

HW14b

Tuesday, March 14, 2023

4:08 PM

6. Consider the following relations that are all relations on A (i.e. $A \leftrightarrow A$) where $A = \{a, b, c, d\}$. Indicate which properties each relation has by circling the property names the relation possesses.

a) for $\{(a,a), (a,b), (d,c)\}$

☐ Reflexive \times

☐ Symmetric \times

☒ Antisymmetric \checkmark

☒ Transitive \checkmark

$(a,a) (a,b) \rightarrow (a,b) \checkmark$

b) for $\{(a,d), (d,a)\}$

☐ Reflexive \times

☒ Symmetric \checkmark

☐ Antisymmetric \times

☐ Transitive \times

$(a,d) (d,a) \rightarrow (a,a) \times$

$(d,a) (a,d) \rightarrow (d,d) \times$

c) for $\{(a,d), (a,b), (c,c)\}$

☐ Reflexive \times

☐ Symmetric \times

☒ Antisymmetric \checkmark

☒ Transitive \checkmark

d) for $\{(a,b), (b,a), (d,d)\}$

☐ Reflexive \times

☒ Symmetric \checkmark

☐ Antisymmetric \times

☐ Transitive \times

$(a,b) (b,a) \rightarrow (a,a) \times$

$(b,a) (a,b) \rightarrow (b,b) \times$

e) for $\{\}$

☐ Reflexive \times

☒ Symmetric \checkmark

☒ Antisymmetric \checkmark

☒ Transitive \checkmark

f) for $\{(a,c), (c,a), (c,c), (a,a)\}$

☐ Reflexive \times

☒ Symmetric \checkmark

☐ Antisymmetric \times

☒ Transitive \checkmark

$(a,c) (c,a) \rightarrow (a,a) \checkmark$

$(c,a) (a,c) \rightarrow (c,c) \checkmark$