

Condition de résolution  
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**Objective Function**

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$$Allocation\ Cost = \sum_{i \in N} \sum_{j \in M} h_{ij} X_{ij}$$

$$Location\ Cost = \sum_{k \in N} f_k L_k$$

$$Connection\ Cost = \sum_{k \in N} \sum_{m \in N} g_{km} Z_{km}$$

$$Objective\ function = \min \left( \sum_{i \in N} \sum_{j \in M} h_{ij} X_{ij} + \sum_{k \in N} f_k L_k + \sum_{k \in N} \sum_{m \in N} g_{km} Z_{km} \right)$$

**Constraint 1.**

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$$\sum_{i \in C} X_{ij} \leq 1$$

**Constraint 2.**

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$$\sum_{j \in M} Y_{jl} = 1$$

**Constraint 3.**

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$$Y_{jk} \leq L_k$$

**Constraint 4.**

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$$\sum_{k \in N} Z_{km} = 2 \times L_k$$

**Constraint 5.**

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$$\sum_{k \in N} \sum_{m \in N} Z_{km} \leq 2(|H| - 1), \forall \subset N, 3 \leq |H|$$

**Constraint 6.**

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$$\sum_{i \in C} X_{ij} \leq U_j^{max}$$

**Constraint 7.**

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$$\sum_{j \in M} \sum_{i \in C} X_{ij} Y_{ik} \leq V_k^{max}$$

**Constraint 8.**

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$$\sum_{k \in N} L_k \geq 3$$

**Condition 9.**

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$$\sum_{i \in C} \sum_{j \in M} X_{ij} \geq \alpha \times |C|$$

**Constraint 10.**

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*Reals* :  $h_{ij}, c_{jk}, g_{km}, f_k, \alpha$

*Integers* :  $U_j^{max}, V_k^{max}$

*Booleans* :  $X_{ij}, Y_{jk}, Z_{km}, L_k$