

# Project

October 31, 2025

## 1 Project Proposal: Simulating a Limit Order Book (LOB) and Market Dynamics

### 1.1 Objective

The goal of this project is to simulate the dynamics of a financial market's limit order book (LOB), such as those used in the TSX or NASDAQ, using discrete-event simulation.

The study will model random arrivals of buy and sell orders, cancellations, and executions, and evaluate the performance of different market-making strategies.

Key goals include:

- Understanding how stochastic order arrivals influence market liquidity and price dynamics.
- Measuring execution speed, bid-ask spreads, and volatility.
- Exploring trade-offs between market maker profit, inventory risk, and system efficiency.

### 1.2 System Description

The system represents an electronic market where traders submit limit and market orders for a single asset.

Each order is modeled as an event in the simulation:

- **Limit orders:** Orders to buy or sell at a specified price; join a price-level queue if not immediately executable.
- **Market orders:** Orders executed immediately at the best available price.
- **Cancellations:** Limit orders may leave the queue before execution (modeled as reneging).
- **Executions:** Orders matched according to price-time priority, removing them from the order book.

The order book is modeled as a set of queues, one for each discrete price level.

Market makers act as servers who post buy/sell orders at different prices.

If a counter-order exists, execution occurs; otherwise, the order waits in the queue.

Key system states include:

- Best bid, best ask, and mid-price
- Queue depth at each price level
- Market maker inventory and profit

The system allows experimentation with:

- Number of market makers (servers)
- Quoting strategies (tight vs. wide spreads, dynamic quotes)
- Arrival rates to simulate volatile periods

### 1.3 Simulation Parameters

Parameter	Example Setting	Rationale
Buy limit order arrival rate	$\lambda_{\text{buy\_limit}} = 10$ orders/min	Poisson arrivals capture stochastic behavior
Sell limit order arrival rate	$\lambda_{\text{sell\_limit}} = 10$ orders/min	Symmetric market assumption
Market order arrival rate	$\lambda_{\text{market}} = 5$ orders/min	Market orders execute immediately
Cancellation rate	$\mu_{\text{cancel}} = 0.1$ /min	Represents reneging or order expiration
Order size	Poisson(1–5) shares	Introduces variability in queue length
Number of market makers	1–3	Server capacity impacts execution speed
Quote placement offset	$\pm k$ ticks from mid-price	Controls liquidity provision and risk exposure

### 1.4 Methodology

The simulation will be implemented as a **discrete-event system** in Python using **SimPy**, with the following structure:

1. **Initialization:**

Empty order book, market maker positions, and simulation clock.

2. **Event generation:**

Random arrivals of buy/sell limit and market orders, plus cancellations.

3. **Event handling:**

- Market orders execute immediately if matching orders exist.
- Limit orders join the appropriate price-level queue.

- Cancellations remove orders from queues (reneging).
  - Market makers act as servers, posting quotes and executing trades.
4. **Data collection:**  
For each replication, track:
- Execution time and waiting time distributions
  - Bid-ask spread and mid-price volatility
  - Fill ratio of orders
  - Market maker P&L and inventory levels
5. **Replication:**  
Perform multiple runs with at least five different random seeds to estimate statistics with 95% confidence intervals.

## 1.5 Analysis

For each scenario (e.g., number of market makers, quoting strategy, arrival rate):

- Compute average and tail metrics across replications.
- Compare performance of different market-making strategies.
- Evaluate trade-offs between execution speed, liquidity, volatility, and profit.
- Examine scenarios under high-order-volume periods to stress-test the system.

## 1.6 Conclusion

The project will quantitatively evaluate how stochastic order flow and market-making policies affect market performance.

Key expected insights include:

- Faster execution and tighter spreads with more active market makers.
- Trade-offs between market maker profit and risk exposure.
- The impact of arrival rates and cancellations on order execution and liquidity.
- Demonstration of discrete-event simulation as a powerful tool for analyzing financial market microstructure.

Optional recommendations may include: - Optimal server (market maker) allocation,  
- Dynamic quoting rules, or  
- Priority adjustments to improve execution speed without significantly increasing risk or volatility.

## 1.7 Future Extensions and Research Directions

If time permits beyond the baseline implementation, we plan to incorporate additional research-oriented extensions to enhance realism and analytical depth:

1. **Adaptive or learning market makers** that adjust spreads dynamically using reinforcement learning or rule-based policies.
2. **Heavy-tailed or self-exciting (Hawkes) order arrivals** to capture volatility clustering and bursty trading behavior.
3. **Latency and information asymmetry effects** to study fairness and instability under heterogeneous agent delays.
4. **Price impact modeling**, where large trades influence the mid-price through nonlinear feedback functions.
5. **Informed versus noise trader dynamics**, linking execution to a latent “fundamental” price process.
6. **Endogenous price formation**, where prices evolve directly from agent interactions and order-book states rather than from an exogenous price process.

The main goal for this course project will be to develop a **simplistic, working limit order book simulation** with correct queueing dynamics, validated through replication and statistical analysis. These extensions represent **potential research enhancements** that we will implement and analyze if time allows.