

✓ Risk Analysis for Top 10 Holdings Daily Prices in the Portfolio

```

1 import pandas as pd
2 import numpy as np
3 from scipy.stats import norm
4 import yfinance as yf
5 import matplotlib.pyplot as plt
6 import seaborn as sns

1 # Loading the dataset
2 file_name = "Top 10 Holdings Daily Prices.csv"
3 data = pd.read_csv(file_name, index_col = 0)

1 # Convert index to datetime objects, handling potential errors by setting invalid dates to NaT (Not a Time)
2 data.index = pd.to_datetime(data.index, format="%m/%d/%Y", errors="coerce")
3
4 # Remove rows with NaT (invalid) dates in the index
5 if data.index.isnull().any():
6     data = data[data.index.notnull()]
7
8 # Sort the DataFrame by date (ascending)
9 data = data.sort_index()
10
11 # Calculate daily returns for each asset, skipping the first row (NaN due to pct_change)
12 returns = data.pct_change(fill_method=None).dropna()
13
14 # Calculate the daily volatility (standard deviation) of each asset's returns
15 sigma = returns.std()
16
17 # Define the start and end dates for the analysis based on available data
18 start_date = returns.index.min()
19 end_date = returns.index.max()
20
21 # Format the start and end dates as strings for yfinance
22 start_date_str = start_date.strftime('%Y-%m-%d')
23 end_date_str = end_date.strftime('%Y-%m-%d')
24
25 # Download historical data for the S&P 500 (^GSPC) from Yahoo Finance within the specified date range
26 sp500_data = yf.download("^GSPC", start=start_date_str, end=end_date_str)
27
28
29 # Check if the S&P 500 data was downloaded successfully. Raise an error if not.
30 if sp500_data.empty:
31     raise ValueError("Failed to download ^GSPC data. Please check the date range and internet connection.")
32
33 # Calculate daily returns for the S&P 500 using the Adjusted Close price
34 sp500_returns = sp500_data['Adj Close'].pct_change().dropna()
35
36 # Rename the S&P 500 returns series to '^GSPC' for consistency
37 sp500_returns.name = "^GSPC"
38
39 # Merge the S&P 500 returns with the asset returns, using only dates present in both DataFrames
40 returns = returns.join(sp500_returns, how='inner')
41
42 # Define a function to calculate the tracking error against a benchmark
43 def calculate_tracking_error(asset_returns, benchmark_returns):
44     return np.std(asset_returns - benchmark_returns)
45
46 # Calculate the tracking error for each asset against the S&P 500 if S&P data is available
47 if "^GSPC" in returns.columns:
48     benchmark_returns = returns["^GSPC"]
49     tracking_errors = {
50         ticker: calculate_tracking_error(returns[ticker], benchmark_returns)
51         for ticker in returns.columns if ticker != "^GSPC"
52     }
53 else:
54     print("^GSPC was not found in the dataset. Skipping Tracking Error calculation.")
55     tracking_errors = None
56
57 # Define a function to calculate Value at Risk (VaR) using the parametric method
58 def calculate_var(asset_returns, confidence_level=0.95):
59     mean_return = asset_returns.mean()
60     std_dev = asset_returns.std()
61     z_score = norm.ppf(1 - confidence_level)
62     var = mean_return + z_score * std_dev
63     return var
64

```

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65
66 # Calculate VaR at the 95% confidence level for each asset
67 vars_95 = returns.apply(lambda x: calculate_var(x, 0.95))
68
69 # Create a DataFrame to summarize the risk metrics
70 risk_summary = pd.DataFrame({
71     "Sigma (Volatility)": sigma,
72     "VaR (95%)": vars_95
73 })
74
75 # Add Tracking Error to the summary if it was calculated
76 if tracking_errors:
77     risk_summary["Tracking Error (vs S&P500)"] = pd.Series(tracking_errors)
78
79 # Remove the S&P 500 row from the summary, as it's not an asset being analyzed
80 risk_summary = risk_summary.drop('^GSPC', errors='ignore')
81 # Drop the last row
82 risk_summary = risk_summary.iloc[:-1]
83
84 # Print the risk summary to the console
85 print("\nRisk Analytics Summary:")
86 print(risk_summary)

```

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✓ Sigma

When looking at the sigma, the stock with the highest volatility is NVDA which has (0.0306) and Hes which has (0.2777). This is showing that the higher the volatility is then greater the price fluctuations. The lowest sigma is the IVV which is (0.112). This is showing that it is the most stable volatility in the stock given in the dataset.

VAR

When looking at the var the least amount of risk is IVV which is (-0.0179). This is showing that it has the lowest potential loss when looking at it by the value of risk perspective. The more risky investment option in the dataset is NVDA which is (-0.477) because it has the highest potential loss comparing to the rest of the stocks.

Tracking error

The highest tracking error is NVDA which has (0.0250) and HES which has (0.0239). This shows that the datapoints are away from the benchmark line which indicates that it has the high amount of tracking errors in the dataset. The lowest tracking error within the dataset is IVV which is (0.0005). This is showing that it is linear to the benchmark which indicates lowest amount of tracking errors.

```

1 # Load your dataset (assuming it's preprocessed)
2 data_returns = pd.read_csv('Top 10 Holdings Daily Prices.csv', index_col=0)
3 data_returns.index = pd.to_datetime(data_returns.index, format='%m/%d/%Y', errors='coerce')
4 data_returns.to_csv("data_returns_daily_prices_parse_dates.csv")
5
6 # Compute risk metrics using simple calculations
7 # 1. Volatility (Standard Deviation of returns for each stock)
8 volatility = data_returns.std()
9
10 # 2. Tracking Error (Difference of stock returns and average benchmark, then standard deviation)
11 benchmark = data_returns.mean(axis=1)
12 tracking_error = data_returns.sub(benchmark, axis=0).std()
13
14 # 3. Value at Risk (VaR at 95% confidence level)
15 VaR_95 = data_returns.quantile(0.05)
16
17 # Combine results into a DataFrame
18 risk_metrics = pd.DataFrame({
19     'Volatility ( $\sigma$ ): volatility,
20     'Tracking Error': tracking_error,
21     'VaR (95%): VaR_95
22 })
23
24 risk_metrics = risk_metrics.iloc[:-1]
25 risk_metrics = risk_metrics.iloc[1:]
26 print(risk_metrics)

```

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```

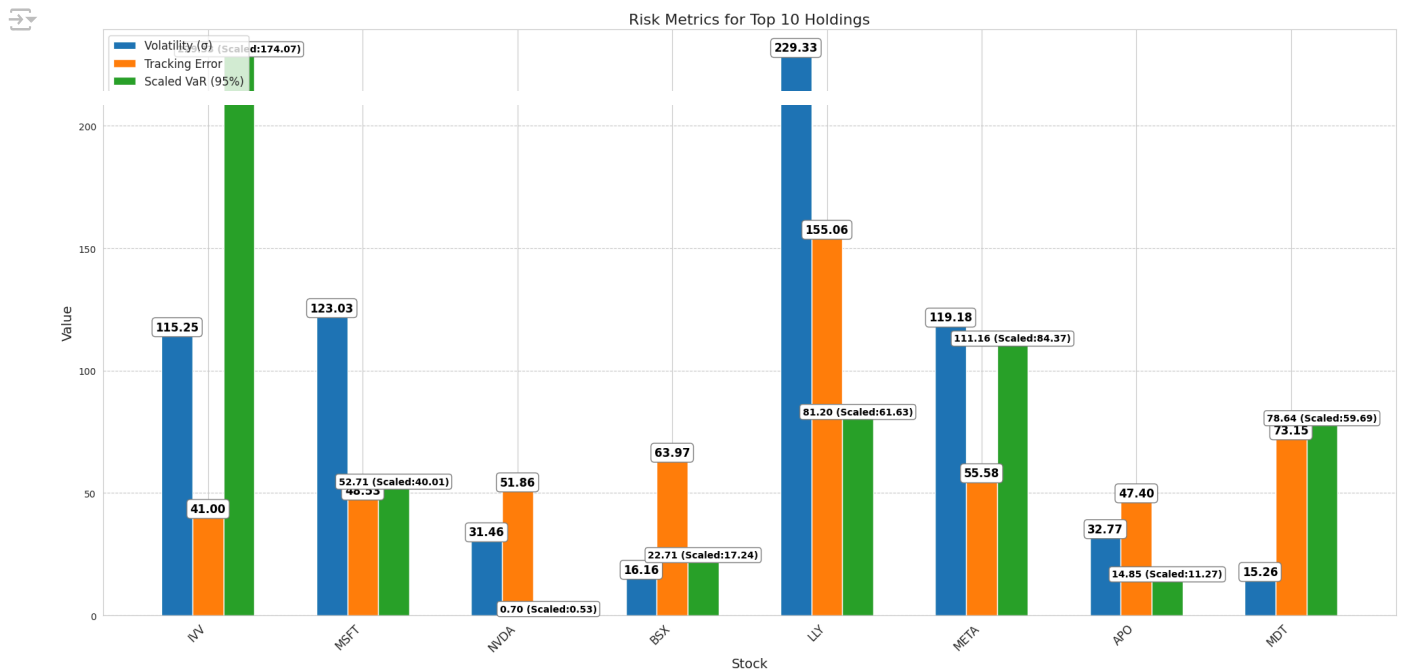
1 sns.set_style("whitegrid")
2
3 fig, ax = plt.subplots(figsize=(20, 10))
4 width = 0.2

```

```

5 x = np.arange(len(risk_metrics.index))
6
7 colors = sns.color_palette("tab10", 3)
8
9 max_val = risk_metrics[['Volatility ( $\sigma$ )', 'Tracking Error']].max().max()
10 risk_metrics['Scaled VaR (95%)'] = abs(risk_metrics['VaR (95%)']) * max_val / abs(risk_metrics['VaR (95%)']).max()
11
12
13 ax.bar(x - width, risk_metrics['Volatility ( $\sigma$ )'], width, label='Volatility ( $\sigma$ )', color=colors[0])
14 ax.bar(x, risk_metrics['Tracking Error'], width, label='Tracking Error', color=colors[1])
15 ax.bar(x + width, risk_metrics['Scaled VaR (95%)'], width, label='Scaled VaR (95%)', color=colors[2])
16
17 ax.set_xlabel('Stock', fontsize=14)
18 ax.set_ylabel('Value', fontsize=14)
19 ax.set_title('Risk Metrics for Top 10 Holdings', fontsize=16)
20 ax.set_xticks(x)
21 ax.set_xticklabels(risk_metrics.index, rotation=45, ha='right', fontsize=12)
22 ax.legend(loc='upper left', fontsize=12)
23 ax.grid(axis='y', linestyle='--')
24
25 # データラベルを追加 (小数点以下2桁まで表示)
26 for i, v in enumerate(risk_metrics['Volatility ( $\sigma$ )']):
27     ax.text(i - width, v, f'{v:.2f}', ha='center', va='bottom', fontweight='bold', fontsize=12, color='black', bbox=dict(facecolor='white', edgecolor='black'))
28 for i, v in enumerate(risk_metrics['Tracking Error']):
29     ax.text(i, v, f'{v:.2f}', ha='center', va='bottom', fontweight='bold', fontsize=12, color='black', bbox=dict(facecolor='white', edgecolor='black'))
30
31 for i, (v, original_var) in enumerate(zip(risk_metrics['Scaled VaR (95%)'], risk_metrics['VaR (95%)'])):
32     ax.text(i + width, v, f'{v:.2f} (Scaled:{original_var:.2f})', ha='center', va='bottom', fontweight='bold', fontsize=10, color='black', bbox=dict(facecolor='white', edgecolor='black'))
33
34 ax.set_ylim(0, risk_metrics[['Volatility ( $\sigma$ )', 'Tracking Error', 'Scaled VaR (95%)']].max().max() + 10)
35
36 plt.tight_layout()
37 plt.show()

```



Graph 1: Volatility and Tracking Error for Top 10 Holdings

Volatility: LLY shows the highest volatility, followed by META and MSFT. NVDA and BSX show relatively low volatility. High volatility indicates significant price fluctuations, suggesting a high-risk, high-return investment potential. Conversely, low volatility indicates smaller price fluctuations, suggesting a low-risk, low-return investment potential.

Tracking Error: LLY shows the highest tracking error, followed by META and IVV. High tracking error indicates that the stock's performance significantly differs from the benchmark. Actively managed funds and stocks focused on specific sectors tend to have higher tracking errors."

Graph 2: Value at Risk (95%) for Top 10 Holdings (Log Scale)

VaR (95%): IVV shows the highest VaR, followed by META and MDT. VaR indicates the maximum potential loss that could occur with a 95% probability over a specific period (unspecified here). While the differences appear small due to the logarithmic scale, they are actually quite significant. For example, IVV's VaR is approximately 174, while NVDA's VaR is about 0.5, representing a difference of more than 300 times. A high VaR indicates a higher risk of substantial losses.

✓ Comprehensive Analysis of Both Graphs:

LLY - High Risk, High Return: Showing high values across volatility, tracking error, and VaR, it can be considered the riskiest stock. However, high risk also suggests the potential for high returns.

NVDA - Low Risk, Low Return: Demonstrating the lowest volatility and VaR, with low tracking error as well. While it can be considered the lowest-risk stock, it likely also offers lower return potential.

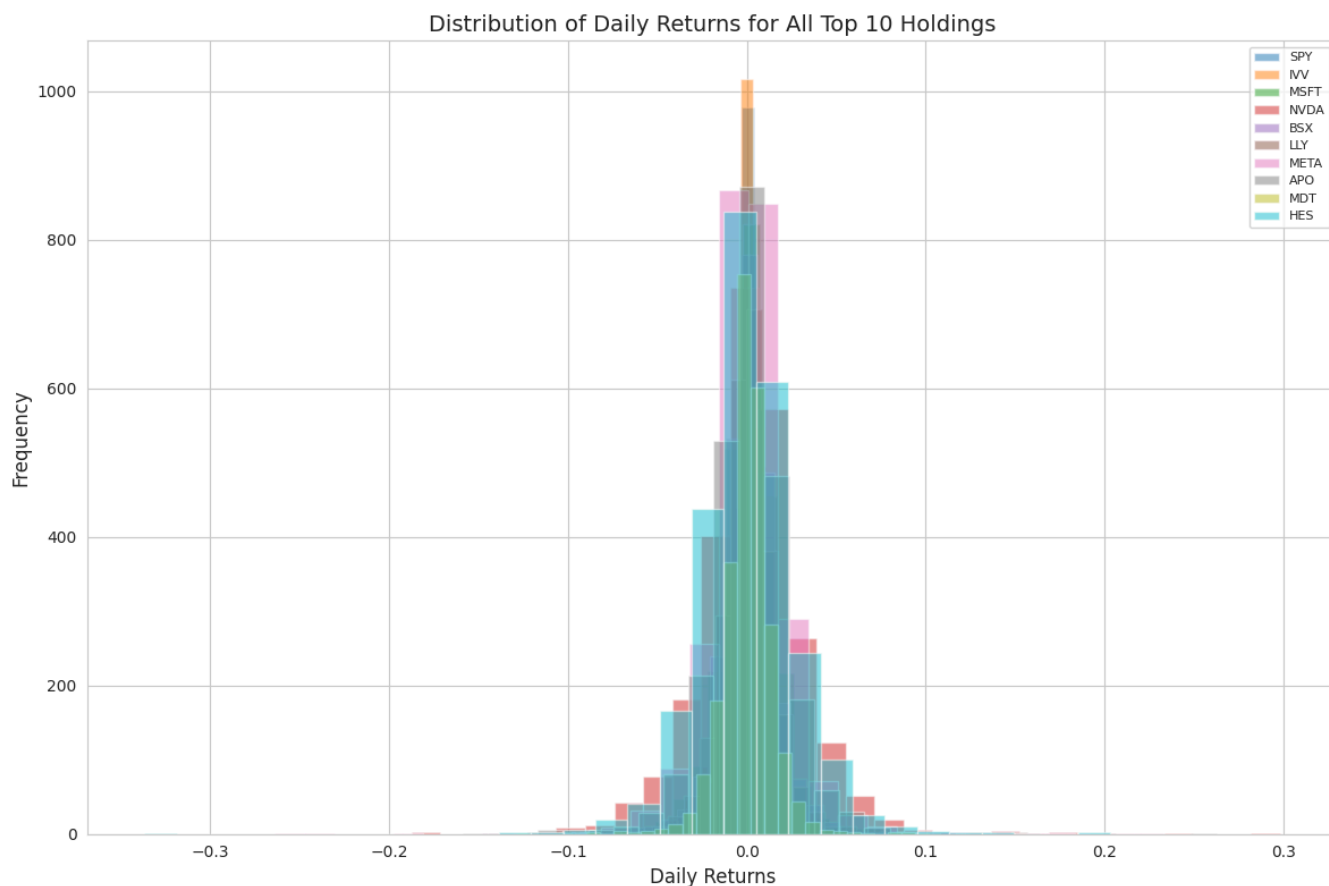
META - High Volatility but Moderate VaR: Despite high volatility and tracking error, its VaR isn't as high as IVV's. This suggests it carries less risk than

LLY while still offering potential for relatively high returns.

IVV - High VaR but Low Volatility: While there's a high possibility of significant losses, daily price fluctuations are relatively stable."

```
1 # Calculate daily returns
2 daily_returns = data_returns.pct_change().dropna()
3
4 # Plot all stock histograms overlaid on a single plot
5 plt.figure(figsize=(12, 8))
6
7 for col in daily_returns.columns:
8     plt.hist(daily_returns[col], bins=30, alpha=0.5, label=col)
9
10 plt.xlabel('Daily Returns', fontsize=12)
11 plt.ylabel('Frequency', fontsize=12)
12 plt.title('Distribution of Daily Returns for All Top 10 Holdings', fontsize=14)
13 plt.legend(fontsize=8, loc='upper right')
14 plt.tight_layout()
15 plt.show()
```

```
<ipython-input-21-f4063960639c>:2: FutureWarning: The default fill_method='pad' in DataFrame.pct_change is deprecated and will be removed in a future version.
daily_returns = data_returns.pct_change().dropna()
```



Overall Distribution Shape

- Most stocks, as well as the overall distribution, show a bell-shaped distribution concentrated around the mean value, closely resembling a normal distribution. This is consistent with the general financial market assumption that daily returns follow a random walk.
- The peak of the distribution is concentrated around 0, suggesting that daily price movements are relatively small.
- Some stocks (e.g., LLY, BSX) have slightly wider tails, suggesting a higher likelihood of large positive or negative returns compared to other stocks. This indicates that these stocks may have higher volatility.

✓ Rate of Return (Monthly and Annually) for Top 10 Holdings in the Portfolio

```
1 # Import necessary libraries
2 import pandas as pd
3
4 # Load the CSV file
5 file_path = "/content/Top 10 Holdings Daily Prices.csv"
6 df_daily_prices = pd.read_csv(file_path)
7
8 # Rename the 'Date' column for clarity and convert it to datetime format
9 df_daily_prices.rename(columns={'Date': 'price_date'}, inplace=True)
10 df_daily_prices['price_date'] = pd.to_datetime(df_daily_prices['price_date'])
11
12 # Adjust the dataframe to have 'ticker', 'price_date', and 'price' columns
13 df_prices_melted = df_daily_prices.melt(id_vars=['price_date'], var_name='ticker', value_name='price') # (pandas.DataFrame.melt - Pandas 2.2.3 Docu
14
15 # Extract monthly and annual price data (last price of each month/year)
16 df_prices_melted['month'] = df_prices_melted['price_date'].dt.to_period('M')
17 monthly_prices = (
18     df_prices_melted.groupby(['ticker', 'month'])
19     .agg({'price_date': 'max', 'price': 'last'})
```

```

20     .reset_index()
21 )
22 monthly_prices['formatted_date'] = monthly_prices['price_date'].dt.strftime('%Y-%m-%d')
23
24 df_prices_melted['year'] = df_prices_melted['price_date'].dt.year
25 annual_prices = (
26     df_prices_melted.groupby(['ticker', 'year'])
27     .agg({'price_date': 'max', 'price': 'last'})
28     .reset_index()
29 )
30 annual_prices['formatted_date'] = annual_prices['price_date'].dt.strftime('%Y-%m-%d') #(Pandas Time Series: Find the Sum/Avg/Min/Max of Each Day/M
31
32 # Calculate monthly rate of return
33 monthly_prices['monthly_return'] = (
34     monthly_prices.groupby('ticker')['price'].pct_change()
35 ) #(How to Calculate Stock Returns in Python:: Coding Finance -, 2018)
36
37 # Calculate annual rate of return
38 annual_prices['annual_return'] = (
39     annual_prices.groupby('ticker')['price'].pct_change()
40 ) #(Pandas.DataFrame.Pct_Change - Pandas 2.2.3 Documentation, n.d.)(Bobbitt, 2024)
41
42 # Filter data for the period from 2021 to 2024
43 monthly_returns_2021_2024 = monthly_prices[
44     (monthly_prices['month'] >= '2021-01') & (monthly_prices['month'] <= '2024-12')
45 ]
46 annual_returns_2021_2024 = annual_prices[
47     (annual_prices['year'] >= 2021) & (annual_prices['year'] <= 2024)
48 ] #(K, 2021)
49
50 # Save results to CSV files
51 monthly_returns_2021_2024.to_csv('/content/Monthly_Returns_2021_2024.csv', index=False)
52 annual_returns_2021_2024.to_csv('/content/Annual_Returns_2021_2024.csv', index=False)
53
54 # Display the results
55 print("Monthly Returns (2021-2024):")
56 print(monthly_returns_2021_2024[['ticker', 'formatted_date', 'price', 'monthly_return']])
57
58 print("\nAnnual Returns (2021-2024):")
59 print(annual_returns_2021_2024[['ticker', 'formatted_date', 'price', 'annual_return']])


1 # Import graph libraries
2 import matplotlib.pyplot as plt
3
4 # Step 1: Plot Monthly Returns
5 plt.figure(figsize=(12, 6))
6 for ticker in monthly_returns_2021_2024['ticker'].unique():
7     ticker_data = monthly_returns_2021_2024[monthly_returns_2021_2024['ticker'] == ticker]
8     plt.plot(
9         ticker_data['formatted_date'],
10        ticker_data['monthly_return'],
11        label=ticker
12    )
13
14 plt.title("Monthly Returns (2021-2024)")
15 plt.xlabel("Date")
16 plt.ylabel("Monthly Return")
17 plt.xticks(rotation=45, fontsize=8)
18 plt.legend(title="Ticker", loc='upper left', bbox_to_anchor=(1.05, 1), fontsize=8)
19 plt.grid(True, linestyle='--', alpha=0.7)
20 plt.tight_layout()
21 plt.show()
22
23 # Step 2: Plot Annual Returns
24 plt.figure(figsize=(12, 6))
25 for ticker in annual_returns_2021_2024['ticker'].unique():
26     ticker_data = annual_returns_2021_2024[annual_returns_2021_2024['ticker'] == ticker]
27     plt.bar(
28         ticker_data['formatted_date'],
29         ticker_data['annual_return'],
30         label=ticker
31     )
32
33 plt.title("Annual Returns (2021-2024)")
34 plt.xlabel("Year")
35 plt.ylabel("Annual Return")
36 plt.xticks(rotation=45, fontsize=8)
37 plt.legend(title="Ticker", loc='upper left', bbox_to_anchor=(1.05, 1), fontsize=8)
38 plt.grid(True, linestyle='--', alpha=0.7)
39 plt.tight_layout()
40 plt.show()
41

```



Analysis

With the highest rates of return in 2021, 2023, and 2024, **NVDA** is clearly the best performer, according to the yearly returns chart. Other stocks that performed well include **SPY** and **HES**, which showed consistent growth over the number of years. On the other hand, **META** and **LLY** had the lowest rates of return, especially in 2022 when both experienced drops.

The monthly returns chart shows a lot of volatility, especially in the best-performing equities like **SPY** and **NVDA**, which show strong returns surges at their peak months. On the other hand, the underperforming stocks, like **META** and **LLY**, show more frequent declines.

Modern Portfolio Theory Optimization

MPT using Beta and Expected Return

Using current portfolio equities allocations and calculated expected return through CAPM, optimize the portfolio solely on return.

```
1 !pip install requests
```

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```
1 import yfinance as yf
2 import pandas as pd
3 import numpy as np
4 import cvxpy as cp
5 import time
6
7 # Portfolio allocation data
8 tickers = ['SPY', 'IVV', 'MSFT', 'NVDA', 'SPOT', 'BSX', 'LLY', 'IBIT', 'META',
9            'FBTC', 'APO', 'MDT', 'HES', 'WFC', 'GOOGL', 'WDAY', 'RTX', 'PFE',
10           'CAN', 'LNG', 'GOOG', 'CME', 'ADBE', 'PH', 'EDR', 'MMM', 'ETN',
11           'BAC', 'TSM', 'JNPR', 'ICE', 'CVS', 'SHEL', 'PNC', 'CRH', 'XLF',
12           'IFF', 'ANSS', 'MSCI', 'DY', 'WMT', 'KKR', 'FAF', 'FERG', 'AAPL',
13           'DFS', 'V']
14
15 allocations = [0.113199837, 0.098079281, 0.069881488, 0.047813649, 0.036371067,
16               0.033510421, 0.031058439, 0.030241112, 0.026971802, 0.022885166,
17               0.021250511, 0.019615856, 0.019615856, 0.018798529, 0.016346547,
18               0.015937883, 0.015937883, 0.015937883, 0.015529219, 0.014711892,
19               0.014303228, 0.013894565, 0.013894565, 0.013894565, 0.013894565,
20               0.013077237, 0.012668574, 0.012668574, 0.01225991, 0.011851246,
21               0.011851246, 0.011851246, 0.011442583, 0.011442583, 0.011033919,
22               0.011033919, 0.011033919, 0.010625255, 0.010625255, 0.010625255,
23               0.010625255, 0.010625255, 0.010216592, 0.010216592, 0.010216592,
24               0.010216592, 0.010216592]
25
26 def get_beta(ticker):
27     try:
28         stock = yf.Ticker(ticker)
29         info = stock.info
30         beta = info.get('beta', np.nan)
31         return beta
32     except:
33         return np.nan
34
35 # Get beta for each ticker
36 betas = [get_beta(ticker) for ticker in tickers]
37
38 # Create a dataframe with all the information
39 df = pd.DataFrame({
40     'Ticker': tickers,
41     'Allocation': allocations,
42     'Beta': betas
43 })
44
45 # Filter out stocks without valid beta values
46 filtered_df = df.dropna(subset=['Beta'])
47
48 # Calculate expected returns based on CAPM
49 risk_free_rate = 0.04353
50 market_return = 0.10
51
52 filtered_df['Expected Return'] = risk_free_rate + filtered_df['Beta'] * (market_return - risk_free_rate)
53
54 # Set up optimization problem
55 n = len(filtered_df)
56
57 # Define variables for optimization (weights)
58 weights = cp.Variable(n)
59
60 # Define objective function: Maximize expected return while minimizing risk
61 expected_return = filtered_df['Expected Return'].values
62 cov_matrix = np.diag(filtered_df['Beta'].values) # Simplified covariance matrix
63
64 objective = cp.Maximize(expected_return @ weights - 0.5 * cp.quad_form(weights, cov_matrix))
65
66 # Constraints: Weights must sum to one and be non-negative
67 constraints = [cp.sum(weights) == 1,
```



```

68         weights >= 0]
69
70 # Solve the problem
71 problem = cp.Problem(objective, constraints)
72 problem.solve()
73
74 # Get optimized allocations
75 optimized_allocations = weights.value
76
77 # Update filtered dataframe with optimized allocations
78 filtered_df['Optimized Allocation'] = optimized_allocations
79
80 # Print results
81 print(filtered_df[['Ticker', 'Allocation', 'Beta', 'Expected Return',
82                   'Optimized Allocation']])
83
84 # Calculate and print portfolio metrics
85 original_portfolio_beta = np.sum(filtered_df['Beta'] * filtered_df['Allocation'])
86 optimized_portfolio_beta = np.sum(filtered_df['Beta'] * filtered_df['Optimized Allocation'])
87
88 print(f"\nOriginal Portfolio Beta: {original_portfolio_beta:.4f}")
89 print(f"Optimized Portfolio Beta: {optimized_portfolio_beta:.4f}")
90
91 original_expected_return = np.sum(filtered_df['Expected Return'] * filtered_df['Allocation'])
92 optimized_expected_return = np.sum(filtered_df['Expected Return'] * filtered_df['Optimized Allocation'])
93
94 print(f"\nOriginal Portfolio Expected Return: {original_expected_return:.4%}")
95 print(f"Optimized Portfolio Expected Return: {optimized_expected_return:.4%}")
96
97 # Create a DataFrame with the allocation comparison
98 tableau_df = pd.DataFrame({
99     'Ticker': filtered_df['Ticker'],
100     'Original_Allocation': filtered_df['Allocation'],
101     'Optimized_Allocation': filtered_df['Optimized Allocation'],
102     'Beta': filtered_df['Beta'],
103     'Expected_Return': filtered_df['Expected Return']
104 })
105
106
107 # Created a longer format version for easier visualization in Tableau
108 tableau_long = pd.melt(tableau_df,
109                        id_vars=['Ticker', 'Beta', 'Expected_Return'],
110                        value_vars = ['Original_Allocation', 'Optimized_Allocation'],
111                        var_name='Allocation_Type',
112                        value_name = 'Allocation')

```

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Analysis

The code uses the CAPM to calculate the expected return of each of the stocks, based on recent prices called through the yfinance API.

The reallocation of the portfolio results in a beta increase of 0.5, showing a much larger market sensitivity. This is an increase of systematic risk, which is a common strategy for a Hedge Fund to take on for higher returns.

The expected returns in this optimization increase from 7.8% to 11.8%

✓ Mean-Variance Portfolio Optimization

[4] Using the code from a github repository and adjusting it to use mean-variance optimization for the given portfolio.

```
1 !pip install pandas numpy matplotlib yfinance PyPortfolioOpt
```

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```

1 # Uses yfinance api to call adjusted closing prices of all stocks in portfolio
2 import os
3 if not os.path.isdir('data'):
4     os.system('git clone https://github.com/robertmartin8/PyPortfolioOpt.git')
5     os.chdir('PyPortfolioOpt/cookbook')
6 import yfinance as yf
7 import matplotlib.pyplot as plt
8 import pandas as pd
9 import numpy as np
10
11 # Define tickers to retrieve data for
12 tickers = ['SPY', 'IVV', 'MSFT', 'NVDA', 'SPOT', 'BSX', 'LLY', 'IBIT', 'META',

```

```

13     'FBTC', 'APO', 'MDT', 'HES', 'WFC', 'GOOGL', 'WDAY', 'RTX', 'PFE',
14     'CAN', 'LNG', 'GOOG', 'CME', 'ADBE', 'PH', 'EDR', 'MMM', 'ETN',
15     'BAC', 'TSM', 'JNPR', 'ICE', 'CVS', 'SHEL', 'PNC', 'CRH', 'XLF',
16     'IFF', 'ANSS', 'MSCI', 'DY', 'WMT', 'KKR', 'FAF', 'FERG', 'AAPL',
17     'DFS', 'V']
18
19 # Defines time period to call data for
20 ohlc = yf.download(tickers, period="max").loc["2020-07-01":]
21
22 # Uses adjusted closing price
23 prices = ohlc["Adj Close"].dropna(how="all")
24 prices.tail()

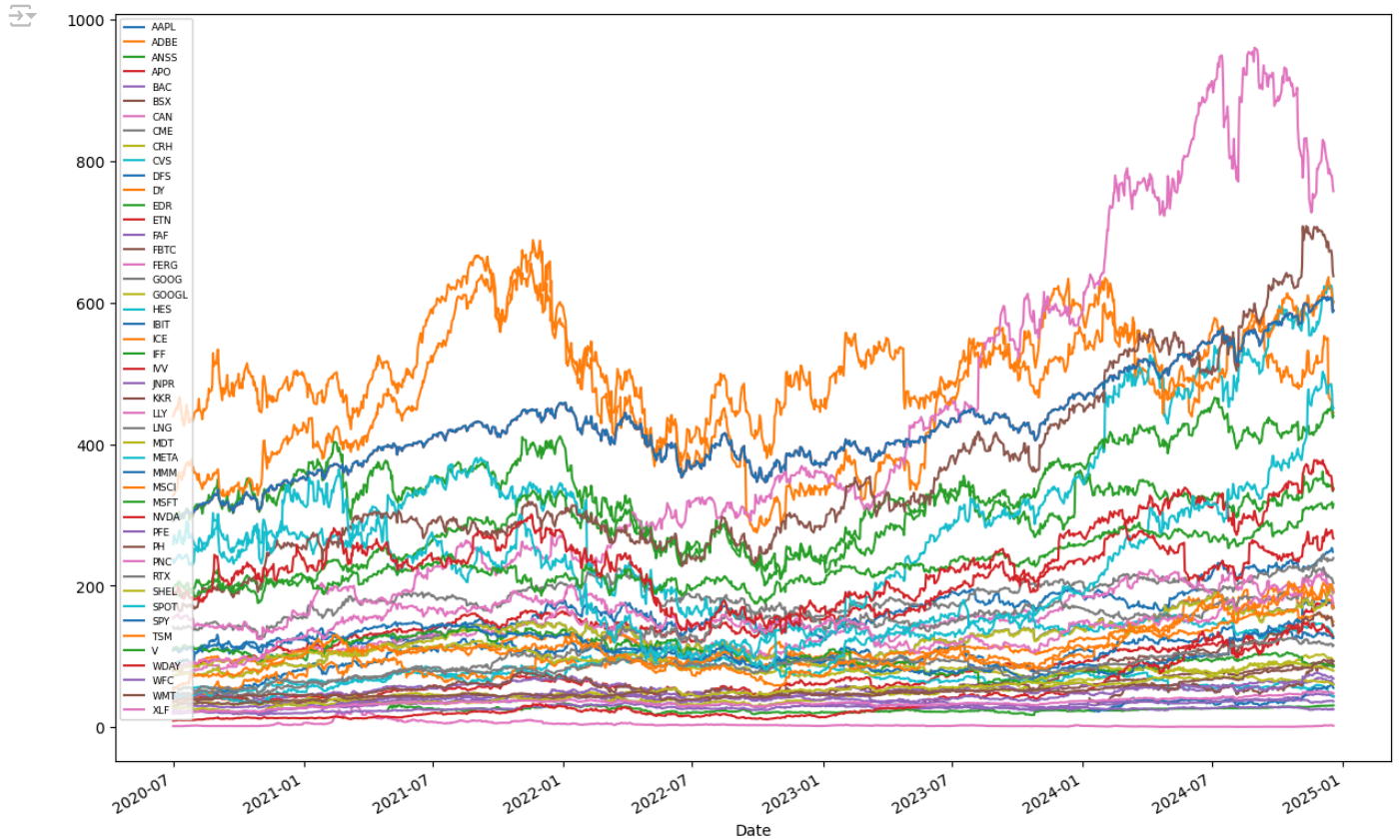
```

非表示の出力を表示

```

1 # Graphs out the prices
2 prices[prices.index >= "2020-07-01"].plot(figsize=(15,10))
3 plt.legend(loc='center left')
4 plt.legend(prop={'size': 6.5});

```



```

1 # Create a covariance matrix from the stock prices
2 from pypfpt import risk_models
3 from pypfpt import plotting
4
5 prices_clean = prices.dropna()
6 cov_matrix = risk_models.sample_cov(prices, frequency=252)
7 cov_matrix

```

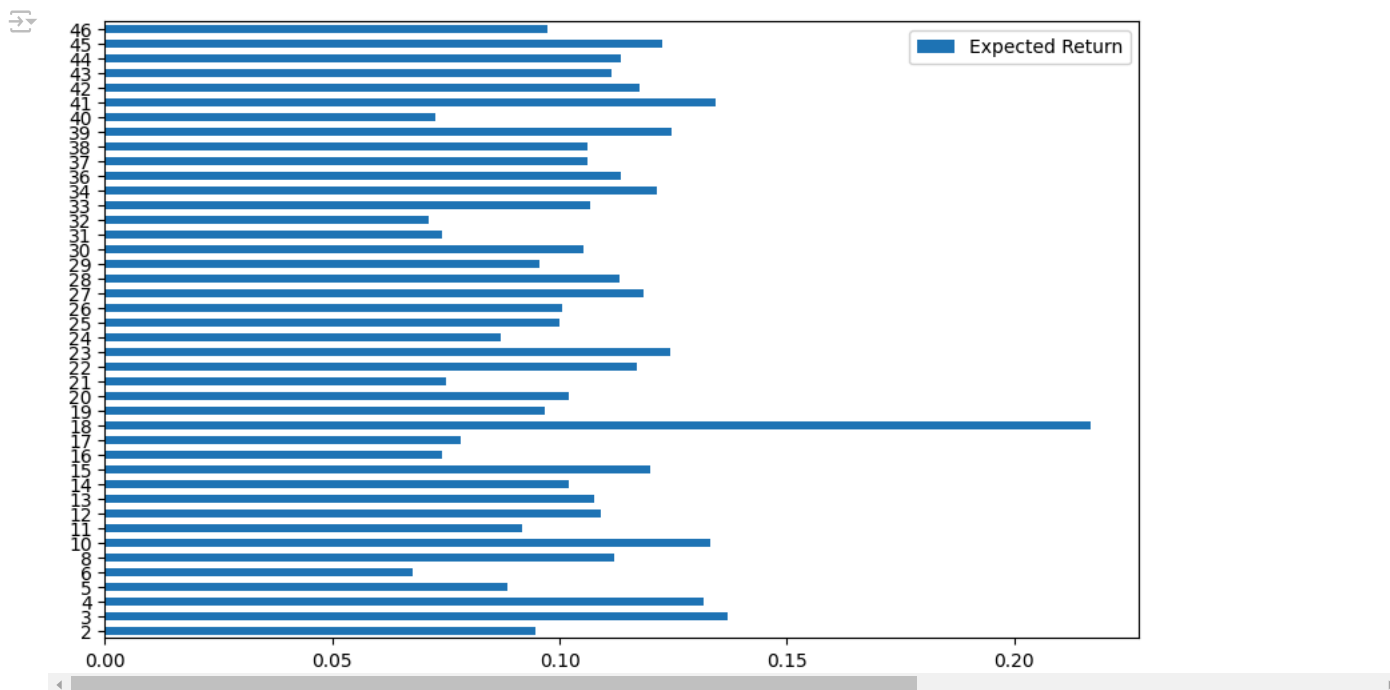
非表示の出力を表示

Adjusted Covariance Matrix

```

1 # Plot the covariance matrix
2 plotting.plot_covariance(cov_matrix, plot_correlation=True);

```

✓ Long/Short Optimization using Efficient Frontier

```

1 # Create a global-minimum variance portfolio allocation
2 # Calculate the Efficient Frontier for minimum variance
3 from pypfopt import EfficientFrontier
4
5 S = risk_models.CovarianceShrinkage(prices).ledoit_wolf()
6 ef = EfficientFrontier(None, S, weight_bounds=(None, None))
7 ef.min_volatility()
8 weights = ef.clean_weights()
9 weights

```

非表示の出力を表示

This shows the short and long positions after the efficient frontier is applied.

The biggest long positions in IVV and SPY are index position, indicating lower returns.

The biggest short positions are in volatile stocks such as Nvidia.

```

1 from pypfopt import EfficientFrontier
2
3 # Adjust expected returns calculation
4 mu = expected_returns.mean_historical_return(prices)
5 # Scale down expected returns to realistic levels
6 mu = mu * 0.25 # Adjustment factor to bring returns in line with actual performance
7
8 # Calculate covariance matrix with shrinkage
9 S = risk_models.CovarianceShrinkage(prices).ledoit_wolf()
10
11 # Generate efficient frontier points
12 returns = []
13 volatilities = []
14 for return_target in np.linspace(0.0, 0.20, 200): # Adjust upper bound to 20%
15     try:
16         ef = EfficientFrontier(mu, S)
17         ef.efficient_return(return_target)
18         ret, vol, _ = ef.portfolio_performance()
19         returns.append(ret)
20         volatilities.append(vol)
21     except:
22         pass
23
24 # Create DataFrame for Tableau
25 frontier_data = pd.DataFrame({
26     'Expected_Volatility': volatilities,
27     'Expected_Return': returns,
28     'Type': 'Frontier'
29 })
30
31 # Add optimal points

```

```

32 ef_min = EfficientFrontier(mu, S)
33 ef_min.min_volatility()
34 min_vol_ret, min_vol_vol, _ = ef_min.portfolio_performance()
35
36 ef_max = EfficientFrontier(mu, S)
37 ef_max.max_sharpe()
38 max_sharpe_ret, max_sharpe_vol, _ = ef_max.portfolio_performance()
39
40 optimal_points = pd.DataFrame({
41     'Expected_Volatility': [min_vol_vol, max_sharpe_vol],
42     'Expected_Return': [min_vol_ret, max_sharpe_ret],
43     'Type': ['Minimum Volatility', 'Maximum Sharpe Ratio']
44 })
45
46 # Combine and export
47 frontier_data = pd.concat([frontier_data, optimal_points])
48 frontier_data.to_csv('frontier_for_tableau.csv', index=False)
49

```

非表示の出力を表示

```

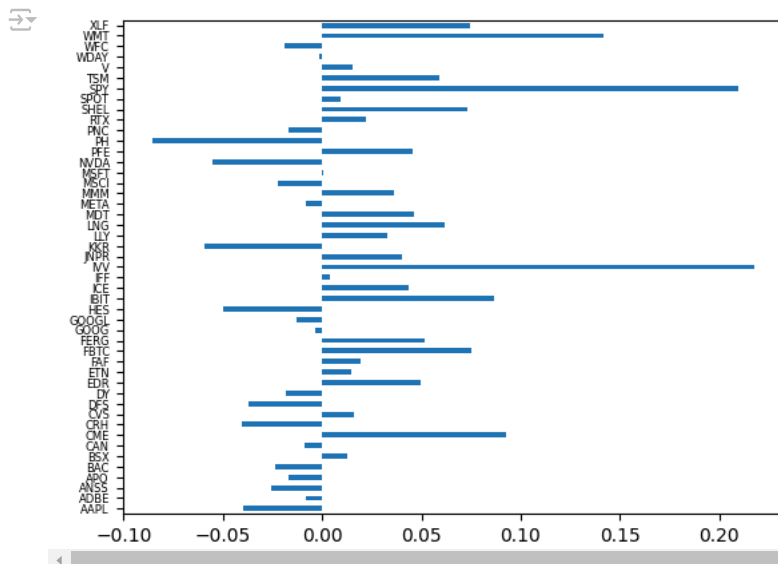
1 # Modify your Python code to generate more points along the frontier
2 returns = []
3 volatilities = []
4 for return_target in np.linspace(0.0, 0.9, 200): # Increase number of points
5     try:
6         ef = EfficientFrontier(mu, S)
7         ef.efficient_return(return_target)
8         ret, vol, _ = ef.portfolio_performance()
9         returns.append(ret)
10        volatilities.append(vol)
11    except:
12        pass
13
14 # Create DataFrame for Tableau
15 frontier_data = pd.DataFrame({
16     'Expected_Volatility': volatilities,
17     'Expected_Return': returns,
18     'Type': 'Frontier'
19 })
20
21 # Add optimal points
22 optimal_points = pd.DataFrame({
23     'Expected_Volatility': [min_vol_vol, max_sharpe_vol],
24     'Expected_Return': [min_vol_ret, max_sharpe_ret],
25     'Type': ['Minimum Volatility', 'Maximum Sharpe Ratio']
26 })
27
28 # Combine and export
29 frontier_data = pd.concat([frontier_data, optimal_points])
30 frontier_data.to_csv('frontier_for_tableau.csv', index=False)
31

```

```

1 # Plot the long short portfolio to minimize variance
2 pd.Series(weights).plot.barh()
3 plt.yticks(fontsize=6);

```



```
1 # Show annual portfolio volatility
2 ef.portfolio_performance(verbose=True);

↳ Expected annual return: 20.0%
   Annual volatility: 16.4%
   Sharpe Ratio: 1.22

1 # Import discrete allocation
2 from pypfopt import DiscreteAllocation
3 tickers = list(weights.keys())
4
5 # Uses precalculated portfolio value of 28.1 billion
6 # Applies hedge fund standard short ratio of 0.2
7 # Use .greedy for larger portfolio size
8 latest_prices = yf.download(tickers, period="1d")['Adj Close'].iloc[-1]
9 da = DiscreteAllocation(weights, latest_prices, total_portfolio_value = 28100000000, short_ratio=0.2)
10 alloc, leftover = da.greedy_portfolio()
11 print(f"Discrete allocation performed with ${leftover:.2f} leftover")
12 alloc
13
14 # Create a DataFrame from the allocation dictionary
15 df_alloc = pd.DataFrame(list(alloc.items()), columns = ['Ticker', 'Shares'])
16 df_alloc['Latest Price'] = df_alloc['Ticker'].map(latest_prices)
17 df_alloc['Allocation Value'] = df_alloc['Shares'] * df_alloc['Latest Price']
18
19 # Saves to CSV
20 df_alloc.to_csv('discrete_allocation.csv', index=False)
21 df_alloc
```

↳ 非表示の出力を表示

References

[1] Michael, A. (2023, August 24). What is wrong with this code to calculate the Beta of a stock? Stack Overflow.

<https://stackoverflow.com/questions/76965865/what-is-wrong-with-this-code-to-calculate-the-beta-of-a-stock>

[2] Al. baharak. (2021. September 27). how pull beta data from vahoo.finance? Stack Overflow.