Ontologies used.