# Super Information Theory The Coherence Conservation Law Unifying the Wave Function, Gravity, and Time

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#### Abstract

Super Information Theory (SIT) proposes a unified gauge-covariant action in which quantum mechanics, classical kinetic theory, and general relativity arise as limiting cases of a framework based on a fundamental complex coherence field  $\psi(x)$  and a real time-density scalar  $\rho_t(x)$  with dimension  $[T^{-1}]$ . The modulus of the coherence field is identified with the dimensionless coherence ratio,  $R_{\rm coh}(x) \equiv |\psi(x)|$ . Variations of this action yield, in flat spacetime, a Brans–Dicke–type scalar–tensor system that reduces to Newtonian gravity plus a small Yukawa correction, remaining compatible with current experimental bounds. In the Boltzmann–Grad scaling, the framework reproduces the Deng–Hani–Ma derivation of the Boltzmann and Navier–Stokes equations.

Spatial gradients of the gauge phase  $\theta(x) \equiv \arg(\psi(x))$ , a component of the complex coherence field, supply the electromagnetic vector potential via  $\partial_i \theta = (e/\hbar) A_i$ , interpreting the magnetic field  $B_i = \varepsilon_{ijk} \partial_j \partial_k \theta$  as a holonomy of the quantum coherence field. This approach connects Aharonov–Bohm phase shifts, optical-lattice clock comparisons, and cold-atom interferometry directly to  $\rho_t$  and its coupling constant  $\alpha$ , predicting a fractional frequency shift / whose coupling constant, , is now quantitatively constrained by state-of-the-art optical clock comparisons. The theory is thus shown to be consistent with precision tests of General Relativity while making falsifiable predictions for future experiments.

Irreversibility in SIT emerges because microstates increasing  $R_{\rm coh}$  are confined to measure-zero submanifolds of phase space, rendered physically inaccessible by chaos and quantum decoherence. This leads to a generalized law of entropy production, identified with the monotonic decay of a global coherence functional, which unifies the Boltzmann H-theorem and gravitational clustering as information-gradient flows on distinct manifolds.

SIT reinterprets wave-function collapse as a local gauge-fixing of the coherence field, removing the need for non-unitary dynamics or multiple universes. Measurement corresponds to local gauge fixing that induces decoherence and yields classical outcomes without a physical collapse or discontinuity in the underlying state. The framework supports testable predictions across quantum and gravitational systems, from Schrödinger-cat interferometers to millimetre-scale atomic clocks and cosmological weak-lensing surveys, all grounded in the same two-field action.

Speculative connections to information processing and computation, including analogies to predictive coding and neural coherence, are discussed in the final section. An intuitive "Conceptual Primer" for non-specialist readers follows the technical exposition.

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# 1 Introduction

# 1.1 Motivation and Theoretical Scope

Super Information Theory (SIT) is built around a single covariant action based on a fundamental complex coherence field  $\psi(x)$  and a real time-density scalar  $\rho_t(x)$  of dimension  $[T^{-1}]$ . The modulus of the coherence field,  $|\psi(x)|$ , is interpreted as the dimensionless coherence ratio. By construction the action reduces, in appropriate limits, to gauge-covariant quantum mechanics, to the Deng-Hani-Ma hard-sphere Boltzmann equation, and to a Brans-Dicke-type scalar-tensor extension of General Relativity. The central motivation is therefore unification: to show that quantum interference, gravitational attraction, and entropy growth arise as different projections of the same information-geometric dynamics. Speculative connections to information processing and cognition are discussed in a later section.

#### 1.2 Evolution from Super Dark Time and Related Work

SIT extends the local time-density concept introduced in *Super Dark Time*, generalises the coherence functional from *SuperTimePosition*, and embeds the entropy law formulated in Micah's New Law of Thermodynamics. Whereas earlier drafts treated magnetism as "gravity at a spectral scale," the present formulation derives the electromagnetic vector potential from gauge holonomy of the Quantum Coherence Field, eliminating the previous 36-order-of-magnitude conflict with laboratory bounds.

#### 1.3 Information as Active Substrate

Information is treated as ontologically active. A spatial gradient in  $R_{\rm coh}$  establishes a local vector potential, while a temporal gradient in  $\rho_t$  deforms proper time. The two gradients together fix the phase of quantum states, the curvature of spacetime, and the flow of macroscopic entropy. In this framework, information is elevated from a bookkeeping device to a physical medium that shapes matter and energy.

#### 1.4 Integrative Trajectory from Information to Physical Reality

SIT synthesises Shannon's bit-based entropy, Wheeler's "It-from-Bit," and the informationenergy equivalence in modern quantum thermodynamics. By treating coherence as a gauge degree of freedom, SIT inherits the Aharonov–Bohm phase holonomy as an experimental handle on information geometry. The Deng–Hani–Ma propagation-of-chaos theorem supplies a rigorous classical limit in which irreversibility appears because phase-space trajectories that would raise  $R_{\rm coh}$  have vanishing measure.

# 1.5 Refined Quantum-Gravitational Unification

Time-density  $\rho_t$  couples to the metric as a Brans-Dicke scalar with coefficient  $\alpha$ . Setting  $\rho_t$  to its vacuum value recovers Einstein gravity, while weak-field expansion yields a Yukawa correction bounded by torsion-balance experiments. In curved backgrounds the local value of  $\rho_t$  rescales the effective Planck constant, providing a geometrical route from quantum decoherence to gravitational red-shift.

# 1.6 Neuroscience-Inspired Predictive Synchronisation

Predictive coding, active inference and the Free Energy Principle are recast as mesoscopic limits of the same action. Neuronal synchrony corresponds to regions where the gauge phase  $\theta(x)$  is smoothly varying, while cortical desynchrony marks decoherence domains. The brain therefore implements SIT's information-gradient flow in biological hardware.

# 1.7 Informational Geometry and Noether Symmetry

Quantum Coherence Coordinates extend 3+1 spacetime without adding dimensions: they attach a gauge fibre whose phase is  $\theta(x)$  and whose modulus determines  $R_{\text{coh}}$ . Noether's

theorem then supplies a conserved coherence current, just as time-translation yields energy and rotation yields angular momentum. Conservation of coherence replaces the ad-hoc collapse postulate; a measurement is merely a local gauge fixing that re-aligns  $\theta$  across observers.

#### 1.8 Informational Torque and Gravitational Curvature

Curvature arises when the phase fiber twists; the corresponding antisymmetric derivative of the stress tensor matches the classical notion of torque. In SIT this "informational torque" replaces the heuristic fractional-spherical-resonance language of earlier drafts and yields the correct Riemann curvature in the small- $\alpha$  limit.

#### 1.9 Wave-Particle Informational Duality

Wave—particle duality becomes coherence—decoherence duality. Perfect coherence produces interference fringes; complete decoherence yields classical trajectories. Intermediate regimes are described by partial gauge holonomy and align with experimental visibility curves in atom interferometers.

#### 1.10 Fractal Interplay across Scales

Because the field equations are scale-free, the same pattern of coherence peaks and decoherence troughs recurs from sub-cellular calcium oscillations to galactic clustering. SIT therefore predicts fractal correlations in CMB lensing maps and in EEG phase-synchrony networks, both traceable to the spectrum of  $\rho_t$  fluctuations.

# 1.11 Information as Evolutionary Attractor

States drift toward maxima of coherence subject to energy and curvature constraints. That drift drives quantum state reduction and structure formation in the universe, with potential analogies to equilibrium-seeking in biology and technology discussed in the outlook.

# 1.12 Objectives of SIT

The remainder of the paper defines  $R_{\rm coh}$  and  $\rho_t$  precisely, derives their coupled field equations, shows their reduction to known physics in three limits, and lists experimental targets. A central objective is to demonstrate that gravitational attraction emerges from spatial gradients in  $\rho_t$  and that laboratory modulation of coherence can produce frequency shifts whose magnitude is now tightly constrained by null results from optical clock metrology, providing a concrete, falsifiable baseline for the theory. Potential extensions to information processing and neuroscience are reserved for the discussion.

#### 1.13 Interdisciplinary Impact and Empirical Roadmap

Section 2 presents the action and its Noether currents. Section 3 gives the weak-field and Boltzmann-Grad limits, recovering Newton, Maxwell, and Deng-Hani-Ma. Section 5 sets out experimental protocols, including optical-clock cavities, cold-atom Aharonov-Bohm loops, and cosmological lensing surveys. A final discussion outlines connections to Loop Quantum Gravity, String Theory, and Causal Sets, and sketches how SIT can be falsified within the next decade. Speculative implications for biological and technological systems are addressed in a separate section.

With gauge holonomy supplying magnetism, chart changes supplanting collapse, and the hard-sphere gas anchoring the entropy law, Super Information Theory now stands as a quantitatively testable unification of quantum mechanics and gravitation. Readers seeking intuitive metaphors, visual analogies, and interdisciplinary context will find a dedicated Conceptual Primer at the end of this paper, following the main technical discussion.

The foundational axiomatic postulate of Super Information Theory is the existence of a single, dynamical complex gauge field,  $\psi(x)$ , which serves as the universal informational substrate. This field is defined on a U(1) fibre bundle over the spacetime manifold. Its modulus is identified as the dimensionless coherence ratio,  $R_{\text{coh}}(x) \equiv |\psi(x)|$ , which dictates gravitational dynamics through its coupling to the time-density field  $\rho_t(x)$ . Its phase,  $\theta(x) \equiv \arg(\psi(x))$ , defines the gauge connection whose holonomy produces electromagnetism from which electromagnetic forces emerge as a consequence of the bundle's geometry. From this single substrate, all relational dynamics—such as informational coincidence, the resonant modes that constitute particles to the coincidence events that define measurement, and the effective coherence between spacetime points—emerge. Consequently, matter, spacetime, and the forces that govern them are understood not as separate entities, but as integrated manifestations of a unified informational geometry.

As detailed in Appendix D, this complex gauge field is formally expressed as the order parameter  $\psi(x) = R_{\rm coh}(x)e^{i\theta(x)}$ . The "phase fibre" over spacetime is shown to be a principal U(1) bundle whose connection and holonomy generate both electromagnetic and relational (adjacency-like) structures. Furthermore, the discussion of local U(1) gauge invariance in Section 2 explicitly treats the transformation  $\psi(x) \to e^{i\alpha(x)}\psi(x)$  as the primitive symmetry from which the dynamics of both  $R_{\rm coh}(x)$  and  $\theta(x)$  are derived.

In practice, terms such as resonance, geometric holonomy, adjacency, or coincidence all refer back to the same underlying gauge-coherence field (x). Whether one speaks of edges in a graph, phase synchrony in an oscillator network, or topological connectivity in a quantum lattice, they are simply different linguistic faces of coherence flowing through the U(1) fibre bundle that  $(x)^2$  and (x) define.

To clarify the novelty and empirical distinctness of Super Information Theory (SIT), we summarize its relationship to several major paradigms in unification physics and informational dynamics.

Theory/Approa	clCore Princi-	Key Ways SIT Dif-
	ple/Mechanism	fers/Extends
Entropic Gravity (Verlinde, Pad- manabhan)	Gravity emerges as a statistical force from changes in information/entropy at holographic screens; entropy gradients drive dynamics	SIT replaces the scalar entropy with a dynamic local coherence field $R_{\rm coh}(x)$ and time-density $\rho_t(x)$ , making "information" a local, gauge-coupled field. SIT's action yields gravity, electromagnetism, and quantum limits from a unified informational action, not as statistical aftereffects.
Tensor Networks, Holographic Codes (Swingle, Pastawski, Hay- den)	Spacetime geometry and entanglement emerge from discrete quantum tensor networks, with the network's entanglement pattern encoding geometry	SIT uses continuous informational fields and is not limited to discrete network structure. Coherence and time-density fields are dynamical and testable in any medium, not just idealized CFT/AdS settings. Predicts measurable macroscopic effects beyond condensed matter or AdS/CFT.
Wheeler's It- from-Bit, Quan- tum Information Gravity	Physics emerges from binary information or quantum entanglement, with space, time, and gravity secondary to informational laws	SIT operationalizes "information" as an explicit field with gauge structure and Lagrangian dynamics, providing precise links to experimental physics, not just philosophical claims.
Brans-Dicke Scalar-Tensor Gravity	Varying gravitational "constant" via dynamical scalar field; modifies Einstein gravity, yields new tests in weak field	SIT's $\rho_t(x)$ field is physically timedensity, not just a dilaton; SIT unifies quantum, gravitational, and electromagnetic phenomena in a single action.
Quantum Causal Sets	Spacetime emerges from discrete, partially ordered sets of events ("causal sets") $= \Omega_i(t) - \frac{\gamma}{2} \Delta \Omega_{ii}(t)$	SIT is formulated as a continuous field theory; the time-density field $\rho_t$ can reduce to discrete-event counts but is defined for smooth and quantum-coherent systems alike.

 $= Q_i(t) - \frac{\gamma}{2} \Delta Q_{ij}(t)$ 

# 2 Operational

Definition
of Information:

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8

where  $0 < \gamma \le 1$  is a dissipation (or coupling) parameter. Over many iterations, such updates drive all  $Q_i$  toward a common value—realizing equilibrium as a computational process.

#### 4.3 Mapping Coherence/Decoherence to Signal Dissipation

The local dissipation rules serve as the microscopic engine for the macroscopic evolution of the theory's central fields:

- The **coherence ratio**  $R_{\text{coh}}(x,t)$  evolves as local subsystems interact and their informational states dissipate differences.
- The **time-density field**  $\rho_t(x,t)$  is driven by the cumulative effect of these microscopic dissipation events, encoding the local density of temporally resolved events.

In SIT,  $Q_i(t)$  can be interpreted as the local quantum coherence amplitude or phase at site i. Coherence between nodes i and j is maximized when  $Q_i = Q_j$ ; decoherence corresponds to persistent differences or fluctuations. Thus, each local dissipation event can be viewed as a micro-level act of coherence reinforcement:

High coherence: 
$$Q_i \approx Q_j \implies \Delta Q_{ij} \approx 0$$
 (1)

Active dissipation: 
$$|\Delta Q_{ij}|$$
 large  $\implies$  system far from equilibrium (low coherence) (2)

The global, macroscopic field evolution—such as the time-density field  $\rho_t(x)$ —emerges from the statistical aggregation of many such micro-level updates. When interpreted as a field, the signal dissipation process maps onto a diffusion-like equation:

$$\frac{\partial Q(x,t)}{\partial t} = D\nabla^2 Q(x,t) \tag{3}$$

where Q(x,t) is the spatially varying property (e.g., coherence amplitude), and D is an effective diffusion constant derived from  $\gamma$  and the interaction network.

# 4.4 Macro-Level Evolution of the Time-Density Field

The collective action of countless signal-dissipation steps at the micro level leads to the smooth evolution of the macro-level time-density field,  $\rho_t(x)$ , governed by its field equation (see Section 8):

$$\Box \rho_t - V'(\rho_t) + \dots = 0$$

Here, the "···" term absorbs all source and coupling terms from matter, coherence, and interactions. The approach to equilibrium (or attractor states) for  $\rho_t$  can be understood as the integrated result of local coherence-dissipation events at every scale.

# 4.5 Information-Theoretic Interpretation: Entropy and Coherence

The signal-dissipation process can be interpreted as local reduction of informational (Shannon or quantum) entropy. As local differences in  $Q_i$  vanish, the system moves toward maximal mutual coherence, corresponding to minimal entropy production. Conversely, persistent incoherence (large  $\Delta Q_{ij}$ ) maintains or increases entropy.

This micro-to-macro bridge justifies the treatment of coherence conservation and time-density evolution as physical processes with direct thermodynamic and computational meaning.

#### 4.6 Example: Coherence Relaxation in a Network

Consider a ring of N oscillators with initial random phases  $Q_i(0)$ . At each time step, each oscillator exchanges phase information with its nearest neighbors according to the local update rule (Eq. 1.13). Over many iterations, all  $Q_i$  converge to a common phase, maximizing global coherence:

$$\lim_{t \to \infty} Q_i(t) = Q_{\text{eq}} \quad \forall i$$

The rate of convergence (relaxation time) depends on  $\gamma$  and network topology. In physical terms, this process models synchronization in neural circuits, quantum decoherence in open systems, or even heat conduction.

This mechanistic foundation ensures that the evolution of  $R_{\rm coh}$  and  $\rho_t$  is not left to abstract principle, but arises from a well-defined, physically computable process:

- Coherence increases as local differences dissipate, corresponding to the growth of order and synchrony in the system.
- Decoherence or disorder results from the persistence or amplification of local differences, inhibiting equilibration.
- The time-density field  $\rho_t(x,t)$  evolves as the statistical outcome of these local interactions, linking the micro-dynamics of dissipation to macroscopic gravitational and temporal effects.

# 4.7 Summary

By formalizing thermodynamic dissipation as a wave-based, local computational process, SIT unifies the dynamics of coherence, entropy, and time-density into a single theoretical framework. The macroscopic field evolution described in Section 8 is thus revealed as the statistical outcome of myriad microscopic signal-dissipation events—a mechanistic bridge between information, computation, and fundamental physics.

# 5 Quantum Coherence Coordinates and the Quasicrystal Analogy

Super Information Theory supplements the ordinary space—time tuple (x, y, z, t) with two gauge—invariant scalars defined at every event. The first is the time-density field  $\rho_t(x,t)$ , introduced in Eq. (4); the second is the dimensionless coherence ratio  $R_{\text{coh}}(x,t) = I_{\text{mutual}}/I_{\text{max}}$  whose definition and regulator appear in Section ??. Together these variables constitute what we call Quantum Coherence Coordinates. No extra geometric axes are added; instead each point of the Lorentz manifold carries an informational fibre

that records the local rate of proper time and the local degree of phase alignment. Although  $\rho_t$  and  $R_{\rm coh}$  are not themselves extra co-ordinates in the usual geometric sense, their global organisation resembles the cut-and-project method that produces quasicrystals.

A higher-dimensional lattice, invisible in the final projection, imprints a long-range aperiodic order on the shadow it casts in three dimensions. In the same way the hidden constraints of gauge holonomy organise the coherence field so that its projection into 3+1 space—time yields the patterns we observe: lensing asymmetries, phase-steered interference fringes, altitude- dependent Bell correlations.

The analogy is literal in the mathematics. A patch of space—time and its associated coherence data form a local section of a cosheaf. Overlaps must agree up to the gauge connection  $A_i = (\hbar/e) \partial_i \arg R_{\rm coh}$ . Gluing all patches with that rule produces a global informational manifold whose structure group is the same U(1) that drives the Aharonov–Bohm effect. What appears, at laboratory scale, as a plain interference fringe encodes long-range order in the hidden "lattice" of phase holonomy just as a Penrose tile encodes five-dimensional periodicity.

Direct measurement still targets ordinary observables, but each experiment fixes one more degree of the hidden lattice. Optical-lattice clocks transported through regions of varying curvature detect the slow drift of  $\rho_t$ ; far-zone interferometers map angular shifts that trace the gradient of  $R_{\rm coh}$ ; mismatched-altitude Bell tests reveal the shared section of the coherence fibre. In every case the data constrain the same two scalars and the same connection, tightening the map between the hidden order and its physical shadow. Quantum Coherence Coordinates are therefore physically real in the only sense required of a scientific variable: they mediate measurable effects and are in principle reconstructible from a sufficiently rich set of observations. They supply the minimum informational structure needed to unify interference, gravitation and entanglement without adding new geometric axes, completing the analogy with quasicrystals while remaining entirely within the dimension of observed space—time.

# 6 Time-Density as the Sole Temporal Scalar

Super Information Theory treats the passage of proper time as a field phenomenon. The scalar  $\rho_t(x,t)$  introduced in Eq. (4) measures the local number of proper–time quanta per unit coordinate time, a quantity with dimensions [time]<sup>-1</sup>. Its vacuum value  $\rho_0$  fixes the reference clock, while deviations  $\delta \rho_t = \rho_t - \rho_0$  encode every observable form of gravitational red– or blue–shift.

In regions of strong phase alignment the coherence ratio  $R_{\text{coh}}$  approaches unity and the master action yields

$$\rho_t(x,t) = \rho_0 \exp[\alpha R_{\rm coh}(x,t)] \frac{E(x,t)}{E_0},$$

where the dimensionless constant  $\alpha = \beta/\kappa_t$  is fixed by the weak-field torsion-balance limit quoted in Section ??. The exponential is a convenient re-summation of the perturbative series that follows from varying Eq. (1); its leading term reproduces exactly the linear relation used in the post-Newtonian expansion. Large  $R_{\rm coh}$  thus slows local clocks, reproducing gravitational time dilation without appeal to extra temporal axes, whereas decoherent zones with small  $R_{\rm coh}$  run fast and flatten curvature.

Spatial gradients of  $\rho_t$  enter the field equations through the gauge connection  $A_i = (\hbar/e) \partial_i \arg R_{\rm coh}$ . In the non-relativistic limit the modified Poisson equation becomes

$$\nabla^2 \Phi(x,t) = 4\pi G \rho_m(x,t) + \beta \nabla^2 \delta \rho_t,$$

so that the Newtonian potential is a functional of  $\rho_t$ . Gravity is therefore informational in origin: the local slowing of time produced by coherence gradients curves space-time exactly as a mass distribution would. Conversely, any attempt to accelerate time—by forcing decoherence—reduces curvature and releases gravitational binding energy, a relationship already implicit in the Deng–Hani–Ma entropy flow and now made explicit by the Noether identity  $\partial^{\mu}J_{\mu}^{\text{coh}} = 0$ .

Because  $\rho_t$  is a single Lorentz scalar, no additional temporal dimensions are needed. All proposals that invoke a second time coordinate or a cyclic "multitemporal" manifold are replaced by this one gauge-covariant field whose value is, in principle, accessible to optical-lattice clocks, VLBI lensing surveys and Bell tests at mismatched altitudes. In the limit  $R_{\rm coh} \to {\rm const}$  the exponential term reduces to unity and general relativity is recovered in its usual form; when  $E \to 0$  the scalar freezes and special relativity emerges. Time-density thus provides a minimal, continuous bridge between quantum coherence, energy density and gravitational curvature.

# 7 Why an Informational Time-Density Field Simplifies Physics

By interpreting gravity as the gradient of a single gauge-covariant scalar, Super Information Theory folds quantum measurement, red-shift, lensing and buoyancy into one computational mechanism: the local balance of coherent and decoherent energy determines how densely the flow of proper time is packed. Mass is simply energy stored in modes that maximise phase alignment and thereby "thicken" time; decoherent energy thins it. All familiar relativistic effects follow from that rule, while quantum phenomena—entanglement, collapse, thermal decoherence—become different regimes of the same field dynamics. No extra geometric axes are needed, no new forces are invoked, and every prediction reduces in tested limits to the forms already verified for Newtonian gravity, post-Newtonian red-shift and standard quantum interference. The informational

time-density field is therefore not an incremental tweak to general relativity but a simpler foundation from which both relativity and quantum theory emerge as coherent and decoherent extremes of one underlying process.

# 8 Action Principle and Field Equations

#### 8.1 Symmetries and Constraints on the Action

Super Information Theory is built on two primary scalar fields: the coherence ratio  $R_{\text{coh}}(x)$  and the time-density  $\rho_t(x)$ . To construct a physically viable theory, the action governing these fields must respect fundamental symmetries, including general covariance (diffeomorphism invariance) and local U(1) gauge invariance associated with the coherence phase. Furthermore, to ensure causality and stability, we exclude higher-derivative operators that lead to Ostrogradsky instabilities. These constraints lead to a unique minimal effective action.

# 8.2 Operational and Mathematical Definitions of Primitive Fields

To ensure clarity and empirical accessibility, we define the two fundamental fields of Super Information Theory (SIT) both operationally and mathematically.

- (1) Complex Coherence Field  $\psi(x)$ : The fundamental coherence field is the complex scalar  $\psi(x)$ . From it, we define the dimensionless Coherence-Decoherence Ratio  $R_{\rm coh}(x)$  as its modulus,  $R_{\rm coh}(x) \equiv |\psi(x)|$ .
  - Operational Definition: For a quantum system, the coherence ratio  $R_{\text{coh}}(x)$  is the normalized measure of local quantum purity or coherence at spacetime point x. In practice, this is realized as the local purity of the reduced density matrix, normalized such that  $R_{\text{coh}} = 1$  for a pure state and  $R_{\text{coh}} = 0$  for a maximally mixed state.
  - Mathematical Definition:

$$R_{\rm coh}(x) = \frac{{\rm Tr}[\rho^2(x)] - \frac{1}{d}}{1 - \frac{1}{d}}$$

where  $\rho(x)$  is the reduced density matrix for the relevant subsystem at x, and d is its Hilbert space dimension. This definition makes  $R_{\text{coh}}(x)$  dimensionless, bounded between 0 (maximal decoherence) and 1 (perfect coherence).

• Transformation Properties:  $R_{\text{coh}}(x)$  transforms as a scalar under spacetime coordinate changes. Its gauge structure is inherited from the underlying phase structure of  $\rho(x)$ .

#### (2) Time-Density Field $\rho_t(x)$ :

- Operational Definition:  $\rho_t(x)$  is the local rate of occurrence of distinguishable events ("time frames") per unit proper time at the spacetime point x. It is operationally measurable via the ticking rate of an idealized clock or via the density of time-stamped quantum measurement events in a local region.
- Mathematical Definition:

$$\rho_t(x) := \lim_{\Delta V \to 0} \frac{\Delta N_{\text{events}}}{\Delta \tau \, \Delta V}$$

where  $\Delta N_{\text{events}}$  is the number of distinguishable events occurring in infinitesimal spacetime volume  $\Delta V$  over proper time interval  $\Delta \tau$  at x. The physical dimension of  $\rho_t(x)$  is  $[T^{-1}]$ .

- Transformation Properties:  $\rho_t(x)$  is a real scalar field under general coordinate transformations.
- (3) Relation to Gauge and Matter Fields: Both primitive fields may couple to matter and electromagnetic sectors via explicit functions  $f_1(\rho_t, R_{\text{coh}})$  and  $f_2(\rho_t, R_{\text{coh}})$  in the SIT action. Their functional form should be chosen to respect general covariance, locality, and (where desired) additional symmetries such as phase invariance.

#### (4) Summary Table:

Field	Operational Definition	Mathematical Definition	Dimension/Transformation
$R_{\rm coh}(x)$	Local quantum purity	$\frac{\operatorname{Tr}[\rho^2(x)] - \frac{1}{d}}{1 - \frac{1}{d}}$	Dimensionless scalar
$\rho_t(x)$	Local event (clock) rate	$\lim_{\Delta V \to 0} \frac{{}^{a}_{\Delta N_{\text{events}}}}{\Delta \tau  \Delta V}$	$[T^{-1}]$ , real scalar

These definitions anchor the SIT formalism to concrete, experimentally accessible quantities, and fix the mathematical roles of the primitive fields in all subsequent equations.

# 8.3 Symmetries and Gauge Structure

Super Information Theory (SIT) is built upon a primitive complex scalar field and a primitive real scalar field, defined over a Lorentzian spacetime manifold  $\mathcal{M}$  with metric  $g_{\mu\nu}$ : - The complex coherence field  $\psi(x)$ , whose modulus  $|\psi(x)| \equiv R_{\rm coh}(x)$  is a dimensionless scalar that quantifies the degree of local quantum coherence. - The time-density field  $\rho_t(x)$ , a real scalar with dimension  $[T^{-1}]$ , encoding the local density of fundamental "time frames" or event cycles.

These fields must respect the following fundamental symmetries:

1. Diffeomorphism Invariance The action must be invariant under smooth coordinate transformations

$$x^{\mu} \to x'^{\mu}(x)$$

implying all terms in the action are constructed from scalars, covariant derivatives, and tensor contractions ensuring general covariance.

2. Local U(1) Gauge Invariance The coherence ratio  $R_{\text{coh}}$  is derived from the local quantum state's phase, which transforms as

$$\psi(x) \to e^{i\alpha(x)}\psi(x),$$

for arbitrary smooth functions  $\alpha(x)$ . Although  $R_{\rm coh}(x)$  itself is gauge-invariant, the underlying phase  $\theta(x)$  transforms as

$$\theta(x) \to \theta(x) + \alpha(x),$$

and the action must be invariant under this local phase shift. This constrains the allowed couplings and kinetic terms to be functions of  $R_{\rm coh}$  and derivatives of gauge-invariant combinations only.

- 3. Discrete Symmetries Time-reversal T, parity P, and charge conjugation C symmetries restrict the presence of terms odd under these transformations, forbidding CPT-violating operators unless explicitly motivated.
- **4. Causality and Locality** The action must produce hyperbolic, causal equations of motion, prohibiting nonlocal terms or higher-derivative operators that generate Ostrogradsky instabilities.

# 8.4 Unified SIT Action and Lagrangian

The total action of SIT, integrating gravitational, informational, and matter contributions, is postulated as:

$$S_{\text{SIT}} = \int d^4x \sqrt{-g} \left[ \frac{R}{16\pi G} + \frac{1}{2} g^{\mu\nu} \partial_{\mu} \rho_t \partial_{\nu} \rho_t - V(\rho_t) \right.$$

$$\left. + \frac{\lambda}{2} g^{\mu\nu} (\partial_{\mu} \psi^*) (\partial_{\nu} \psi) - U(|\psi|) - U_{\text{link}}(\rho_t, |\psi|) \right.$$

$$\left. + \mathcal{L}_{\text{m}} - \sum_{\psi} f_1(\rho_t, |\psi|) m_{\psi} \bar{\psi} \psi - \frac{1}{4} f_2(\rho_t, |\psi|) F_{\mu\nu} F^{\mu\nu} \right.$$

$$\left. + \mathcal{L}_{\text{int}}(\rho_t, |\psi|) \right]$$

$$\left. + \mathcal{L}_{\text{int}}(\rho_t, |\psi|) \right]$$

$$(4)$$

Here:

- R is the Ricci scalar of the spacetime metric  $g_{\mu\nu}$ .
- $V(\rho_t)$  and  $U(R_{\rm coh})$  are potential terms for the respective scalar fields.
- $f_1$ ,  $f_2$  are targeted couplings:  $f_1$  shifts fermion mass terms and  $f_2$  rescales the gauge–kinetic term  $F_{\mu\nu}F^{\mu\nu}$  (no global factor multiplying  $\mathcal{L}_{\rm m}$ ).
- $\mathcal{L}_{\rm m}$  is the standard matter Lagrangian; the electromagnetic term is written explicitly as  $-\frac{1}{4}F_{\mu\nu}F^{\mu\nu}$ .
- $\lambda$  is a coupling constant.
- $\mathcal{L}_{\text{int}}$  contains additional interactions such as derivative couplings and mixing between  $\rho_t$  and  $R_{\text{coh}}$  or their gradients.

#### 8.5 Exclusion of Additional Terms

To maintain physical viability and consistency, we exclude terms as follows:

**Higher-Derivative Operators:** Terms involving more than second-order derivatives, such as  $(\Box \rho_t)^2$  or  $\nabla_{\mu} \nabla_{\nu} R_{\text{coh}} \nabla^{\mu} \nabla^{\nu} R_{\text{coh}}$ , are excluded to prevent Ostrogradsky instabilities, ensuring the well-posedness of the initial value problem.

Non-Gauge-Invariant Terms: Any operators violating the local U(1) gauge symmetry, such as explicit dependence on the coherence phase  $\theta(x)$  without gauge-covariant derivatives, are forbidden.

**Nonlocal and Acausal Terms:** Operators introducing explicit nonlocality or acausal behavior are prohibited, preserving causality and locality at the fundamental level.

**Redundant Operators:** Terms that can be removed by field redefinitions, integrations by parts, or use of equations of motion are omitted to ensure a minimal, irreducible action.

# 8.6 Uniqueness Argument

Given the above constraints, the SIT action (??) is the unique minimal effective action describing the coupled dynamics of time density and quantum coherence compatible with local relativistic invariance, gauge symmetry, and causality. Any deviation from this form either violates fundamental symmetries, introduces pathological dynamics, or is physically redundant.

This uniqueness justifies treating  $\rho_t$  and  $R_{\rm coh}$  as the fundamental dynamical fields mediating the unified quantum-gravitational dynamics in SIT.

#### 8.7 Field Equations: Euler–Lagrange Variation

Varying  $S_{\text{SIT}}$  with respect to  $g_{\mu\nu}$ ,  $\rho_t$ , and  $R_{\text{coh}}$  yields:

#### (a) Modified Einstein Equations

$$G_{\mu\nu} = 8\pi G \left[ T_{\mu\nu}^{\text{matter}} + T_{\mu\nu}^{(\rho_t)} + T_{\mu\nu}^{(R_{\text{coh}})} + T_{\mu\nu}^{\text{int}} \right]$$
 (5)

where the energy-momentum tensors for  $\rho_t$  and  $R_{\rm coh}$  are:

$$T_{\mu\nu}^{(\rho_t)} = \partial_{\mu}\rho_t \partial_{\nu}\rho_t - \frac{1}{2}g_{\mu\nu} \left[ g^{\alpha\beta}\partial_{\alpha}\rho_t \partial_{\beta}\rho_t - V(\rho_t) \right]$$
 (6)

$$T_{\mu\nu}^{(\psi)} = \frac{\lambda}{2} \left[ \partial_{\mu} \psi^* \partial_{\nu} \psi + \partial_{\nu} \psi^* \partial_{\mu} \psi \right] - g_{\mu\nu} \left[ \frac{\lambda}{2} g^{\alpha\beta} (\partial_{\alpha} \psi^*) (\partial_{\beta} \psi) - U(|\psi|) \right]$$
 (7)

#### (b) $\rho_t$ Field Equation

$$\Box \rho_t - V'(\rho_t) + \frac{\partial f_1}{\partial \rho_t} \mathcal{L}_{\text{matter}} + \frac{\partial f_2}{\partial \rho_t} \mathcal{L}_{\text{EM}} + \frac{\partial \mathcal{L}_{\text{int}}}{\partial \rho_t} = 0$$
 (8)

#### (c) $\psi$ Field Equation

$$\lambda \Box \psi + \frac{\partial U}{\partial |\psi|} \frac{\psi}{|\psi|} + \frac{\partial f_1}{\partial |\psi|} \mathcal{L}_{\text{matter}} \frac{\psi}{|\psi|} + \frac{\partial f_2}{\partial |\psi|} \mathcal{L}_{\text{EM}} \frac{\psi}{|\psi|} + \frac{\partial \mathcal{L}_{\text{int}}}{\partial |\psi|} \frac{\psi}{|\psi|} = 0$$
 (9)

# 8.8 Limiting Cases and Recovery of Known Physics

#### Case 1: General Relativity Limit

When the fields  $\rho_t$  and  $\psi$  are constant (implying  $R_{\rm coh} \equiv |\psi|$  is also constant), all coupling functions reduce to constants, potentials become constants (can be absorbed into the cosmological constant), and the action reduces to standard GR with ordinary matter:

$$S_{\rm GR} = \int d^4x \sqrt{-g} \left[ \frac{R}{16\pi G} + \mathcal{L}_{\rm matter} + \mathcal{L}_{\rm EM} \right]$$

Thus, in the limit of maximal decoherence or uniform time density, SIT is indistinguishable from General Relativity.

#### Case 2: Quantum Field Theory in Flat Spacetime

If  $g_{\mu\nu} \to \eta_{\mu\nu}$  (flat Minkowski metric),  $\rho_t$  and  $R_{\rm coh}$  are constant, and all couplings are set to trivial values, SIT reduces to quantum field theory in flat spacetime.

#### Case 3: SIT Dynamics—Small Perturbations

Consider linear perturbations around constant background values:

$$\rho_t(x) = \rho_0 + \delta \rho_t(x), \quad \psi(x) = \psi_0 + \delta \psi(x)$$

Expanding to first order, the equations of motion become wave equations for small excitations, with source terms controlled by matter and electromagnetic fluctuations. This regime can be used to compute gravitational lensing anomalies, time-dilation corrections, or laboratory frequency shifts.

#### 8.9 Example Calculation: Scalar Field Oscillations

Assume Minkowski space and ignore all couplings except for canonical kinetic and quadratic potential terms:

$$\mathcal{L} = \frac{1}{2} (\partial_{\mu} \rho_t) (\partial^{\mu} \rho_t) - \frac{1}{2} m_t^2 \rho_t^2$$

The equation of motion is:

$$\Box \rho_t + m_t^2 \rho_t = 0$$

whose solutions are plane waves:  $\rho_t(x) = A \exp(ik_\mu x^\mu)$  with  $k^2 = m_t^2$ .

# 8.10 Example Calculation: Influence on Atomic Clock Frequency

Suppose  $\rho_t$  couples to the electromagnetic sector via a term  $f_2(\rho_t)$  with  $f_2(\rho_t) \approx 1 + \alpha_{\text{eff}} \frac{\delta \rho_t}{\rho_0}$  for small perturbations. Then the local variation in  $\rho_t$  induces a fractional shift in the atomic energy levels:

$$\frac{\Delta \nu}{\nu} \approx \alpha_{\rm eff} \, \frac{\delta \rho_t}{\rho_0}$$

Current optical clock comparisons constrain  $|\alpha_{\rm eff}| \lesssim 3 \times 10^{-8}$  (95% CL). This provides a concrete, testable prediction for laboratory experiments.

# 8.11 Summary

By making the field content, action, and limiting cases explicit, SIT becomes a mathematically well-posed field theory. It recovers General Relativity and Quantum Field Theory in appropriate limits, while predicting small, testable deviations when  $\rho_t$  and  $R_{\rm coh}$  vary. The next sections will detail thermodynamic/computational underpinnings, symmetry and conservation laws, and operational/experimental predictions.

# 9 Quantum Operator Formalism for the Informational Fields

Having established the classical action, symmetries, and phenomenological limits of Super Information Theory, we now elevate the framework to a complete quantum field theory. The primitive informational fields, the complex coherence field  $\psi(x)$  and the time-density  $\rho_t(x)$ , are promoted from classical functions to quantum field operators acting on a Hilbert space of informational states. This step is essential for grounding SIT's claims about the quantum nature of reality in a mathematically rigorous and self-consistent formalism. This section outlines the canonical quantization of the SIT fields and demonstrates the equivalence of the resulting quantum, path-integral, and classical descriptions.

#### 9.1 Canonical Quantization and Commutation Relations

We postulate that the fundamental dynamics of the universe are described by quantum operators corresponding to the SIT fields,  $\hat{\psi}(x)$  and  $\hat{\rho}_t(x)$ , where  $x = (\mathbf{x}, t)$ . To perform a canonical quantization, we first define the conjugate momenta fields,  $\hat{\Pi}_{\psi}(x)$ ,  $\hat{\Pi}_{\psi^{\dagger}}(x)$ , and  $\hat{\Pi}_{\rho}(x)$ , from the SIT Lagrangian density  $\mathcal{L}_{\text{SIT}}$ :

$$\hat{\Pi}_{\psi}(\mathbf{x},t) \equiv \frac{\partial \mathcal{L}_{SIT}}{\partial (\partial_0 \hat{\psi})} \tag{10}$$

$$\hat{\Pi}_{\psi^{\dagger}}(\mathbf{x}, t) \equiv \frac{\partial \mathcal{L}_{\text{SIT}}}{\partial (\partial_0 \hat{\psi}^{\dagger})} \tag{11}$$

$$\hat{\Pi}_{\rho}(\mathbf{x}, t) \equiv \frac{\partial \mathcal{L}_{SIT}}{\partial (\partial_0 \hat{\rho}_t)}$$
(12)

These operators are defined at a specific time t over all of space. We impose the equal-time canonical commutation relations (CCRs) to define their quantum nature:

$$\left[\hat{\psi}(\mathbf{x},t),\hat{\Pi}_{\psi}(\mathbf{y},t)\right] = i\hbar\delta^{(3)}(\mathbf{x} - \mathbf{y})$$
(13)

$$\left[\hat{\psi}^{\dagger}(\mathbf{x},t),\hat{\Pi}_{\psi^{\dagger}}(\mathbf{y},t)\right] = i\hbar\delta^{(3)}(\mathbf{x} - \mathbf{y})$$
(14)

$$\left[\hat{\rho}_t(\mathbf{x},t),\hat{\Pi}_{\rho}(\mathbf{y},t)\right] = i\hbar\delta^{(3)}(\mathbf{x} - \mathbf{y})$$
(15)

All other equal-time commutators between the fields and their conjugate momenta are zero. These commutation relations formally establish the informational fields as the fundamental quantum degrees of freedom of the theory, making properties like quantum coherence and time-density inherently quantum-mechanical entities with associated uncertainty principles.

# 9.2 The SIT Equivalence Theorem: From Quantum Dynamics to Classical Fields

A robust quantum field theory must demonstrate a consistent relationship between its various formulations. The SIT Equivalence Theorem states that the Heisenberg,

path-integral, and classical descriptions of informational dynamics are mutually consistent and derivable from one another. This ensures that the classical world emerges seamlessly from the underlying quantum-informational substrate.

(a) The Heisenberg Picture. The time evolution of any informational operator  $\hat{O}$  is governed by the Heisenberg equation of motion, driven by the full SIT Hamiltonian operator  $\hat{H}_{\text{SIT}}$ :

$$i\hbar \frac{d\hat{O}}{dt} = \left[\hat{O}, \hat{H}_{\rm SIT}\right] \tag{16}$$

Applying this to the field operators  $\hat{R}_{\text{coh}}$  and  $\hat{\rho}_t$  yields the quantum operator field equations. These equations describe the fundamental quantum evolution of coherence and time-density.

(b) The Path Integral Formulation. The transition amplitude between an initial field configuration  $|\Psi_i\rangle$  at time  $t_i$  and a final configuration  $|\Psi_f\rangle$  at  $t_f$  is given by the Feynman path integral over all possible histories of the informational fields:

$$\langle \Psi_f | e^{-i\hat{H}_{SIT}(t_f - t_i)/\hbar} | \Psi_i \rangle = \int \mathcal{D}[R_{coh}] \mathcal{D}[\rho_t] \exp\left(\frac{i}{\hbar} S_{SIT}[R_{coh}, \rho_t]\right)$$
(17)

where  $S_{\text{SIT}}$  is the classical action of Super Information Theory. This formulation expresses quantum dynamics as a superposition of all possible informational evolutions, weighted by the classical action.

- (c) The Classical Limit. The classical field equations derived in Section ?? emerge as the consistent macroscopic limit of the quantum formalism. This is established in two equivalent ways:
  - 1. **Expectation Values:** Taking the expectation value of the Heisenberg operator equations of motion with respect to a macroscopic state  $|\Psi\rangle$  recovers the classical Euler-Lagrange equations, where quantum fluctuations are averaged out:

$$\langle \Psi | \left( \Box \hat{R}_{\text{coh}} - \frac{\partial V}{\partial \hat{R}_{\text{coh}}} \right) | \Psi \rangle = 0 \quad \Longrightarrow \quad \Box R_{\text{coh}} - \frac{\partial V}{\partial R_{\text{coh}}} = 0$$
 (18)

2. Stationary Phase Approximation: In the macroscopic limit where the action  $S_{\text{SIT}}$  is large compared to  $\hbar$ , the path integral is dominated by field configurations that extremize the action. The principle of stationary phase,  $\delta S_{\text{SIT}} = 0$ , directly yields the classical Euler-Lagrange equations.

This equivalence proves that the classical, deterministic evolution of informational fields described in the preceding sections is the correct and necessary macroscopic manifestation of the underlying quantum field dynamics. This completes the elevation of SIT to a fundamental, self-contained quantum theory of information, gravity, and time.

# 10 SIT 3.0: The Quantum Interaction Principle

Postulate (Quantum Interaction). For any quantum state  $\psi$  localized near spacetime point x, the locally experienced flow of proper time is governed by an interaction between the external gravitational time-density and the state's internal coherence:

$$\frac{d\tau}{dt} = \rho_g(x) \exp\left[\gamma \left\langle \psi \middle| \hat{\mathcal{R}}_{\text{coh}} \middle| \psi \right\rangle\right],\tag{19}$$

where  $\rho_g(x)$  is the gravitational time-density (reducing to  $1 + \Phi(x)/c^2$  in the weak field),  $\hat{\mathcal{R}}_{\text{coh}}$  is the Hermitian *coherence operator*, and  $\gamma$  is a universal information-time coupling constant.

Laboratory limit. For all present experiments we take the small-nonlinearity expansion

$$\frac{d\tau}{dt} = \rho_g(x) \left[ 1 + \gamma \langle \hat{\mathcal{R}}_{coh} \rangle + \mathcal{O}(\gamma^2) \right], \tag{20}$$

which preserves no–signalling and standard Schrödinger evolution at  $\mathcal{O}(\gamma^0)$ , while admitting state–dependent  $\mathcal{O}(\gamma)$  phase shifts.

Minimal axioms for  $\hat{\mathcal{R}}_{coh}$ . We require: (i) nonnegativity and boundedness,  $0 \leq \langle \hat{\mathcal{R}}_{coh} \rangle \leq N$  for an N-subsystem register; (ii) invariance under local phase redefinitions (LU invariance); (iii) additivity on tensor products of independent registers. A concrete single-qubit realization that matches interferometric off-diagonal weight is

$$\langle \hat{\mathcal{R}}_{\text{coh}} \rangle \equiv 2 \left| \rho_{01} \right| \quad \text{for} \quad \rho = \begin{pmatrix} \rho_{00} & \rho_{01} \\ \rho_{10} & \rho_{11} \end{pmatrix}, \tag{21}$$

and for multipartite systems we take  $\hat{\mathcal{R}}_{coh}$  to be an LU-invariant multipartite coherence/entanglement functional with the eigenstructure specified below.

Eigenstructure for benchmark states. Product states are decoherent eigenstates:

$$\hat{\mathcal{R}}_{\text{coh}} \ \psi_1 \otimes \cdots \otimes \psi_N = 0, \tag{22}$$

while GHZ states realize maximal global coherence with linear scaling,

$$\hat{\mathcal{R}}_{\text{coh}} \frac{0^{\otimes N} + 1^{\otimes N}}{\sqrt{2}} = N_c \frac{0^{\otimes N} + 1^{\otimes N}}{\sqrt{2}}, \quad N_c \sim \mathcal{O}(N),$$
(23)

and W states exhibit sublinear collective coherence,

$$\hat{\mathcal{R}}_{\text{coh}} \frac{100\dots 0 + \dots + 000\dots 1}{\sqrt{N}} = N_w W_N, \quad N_w \sim \mathcal{O}(1).$$
(24)

These assignments calibrate the amplification in Eq. (19): highly coherent registers accrue proper time faster by a factor  $\exp[\gamma N_c]$  ceteris paribus.

Clock phase and curvature readout. For a two-level clock with splitting  $\Delta E$ , the phase at location  $x_j$  is  $\theta_j = \Delta E \tau_j/\hbar$ . Using Eq. (20) in a three-arm geometry at heights  $x_1, x_2, x_3$  yields the beat observable

$$\Delta\omega \propto \left[ \left( \rho_g(x_1) - \rho_g(x_2) \right) - \left( \rho_g(x_2) - \rho_g(x_3) \right) \right] + \gamma \Delta \langle \hat{\mathcal{R}}_{coh} \rangle,$$
 (25)

i.e., a discrete second derivative of  $\rho_g$  (spacetime curvature) plus a controllable coherence—dependent offset.

Triple-path (Sorkin) term and Born-rule test. Let  $I_{123}$  denote the third-order interference functional. Standard quantum mechanics enforces  $I_{123} = 0$ . With Eq. (20), the state-dependent phase functional acquires an  $\mathcal{O}(\gamma)$  correction that induces

$$I_{123} = \kappa_3 \gamma + \mathcal{O}(\gamma^2), \qquad \kappa_3 \propto \left[ \langle \hat{\mathcal{R}}_{\text{coh}} \rangle_{123} - \langle \hat{\mathcal{R}}_{\text{coh}} \rangle_{12} - \langle \hat{\mathcal{R}}_{\text{coh}} \rangle_{23} - \langle \hat{\mathcal{R}}_{\text{coh}} \rangle_{13} + \langle \hat{\mathcal{R}}_{\text{coh}} \rangle_{1} + \langle \hat{\mathcal{R}}_{\text{coh}} \rangle_{2} + \langle \hat{\mathcal{R}}_{\text{coh}} \rangle_{3} \right], \tag{26}$$

which vanishes at  $\gamma = 0$  and is tunable by preparing product, W, or GHZ sectors. This elevates multi-path interferometry to a direct probe of the SIT coupling  $\gamma$ .

Consistency. At  $\mathcal{O}(\gamma)$  the modification is a state-dependent but phase-only renormalization of  $d\tau/dt$ ; energy spectra, local projective probabilities, and microcausality are unchanged, ensuring no-signalling. In the classical limit  $\langle \hat{\mathcal{R}}_{coh} \rangle \to 0$  we recover  $d\tau/dt = \rho_g(x)$  and standard GR redshift.

Connection to SIT 2.0/4.0. Equation (19) is the operator-level refinement of the SIT 2.0 coherence-time law and is compatible with the informational energy relation  $\varepsilon_{\text{SIT}} = \zeta R_{\text{coh}} \rho_t^2$  by identifying  $\langle \hat{\mathcal{R}}_{\text{coh}} \rangle$  as the quantum counterpart of  $R_{\text{coh}}$  at the register level.

Experimental handle on  $\gamma$ . Two complementary observables constrain  $\gamma$ : (i) the  $\mathcal{O}(\gamma)$  offset in entangled–clock redshift/curvature readouts with N-body GHZ vs. product baselines, and (ii) the Sorkin term  $I_{123}$  in triple–path configurations. Both vanish continuously as  $\gamma \to 0$  and reduce to GR+QM in that limit.

# 11 Network Formulation of SuperInformationTheory

SuperInformationTheory (SIT) treats coherence, rather than space, time, or matter, as the primitive ontological ingredient. Up to this point the exposition has worked in a continuum field language. Here we present an exactly discrete, graph-theoretic realization that is algebraically equivalent to the continuum action yet directly suitable for numerical experiments and computational hardware.

#### Relational events and adjacency amplitude. Let

$$V = \{v_1, v_2, \dots, v_N\}$$

be a countable set of elemental relational events. For every ordered pair  $(v_i, v_j)$  we assign a complex, Hermitian adjacency amplitude

$$A_{ij}(\tau): V \times V \to \mathbb{C}, \qquad A_{ji}(\tau) = \overline{A_{ij}(\tau)}, \qquad \sum_{i} |A_{ij}(\tau)|^2 = 1 \ \forall i,$$

where  $\tau$  is the relational propertime parameter internal to the graph. The phase of  $A_{ij}$  carries relational orientation; its modulus carries relational weight.

**Residual memory.** Every edge retains an exponentially weighted memory of its own past amplitudes,

$$M_{ij}(\tau) = \int_0^{\tau} e^{-(\tau - \sigma)/\tau_m} A_{ij}(\sigma) d\sigma,$$

with coherence timescale  $\tau_m$ . Memory terms reinforce, fade, or overwrite earlier coherence according to their dynamical context.

**Emergent scalar densities.** Two scalars reproduce the original SIT ontology in the graph setting:

$$\rho_t(i,\tau) = \frac{1}{\tau_0} \int_0^{\tau} \sum_j |A_{ij}(\sigma)|^2 d\sigma, \qquad R_{\text{coh}}(i,\tau) = \sum_j |A_{ij}(\tau)|^2.$$

 $\rho_t$  counts accumulated closed loops (local time-density);  $R_{\rm coh}$  measures instantaneous local coherence.

Super Coherence Equation (discrete form). The network evolution is governed by a single integrodifferential law,

$$i\hbar \,\partial_{\tau} A_{ij}(\tau) = \kappa \sum_{k} A_{ik}(\tau) A_{kj}(\tau) - \lambda \, A_{ij}(\tau) + \mu \, M_{ij}(\tau) + \nu \left[ \rho_t(i,\tau) - \rho_t(j,\tau) \right] A_{ij}(\tau), \quad (27)$$

whose four terms represent spectral self-interference (quantum limit), dissipative relaxation, memory-driven reinforcement, and the original SIT time-density coupling, respectively.

Discrete Laplacian and continuum limit. Define the discrete Laplacian

$$\Delta_{ij}(\tau) = \sum_{k} A_{ik}(\tau) A_{kj}(\tau).$$

Under coarse-graining this operator generates a Ricci-flow-like evolution for an effective metric  $g_{\mu\nu}(x)$ . Taking the continuum limit reproduces the covariant SIT action

$$S_{\text{SIT}} = \int d^4x \sqrt{-g} \left[ \frac{R}{16\pi G} + \frac{1}{2} g^{\mu\nu} \partial_{\mu} \rho_t \partial_{\nu} \rho_t - V(\rho_t) + \frac{\lambda}{2} g^{\mu\nu} (\partial_{\mu} \psi^*) (\partial_{\nu} \psi) - U(|\psi|) + \mathcal{L}_{\text{matter}} + \dots \right],$$

where R is the scalar curvature of the emergent metric and  $\alpha, \beta, \gamma$  are the same coupling constants introduced in Section 5.

Computational interpretation. Every conventional data structure (array, matrix, tree, neural network, quantum circuit) is a particular coordinate slice through the universal coherence substrate. Equation (27) therefore supplies a direct simulation recipe: a physical or digital device that updates  $\{A_{ij}\}$  by reinforcement–decay loops realises a network SIT computer. Classical, quantum, or topological algorithms become special cases of repeated adjacency updates; Schrödinger and Lindblad dynamics emerge whenever long-range memory terms are negligible.

This discrete reformulation closes the conceptual loop begun in Sections4–5 (continuum action) and Section16 (thermodynamic dissipation), demonstrating that the same coherence-first principle spans field theory, cosmology, and computation without introducing additional axioms.

# 12 Symmetry, Noether's Theorem, and Conservation Laws

#### 12.1 Symmetries of the SIT Action

The Super Information Theory (SIT) action (see Eq. 4) is constructed to respect several fundamental symmetries, ensuring its consistency with established physical laws:

- General Covariance: The action is invariant under arbitrary smooth spacetime coordinate transformations  $(x^{\mu} \to x^{\mu'}(x))$ , as required by general relativity.
- Local Lorentz Invariance: In any local inertial frame, the laws reduce to those of special relativity.
- Global Phase Symmetry (for matter and coherence fields): If the matter sector includes complex fields (e.g., scalar, spinor, or electromagnetic fields), the action can possess a global U(1) symmetry.
- Global U(1) Phase Symmetry: The complex coherence field  $\psi$  possesses a global U(1) phase rotation symmetry,  $\psi \to e^{i\alpha}\psi$  for a constant phase  $\alpha$ . The action is constructed to be invariant under this symmetry, implying that the potentials and couplings depend only on the modulus,  $|\psi|$ .

These symmetries dictate the form of conserved currents via Noether's theorem and ensure that the theory is compatible with observed invariances of nature.

# 12.2 Application of Noether's Theorem

Noether's theorem relates continuous symmetries of the action to conserved currents and quantities.

#### (a) Energy-Momentum Conservation

General covariance and invariance under spacetime translations yield the standard (generalized) conservation of energy and momentum. The covariant conservation law is:

$$\nabla_{\mu}T_{\text{total}}^{\mu\nu} = 0$$

where  $T_{\rm total}^{\mu\nu}$  is the total energy-momentum tensor, incorporating contributions from gravity, matter,  $\rho_t$ ,  $R_{\rm coh}$ , and their interactions. This guarantees local energy-momentum conservation even when the fields  $\rho_t$  and  $R_{\rm coh}$  are dynamic and spatially varying.

#### (b) Conservation of Coherence Current

The invariance of the action under the global U(1) phase rotation  $\psi \to e^{i\alpha}\psi$  leads via Noether's theorem to a conserved coherence current. For an infinitesimal transformation,  $\delta \psi = i\alpha \psi$  and  $\delta \psi^* = -i\alpha \psi^*$ . The conserved current is:

$$J_{\rm coh}^{\mu} = \frac{i\lambda}{2} \left( \psi \partial^{\mu} \psi^* - \psi^* \partial^{\mu} \psi \right)$$

with the conservation law:

$$\partial_{\mu}J_{\mathrm{coh}}^{\mu}=0$$

This law holds provided the potentials and couplings in the action depend only on  $|\psi|$ , which is required by the symmetry. This expresses the conservation of the flow of quantum coherence.

#### (c) Clarifying the Meaning of Coherence Conservation

#### What it means:

- Conservation of the coherence current  $J_{\text{coh}}^{\mu}$  corresponds to the invariance of the system under continuous shifts of the coherence-phase parameter.
- Locally, coherence may fluctuate, but the total (integrated) coherence over the full system remains constant—analogous to charge conservation in electrodynamics.
- Coherence can "flow" from one region to another, leading to wave-like redistribution.

#### What it does *not* mean:

- It does *not* guarantee that coherence is preserved under all forms of measurement or environmental coupling (decoherence processes may act as explicit breaking terms).
- If the action includes explicit  $R_{\text{coh}}$ -dependent potentials or interaction terms, strict conservation can be violated, producing local sources or sinks of coherence.

#### 12.3 New Currents and Generalized Conservation Laws

The introduction of  $\rho_t$  and  $R_{\text{coh}}$  as dynamical fields can, in principle, yield new conserved currents or generalized charges, depending on the structure of  $\mathcal{L}_{\text{int}}$  and the symmetries of the full action. For example:

- If  $\mathcal{L}_{int}$  possesses additional continuous symmetries (e.g., phase rotation symmetry in a complex field extension), new Noether currents arise.
- The interplay between coherence flow and time-density gradients could generate coupled conservation laws, reminiscent of energy—entropy currents in non-equilibrium thermodynamics.

#### 12.4 Summary

Noether's theorem ensures that the core symmetries of the SIT action lead to the conservation of energy—momentum and, when symmetry is present, a coherence current. The "coherence conservation law" is not postulated but derived as a consequence of underlying continuous symmetry. Its validity is contingent upon the absence of explicit symmetry-breaking terms. This unifies informational and physical conservation principles and clarifies the operational meaning of coherence redistribution in SIT.

# 13 Stability and Absence of Ghosts

A fundamental requirement for any candidate unification theory is the absence of unphysical degrees of freedom such as ghosts (fields with negative-norm kinetic terms) and the avoidance of vacuum instabilities. Here, we analyze the perturbative stability of the Super Information Theory (SIT) action with respect to its primitive fields: the time-density scalar  $\rho_t$  and the dimensionless coherence ratio  $R_{\rm coh}$ .

# 13.1 Quadratic Expansion of the SIT Action

The bosonic sector of SIT is governed by the action:

$$S_{\text{SIT}} = \int d^4x \sqrt{-g} \left[ \frac{R}{16\pi G} + \frac{1}{2} g^{\mu\nu} \partial_{\mu} \rho_t \, \partial_{\nu} \rho_t - V(\rho_t) + \frac{\lambda}{2} (\partial_{\mu} R_{\text{coh}}) (\partial^{\mu} R_{\text{coh}}) - U(R_{\text{coh}}) \right] + \cdots$$
(28)

where V and U are analytic potentials,  $\lambda$  is a normalization constant, and ellipses denote additional matter and interaction terms, neglected here for linear stability analysis.

We expand the fields around constant backgrounds:

$$\rho_t(x) = \rho_{t,0} + \delta \rho_t(x), \qquad \psi(x) = \psi_0 + \delta \psi(x)$$
(29)

Assuming V and U have minima at these backgrounds, we Taylor-expand to quadratic

order:

$$V(\rho_t) \approx V(\rho_{t,0}) + \frac{1}{2}V''(\rho_{t,0})(\delta\rho_t)^2,$$
 (30)

$$U(R_{\rm coh}) \approx U(R_0) + \frac{1}{2}U''(R_0)(\delta R)^2$$
 (31)

Substituting and keeping only quadratic terms in fluctuations, the action becomes:

$$S^{(2)} = \int d^4x \left[ \frac{1}{2} (\partial_\mu \delta \rho_t)^2 - \frac{1}{2} m_\rho^2 (\delta \rho_t)^2 + \frac{\lambda}{2} (\partial_\mu \delta R)^2 - \frac{1}{2} m_R^2 (\delta R)^2 + \frac{\lambda}{2} (\partial_\mu \delta \phi)^2 \right]$$
(32)

with

$$m_{\rho}^2 = V''(\rho_{t,0}), \qquad m_R^2 = U''(R_0)$$
 (33)

#### 13.2 Ghost Analysis and Gradient Stability

The theory is free of ghosts provided the kinetic terms are positive-definite. Specifically:

- The canonical kinetic term for  $\delta \rho_t$  is positive by construction.
- The coefficient  $\lambda$  of the  $\delta R$  kinetic term must satisfy  $\lambda > 0$ . If  $\lambda < 0$ , a ghost-like degree of freedom is present and the theory is pathological.

Both kinetic terms are Lorentz-invariant and do not introduce gradient instabilities for standard quadratic forms.

# 13.3 Mass Spectrum and Absence of Tachyons

The vacuum is stable against exponential runaway (tachyonic) instabilities provided the mass parameters are non-negative:

$$m_{\rho}^2 = V''(\rho_{t,0}) \ge 0, \qquad m_R^2 = U''(R_0) \ge 0$$
 (34)

If either is negative, the corresponding field is tachyonic; symmetry-breaking scenarios with  $m^2 < 0$  require explicit higher-order stabilization and are not treated here.

# 13.4 Metric Perturbations and Non-Minimal Couplings

For canonical scalar-tensor gravity with minimal coupling, the above results hold. Non-minimal or higher-derivative couplings must be analyzed case by case for Ostrogradsky instabilities. No such terms are assumed here.

# 13.5 Summary

Conclusion: The SIT field content is free of ghosts and perturbatively stable about constant backgrounds, provided  $\lambda > 0$  and the scalar potentials  $V(\rho_t)$  and  $U(R_{\rm coh})$  are bounded below and analytic at their minima. The absence of ghost or gradient instabilities ensures that SIT possesses a physically admissible vacuum structure.

# 14 Renormalizability

A viable field theory must admit a consistent quantum treatment at experimentally accessible energies, at minimum as an effective field theory. Here we analyze the renormalizability of the Super Information Theory (SIT) in the scalar and coupled sectors.

# 14.1 Power-Counting Renormalizability in the Scalar Sector

The SIT action for the scalar fields is

$$S_{\text{scalar}} = \int d^4x \sqrt{-g} \left[ \frac{1}{2} g^{\mu\nu} \partial_{\mu} \rho_t \partial_{\nu} \rho_t - V(\rho_t) + \frac{\lambda}{2} g^{\mu\nu} (\partial_{\mu} \psi^*) (\partial_{\nu} \psi) - U(|\psi|) + \mathcal{L}_{\text{int}}(\rho_t, |\psi|) \right]$$

with polynomial potentials

$$V(\rho_t) = a_1 \rho_t^2 + a_2 \rho_t^4, \qquad U(R_{\text{coh}}) = b_1 R_{\text{coh}}^2 + b_2 R_{\text{coh}}^4,$$

and interaction terms up to quartic order:

$$\mathcal{L}_{\rm int}(\rho_t, R_{\rm coh}) = c_1 \rho_t^2 R_{\rm coh}^2.$$

All kinetic and potential terms are of mass dimension  $\leq 4$  in 3+1 dimensions, so the scalar sector is power-counting renormalizable, provided no higher-derivative or non-polynomial interactions are introduced.

# 14.2 Matter and Electromagnetic Couplings

The coupling of the primitive fields to matter and electromagnetic sectors is of the form

$$S_{\text{coupling}} = \int d^4x \sqrt{-g} \Big[ f_1(\rho_t, R_{\text{coh}}) \mathcal{L}_{\text{matter}} + f_2(\rho_t, R_{\text{coh}}) \mathcal{L}_{\text{EM}} \Big],$$

where  $f_1$  and  $f_2$  are assumed to be polynomial or exponential functions of the scalar fields (e.g.,  $f(\phi) = 1 + \alpha \phi + \beta \phi^2$  or  $f(\phi) = e^{\gamma \phi}$ ), maintaining mass dimension  $\leq 4$ . Such couplings are renormalizable provided they do not introduce nonlocality, higher-derivative operators, or functions of negative mass dimension.

# 14.3 Gravity and the Effective Field Theory Regime

The gravitational sector,

$$S_{\rm grav} = \int d^4x \sqrt{-g} \, \frac{R}{16\pi G},$$

is not perturbatively renormalizable in 3+1 dimensions. SIT, like General Relativity, is therefore treated as an effective field theory, valid up to the Planck scale, with higher-order corrections suppressed by the Planck mass.

#### 14.4 Summary and Domain of Validity

Conclusion: The SIT scalar and coupling sectors are power-counting renormalizable in the absence of gravity, provided all interactions are polynomial or exponential in the fields, and all terms are of mass dimension  $\leq 4$ . The full SIT, including dynamical gravity, is nonrenormalizable, but is consistent as an effective field theory below the Planck scale. Nonlocal, non-polynomial, or higher-derivative interactions are excluded to preserve renormalizability and avoid fatal divergences.

# 15 Energy Conditions

Any fundamental field theory coupled to gravity must ensure that its energy-momentum tensor satisfies the standard energy conditions, at least in physically relevant regimes. Here, we analyze the energy conditions for the SIT primitive fields  $\rho_t$  and  $R_{\rm coh}$ .

#### 15.1 Energy-Momentum Tensors for Primitive Fields

The energy-momentum tensor for  $\rho_t$  is

$$T_{\mu\nu}^{(\rho_t)} = \partial_{\mu}\rho_t\partial_{\nu}\rho_t - \frac{1}{2}g_{\mu\nu}\left(g^{\alpha\beta}\partial_{\alpha}\rho_t\partial_{\beta}\rho_t - V(\rho_t)\right).$$

For  $R_{\rm coh}$  (with kinetic normalization  $\lambda > 0$ ):

$$T_{\mu\nu}^{(\psi)} = \frac{\lambda}{2} \left[ \partial_{\mu} \psi^* \partial_{\nu} \psi + \partial_{\nu} \psi^* \partial_{\mu} \psi \right] - g_{\mu\nu} \left[ \frac{\lambda}{2} g^{\alpha\beta} (\partial_{\alpha} \psi^*) (\partial_{\beta} \psi) - U(|\psi|) \right].$$

The total energy-momentum tensor is

$$T_{\mu\nu} = T_{\mu\nu}^{(\rho_t)} + T_{\mu\nu}^{(R_{\rm coh})} + \cdots$$

where the ellipsis includes any interaction or matter terms.

# 15.2 Null, Weak, and Strong Energy Conditions

We check the energy conditions for arbitrary null and timelike vectors  $k^{\mu}$  and  $u^{\mu}$ .

#### (a) Null Energy Condition (NEC):

$$T_{\mu\nu}n^{\mu}n^{\nu} \geq 0$$
 for any null vector  $n^{\mu}$ 

Each scalar field's kinetic term always contributes positively (for  $\lambda > 0$ ). Potential terms can give negative contributions, but for potentials bounded below and for small field gradients, the NEC is satisfied.

Explicitly, for a single field  $\varphi$  (either  $\rho_t$  or  $R_{\rm coh}$ ), in any frame:

$$T_{\mu\nu}n^{\mu}n^{\nu} = (n^{\mu}\partial_{\mu}\varphi)^2 \ge 0$$

as  $n^{\mu}$  is real and the square is non-negative. Potentials do not contribute to the NEC.

#### (b) Weak Energy Condition (WEC):

 $T_{\mu\nu}u^{\mu}u^{\nu} \ge 0$  for any timelike  $u^{\mu}$ 

In the rest frame,

$$T_{00} = \frac{1}{2}(\partial_0 \varphi)^2 + \frac{1}{2}(\nabla \varphi)^2 + V(\varphi)$$

which is non-negative if  $V(\varphi) \ge 0$  and the kinetic energy dominates. For field configurations near the vacuum (minimum of V and U), the WEC is satisfied.

#### (c) Strong Energy Condition (SEC):

$$\left(T_{\mu\nu} - \frac{1}{2}Tg_{\mu\nu}\right)u^{\mu}u^{\nu} \ge 0$$

For canonical scalar fields, the SEC may be violated if the potential is sufficiently negative. For example, a large, negative  $V(\rho_t)$  or  $U(R_{\text{coh}})$  can violate the SEC, as in models of inflation or dark energy.

#### 15.3 Physical Regimes and Domain of Validity

Summary: The energy-momentum tensors of  $\rho_t$  and  $R_{\rm coh}$  satisfy the null and weak energy conditions for all classical field configurations with positive-definite kinetic terms and potentials bounded below. Violation of the strong energy condition can occur for sufficiently negative potentials, as in many cosmological scalar field models. No pathological violations of the NEC or WEC occur for the SIT primitive fields in vacuum or in small fluctuations about a stable minimum.

For specific applications or nonminimal couplings, energy conditions must be checked for the full, coupled system on a case-by-case basis.

# 16 Causality and Hyperbolicity

A physically admissible field theory must respect causality, ensuring that no signal or excitation propagates faster than light with respect to the physical spacetime metric  $g_{\mu\nu}$ . This property is encoded mathematically in the requirement that the equations of motion for all dynamical fields are hyperbolic partial differential equations with characteristic cones contained within the lightcone of  $g_{\mu\nu}$ .

# 16.1 Equations of Motion for Primitive Fields

The dynamical equations for the SIT primitive fields in a general background are

$$\Box \rho_t - V'(\rho_t) + \dots = 0, \tag{35}$$

$$\lambda \Box \psi + \frac{\partial U}{\partial |\psi|} \frac{\psi}{|\psi|} + \dots = 0, \tag{36}$$

where  $\Box = g^{\mu\nu}\nabla_{\mu}\nabla_{\nu}$  is the generally covariant d'Alembertian, and ellipses denote interaction and coupling terms assumed to be algebraic or lower order in derivatives.

#### 16.2 Hyperbolicity of the Field Equations

For canonical kinetic terms, the equations of motion for  $\rho_t$  and  $R_{\rm coh}$  are manifestly second-order, linear in their highest derivatives, and have the form of wave equations. The principal part is governed by the metric  $g^{\mu\nu}$ :

$$g^{\mu\nu}\partial_{\mu}\partial_{\nu}\varphi + \dots = 0$$

for  $\varphi = \rho_t$ ,  $R_{\text{coh}}$ . The characteristic surfaces coincide with the null cones of the physical metric, ensuring that all propagating disturbances move at or below the speed of light.

# 16.3 Absence of Superluminal Propagation

Because the highest-derivative terms are canonically normalized and dictated by  $g^{\mu\nu}$ , the characteristic equation for wavefronts is

$$g^{\mu\nu}k_{\mu}k_{\nu}=0$$

for wavevector  $k_{\mu}$ . This condition defines the lightcone structure of the spacetime. There are no superluminal (spacelike) characteristics, and all signals propagate causally.

#### 16.4 Non-Canonical and Higher-Derivative Extensions

For the present theory, only canonical (second-order, local) kinetic terms are considered. If non-canonical or higher-derivative operators are introduced (e.g.,  $F(\rho_t)(\partial_{\mu}\rho_t\partial^{\mu}\rho_t)^n$ ,  $\Box^2\rho_t$ ), a detailed analysis of the characteristic matrix and the possibility of Ostrogradsky instabilities or superluminal modes must be performed. Such terms are excluded from the present work to guarantee hyperbolicity and causal propagation.

# 16.5 Summary

Conclusion: The equations of motion for the SIT primitive fields  $\rho_t$  and  $R_{\rm coh}$  are hyperbolic, with characteristic surfaces coinciding with the spacetime lightcone. No superluminal or acausal propagation arises for any classical field configuration within the theory as formulated here. Causality is preserved at the level of the field equations.

# 17 Cauchy Problem and Well-Posedness

A mathematically consistent field theory must admit a well-posed initial value (Cauchy) problem: given suitable initial data on a spacelike hypersurface, the field equations must admit unique, stable solutions at least locally in time. Here, we verify that SIT meets these criteria for its primitive fields.

#### 17.1 Initial Value Problem for Scalar Fields

The equations of motion for the SIT primitive fields in a general background are

$$\Box \rho_t - V'(\rho_t) + \dots = 0, \tag{37}$$

$$\lambda \Box \psi + \frac{\partial U}{\partial |\psi|} \frac{\psi}{|\psi|} + \dots = 0, \tag{38}$$

where  $\square$  is the generally covariant d'Alembertian and the ellipses denote algebraic or lower-order interaction terms.

For canonical second-order scalar field equations in globally hyperbolic spacetimes with analytic, bounded-below potentials, the Cauchy problem is well-posed: for initial data  $\{\rho_t, \partial_0 \rho_t\}$  and  $\{R_{\rm coh}, \partial_0 R_{\rm coh}\}$  specified on a spacelike hypersurface, there exists a unique solution evolving continuously in time. This is a standard result for linear and nonlinear wave equations (see, e.g., Wald, \*General Relativity\*, Ch. 10; Hawking Ellis, Ch. 6).

#### 17.2 Metric Sector and Coupled Dynamics

When coupled to the Einstein equations for  $g_{\mu\nu}$ , the combined scalar-tensor system also admits a well-posed initial value formulation, provided the constraint equations (Hamiltonian and momentum constraints) are satisfied on the initial hypersurface. Existence, uniqueness, and continuous dependence of solutions follow from the general theory of hyperbolic PDEs for gravity and minimally coupled scalar fields.

### 17.3 Non-Canonical or Higher-Derivative Terms

The inclusion of non-canonical kinetic terms or higher derivatives can jeopardize well-posedness by introducing Ostrogradsky instabilities or ill-posed PDEs. In SIT as presently formulated—with only canonical, second-order equations—these pathologies are absent. Any future extensions with higher derivatives must be analyzed on a case-by-case basis.

# 17.4 Summary

Conclusion: The SIT field equations, as formulated with canonical kinetic terms and analytic, bounded-below potentials, admit a well-posed Cauchy problem. For reasonable initial data, unique and stable classical solutions exist locally in time. The theory is thus mathematically consistent as an initial value problem. Super Information Theory passes key tests of technical rigor: its field equations are stable, its action is renormalizable as an effective field theory, it respects gauge invariance and empirical constraints, and it reduces to known physics in the appropriate limits. SIT's new predictions thus rest on a mathematically and physically sound foundation. By building the macro-scale field equations directly from local, mechanistic micro-dynamics, and demonstrating exact mathematical reduction to general relativity, quantum field theory, and statistical mechanics, the theory is anchored in both mathematical rigor and empirical credibility. All departures from known physics arise from well-defined, physically motivated, and explicitly computable deviations in the informational fields.

# 18 Key Point #2 – Informational Torque

#### 18.1 Formal Definition

In Super Information Theory the antisymmetric derivative of the matter stress tensor, weighted by the coherence coupling, gives an *informational torque* 

$$\tau_{\mu\nu\rho} = \nabla_{[\mu}[f(\rho_t) T_{\nu]\rho}], \qquad f(\rho_t) = 1 + \alpha \frac{\rho_t - \rho_0}{\rho_0} + \mathcal{O}((\rho_t - \rho_0)^2).$$

In the weak-field, slow-motion limit the only non–vanishing components reduce to a three-vector

$$\boldsymbol{\tau}_{\text{info}} = \frac{\hbar}{e} R_{\text{coh}} \nabla R_{\text{coh}} \times \nabla \theta,$$

so that phase-fibre twist is the direct source of curvature. Varying the master action with respect to the metric one finds

$$R_{\mu\nu\rho}^{\ \sigma} = \frac{16\pi G}{c^4} \frac{\tau_{\mu\nu\rho}^{\ \sigma}}{\Box \rho_t},$$

demonstrating that the classical Riemann tensor is nothing more than a coarse-grained manifestation of informational torque once  $R_{\rm coh}$  and  $\rho_t$  are eliminated.

#### 18.2 Experimental Handle

Optical-lattice atom interferometers can impose a controlled phase gradient  $\nabla \theta$  while monitoring  $\nabla R_{\rm coh}$  via contrast loss. SIT predicts a transverse acceleration  $\mathbf{a}_{\perp} = c^2 \, \boldsymbol{\tau}_{\rm info} / E$  for the interference packet, yielding displacements at the 10 pm level over a metre baseline—measurable with existing cold-atom fountains.

# 18.3 Visual Outreach Metaphors

Although not part of the derivation, three images help convey the idea to non-specialists:

- (a) **Twisting Fabric.** Aligned phase waves "wring" spacetime like cloth; the tighter the twist, the deeper the curvature.
- (b) Choreographed Dancers. Synchronised rotation pulls the dancers inward; loss of rhythm lets the circle slacken. Coherence does the same for geodesics.
- (c) Water Vortex. Co-phased surface ripples amplify into a whirlpool; decoherence breaks the vortex apart.

These metaphors can be placed in sidebars or figure captions; omitting them from the core argument keeps the mathematical chain from  $\tau_{\mu\nu\rho}$  to  $R_{\mu\nu\rho}^{\ \sigma}$  logically tight.

# 19 Time Density and Phase–Rate Dynamics

Super Information Theory identifies a scalar time-density field  $\rho_t(x)$ , with physical dimension [T<sup>-1</sup>], as one of its two primitive variables. Its operational meaning is set by the phase accumulation of a reference clock carried along any world-line. Let  $\varphi(x)$  denote the phase of the locally maximally coherent mode. We postulate

$$\dot{\varphi}(x) = \frac{S_{\text{coh}}(x)}{\hbar_{\text{eff}}}, \qquad \rho_t(x) = \rho_0 \left( \dot{\varphi}_0 / \dot{\varphi}(x) \right), \tag{39}$$

where  $S_{\text{coh}}$  is the density of the coherence action and  $\hbar_{\text{eff}}$  is a fixed microscopic constant that calibrates informational action in ordinary SI units. Equation (39) replaces the older "quantum stopwatch" metaphor with a dimensionally explicit relation: slower phase advance (smaller  $\dot{\varphi}$ ) corresponds to larger  $\rho_t$  and hence stronger scalar—tensor back-reaction in the action of Sec. ??. The converse holds for decoherence-dominated regions. Linearising the scalar—tensor field equations around Minkowski space gives the modified Poisson law

$$\nabla^2 \Phi = 4\pi G \rho_m + \beta \nabla^2 \delta \rho_t,$$

with  $\beta = \alpha \rho_0$ . Laboratory torsion-balance data bound  $|\beta| < 10^{-5}$ , fixing the absolute scale of  $\rho_t$  once  $\alpha$  is chosen. High-accuracy transportable optical clocks can in turn test Eq. (39) by monitoring the fractional shift  $\Delta \nu / \nu = \frac{1}{2} \alpha \, \Delta \rho_t / \rho_0$  when the local phase-rate is modulated, providing the principal tabletop probe of the time-density sector.

# 19.1 Self-Organising Feedback and Coherence Flow

The continuity equation

$$\nabla_{\mu} J_{\rm coh}^{\mu} = 0, \qquad J_{\rm coh}^{\mu} = R_{\rm coh} \, \frac{\partial \mathcal{L}_{\rm SIT}}{\partial (\nabla_{\mu} R_{\rm coh})},$$

shows that  $R_{\rm coh}$  and  $\rho_t$  are coupled through a conserved informational current. In regions where  $\nabla_{\mu}R_{\rm coh}$  and  $\nabla_{\mu}\rho_t$  are non-parallel the antisymmetric tensor

$$\tau_{\mu\nu\rho} = \beta \nabla_{[\mu} R_{\rm coh} \nabla_{\nu]} \rho_t \, u_\rho$$

feeds back into the Einstein sector as an effective source of curvature. This mechanism replaces the earlier "informational torque" prose while retaining the observable prediction that cold-atom fountains will register centimetre-scale transverse accelerations scaling with  $|\nabla R_{\rm coh} \times \nabla \rho_t|$ .

# 19.2 Relation to Quantum Interference

Because  $\rho_t$  is tied directly to the phase rate, any spatial modulation of  $R_{\rm coh}$  induces a calculable shift in interference fringes. In the Aharonov–Bohm geometry one finds

$$\theta_{\rm AB} = \frac{e}{\hbar} \oint (\nabla \theta) \cdot d\ell,$$

demonstrating that the canonical phase holonomy already measured in electron interferometers constrains the product  $\lambda R_{\rm coh}$  entering the core action. No additional "frequency-specific gravity" assumption is required.

#### 19.3 Material Moved to Appendix S

Earlier drafts located wide-ranging speculations on fractal cross-scale resonance, cognitive loops and technological evolution inside this section. Those ideas remain valuable but are now collected in  $Appendix\ S$  so that the main text keeps a tight focus on the experimentally anchored physics of  $\rho_t$  and  $R_{\rm coh}$ . [12pt]article amsmath geometry letterpaper, margin=1in

# 20 The Wavefunction as Gravity: SIT's Mathematical and Conceptual Identity

The conventional separation of quantum mechanics and general relativity marks the primary unresolved challenge of modern physics. Quantum theory describes the evolution of the wavefunction, while general relativity describes gravity as spacetime curvature sourced by stress-energy. Super Information Theory (SIT) proposes a radical unification based on a direct identity: the wavefunction is not a separate entity that *generates* gravity, but is the very informational substrate as which gravity manifests. Gravity, in this framework, is the macroscopic expression of the wavefunction's structure, governed by the principle of coherence.

# 20.1 The Physical Mechanism: From Coherence to Curvature

SIT models this identity by introducing a classical scalar field, the time-density field  $\rho_t(x)$ , which functions as the physical mediator between quantum coherence and spacetime geometry. This field is sourced by the **coherence ratio**  $R_{\mathbf{coh}}(x)$ , a dimensionless and operationally defined measure of local quantum phase alignment.

• Operationally,  $R_{\rm coh}$  is a measurable quantity. In a Bose-Einstein Condensate (BEC), it is proportional to the local condensate fraction. In a laser beam, it relates to the photon correlation functions. A value of  $R_{\rm coh} \approx 1$  signifies near-perfect phase alignment, while  $R_{\rm coh} \approx 0$  signifies a decoherent, random phase state.

The dynamics of this system are governed by the SIT action, which extends the Einstein-Hilbert action with terms for the new scalar field:

$$S_{\text{SIT}} = \int d^4x \sqrt{-g} \left[ \frac{R}{16\pi G} + \mathcal{L}_{\text{SM}} + \frac{1}{2} g^{\mu\nu} \partial_{\mu} \rho_t \partial_{\nu} \rho_t - V(\rho_t) + \frac{\lambda}{2} g^{\mu\nu} (\partial_{\mu} \psi^*) (\partial_{\nu} \psi) - U(|\psi|) - \mathcal{L}_{\text{int}}(\rho_t, |\psi|, \text{matter}) \right]$$

$$(40)$$

Here,  $V(\rho_t)$  is the scalar field's potential and  $\mathcal{L}_{int}$  models its coupling to Standard Model fields. A central axiom of SIT is that  $\rho_t$  is sourced by  $R_{coh}$ , for instance through a relation like  $\rho_t = \rho_0 \exp[\alpha R_{coh}]$ .

The field equations derived from this action show that the geometry of spacetime is sculpted not only by the stress-energy of matter  $(T_{\mu\nu}(\text{matter}))$  but also by the stress-energy of the time-density field  $(T_{\mu\nu}(\rho_t))$ . Because  $\rho_t$  is sourced by coherence, spacetime curvature becomes a direct function of the organization and flow of quantum information.

#### 20.2 Reinterpreting Quantum Phenomena

This framework provides a new physical basis for understanding core quantum concepts:

- Measurement: A measurement interaction is a physical process that enforces local phase alignment between a quantum system and the apparatus. This raises the local value of  $R_{\text{coh}}$ , which in turn sources a stronger  $\rho_t$  field. The stress-energy associated with this transient  $\rho_t$  field creates a localized, temporary modulation of spacetime curvature—a measurable gravitational effect. This provides a physical, deterministic mechanism for what is often termed "collapse."
- Wave-Particle Duality: This duality is re-framed as a duality of field configurations. A "particle" is identified with a stable, localized field configuration characterized by high  $R_{\text{coh}}$ . This configuration sources a significant, localized  $\rho_t$  field, whose stressenergy generates a persistent gravitational potential. In contrast, a "wave" corresponds to a propagating, delocalized solution where  $R_{\text{coh}}$  is low, the  $\rho_t$  field is diffuse, and the associated gravitational effect is negligible.

### 20.3 Coherence, Energy, and the Equivalence Principle

At first glance, the assertion that "organized energy" gravitates more strongly than disorganized energy seems to challenge the Equivalence Principle. SIT refines this concept without violating the core principle.

In SIT, the total source of gravity is the total stress-energy tensor:

$$T_{\mu\nu}(\text{total}) = T_{\mu\nu}(\text{matter}) + T_{\mu\nu}(\rho_t).$$

- 1. The stress-energy of matter and radiation,  $T_{\mu\nu}$  (matter), sources gravity in exact accordance with the Equivalence Principle. All forms of energy in this term gravitate equally.
- 2. However, coherent configurations of matter are vastly more effective at sourcing a strong, localized **time-density field**  $\rho_t$ .
- 3. This  $\rho_t$  field itself possesses stress-energy,  $T_{\mu\nu}(\rho_t)$ , which also contributes to the curvature of spacetime.

Therefore, a coherent system (like a BEC) produces a stronger total gravitational effect than an incoherent one (a thermal gas) of the same mass-energy. This is not because the energy itself "weighs more," but because the coherent state generates a powerful secondary field that contributes to the total source of gravity. The framework thus proposes a coherence-dependent total gravitational effect while preserving the fundamental principle that the stress-energy tensor is the universal source of curvature.

# 20.4 Comparison to Emergent Gravity and Experimental Signatures

Like theories proposing spacetime emerges from entanglement (e.g., ER=EPR), SIT identifies a quantum-informational basis for gravity. However, SIT proposes a more direct, testable mechanism: a dynamical field theory where spacetime curvature is modulated by  $R_{\rm coh}$ , a measurable quantity.

This leads to concrete experimental predictions. Variations in coherence should produce measurable gravitational anomalies not attributable to energy density alone.

• Lasers and BECs: These highly coherent systems are the ideal laboratories. Precision experiments comparing the gravitational influence of a BEC to a thermal atomic cloud, or a coherent laser to an incoherent light source of identical energy, can directly test SIT's central claim. A successful observation would provide direct support for the identity between the wavefunction's coherent structure and the phenomenon of gravity.

Theoretically, this framework provides a path toward a unified physics where measurement, information, and geometry are not disparate domains, but expressions of a single, underlying law of coherence dynamics.