

POLYNOMIAL

EXPRESSIONS, SUCH AS $2x$, $x+3$ AND $x-5$, HAVE SIMILAR TERMS. IF AN EXPRESSION CONTAINS TWO OR MORE TERMS, IT IS CALLED A POLYNOMIAL HAVING THE SAME POWER OF THE SAME LETTER (HERE x). IN THE LIKE MANNER, $2x^2-8$, $5x^2$ AND x^2+3 HAVE SIMILAR TERMS (HERE x^2).

IN ALGEBRAIC ADDITION, SUCH EXPRESSION ARE COMBINED. ALGEBRAIC ADDITION Ex 1: JACK HAS 3 APPLES, 2 PEARS, AND 5 BANANAS, AND HENRY HAS 2 APPLES, 1 PEAR, AND 3 BANANAS, TOGETHER THEY HAVE 5 APPLES, 3 PEARS, AND 8 BANANAS. USING a FOR APPLES, p FOR PEARS, AND b FOR BANANAS:

$$3a + 5b + 2p + 2a + 1p + 3b = 5a + 3p + 8b$$

JUST AS WE USUALLY COMBINE ONLY LIKE OBJECTS IN ARITHMETIC, WE ADD ONLY SIMILAR TERMS IN ALGEBRA.

Ex 2: $3x - 2y + 2z + 2z + 2y$ $5x - 2x - 2y + 10z$

Ex 3: $x^2 + 5x - 8 + 2x^2 - 7x + 3 = 3x^2 - 2x - 5$

26. MULTIPLICATION OF BINOMIALS

SOMETIMES IT IS NECESSARY TO MULTIPLY TWO BINOMIAL EXPRESSIONS IN ORDER TO SOLVE A QUADRATIC EQUATION.

Ex 1: WHAT IS THE SIDE OF A SQUARE SUCH THAT WHEN ONE SIDE IS DIMINISHED BY 3 UNITS AND THE OTHER INCREASED BY 3 UNITS, THE AREA OF THE RESULTING RECTANGLE IS 48 SQUARE UNITS? THE ALGEBRAIC STATEMENT OF THIS PROBLEM IS

$$(x-3)(x+3) = 48$$

LET $x = 4$ THEN $(4-3)(4+3) = 1 \times 7 = 7$. SUPPOSE WE HAD MULTIPLIED EACH NUMBER IN THE FIRST PARENTHESES BY EACH 1 IN THE SECOND AND ADDED THE RESULTS INSTEAD OF COMBINING WITHIN PARENTHESES FIRST. THEN WE SHOULD HAVE HAD:

$$4^2 + 4 \times 3 - 3 \times 4 - 3 \times 3 = 16 + 12 - 12 - 9 = 36 - 9 = 27$$

WHICH INDICATES THE METHOD FOR MULTIPLYING THE TWO EXPRESSIONS

$$(x-3)(x+3) = x^2 + 3x - 3x - 9 = x^2 - 9$$

$$\rightarrow \text{book: } x^2 + 2x - 15$$

SINCE $3 \times 3 = 9$, IT IS SAID TO HAVE TWO FACTORS, 3 AND 3,

SIMILARLY, SINCE $(x-3)(x+3) = x^2 + 2x - 15$, $x^2 + 2x - 15$ IS

SAID TO HAVE TWO FACTORS, $(x-3)$ AND $(x+5)$.