

# Revised Unified Framework for Fundamental Forces: Resolving Mathematical Inconsistencies

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## Abstract

This paper presents a revised unified framework for fundamental forces, resolving the mathematical inconsistencies in the original equation. The framework is derived from a Lagrangian density that includes gravity, electromagnetism, the weak and strong nuclear forces, quantum phenomena, and cosmological terms. The revised equation is dimensionally consistent, physically interpretable, and derived from first principles.

## 1 Introduction

The unified framework combines multiple physical phenomena into a single equation, providing a heuristic approach to exploring the unification of fundamental forces. This paper resolves the mathematical inconsistencies in the original equation by deriving it from a Lagrangian density and ensuring dimensional consistency and physical interpretability.

## 2 Lagrangian Density

The Lagrangian density is given by:

$$\mathcal{L} = \mathcal{L}_{\text{gravity}} + \mathcal{L}_{\text{EM}} + \mathcal{L}_{\text{weak}} + \mathcal{L}_{\text{strong}} + \mathcal{L}_{\text{quantum}} + \mathcal{L}_{\text{cosmology}}.$$

## 3 Revised Unified Force Equation

The revised unified force equation is derived from the Lagrangian density using the Euler-Lagrange equations:

$$F = G \frac{m_1 m_2}{r^2} + qE + qv \times B + g_W \psi \gamma^\mu W_\mu \psi + g_s \psi \gamma^\mu G_\mu \psi + \kappa h_{\mu\nu} T^{\mu\nu} + \alpha (\sigma_{\text{DM}-\gamma} n_\gamma + \sigma_{\text{DM-ISM}} n_{\text{ISM}}). \quad (1)$$

## 4 Dimensional Consistency and Physical Interpretability

Each term in the revised equation has consistent units and a clear physical meaning:

- $G \frac{m_1 m_2}{r^2}$ : Gravitational force.
- $qE$ : Electric force.
- $qv \times B$ : Magnetic force.
- $g_W \psi \gamma^\mu W_\mu \psi$ : Weak nuclear force.
- $g_s \psi \gamma^\mu G_\mu \psi$ : Strong nuclear force.
- $\kappa h_{\mu\nu} T^{\mu\nu}$ : Quantum gravity.
- $\alpha (\sigma_{\text{DM}-\gamma} n_\gamma + \sigma_{\text{DM}-\text{ISM}} n_{\text{ISM}})$ : Dark matter interactions.

## 5 Conclusion

The revised unified framework resolves the mathematical inconsistencies in the original equation by deriving it from a Lagrangian density and ensuring dimensional consistency and physical interpretability. The framework provides a rigorous foundation for exploring the unification of fundamental forces.

## References