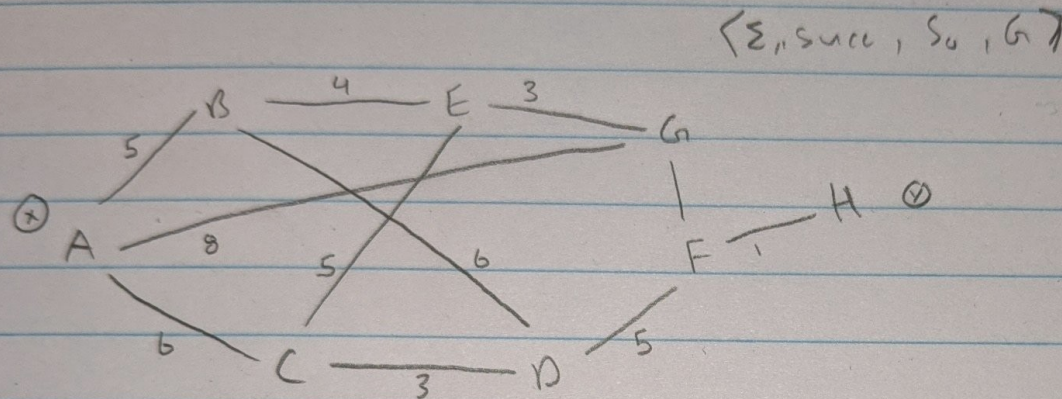


# Assignment #1



30/30

a)

Each state is a pair of cities indicating the location of  $x$  and the location of  $y$  (e.g.,  $(A, H)$ ). Something like:

$\begin{matrix} \uparrow & \uparrow \\ x & y \end{matrix}$

location   location

$A = \{A, B, C, D, E, F, G, H\}$   
 $B = A \times A$   
 $\Sigma = \{A, B \mid A \in B\} ???$

$\Sigma = \text{set of states} = \{(A, A), (B, B), (C, C), (D, D), (E, E), (F, F), (G, G), (H, H),$   
 $(A, B), (B, A), (C, A), (D, A), (E, A), (F, A), (G, A), (H, A),$   
 $(A, C), (B, C), (C, B), (D, B), (E, B), (F, B), (G, B), (H, B),$   
 $(A, D), (B, D), (C, D), (D, C), (E, C), (F, C), (G, C), (H, C),$   
 $(A, E), (B, E), (C, E), (D, E), (E, D), (F, D), (G, D), (H, D),$   
 $(A, F), (B, F), (C, F), (D, F), (E, F), (F, E), (G, E), (H, E),$   
 $(A, G), (B, G), (C, G), (D, G), (E, G), (F, G), (G, F), (H, F),$   
 $(A, H), (B, H), (C, H), (D, H), (E, H), (F, H), (G, H), (H, G)\}$

Yes, it is long if you list every element. See my solution.

b)

The tree...

} that's long...



$(A,C), (B,C), (C,B), (D,B), (E,B), (F,B), (G,B), (H,B)$   
 $(A,D), (B,D), (C,D), (D,C), (E,C), (F,C), (G,C), (H,C)$   
 $(A,E), (B,E), (C,E), (D,E), (E,D), (F,D), (G,D), (H,D)$   
 $(A,F), (B,F), (C,F), (D,F), (E,F), (F,E), (G,E), (H,E)$   
 $(A,G), (B,G), (C,G), (D,G), (E,G), (F,G), (G,F), (H,F)$   
 $(A,H), (B,H), (C,H), (D,H), (E,H), (F,H), (G,H), (H,G)$

} that's long... needs a more-precise formulation for succ

20/40 b) The transition between states are when  $x$  and  $y$  move to a new location, (succ). Such as  $(A,H) \rightarrow (C,F) \rightarrow (D,D)$ .

I think the way to represent this is:  $\{\text{succ} \subseteq \Sigma \mid (x,y) \in \text{succ}\} \subseteq \Sigma^2$ ?

10/10 d)  $G = \{(A,A), (B,B), (C,C), (D,D), (E,E), (F,F), (G,G), (H,H)\}$

10/10 c)  $\delta = \{(A,H)\}$

10/10 e)  $N = \# \text{ of nodes which is } 8$  so  $N^2 = 64$ , there are 64 states. In other words, there are 64 different combinations to the locations  $x$  and  $y$  can have with 8 of them being the same.