

# heemod TB population Markov model

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```
# see: https://cran.r-project.org/web/packages/heemod/vignettes/d\_non\_homogeneous.html

# NOTE:
# transitions happen at the beginning of each year (equivalent to transition happening at
# the end + ignoring the first year) with method = "beginning".
# Since with this method the first year is actually the second,
# costs should be discounted from the start with the argument first = TRUE in discount().

library(heemod)
library(purrr)
library(dplyr)

# age-dependent probability of death, TB and QoL weighting
pdeath_QoL <-
  read.csv(here::here("raw data", "pdeath_QoL.csv"))

# probabilistic realisations of starting state probabilities
# generated from decision tree
load(file = here::here("data", "init_states.RData"))
head(init_states)

##   noLTBI completeTx incompleteTx      noTx activeTB dead
## 1  0.643 0.04429927 0.068075534 0.2446252         0    0
## 2  0.683 0.02576789 0.019090692 0.2721414         0    0
## 3  0.672 0.04943117 0.030844729 0.2477241         0    0
## 4  0.742 0.05223975 0.001835084 0.2039252         0    0
## 5  0.726 0.02743526 0.010678055 0.2358867         0    0
## 6  0.650 0.05570397 0.024181029 0.2701150         0    0

# define the model heemod parameters
param <- define_parameters(
  age_init = 34,                # starting age
  age = age_init + markov_cycle, # increment age annually

  # transition probabilities
  pReact_comp = 0.0006779,      # TB after completed LTBI treatment
  pReact_incomp = 0.0015301,    # TB after LTBI treatment dropout
  pReact = 0.0019369,          # TB after no treatment

  TB_cost = 4925.76,            # cost of TB treatment (£)
  d = 0.035,                    # annual discount factor

  # match prob death to age
```

```

pdeath = look_up(data = pdeath_QoL,
                  value = "pDeath",
                  age = age),
pdeathTB = look_up(data = pdeath_QoL,
                   value = "pDeath_TB",
                   age = age),

# match QoL weight to age
QoL = look_up(data = pdeath_QoL,
              value = "QoL_weight",
              age = age)
)

## Warning: markov_cycle was deprecated in heemod 0.16.0.
## i Please use model_time instead.
## i The deprecated feature was likely used in the base package.
## Please report the issue to the authors.
## This warning is displayed once every 8 hours.
## Call `lifecycle::last_lifecycle_warnings()` to see where this warning was
## generated.

# create transition matrix
mat_trans <- define_transition(
  state_names = c(
    "noLTBI",
    "completeTx",
    "incompleteTx",
    "noTx",
    "activeTB",
    "dead"
  ),

  # from-to probability matrix
  # C represent complements
  C, 0, 0, 0, 0, pdeath,
  0, C, 0, 0, pReact_comp, pdeath,
  0, 0, C, 0, pReact_incomp, pdeath,
  0, 0, 0, C, pReact, pdeath,
  C, 0, 0, 0, 0, pdeathTB,
  0, 0, 0, 0, 0, 1
)

# define starting state populations
init_states <- select(.data = init_states,
                     noLTBI,
                     completeTx,
                     incompleteTx,
                     noTx)

init_states <- data.frame(init_states,
                         activeTB = 0,
                         dead = 0)

# define cost and utility values associated with each state

```

```

noLTBI <- define_state(
  cost = 0,
  utility = discount(QoL, d, first = TRUE)
)

completeTx <- define_state(
  cost = 0,
  utility = discount(QoL, d, first = TRUE)
)

incompleteTx <- define_state(
  cost = 0,
  utility = discount(QoL, d, first = TRUE)
)

noTx <- define_state(
  cost = 0,
  utility = discount(QoL, d, first = TRUE)
)

activeTB <- define_state(
  cost = discount(TB_cost, d, first = TRUE),
  utility = discount(QoL - 0.15, d, first = TRUE)
)

dead <- define_state(
  cost = 0,
  utility = 0
)

# combine all of the model elements to form
# a 'strategy' consisting of a transition
# matrix and states states with properties attached
strat <- define_strategy(
  transition = mat_trans,
  noLTBI = noLTBI,
  completeTx = completeTx,
  incompleteTx = incompleteTx,
  noTx = noTx,
  activeTB = activeTB,
  dead = dead
)

save(strat, params, cost, utility,
      file = "data/ltbi_heemod.RData")

# run a single simulation
res_mod <-
  run_model(
    init = 1000 * init_states[1, ], # initial population sizes
    method = "end",
    strat,
    parameters = param,
    cycles = 66, # number of time steps
  )

```

```

    cost = cost,
    effect = utility
)

```

## No named model -> generating names.

## Run multiple simulations

Using the sample of starting state probabilities

```

res_mod <- list()

for (i in 1:nrow(init_states)) {

  res_mod[[i]] <-
    suppressMessages(
      run_model(
        # init = c(674.0588764, # hard-code values
        #          168.0253748,
        #          42.42724895,
        #          115.4884998,
        #          0,
        #          0),
        init = 1000 * init_states[i, ], # population sizes
        method = "end",
        strat,
        parameters = param,
        cycles = 66,
        cost = cost,
        effect = utility
      ))
}

```

## Results

```

res_mod[[1]]

## 1 strategy run for 66 cycles.
##
## Initial state counts:
##
## noLTBI = 643
## completeTx = 44.2992721299233
## incompleteTx = 68.0755335064717
## noTx = 244.625194363605
## activeTB = 0
## dead = 0
##
## Counting method: 'end'.
##
## Values:
##
##      cost  utility
## I 64939.64 18735.25

```

```
# extract the cost and utility values
c1 <- map_df(res_mod, "run_model")$cost
h1 <- map_df(res_mod, "run_model")$utility
```

```
get_counts(res_mod[[1]])
```

```
## # A tibble: 396 x 4
##   .strategy_names model_time state_names count
##   <chr>           <int> <chr>      <dbl>
## 1 I               1 noLTBI    642.
## 2 I               2 noLTBI    643.
## 3 I               3 noLTBI    643.
## 4 I               4 noLTBI    642.
## 5 I               5 noLTBI    642.
## 6 I               6 noLTBI    642.
## 7 I               7 noLTBI    642.
## 8 I               8 noLTBI    642.
## 9 I               9 noLTBI    641.
## 10 I             10 noLTBI    641.
## # i 386 more rows
```

```
get_values(res_mod[[1]])
```

```
##   model_time .strategy_names value_names      value
## 1         1             I      cost 2893.6217181
## 2         2             I      cost 2788.4685562
## 3         3             I      cost 2686.9630890
## 4         4             I      cost 2589.0048654
## 5         5             I      cost 2494.3029316
## 6         6             I      cost 2402.9158522
## 7         7             I      cost 2314.6079384
## 8         8             I      cost 2229.3845530
## 9         9             I      cost 2147.0354045
## 10        10            I      cost 2067.5602321
## 11        11            I      cost 1990.6994981
## 12        12            I      cost 1916.4105829
## 13        13            I      cost 1844.6932493
## 14        14            I      cost 1775.3801128
## 15        15            I      cost 1708.4451018
## 16        16            I      cost 1643.6450770
## 17        17            I      cost 1580.9234648
## 18        18            I      cost 1520.2998884
## 19        19            I      cost 1461.6662675
## 20        20            I      cost 1404.8697286
## 21        21            I      cost 1349.8350639
## 22        22            I      cost 1296.4699955
## 23        23            I      cost 1244.7507045
## 24        24            I      cost 1194.4873875
## 25        25            I      cost 1145.7691008
## 26        26            I      cost 1098.3958630
## 27        27            I      cost 1052.2756949
## 28        28            I      cost 1007.5182217
## 29        29            I      cost  964.0011471
## 30        30            I      cost  921.6721968
```

## 31	31	I	cost	880.5389973
## 32	32	I	cost	840.5856673
## 33	33	I	cost	801.9526687
## 34	34	I	cost	764.1848705
## 35	35	I	cost	727.2389153
## 36	36	I	cost	691.0301963
## 37	37	I	cost	655.6061620
## 38	38	I	cost	620.9247593
## 39	39	I	cost	586.5875311
## 40	40	I	cost	552.9029239
## 41	41	I	cost	519.7202225
## 42	42	I	cost	487.3073234
## 43	43	I	cost	455.5072152
## 44	44	I	cost	424.3748705
## 45	45	I	cost	393.7646992
## 46	46	I	cost	363.6181185
## 47	47	I	cost	333.6484722
## 48	48	I	cost	304.3522703
## 49	49	I	cost	275.4194877
## 50	50	I	cost	247.2334057
## 51	51	I	cost	219.8060264
## 52	52	I	cost	193.2614457
## 53	53	I	cost	168.0387193
## 54	54	I	cost	144.1360339
## 55	55	I	cost	121.8242521
## 56	56	I	cost	101.2858046
## 57	57	I	cost	82.6780498
## 58	58	I	cost	66.3118896
## 59	59	I	cost	51.9160178
## 60	60	I	cost	39.5652209
## 61	61	I	cost	29.5376199
## 62	62	I	cost	21.4867125
## 63	63	I	cost	15.2944047
## 64	64	I	cost	10.5076250
## 65	65	I	cost	6.9552518
## 66	66	I	cost	4.4602567
## 67	1	I	utility	878.4298395
## 68	2	I	utility	847.9796437
## 69	3	I	utility	818.5383220
## 70	4	I	utility	790.0196004
## 71	5	I	utility	762.4472174
## 72	6	I	utility	735.7517380
## 73	7	I	utility	709.9398032
## 74	8	I	utility	684.9494409
## 75	9	I	utility	660.7851933
## 76	10	I	utility	637.3687936
## 77	11	I	utility	574.1453476
## 78	12	I	utility	553.6448161
## 79	13	I	utility	533.7923691
## 80	14	I	utility	514.5837727
## 81	15	I	utility	495.9494006
## 82	16	I	utility	477.8753901
## 83	17	I	utility	460.3707879
## 84	18	I	utility	443.4060424

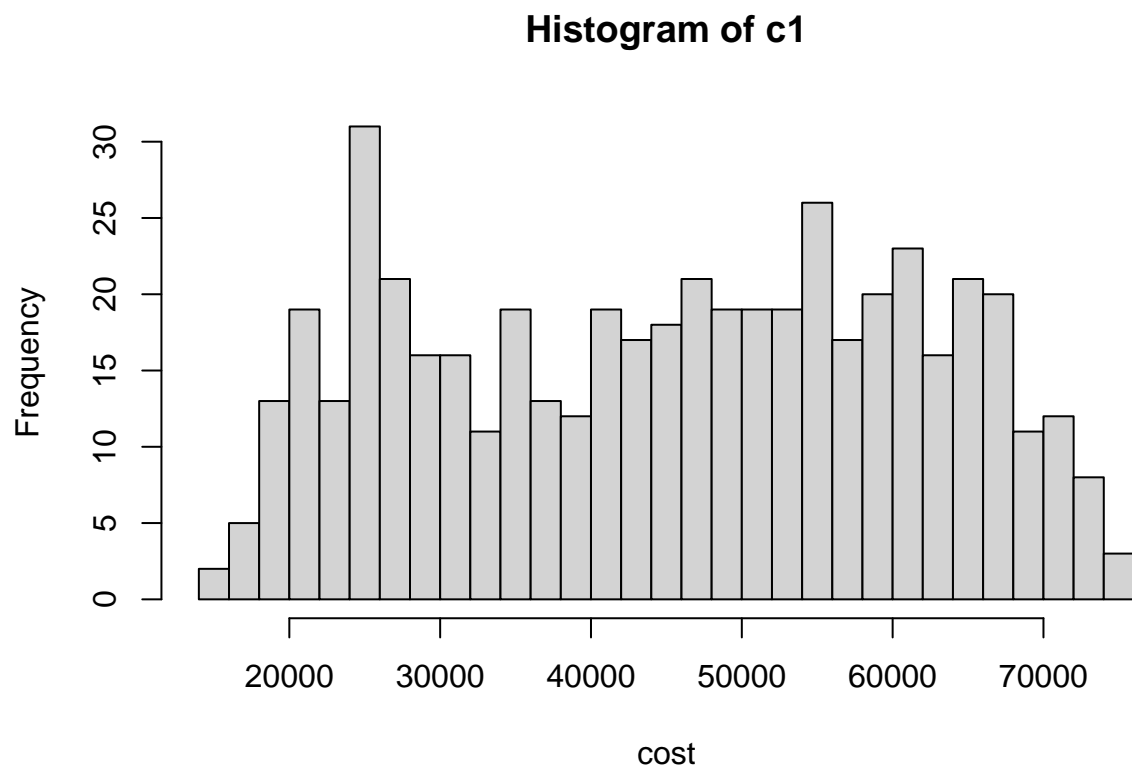
## 85	19	I	utility	426.9378036
## 86	20	I	utility	410.9459951
## 87	21	I	utility	372.1436459
## 88	22	I	utility	357.9371158
## 89	23	I	utility	344.0983823
## 90	24	I	utility	330.6551502
## 91	25	I	utility	317.5519374
## 92	26	I	utility	304.7640740
## 93	27	I	utility	292.3250666
## 94	28	I	utility	280.2013944
## 95	29	I	utility	268.3796387
## 96	30	I	utility	256.8637124
## 97	31	I	utility	239.4907084
## 98	32	I	utility	228.8785935
## 99	33	I	utility	218.4770364
## 100	34	I	utility	208.2747816
## 101	35	I	utility	198.2486822
## 102	36	I	utility	188.4132946
## 103	37	I	utility	178.7575629
## 104	38	I	utility	169.1677942
## 105	39	I	utility	159.7332680
## 106	40	I	utility	150.4112925
## 107	41	I	utility	132.2225432
## 108	42	I	utility	123.8134117
## 109	43	I	utility	115.5567282
## 110	44	I	utility	107.4136681
## 111	45	I	utility	99.3688475
## 112	46	I	utility	91.3444637
## 113	47	I	utility	83.4764501
## 114	48	I	utility	75.6805993
## 115	49	I	utility	68.0624950
## 116	50	I	utility	60.6263134
## 117	51	I	utility	53.4071482
## 118	52	I	utility	46.5273300
## 119	53	I	utility	39.9880969
## 120	54	I	utility	33.8662986
## 121	55	I	utility	28.2148059
## 122	56	I	utility	23.0799343
## 123	57	I	utility	18.5512301
## 124	58	I	utility	14.5562346
## 125	59	I	utility	11.1189004
## 126	60	I	utility	8.3205496
## 127	61	I	utility	6.0674994
## 128	62	I	utility	4.3297883
## 129	63	I	utility	2.9825219
## 130	64	I	utility	1.9796768
## 131	65	I	utility	1.2731980
## 132	66	I	utility	0.7895506

```
summary(res_mod[[4]])
```

```
## 1 strategy run for 66 cycles.
##
## Initial state counts:
##
```

```
## noLTBI = 742
## completeTx = 52.2397525531171
## incompleteTx = 1.83508364108649
## noTx = 203.925163805796
## activeTB = 0
## dead = 0
##
## Counting method: 'end'.
##
## Values:
##
##      cost  utility
## I 46249.04 18737.91
```

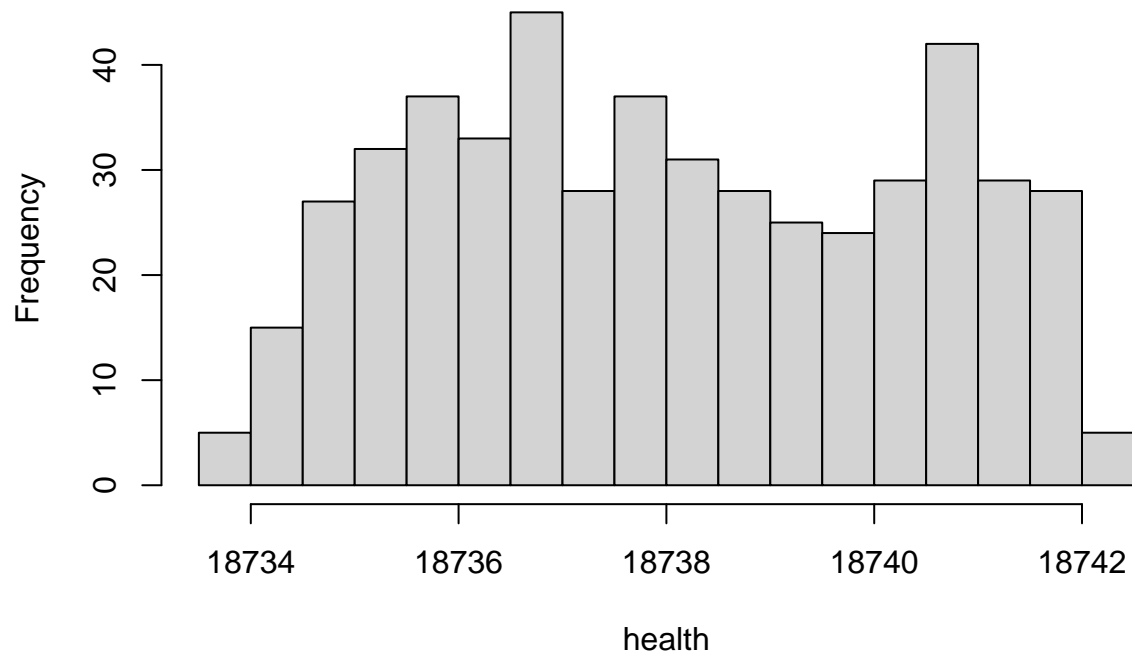
```
# plots
hist(c1, breaks = 30, xlab = "cost")
```



```
hist(h1, breaks = 30, xlab = "health")
```



# Histogram of h1



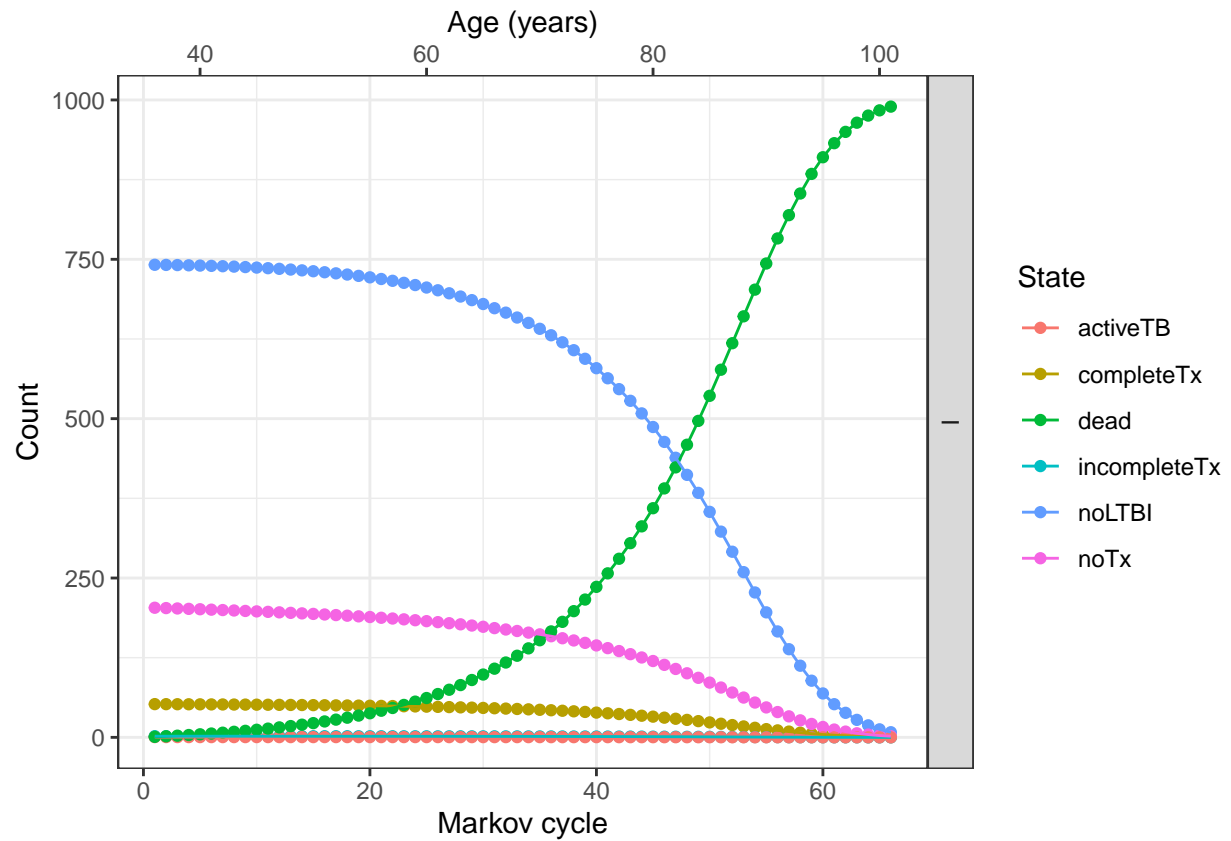
```
library(ggplot2)
```

```
## Warning: package 'ggplot2' was built under R version 4.3.3
```

```
plot(res_mod[[4]]) +  
  scale_x_continuous(sec.axis = sec_axis(~ . + 35, name = "Age (years)")) +  
  theme_bw()
```

```
## Scale for x is already present.
```

```
## Adding another scale for x, which will replace the existing scale.
```



```
# state-edge graph
plot(mat_trans, arr.type = "simple")

## Loading required namespace: diagram
```

